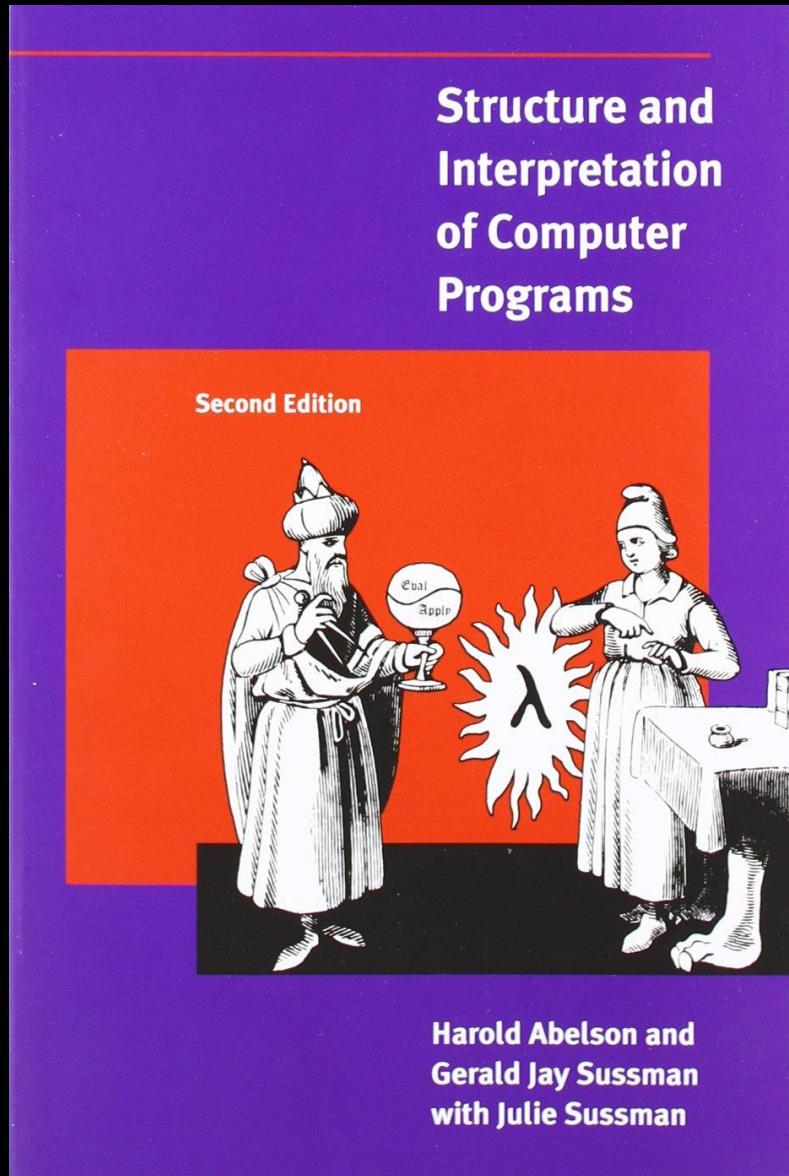


meetup



Structure and Interpretation of Computer Programs

Chapter 2.2 1/2

Before we start ...

