

$$\omega_d = \omega_0 \sqrt{1 - \zeta^2}$$

$$f = A_1 e^{-\zeta \omega_d t_1} \sin(\omega_d t + \omega_d t_1)$$

$$g = A_2 e^{-\zeta \omega_d t_2} \sin(\omega_d t + \omega_d t_2)$$

$$f = A_1 e^{-\zeta \omega_d t_1} \sin(\omega_d t) \cos(\omega_d t_1) + A_1 e^{-\zeta \omega_d t_1} \cos(\omega_d t) \sin(\omega_d t_1)$$

$$g = A_2 e^{-\zeta \omega_d t_2} \sin(\omega_d t) \cos(\omega_d t_2) + A_2 e^{-\zeta \omega_d t_2} \cos(\omega_d t) \sin(\omega_d t_2)$$

$$u_1 = A_1 e^{-\zeta \omega_d t_1} \cos(\omega_d t_1)$$

$$v_1 = A_1 e^{-\zeta \omega_d t_1} \sin(\omega_d t_1)$$

$$u_2 = A_2 e^{-\zeta \omega_d t_2} \cos(\omega_d t_2)$$

$$v_2 = A_2 e^{-\zeta \omega_d t_2} \sin(\omega_d t_2)$$

$$u_1 \sin(\omega_d t) + v_1 \cos(\omega_d t) + u_2 \sin(\omega_d t) + v_2 \cos(\omega_d t) = (u_1 + u_2) \sin(\omega_d t) + (v_1 + v_2) \cos(\omega_d t)$$

$$A_{amp} = \sqrt{(u_1 + u_2)^2 + (v_1 + v_2)^2}$$

$$A_{amp} = \sqrt{\left(\sum_{i=1}^n u_i\right)^2 + \left(\sum_{i=1}^n v_i\right)^2}$$