### **Program Structures & Algorithms**

#### **Assignment 4 (Parallel Sorting)**

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#### Task:

Your task is to implement a parallel sorting algorithm such that each partition of the array is sorted in parallel. You will consider two different schemes for deciding whether to sort in parallel.

- 1. A cutoff (defaults to, say, 1000) which you will update according to the first argument in the command line when running. It's your job to experiment and come up with a good value for this cutoff. If there are fewer elements to sort than the cutoff, then you should use the system sort instead.
- 2. Recursion depth or the number of available threads. Using this determination, you might decide on an ideal number (*t*) of separate threads (stick to powers of 2) and arrange for that number of partitions to be parallelized (by preventing recursion after the depth of *lg t* is reached).
- 3. An appropriate combination of these.

#### **Relationship Conclusions:**

- 1. As per the cutoff ratio (cutoff/size of the array), we see that irrespective of the array sizes, and the number of threads available for parallel sorting, there is a range of cutoff ratio between 0.1 and 0.55 for which parallel sort can be an optimal solution
- 2. As per performing analysis on different sizes of arrays (2 Million and 16 Million), for a number of different threads ranging from 2 to 16, we see that 6 threads works as a best case scenario

Evidence to support the conclusion:

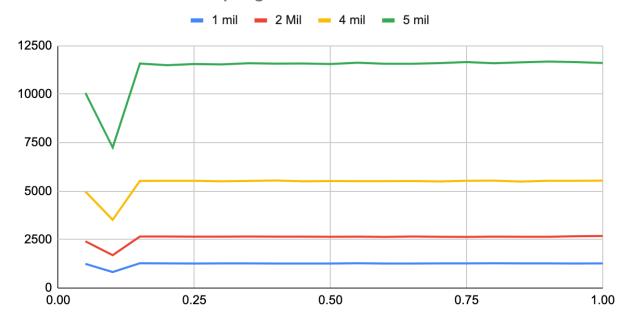
1. Finding the optimal cutoff value, for different sizes of input array(No of threads constant)

**Threads 2,** Array sizes varied from : 1 Million to 6 Million, doubling each run. Cutoff ratio: (Cutoff value/Size of the array): Ranging from 0.05 to to 1.0 in increments of 0.05

Cutoff ratio	1 Million	2 Million	4 Million	8 Million	16 Million
0.05	676	1245	2412	4971	10058
0.1	397	825	1694	3520	7254
0.15	617	1279	2657	5526	11580
0.2	607	1269	2656	5533	11499
0.25	603	1264	2653	5531	11557
0.3	605	1271	2650	5507	11539
0.35	596	1270	2658	5528	11595
0.4	602	1266	2650	5549	11575
0.45	606	1267	2651	5504	11583
0.5	599	1267	2645	5516	11560
0.55	601	1275	2654	5510	11625
0.6	599	1262	2637	5512	11570
0.65	597	1262	2658	5522	11568
0.7	600	1269	2647	5501	11604
0.75	602	1270	2635	5534	11656
0.8	600	1275	2649	5537	11600
0.85	600	1269	2644	5490	11646
0.9	599	1272	2643	5531	11687

0.95	601	1266	2672	5530	11659
1.00	598	1272	2685	5540	11609

## Relationship between cutoff ratio vs time for a program with 2 threads.

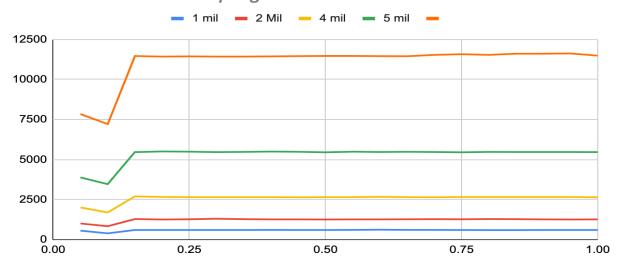


Threads: 4
Array sizes varied from: 1 Million to 6 Million, doubling each run. Cutoff ratio: (Cutoff value/Size of the array): Ranging from 0.05 to to 1.0 in increments of 0.05