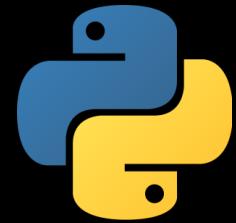


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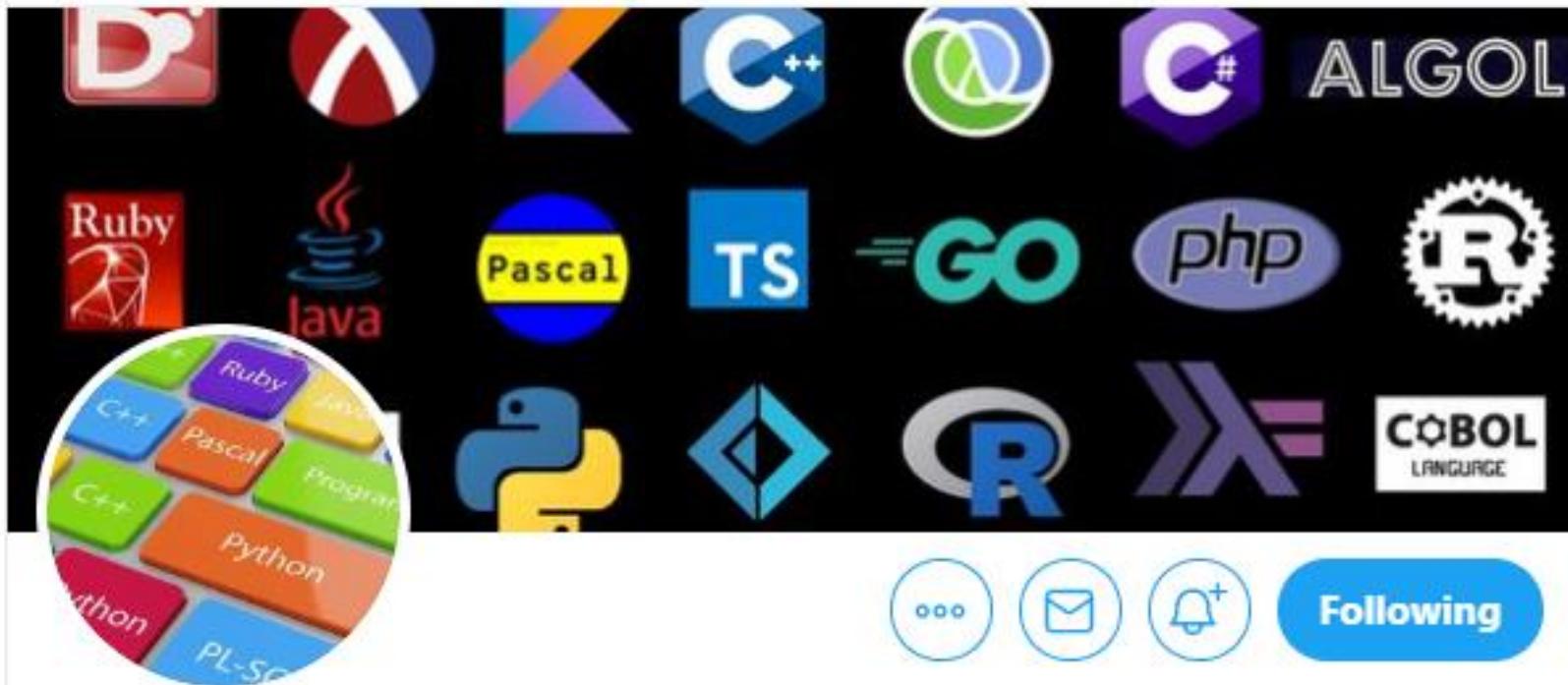
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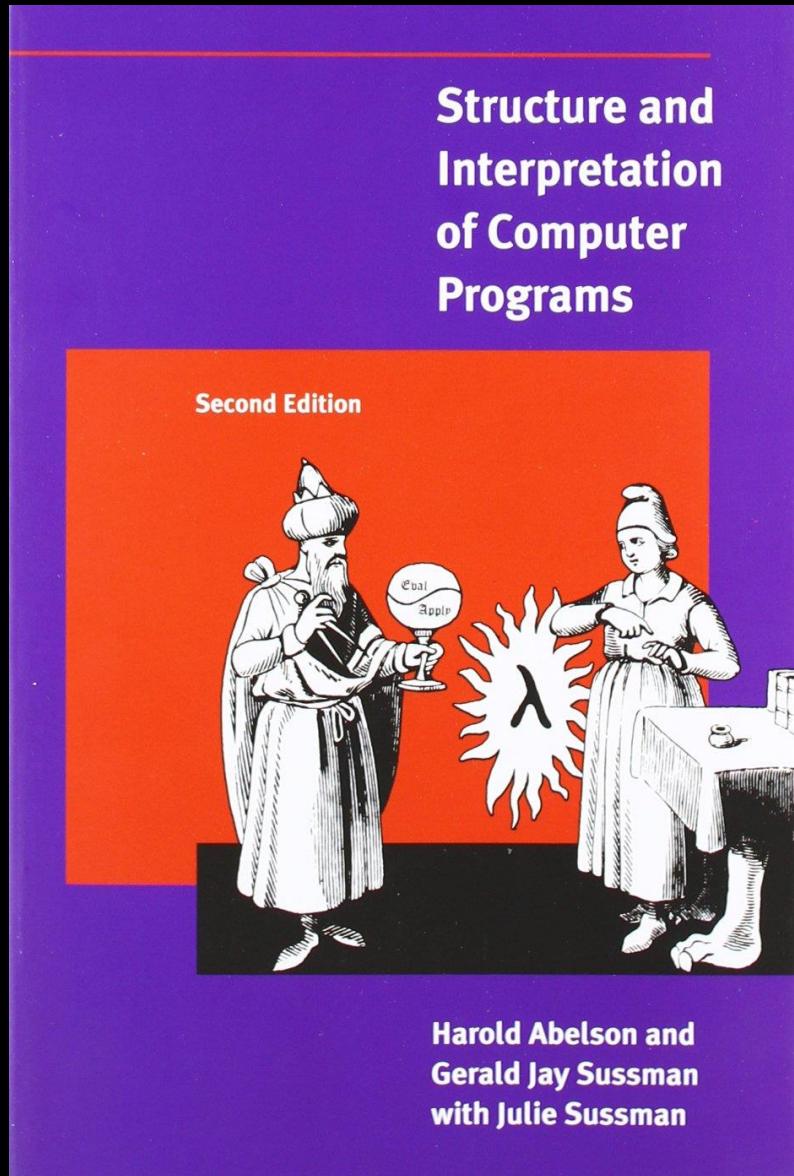
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Joined March 2020



Structure and Interpretation of Computer Programs

Chapter 2.2

1/2

2.2	Hierarchical Data and the Closure Property	132
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2.2.3	Sequences as Conventional Interfaces	154
2.2.4	Example: A Picture Language	172

The ability to create pairs whose elements are pairs is the essence of list structure's importance as a representational tool. We refer to this ability as the *closure property* of cons. In general, an operation for combining data objects satisfies the closure property if the results of combining things with that operation can themselves be combined using the same operation.⁶

We describe some conventional techniques for using pairs to represent sequences and trees, and we exhibit a graphics language that illustrates closure in a vivid way.⁷

BASIC



⁶The use of the word “closure” here comes from abstract algebra, where a set of elements is said to be closed under an operation if applying the operation to elements in the set produces an element that is again an element of the set. The Lisp community also (unfortunately) uses the word “closure” to describe a totally unrelated concept: A closure is an implementation technique for representing procedures with free variables. We do not use the word “closure” in this second sense in this book.

⁷The notion that a means of combination should satisfy closure is a straightforward idea. Unfortunately, the data combiners provided in many popular programming languages do not satisfy closure, or make closure cumbersome to exploit. In Fortran or Basic, one typically combines data elements by assembling them into arrays—but one cannot form arrays whose elements are themselves arrays. Pascal and C admit structures whose elements are structures. However, this requires that the programmer manipulate pointers explicitly, and adhere to the restriction that each field of a structure can contain only elements of a prespecified form. Unlike Lisp with its pairs, these languages have no built-in general-purpose glue that makes it easy to manipulate compound data in a uniform way. This limitation lies behind Alan Perlis’s comment in his foreword to this book: “In Pascal the plethora of declarable data structures induces a specialization within functions that inhibits and penalizes casual cooperation. It is better to have 100 functions operate on one data structure than to have 10 functions operate on 10 data structures.”



