

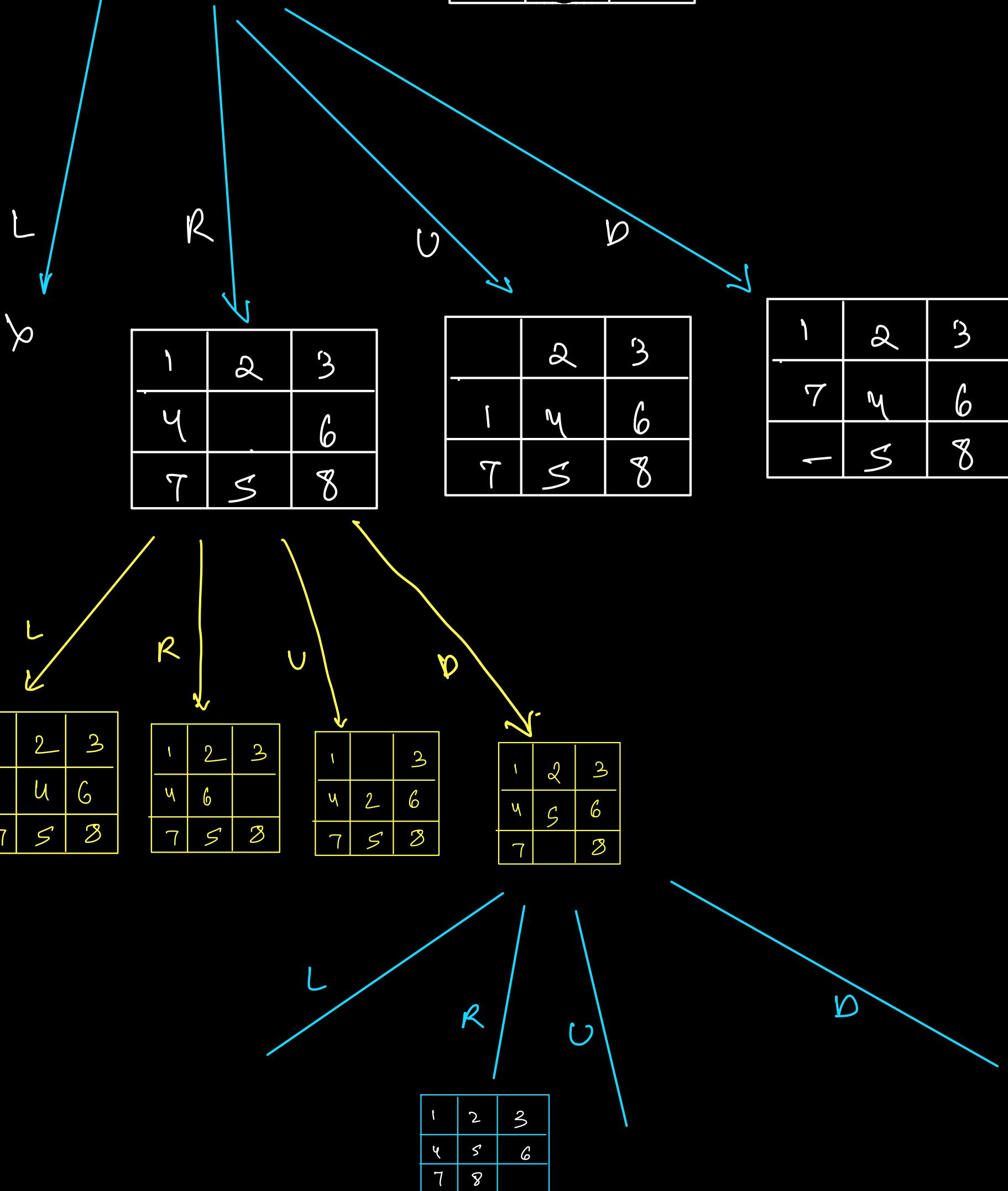
8 Puzzle Problem: { Without Heuristic }

Start State

1	2	3
4		6
7	5	8

1	2	3
4	5	6
7	8	

Goal state



Heuristic in AI (Rule of Thumb): {what, why, how?}.