Cutoff ratio	1 Million	2 Million	4 Million	8 Million	16 Million
0.05	563	1006	2009	3883	7841
0.1	392	839	1696	3462	7211
0.15	603	1281	2695	5467	11462

0.2	600	1256	2664	5509	11431
0.25	600	1269	2654	5493	11440
0.3	601	1304	2653	5464	11431
0.35	600	1279	2648	5480	11429
0.4	604	1265	2648	5496	11445
0.45	600	1263	2642	5484	11458
0.5	600	1254	2649	5450	11470
0.55	606	1261	2653	5493	11472
0.6	618	1261	2670	5472	11454
0.65	608	1268	2650	5487	11447
0.7	607	1279	2641	5473	11539
0.75	601	1271	2658	5453	11575
0.8	597	1284	2658	5477	11538
0.85	597	1278	2656	5475	11611
0.9	599	1262	2655	5472	11613
0.95	601	1260	2656	5470	11621
1.00	599	1264	2644	5465	11491

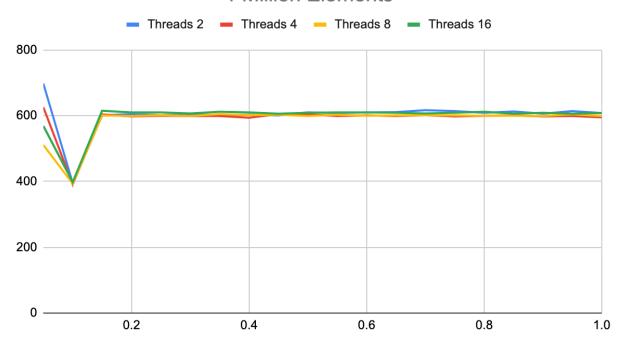
## Relationship between cutoff ratio vs time for a program with 4 threads.



# 2. Checking for different threads from 2 to 16 for an array of 1000000 elements, with cutoff ratios changing from 0.05 to 1.0 $\,$

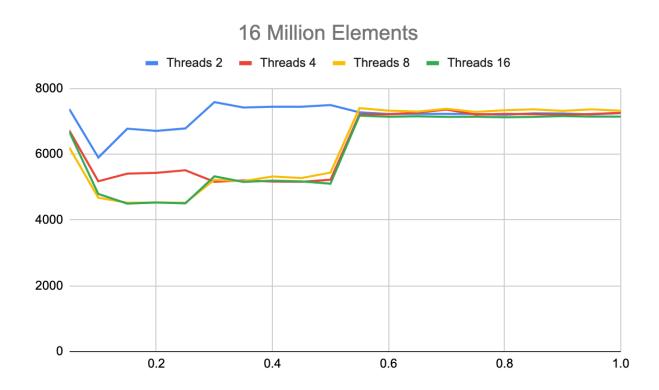
Cutoff ratio	Threads 2	Threads 4	Threads 8	Threads 16
0.05	698	626	511	569
0.1	395	391	393	398
0.15	601	604	601	615
0.2	605	598	599	610
0.25	602	600	602	610
0.3	604	599	599	607
0.35	602	599	605	612
0.4	603	594	602	610
0.45	601	605	603	606
0.5	610	604	599	609
0.55	608	599	603	610
0.6	610	601	600	610
0.65	611	599	601	609
0.7	617	602	602	607
0.75	614	598	601	609
0.8	609	600	600	612
0.85	613	601	600	606
0.9	606	598	599	609
0.95	614	599	604	606
1	608	595	599	608

### 1 Million Elements



Cutoff ratio	Threads 2	Threads 4	Threads 8	Threads 16
0.05	7373	6720	6202	6679
0.1	5901	5177	4676	4792
0.15	6776	5410	4524	4498
0.2	6710	5433	4528	4533
0.25	6784	5512	4525	4507
0.3	7585	5162	5220	5327
0.35	7422	5205	5180	5159
0.4	7445	5168	5324	5196
0.45	7443	5162	5274	5174
0.5	7494	5223	5441	5105
0.55	7273	7211	7402	7171
0.6	7222	7214	7327	7139