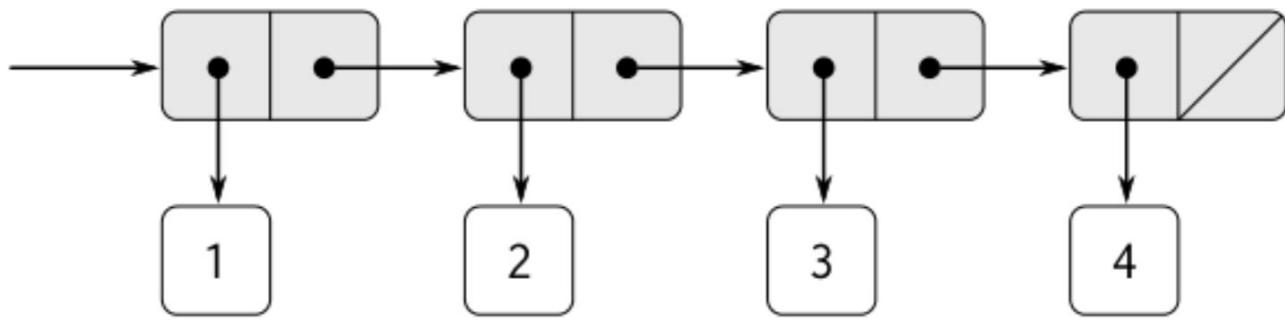
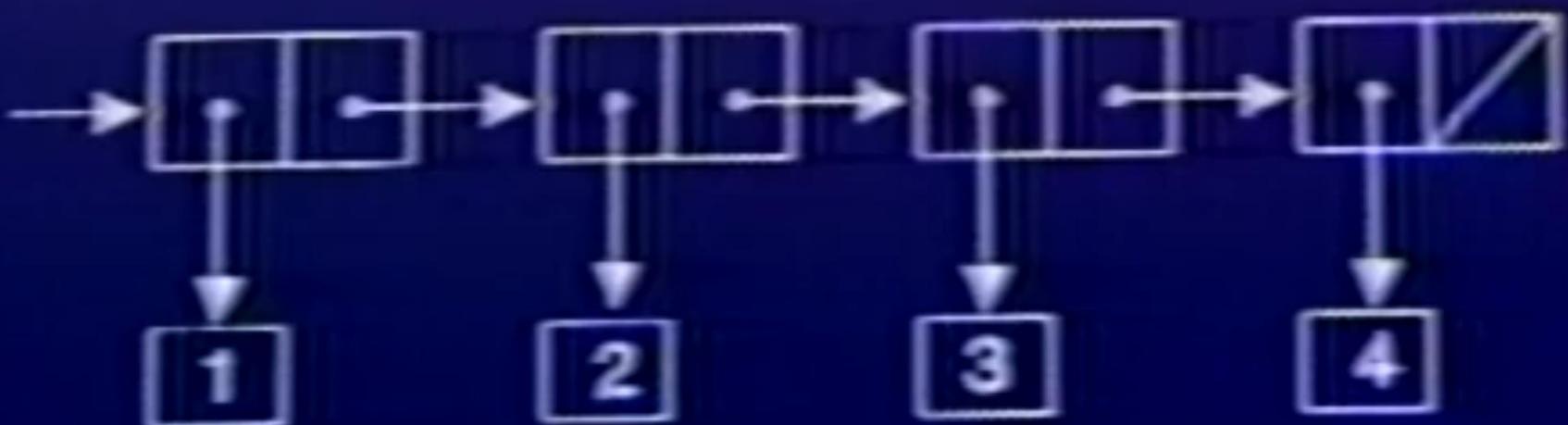


Figure 2.4: The sequence 1, 2, 3, 4 represented as a chain of pairs.

```
(cons 1  
      (cons 2  
              (cons 3  
                      (cons 4 nil))))
```



```
(cons 1  
      (cons 2  
              (cons 3  
                      (cons 4 nil)))))
```

⁹Since nested applications of car and cdr are cumbersome to write, Lisp dialects provide abbreviations for them—for instance,

`(cadr <arg>) = (car (cdr <arg>))`

The names of all such procedures start with c and end with r. Each a between them stands for a car operation and each d for a cdr operation, to be applied in the same order in which they appear in the name. The names car and cdr persist because simple combinations like `cadr` are pronounceable.



¹⁰It's remarkable how much energy in the standardization of Lisp dialects has been dissipated in arguments that are literally over nothing: Should `nil` be an ordinary name? Should the value of `nil` be a symbol? Should it be a list? Should it be a pair? In Scheme, `nil` is an ordinary name, which we use in this section as a variable whose value is the end-of-list marker (just as `true` is an ordinary variable that has a true value). Other dialects of Lisp, including Common Lisp, treat `nil` as a special symbol. The authors of this book, who have endured too many language standardization brawls, would like to avoid the entire issue. Once we have introduced quotation in [Section 2.3](#), we will denote the empty list as '`()`' and dispense with the variable `nil` entirely.