Search Space Possible	IS puzzle problem	24 puzzle prob.
8 puzzle problem 3^{20}	10^{13}	10^{24}

(Non polynomial) \rightarrow Polynomial.

Exponential time.

- # How:
1. Euclidean Distance
 2. Manhattan Distance
 3. Misplaced tiles

A Heuristic funcⁿ is a technique used to solve problems quickly by making assumptions / guesses. It helps to find a quick solⁿ without exploring every possibility. In maths, heuristics are used to simplify problems like assuming values to solve ques faster. Ex: \rightarrow Assuming $a = 100$ for cost - price calculations.

Heuristics Values in A*:

Heuristics help make uninformed decisions by providing a value that indicates how close a particular state is to be goal-state. Heuristics values are used to guide such process towards the most promising space in a search space.

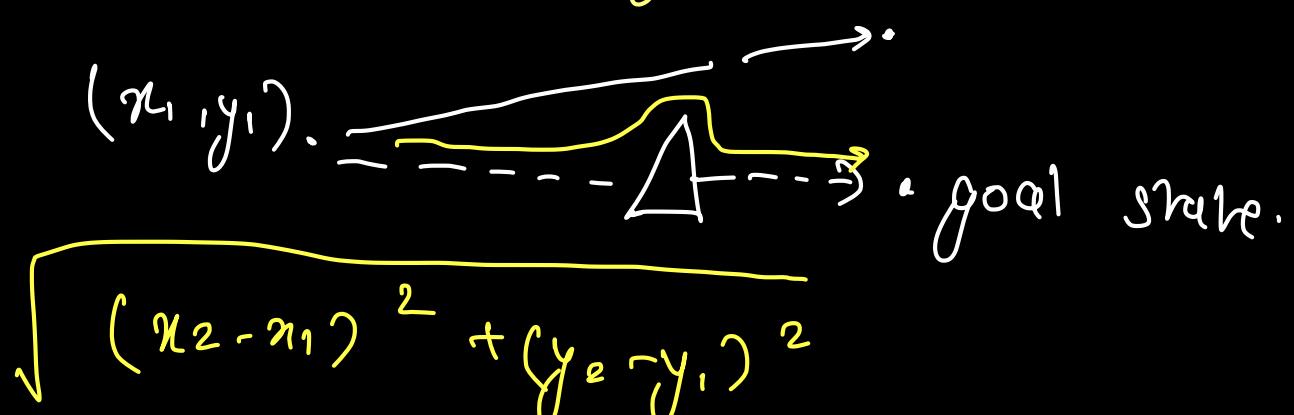
Why Do we use Heuristics:

1. Unlike uninformed search (blind search), Heuristics provide a guide to solve the problem more quickly.
2. It gives the guarantee to find out the good solⁿ.
3. Real life examples, in navigation Heuristics can guide you towards the shortest route without having to explore all possible paths
4. It converts non-polynomial into polynomial time.

How do we calculate Heuristic values:

* Several methods are used to calculate Heuristic values:

1. Euclidean Distance (Straight line Distance)



$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

used when movement is allowed in any dirⁿ, ex: mps.

2. Manhattan Distance:

8 puzzle problem.

$\mathcal{S} =$

1	3	2
6	5	4
8	7	

$\mathcal{G} =$

1	2	3
4	5	6
7	8	

Measures the total vertical and horizontal distance.
Used in problems where movement is restricted to grid like paths.