0.65	7225	7268	7297	7150
0.7	7225	7356	7380	7135
0.75	7224	7208	7285	7138
0.8	7198	7226	7339	7123
0.85	7242	7219	7366	7137
0.9	7239	7203	7319	7161
0.95	7211	7222	7366	7145
1	7250	7260	7320	7144



Screenshots proof for conclusion 1

```
processArgs(args);
                Random random = new Random():
                int[] array = new int[2000000];
   Degree of parallelism: 2
   cutoff: 1000000
                       10times Time:1279ms
                       10times Time:1269ms
÷.
   cutoff: 5000000
                       10times Time:1264ms
                       10times Time:1271ms
   cutoff: 8000000
   cutoff: 9000000
                       10times Time:1267ms
   cutoff: 10000000
                           10times Time:1267ms
                           10times Time:1262ms
                           10times Time:1262ms
   cutoff: 14000000
                           10times Time:1269ms
                           10times Time:1270ms
                            10times Time:1275ms
    cutoff: 18000000
                            10times Time:1272ms
    cutoff: 19000000
                            10times Time: 1266ms
                            10times Time:1272ms
```

```
long startTime = System.currentTimeMillis();
                   long endTime = System.currentTimeMillis();
   Degree of parallelism: 2
   cutoff: 2000000
                       10times Time:607ms
÷
   cutoff: 3000000
                       10times Time:605ms
   cutoff: 3500000
                       10times Time:596ms
   cutoff: 4000000
                       10times Time:602ms
    cutoff: 4500000
    cutoff: 5000000
    cutoff: 8000000
                       10times Time:600ms
    cutoff: 8500000
                       10times Time:600ms
                       10times Time:599ms
    cutoff: 9000000
    cutoff: 9500000
                       10times Time:601ms
    cutoff: 10000000
                           10times Time:598ms
```

```
public static void main(String[] args) {
            processArgs(args);
            System.out.println("Degree of parallelism: " + myPool.getParallelism());
                long startTime = System.currentTimeMillis();
Degree of parallelism: 2
cutoff: 4000000
                   10times Time:1694ms
cutoff: 6000000
cutoff: 8000000
                   10times Time: 2656ms
cutoff: 12000000
                      10times Time:2650ms
cutoff: 14000000
                     10times Time:2658ms
cutoff: 16000000
cutoff: 18000000
                      10times Time:2651ms
                     10times Time:2645ms
cutoff: 20000000
cutoff: 22000000
                     10times Time:2637ms
cutoff: 26000000
cutoff: 28000000
                       10times Time: 2647ms
cutoff: 30000000
                      10times Time: 2635ms
                     10times Time:2649ms
cutoff: 34000000
cutoff: 36000000
                       10times Time:2643ms
                      10times Time:2672ms
cutoff: 38000000
cutoff: 40000000
                      10times Time:2685ms
```

```
public static void main(String[] args) {
              processArgs(args);
             Random random = new Random();
int[] array = new int[8000000];
                  ParSort.cutoff = 4000000 * (j + 1);
                  long time;
                  long startTime = System.currentTimeMillis();
 Degree of parallelism: 2
cutoff: 8000000
                     10times Time:3520ms
cutoff: 12000000
                       10times Time:5526ms
cutoff: 20000000
                         10times Time:5531ms
                         10times Time:5507ms
cutoff: 24000000
                         10times Time:5528ms
 cutoff: 36000000
                         10times Time:5504ms
 cutoff: 40000000
                         10times Time:5516ms
cutoff: 48000000
                         10times Time:5512ms
 cutoff: 60000000
                         10times Time:5534ms
                         10times Time:5490ms
 cutoff: 72000000
                         10times Time:5531ms
                         10times Time:5540ms
```

```
public static void main(String[] args) {
                    processArgs(args);
                    int[] array = new int[16000000];
                      long startTime = System.currentTimeMillis();
       Degree of parallelism: 2
       cutoff: 8000000 10times Time:10058ms
                              10times Time:11499ms
                             10times Time:11557ms
                              10times Time:11539ms
   ŧ
       cutoff: 56000000
                             10times Time:11595ms
==
       cutoff: 64000000
                              10times Time:11575ms
                              10times Time:11583ms
       cutoff: 88000000
                              10times Time:11625ms
                              10times Time:11570ms
                              10times Time:11604ms
       cutoff: 112000000
       cutoff: 120000000
                              10times Time:11656ms
                              10times Time:11646ms
       cutoff: 136000000
                              10times Time:11687ms
       cutoff: 144000000
                              10times Time:11659ms
```

```
honito praito Anto math(pri.thAll qi.Ap) /
                    processArgs(args);
                    System.out.println("Degree of parallelism: " + myPool.getParallelism());
                    int[] array = new int[16000000];
                       ParSort.cutoff = 8000000 * (j + 1);
                        long startTime = System.currentTimeMillis();
       Degree of parallelism: 4