Exercise 2.17: Define a procedure `last-pair` that returns the list that contains only the last element of a given (nonempty) list:



;; Exercise 2.17

;; Solution 1

(**require** threading)

```
(define (last-pair lst)
  (~> lst
      reverse
      car))
```



;; Solution 2

```
(define (last-pair lst)
  (list-ref lst (- (length lst) 1)))
```



;; Solution 3

```
(define (last-pair lst)
  (if (null? (cdr lst))
      (car lst)
      (last-pair (cdr lst)))))
```

Exercise 2.18: Define a procedure `reverse` that takes a list as argument and returns a list of the same elements in reverse order:

```
(reverse (list 1 4 9 16 25))  
(25 16 9 4 1)
```



;; Exercise 2.18

```
(define (reverse lst)
  (define (iter lst acc)
    (if (null? lst)
        acc
        (iter (cdr lst) (cons (car lst) acc))))
  (iter lst '()))
```

Exercise 2.20:

```
(define (f x y . z) <body>)
```

Use this notation to write a procedure same-parity that takes one or more integers and returns a list of all the arguments that have the same even-odd parity as the first argument. For example,

```
(same-parity 1 2 3 4 5 6 7)
```

```
(1 3 5 7)
```

```
(same-parity 2 3 4 5 6 7)
```

```
(2 4 6)
```



```
(define (same-parity x . xs)
  (filter (λ (n) (= (remainder x 2)
                      (remainder n 2)))
          xs))

;; > (same-parity 1 1 2 3 4 5)
;; '(1 3 5)
;; > (same-parity 2 1 2 3 4 5)
;; '(2 4)
```

Exercise 2.21: The procedure square-list takes a list of numbers as argument and returns a list of the squares of those numbers.

```
(square-list (list 1 2 3 4))  
(1 4 9 16)
```

Here are two different definitions of square-list. Complete both of them by filling in the missing expressions:

```
(define (square-list items)  
  (if (null? items)  
      nil  
      (cons <??> <??>)))  
(define (square-list items)  
  (map <??> <??>))
```



;; Exercise 2.21

```
(define (sq x) (* x x))
```

```
(define (square-list items)
  (if (null? items)
      '()
      (cons (sq (car items))
            (square-list (cdr items))))))
```

```
(define (square-list2 items)
  (map sq items))
```

Exercise 2.23: The procedure `for-each` is similar to `map`. It takes as arguments a procedure and a list of elements. However, rather than forming a list of the results, `for-each` just applies the procedure to each of the elements in turn, from left to right. The values returned by applying the procedure to the elements are not used at all—`for-each` is used with procedures that perform an action, such as printing. For example,

```
(for-each (lambda (x)
                    (newline)
                    (display x))
                  (list 57 321 88))
```

57

321

88

The value returned by the call to `for-each` (not illustrated above) can be something arbitrary, such as `true`. Give an implementation of `for-each`.



;; Exercise 2.23

```
;; this fails :(  
(define (for-each proc lst)  
  (if (null? lst)  
      (λ (x) (x))  
      ((proc (car lst))  
       (for-each proc (cdr lst))))))
```



```
;; this prints a #t at the end :(  
(define (for-each proc lst)  
  (cond ((null? lst) #t)  
        (else (proc (car lst))  
              (for-each proc (cdr lst))))))
```



```
;; this works  
(define (for-each proc lst)  
  (cond ((null? (cdr lst)) (proc (car lst)))  
        (else (proc (car lst))  
              (for-each proc (cdr lst)))))
```

```
(define (for-each proc list)
  (cond ((null? list) "done")
        (else (proc (car list))
               (for-each proc
                         (cdr list))))))
```

DO IT TO THE
FIRST ELEMENT

DO IT TO THE
REST OF THE
LIST

2.2	Hierarchical Data and the Closure Property	132
✓ 2.2.1	Representing Sequences	134
→ 2.2.2	Hierarchical Structures	147
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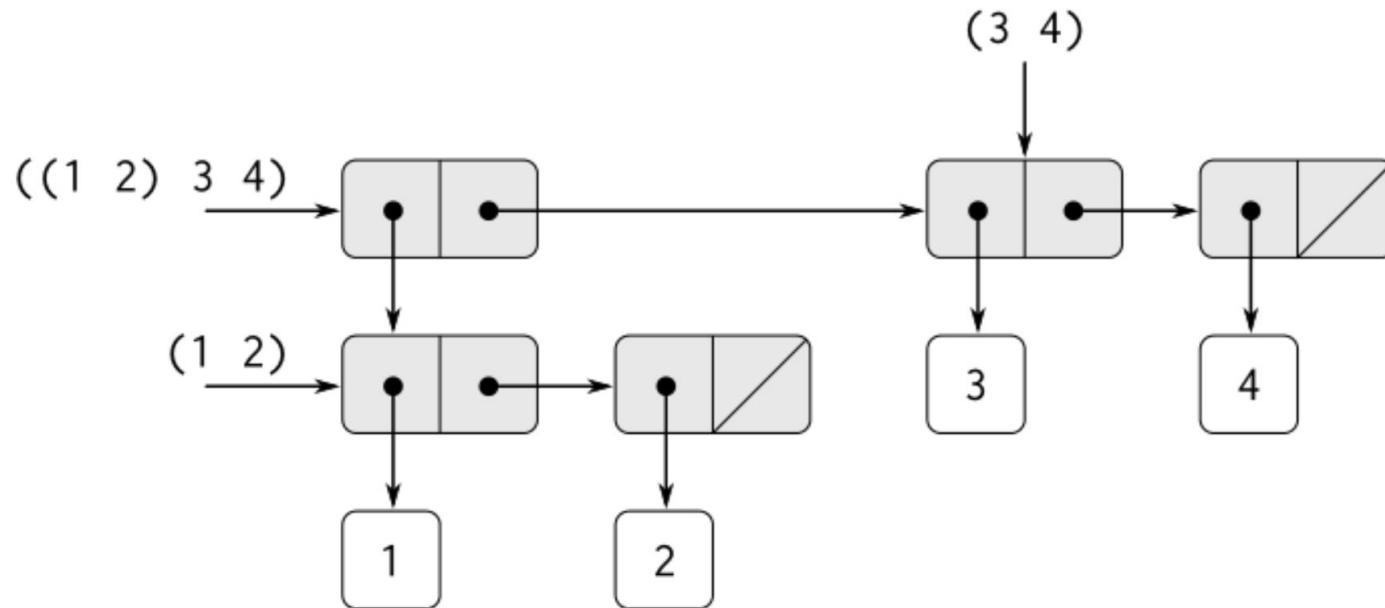


Figure 2.5: Structure formed by `(cons (list 1 2) (list 3 4))`.

