

① Find the left most derivation and Right most derivation for the given grammars.

$$S \rightarrow 0B \mid 1A$$

$$A \rightarrow 0 \mid 0S \mid 1AA$$

$$B \rightarrow 1 \mid 1S \mid 0BB \quad W: 00110101.$$

Sol: Given $S \rightarrow 0B \mid 1A$

$$A \rightarrow 0 \mid 0S \mid 1AA$$

$$B \rightarrow 1 \mid 1S \mid 0BB \quad W: 00110101$$

Left derivation

$$S \rightarrow 0B$$

$$\rightarrow 00BB$$

$$\rightarrow 001SB$$

$$\rightarrow 0011AB$$

$$\rightarrow 001101AB$$

$$\rightarrow 0011010B$$

$$\rightarrow 0011010B$$

Right most derivation

$$S \rightarrow 0B$$

$$\rightarrow 00BB$$

$$\rightarrow 00B1$$

$$\rightarrow 001S1$$

$$\rightarrow 0011A1$$

$$\rightarrow 00110S1$$

$$\rightarrow 001101A1$$

$$\rightarrow 00110101$$

② Check wheathes the following grammars is am biguous or not

$$S \rightarrow aSb \mid aA'b \mid ab$$

$$A \rightarrow aA \mid a$$

$$B \rightarrow Bb \mid b.$$

Sol: $S \rightarrow aSb \mid aAb \mid aBb.$

$$A \rightarrow aA \mid a$$

$$B \rightarrow Bb \mid b.$$

lets take a string
 $W = aabbb$

Reduction :- $S \rightarrow \text{asb}$
derivation.

$\rightarrow aabb$

$\rightarrow aabbb$.

~~A here are no more than~~

A here are no more than derivation for the string,
the grammar is not ambiguous

3) minimise the given CFG.

sol: $S \rightarrow A|oc$
 $A \rightarrow B|o1|10$
 $C \rightarrow E|CD$

Given CFG

$S \rightarrow A|oc$

$A \rightarrow B|o1|10$

$C \rightarrow E|CA$

minimisation:-

$A \rightarrow B|o1|10 \rightarrow$ eliminates $A \rightarrow B$ as it is a unit production.

$S \rightarrow A|oc \rightarrow$ replace A with its production.

$C \rightarrow E|CD$ eliminate E production.

minimised CFG:

$S \rightarrow o1|10|oc$

$A \rightarrow o1|10$

$C \rightarrow CD$