       cutoff: 8000000 10times Time:7841ms
عر
       cutoff: 16000000
       cutoff: 24000000
       cutoff: 32000000
                               10times Time:11431ms
   = cutoff: 40000000
                               10times Time:11440ms
   cutoff: 48000000
                               10times Time:11431ms
       cutoff: 56000000
==
       cutoff: 64000000
                               10times Time:11445ms
       cutoff: 72000000
                               10times Time:11458ms
*
       cutoff: 80000000
                               10times Time:11470ms
       cutoff: 88000000
                               10times Time:11472ms
                               10times Time:11454ms
       cutoff: 96000000
                               10times Time:11447ms
       cutoff: 104000000
       cutoff: 112000000
                               10times Time:11539ms
       cutoff: 120000000
                               10times Time:11575ms
       cutoff: 128000000
                               10times Time:11538ms
       cutoff: 136000000
                               10times Time:11611ms
       cutoff: 144000000
                               10times Time:11613ms
       cutoff: 152000000
                               10times Time:11621ms
       cutoff: 160000000
                               10times Time:11491ms
```

```
public static int threadCount = 4;
                 processArgs(args);
                 Random random = new Random();
    Degree of parallelism: 4
    cutoff: 4000000
<u>≕</u>
    cutoff: 16000000
                            10times Time:5509ms
    cutoff: 20000000
                            10times Time:5493ms
                            10times Time:5464ms
    cutoff: 36000000
                            10times Time:5484ms
    cutoff: 40000000
                            10times Time:5450ms
    cutoff: 44000000
                            10times Time:5493ms
                            10times Time:5487ms
    cutoff: 56000000
                            10times Time:5473ms
    cutoff: 60000000
                            10times Time:5453ms
    cutoff: 64000000
                            10times Time:5477ms
    cutoff: 72000000
                            10times Time:5472ms
    cutoff: 76000000
                            10times Time:5470ms
```

```
public static ForkJoinPool myPool = new ForkJoinPool(threadCount);
                 processArgs(args);
    Degree of parallelism: 4
                        10times Time:2009ms
    cutoff: 2000000
                        10times Time:1696ms
    cutoff: 4000000
                        10times Time:2695ms
<u>=</u>
   cutoff: 8000000
=
                          10times Time:2654ms
   cutoff: 10000000
   cutoff: 12000000
                            10times Time: 2653ms
    cutoff: 14000000
                            10times Time: 2648ms
    cutoff: 16000000
                            10times Time:2648ms
                            10times Time:2642ms
    cutoff: 22000000
                            10times Time:2653ms
    cutoff: 24000000
                            10times Time:2670ms
    cutoff: 26000000
                            10times Time: 2650ms
    cutoff: 28000000
                            10times Time: 2641ms
    cutoff: 34000000
                            10times Time:2656ms
    cutoff: 36000000
                            10times Time: 2655ms
    cutoff: 38000000
                            10times Time: 2656ms
```

```
public static ForkJoinPool myPool = new ForkJoinPool(threadCount);
             public static void main(String[] args) {
                 processArgs(args);
                int[] array = new int[2000000];
    Degree of parallelism: 4
    cutoff: 2000000
                       10times Time:839ms
cutoff: 4000000
                       10times Time:1256ms
= cutoff: 5000000
                       10times Time:1269ms
    cutoff: 6000000
                       10times Time:1304ms
    cutoff: 8000000
                       10times Time:1265ms
    cutoff: 11000000
                           10times Time:1261ms
    cutoff: 12000000
                          10times Time:1261ms
    cutoff: 13000000
                           10times Time:1268ms
    cutoff: 14000000
                           10times Time:1279ms
    cutoff: 15000000
                           10times Time:1271ms
    cutoff: 18000000
                           10times Time:1262ms
```

```
public static void main(String[] args) {
                    processArgs(args);
                    int[] array = new int[1000000];
Run: 🗐 Main
       Degree of parallelism: 4
       cutoff: 500000
       cutoff: 1000000
                           10times Time:392ms
                           10times Time:603ms
      cutoff: 2000000
                          10times Time:600ms
   =
      cutoff: 3000000
                          10times Time:601ms
                          10times Time:600ms
       cutoff: 3500000
==
       cutoff: 4000000
                          10times Time:604ms
       cutoff: 4500000
       cutoff: 5500000
                           10times Time:606ms
       cutoff: 6000000
                          10times Time:618ms
       cutoff: 6500000
       cutoff: 7000000
                           10times Time:607ms
       cutoff: 7500000
       cutoff: 9000000
                           10times Time:599ms
        cutoff: 9500000
                           10times Time:601ms
       cutoff: 10000000
                              10times Time:599ms
```