`(cons (list 1 2) (list 3 4))`

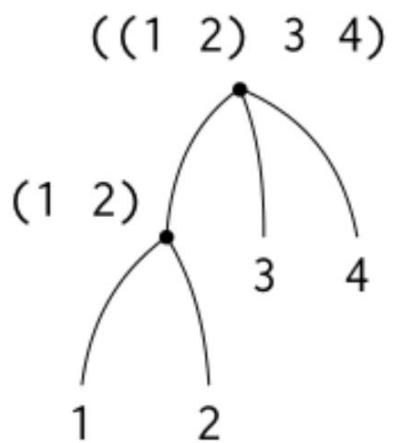


Figure 2.6: The list structure in [Figure 2.5](#) viewed as a tree.

Exercise 2.25: Give combinations of cars and cdrs that will pick 7 from each of the following lists:

(1 3 (5 7) 9)

((7))

(1 (2 (3 (4 (5 (6 7)))))))



```
> (define x '(1 3 (5 7) 9))  
> (car (cdaddr x))  
;; 7
```



```
> (define x '((7)))
> (caar x)
;; 7
```



```
(require threading)
```

```
> (define x '(1 (2 (3 (4 (5 (6 7))))))))
```

```
> (~> x
```

```
    cadadr
```

```
    cadadr
```

```
    cadadr)
```

```
;; 7
```

Exercise 2.27: Modify your reverse procedure of [Exercise 2.18](#) to produce a deep-reverse procedure that takes a list as argument and returns as its value the list with its elements reversed and with all sublists deep-reversed as well. For example,

```
(define x (list (list 1 2) (list 3 4)))  
x  
((1 2) (3 4))  
(reverse x)  
((3 4) (1 2))  
(deep-reverse x)  
((4 3) (2 1))
```



;; Exercise 2.27

```
(define (deep-reverse lst)
  (define (iter lst acc)
    (if (null? lst)
        acc
        (let ((fst (car lst)))
          (iter (cdr lst)
                (cons (if (list? fst)
                          (reverse fst)
                          fst)
                      acc))))))
  (iter lst '()))
```

Exercise 2.28: Write a procedure `fringe` that takes as argument a tree (represented as a list) and returns a list whose elements are all the leaves of the tree arranged in left-to-right order. For example,



;; Exercise 2.28

;; Solution 1

(**define** fringe flatten) ; :p



;; Solution 2

```
(define (fringe tree)
  (if (null? tree)
      '()
      (let ((x (car tree)))
        (append (if (list? x)
                    (fringe x)
                    (list x))
                (fringe (cdr tree)))))))
```



;; Example from book



;; Example from book

```
(define (scale-tree tree factor)
  (map (λ (sub-tree)
    (if (pair? sub-tree)
        (scale-tree sub-tree factor)
        (* sub-tree factor)))
  tree))
```

Exercise 2.30: Define a procedure square-tree analogous to the square-list procedure of [Exercise 2.21](#). That is, square-tree should behave as follows:

```
(square-tree
  (list 1
    (list 2 (list 3 4) 5)
    (list 6 7)))
(1 (4 (9 16) 25) (36 49))
```

Define square-tree both directly (i.e., without using any higher-order procedures) and also by using `map` and recursion.



;; Exercise 2.30 (direct)

```
(define (square-tree tree)
  (cond ((null? tree) '())
        ((not (pair? tree)) (sq tree))
        (else (cons (square-tree (car tree))
                    (square-tree (cdr tree)))))))
```



;; Exercise 2.30 (map)

```
(define (square-tree tree)
  (map (λ (sub-tree)
    (if (pair? sub-tree)
        (square-tree sub-tree)
        (sq sub-tree)))
  tree))
```

Exercise 2.31: Abstract your answer to [Exercise 2.30](#) to produce a procedure `tree-map` with the property that `square-tree` could be defined as

```
(define (square-tree tree) (tree-map square tree))
```



;; Exercise 2.31

```
(define (tree-map tree proc)
```

```
  (map (λ (sub-tree)
```

```
        (if (pair? sub-tree)
```

```
            (tree-map sub-tree proc)
```

```
            (proc sub-tree)))
```

```
  tree))
```

```
(define (square-tree tree) (tree-map tree sq))
```

```
(define (scale-tree tree factor) (tree-map tree (λ (x) (* x factor))))
```

Structure & Interpretation of Computer Programs

Harold
Abelson

Gerald Jay
Sussman



“**cdr**-ing down the list”

Hal Abelson

Lecture 3A, SICP

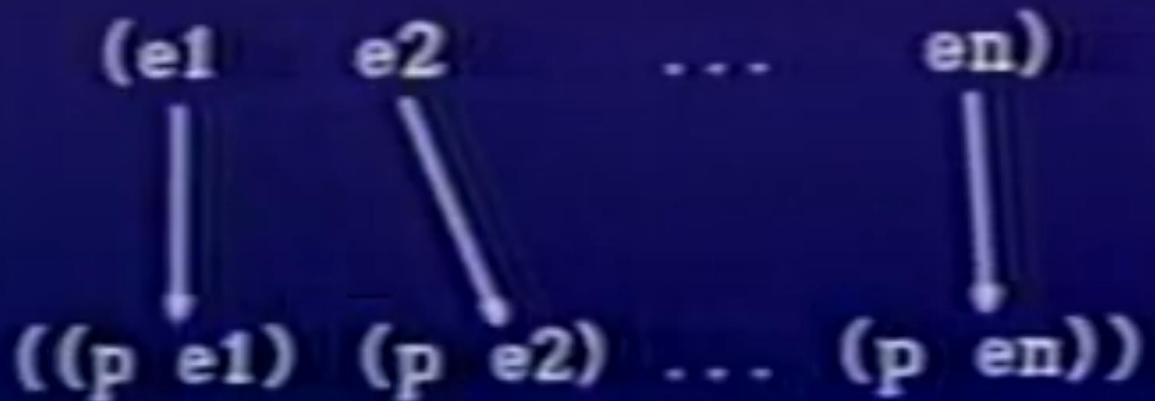
CDR-ing down a list

```
(define (scale-list s l)
  (if (null? l)
      nil
      (cons ((* (car l) s)
              ((scale-list s (cdr l)))))))
```



FIRST ELEMENT
OF SCALED LIST

REST OF SCALED
LIST



```
(define (map p l)
  (if (null? l)
      nil
      (cons (p (car l))
             (map p (cdr l))))))
```

APPLY P TO
FIRST ELEMENT

MAP DOWN THE
REST OF THE
LIST

“once you start thinking in terms of **map** ...
you stop thinking about the particular
control structure or order.

This is a **very, very important idea** ...

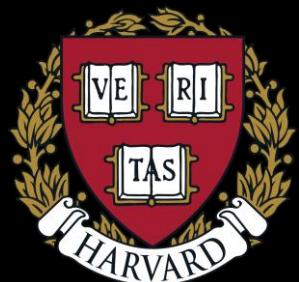
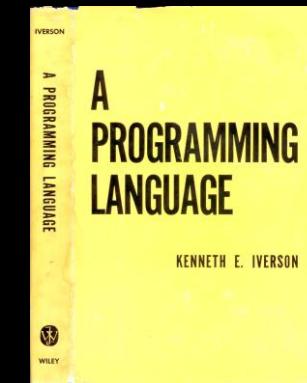
Hal Abelson
Lecture 3A, SICP

“... it really comes out of **APL**. It is the
really important idea in **APL** - that you stop
thinking about control structures and you start
thinking about **operations on aggregates**.

Hal Abelson
Lecture 3A, SICP

Who is Kenneth Iverson?

- Creator of APL
- Co-creator of J
- Won the 1979 Turing Award
- Author or 1962 “A Programming Language”
- Bachelors at Queens, PhD at Harvard where he developed Iverson Notation
- Worked at IBM in 70s, 80s then left to IPSA
- Bill Gates visited IPSA in the early 80s to inquire about the possibility of APL on PC



LANGUAGE HISTORY CHART

First letter of each name has been aligned with the approximate date on which work began.

THIS TYPE STYLE indicates languages of major importance, because of their wide usage or technical significance.

THIS TYPE STYLE indicates languages of moderate importance.

THIS TYPE STYLE is used for all other languages.

Parentheses were used to indicate alternate names, or the later addition of the sequence number "1."

— indicates that the second language is a direct extension of the first

— indicates that the second language is an approximate extension of the first, i.e., very similar to the first, but not completely upward compatible

— indicates strong influence; sometimes the second language is "like, or in the style of" the first

— indicates an approximate subset

Each of the following marks is associated with the language above or to its left:

- indicates preliminary or informal specifications or manual

- indicates a public manual, or formal publication via technical paper, or public presentation

- ▲ release for usage outside development group

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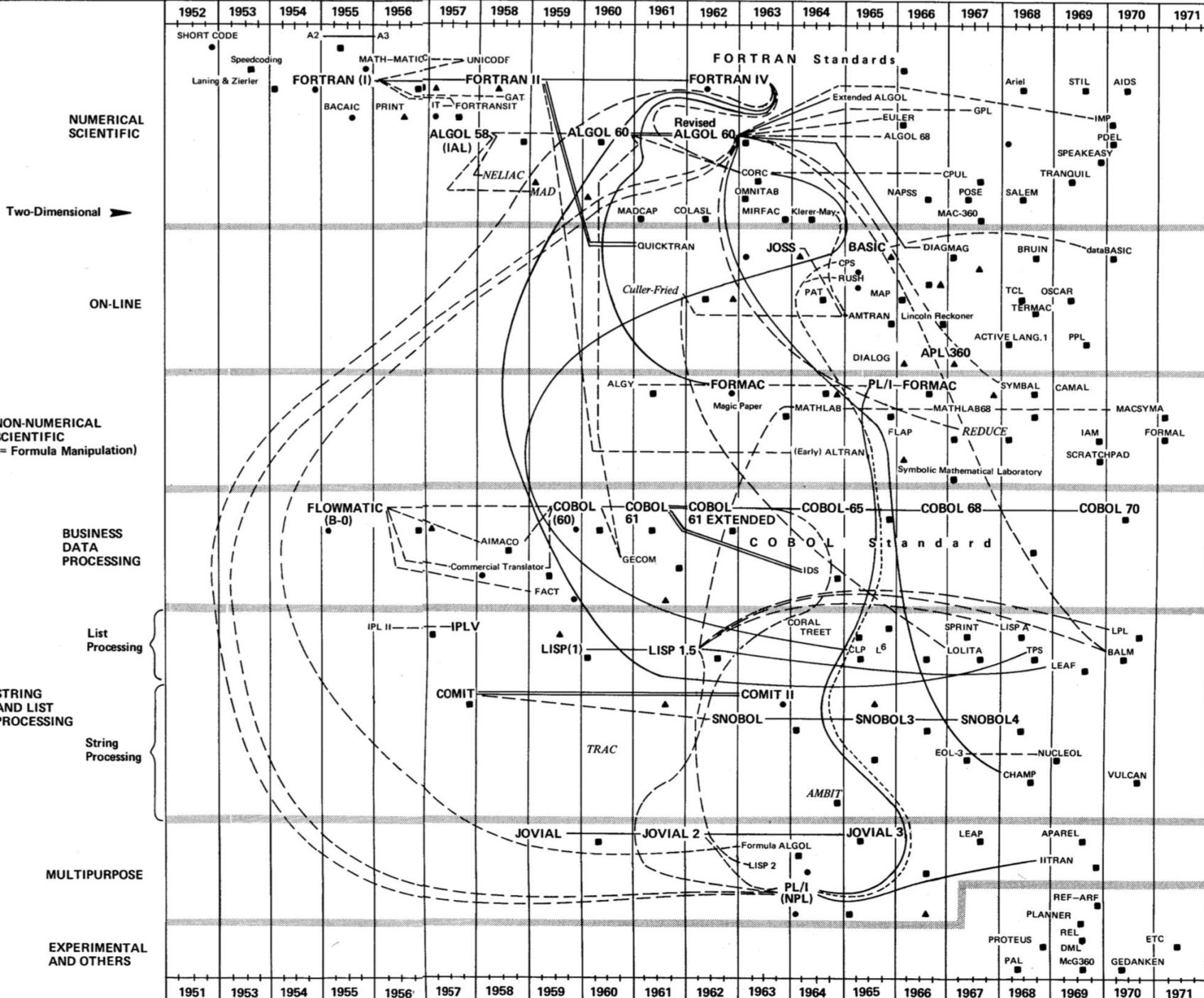
The information for languages in 1971 is based solely on those listed in "Roster of Programming Languages-1971," Computers and Automation, Vol. 20, No. 6B (June 1971), pp. 6-13.