### **Sample Output for Conclusion 2:**

For array size: 1 Million, varying threads from 2 to 16

```
public class Main {
       public static int threadCount = 2;
             processArgs(args);
Degree of parallelism: 2
cutoff: 500000
                   10times Time:698ms
cutoff: 1000000
                    10times Time:395ms
                    10times Time:601ms
cutoff: 2500000
                   10times Time:602ms
cutoff: 3000000
                    10times Time:604ms
cutoff: 4500000
                    10times Time:601ms
cutoff: 5000000
                    10times Time:610ms
cutoff: 6000000
                   10times Time:611ms
cutoff: 7000000
                   10times Time:617ms
cutoff: 7500000
                    10times Time:614ms
cutoff: 8000000
cutoff: 8500000
                    10times Time:613ms
cutoff: 9000000
                    10times Time:606ms
cutoff: 9500000
                   10times Time:614ms
                       10times Time:608ms
```

```
© Main.java × © ParSort.java
            public static void main(String[] args) {
               processArgs(args);
               int[] array = new int[1000000];
                ArrayList<Long> timeList = new ArrayList<>();
                   ParSort.cutoff = 500000 * (j + 1);
   Degree of parallelism: 8
   cutoff: 500000 10times Time:511ms
   cutoff: 1000000
                     10times Time:393ms
   cutoff: 2000000
                      10times Time:599ms
   cutoff: 2500000
                      10times Time:602ms
-
   cutoff: 3000000
                      10times Time:599ms
   cutoff: 3500000
                      10times Time:605ms
   cutoff: 4000000 10times Time:602ms
   cutoff: 4500000 10times Time:603ms
   cutoff: 5000000 10times Time:599ms
   cutoff: 5500000 10times Time:603ms
   cutoff: 6000000
                      10times Time:600ms
                      10times Time:601ms
   cutoff: 6500000
   cutoff: 7000000
                      10times Time:602ms
   cutoff: 7500000
   cutoff: 8000000
                       10times Time:600ms
   cutoff: 8500000
                       10times Time:600ms
   cutoff: 9000000
                      10times Time:599ms
   cutoff: 9500000
                      10times Time:604ms
   cutoff: 10000000
                        10times Time:599ms
```

```
public static ForkJoinPool myPool = new ForkJoinPool(threadCount);
                public static void main(String[] args) {
                   processArgs(args);
                   ArrayList<Long> timeList = new ArrayList<>();
       Degree of parallelism: 16
                          10times Time:4792ms
       cutoff: 1600000
                          10times Time:4498ms
   ± cutoff: 3200000
                          10times Time:4533ms
   = cutoff: 4000000
                          10times Time:4507ms
   t cutoff: 4800000
                          10times Time:5327ms
       cutoff: 5600000
       cutoff: 6400000
                          10times Time:5196ms
==
       cutoff: 8000000
                          10times Time:5105ms
       cutoff: 8800000
                          10times Time:7171ms
       cutoff: 9600000
                          10times Time:7139ms
                           10times Time:7150ms
       cutoff: 11200000
                             10times Time:7135ms
       cutoff: 12800000
                            10times Time:7123ms
                            10times Time:7137ms
       cutoff: 14400000
                              10times Time:7161ms
                              10times Time:7145ms
       cutoff: 16000000
                             10times Time:7144ms