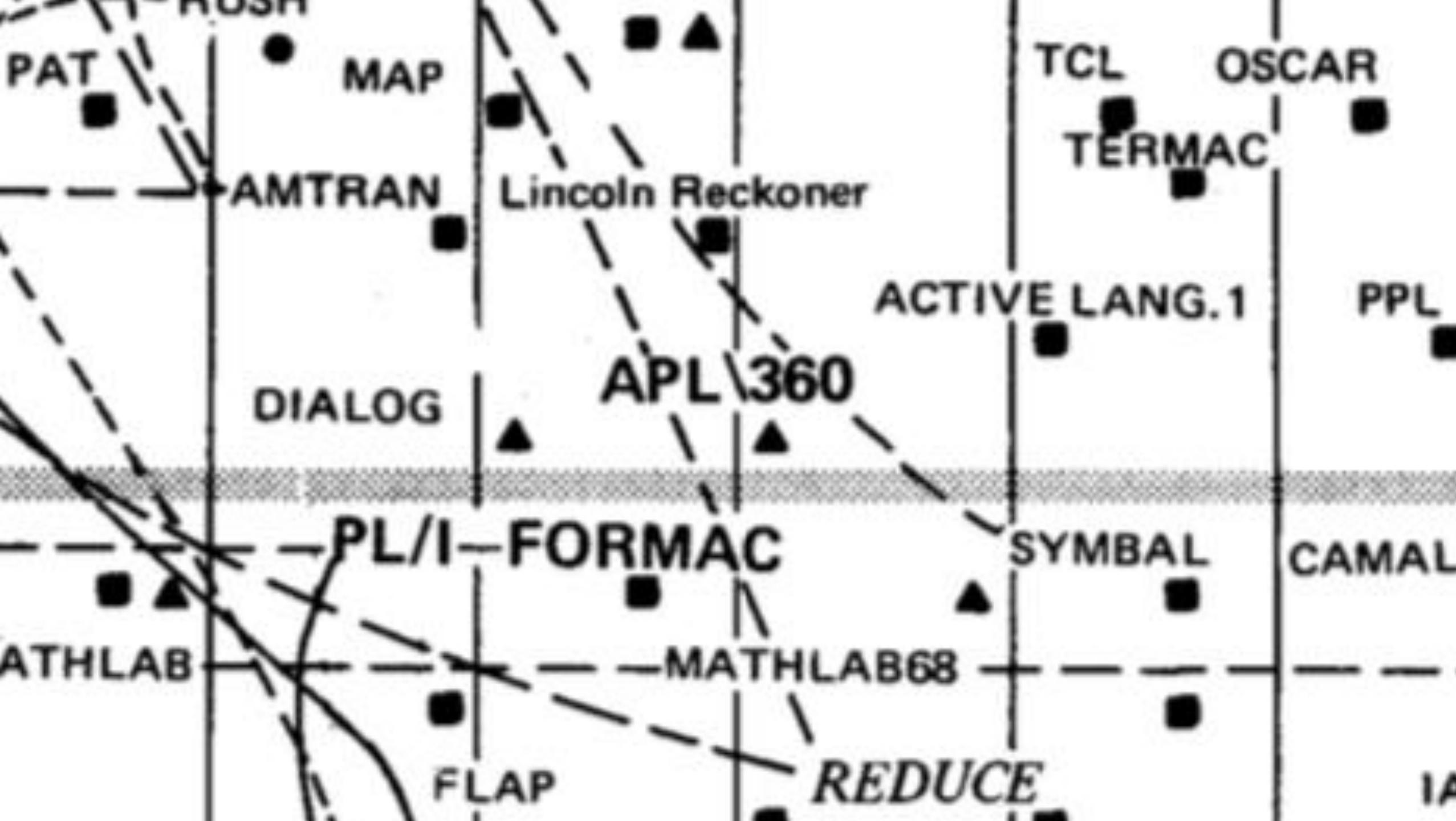
In most cases, dialects with differing names have been omitted. This has the unfortunate effect of appearing to minimize the importance of some languages which spawned numerous versions under differing names (e.g., JOSS).

Languages for specialized application areas (e.g., simulation, machine tool control, civil engineering, systems programming) have not been included because of space considerations. This explains the absence of such obvious languages as APT, GPSS, SIMSCRIPT, COGO, BLISS.

Acknowledgment: The idea for such a chart in such a format came from the one by Christopher J. Shaw entitled "Milestones in Computer Programming" and included with the [ACM Los Angeles Chapter] SIGPLAN notices, February 1965.

"Programming Languages: History and Future" by Jean E. Sammet Communications of the ACM, Vol. 15, July 1972 © 1972, Association for Computing Machinery, Inc.





LANGUAGE HISTORY CHART

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THIS TYPE STYLE indicates languages of major importance, because of their wide usage or technical significance.

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subset

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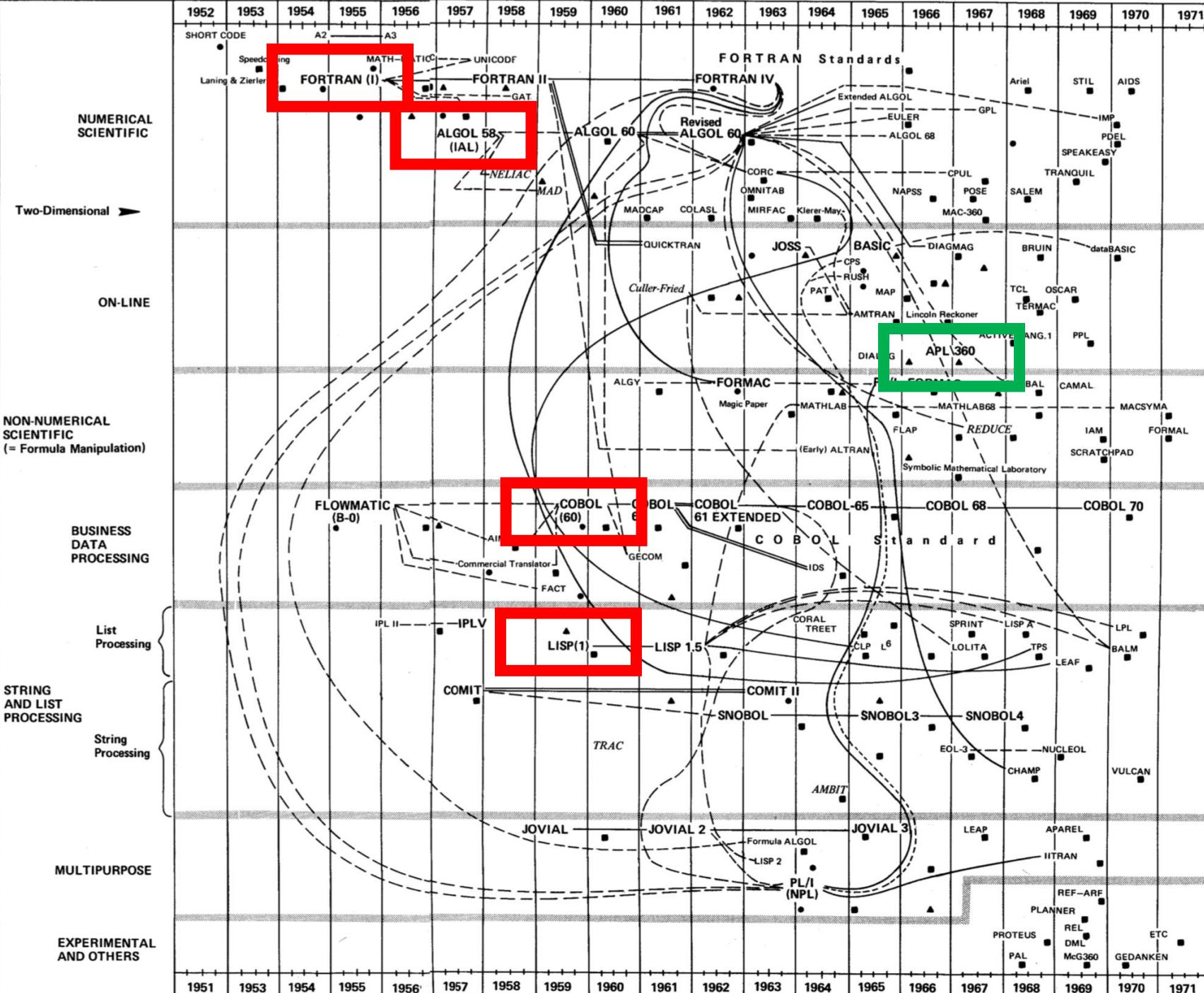
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AGENDA

- Background
- FORTRAN (1957)
- LISP (1959)
- ALGOL (1960)
- COBOL (1960)
-

"All of this has happened before, and it will all happen again." by Mark Allen

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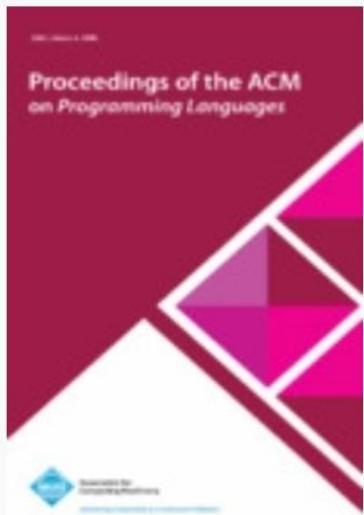
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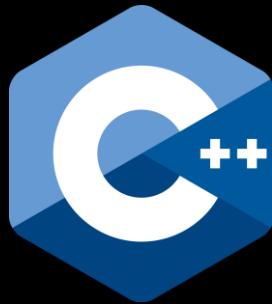
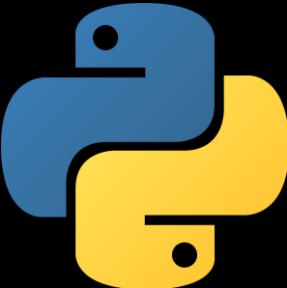
APL Since 1978

ROGER K.W. HUI, Dyalog Limited, Canada

MORTEN J. KROMBERG, Dyalog Limited, United Kingdom

Shepherd: Guy L. Steele Jr., Oracle Labs, USA

The Evolution of APL, the HOPL I paper by Falkoff and Iverson on APL, recounted the fundamental design principles which shaped the implementation of the APL language in 1966, and the early uses and other influences which shaped its first decade of enhancements.



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