       Process finished with exit code 0
```

```
public static ForkJoinPool myPool = new ForkJoinPool(threadCount);
                processArgs(args);
                System.out.println("Degree of parallelism: " + myPool.getParallelism());
    Degree of parallelism: 4
    cutoff: 800000
                     10times Time:6720ms
   cutoff: 1600000
                       10times Time:5177ms
                    10times Time:5410ms
                       10times Time:5433ms
-
   cutoff: 4000000
                       10times Time:5512ms
                       10times Time:5162ms
   cutoff: 4800000
   cutoff: 5600000
                      10times Time:5205ms
                      10times Time:5168ms
   cutoff: 7200000
                       10times Time:5162ms
    cutoff: 8000000
                        10times Time:5223ms
    cutoff: 8800000
                       10times Time:7211ms
                       10times Time:7214ms
   cutoff: 9600000
   cutoff: 10400000
                           10times Time: 7268ms
   cutoff: 11200000
                           10times Time:7356ms
    cutoff: 12000000
                           10times Time:7208ms
   cutoff: 12800000
                           10times Time:7226ms
    cutoff: 14400000
                           10times Time:7203ms
    cutoff: 15200000
                           10times Time:7222ms
    cutoff: 16000000
                            10times Time: 7260ms
```

```
C ParSort.java
            public class Main {
             public static int threadCount = 2;
                public static ForkJoinPool myPool = new ForkJoinPool(threadCount);
                public static void main(String[] args) {
                    processArgs(args);
                    System.out.println("Degree of parallelism: " + myPool.getParallelism());
                    Random random = new Random();
                    int[] array = new int[16000000];
                    ArrayList<Long> timeList = new ArrayList<>();
                    for (int j = 0; j < 20; j++) {
                        ParSort.cutoff = 800000 * (j + 1);
tun: 🔳 Main
       Degree of parallelism: 2
       cutoff: 800000
                           10times Time:7373ms
       cutoff: 1600000
                           10times Time:5901ms
      cutoff: 2400000
                           10times Time: 6776ms
  <u>=</u>±
      cutoff: 3200000
                           10times Time:6710ms
       cutoff: 4000000
                           10times Time:6784ms
  =
       cutoff: 4800000
                           10times Time: 7585ms
       cutoff: 5600000
                           10times Time:7422ms
       cutoff: 6400000
                           10times Time:7445ms
       cutoff: 7200000
                           10times Time:7443ms
       cutoff: 8000000
                           10times Time: 7494ms
       cutoff: 8800000
                           10times Time:7273ms
       cutoff: 9600000
                           10times Time:7222ms
       cutoff: 10400000
                               10times Time: 7225ms
       cutoff: 11200000
                               10times Time:7225ms
       cutoff: 12000000
                               10times Time:7224ms
       cutoff: 12800000
                                10times Time:7198ms
       cutoff: 13600000
                               10times Time:7242ms
       cutoff: 14400000
                               10times Time:7239ms
                               10times Time:7211ms
       cutoff: 15200000
       cutoff: 16000000
                                10times Time:7250ms
```