3. Misplaced tiles

Calculate the heuristic values \rightarrow

$\mathcal{S} =$

1	3	2
6	5	4
8	7	

$\mathcal{G} =$

1	2	3
4	5	6
7	8	

$$\Rightarrow 0 + 1 + 1 + 2 + 0 + 2 + 2 \\ + 0 = \frac{8}{\downarrow}$$

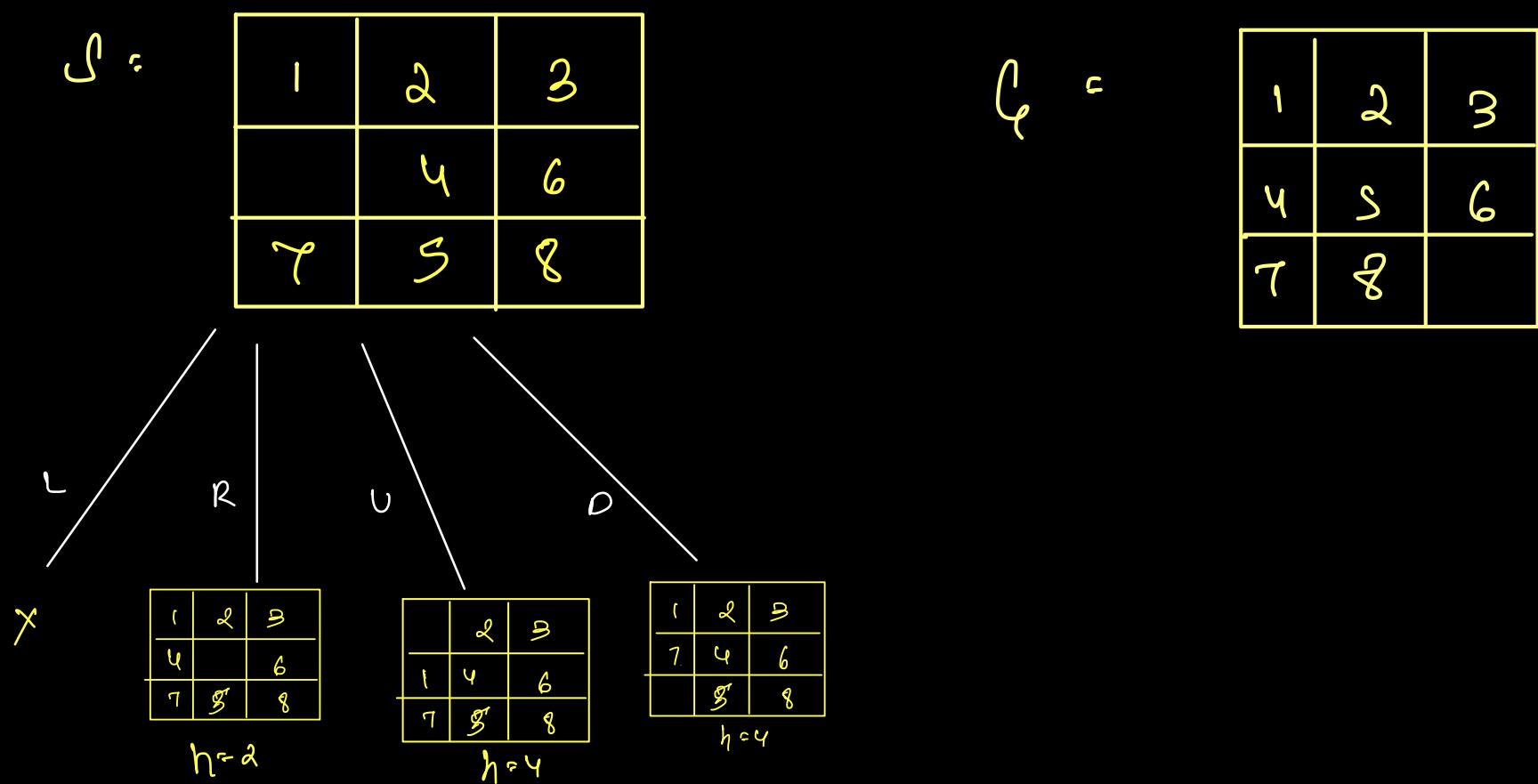
heuristic value.

* Counts how many tiles are in wrong position compared to goal state. Example given above.

4. Limitations of Heuristic:

- Heuristics guarantee a good solⁿ but they do not always guarantee an optimal solⁿ. For ex, in some cases the best heuristic path might not be optimal one. Eg, obstacles like mountain might make the straight line path in physiol.

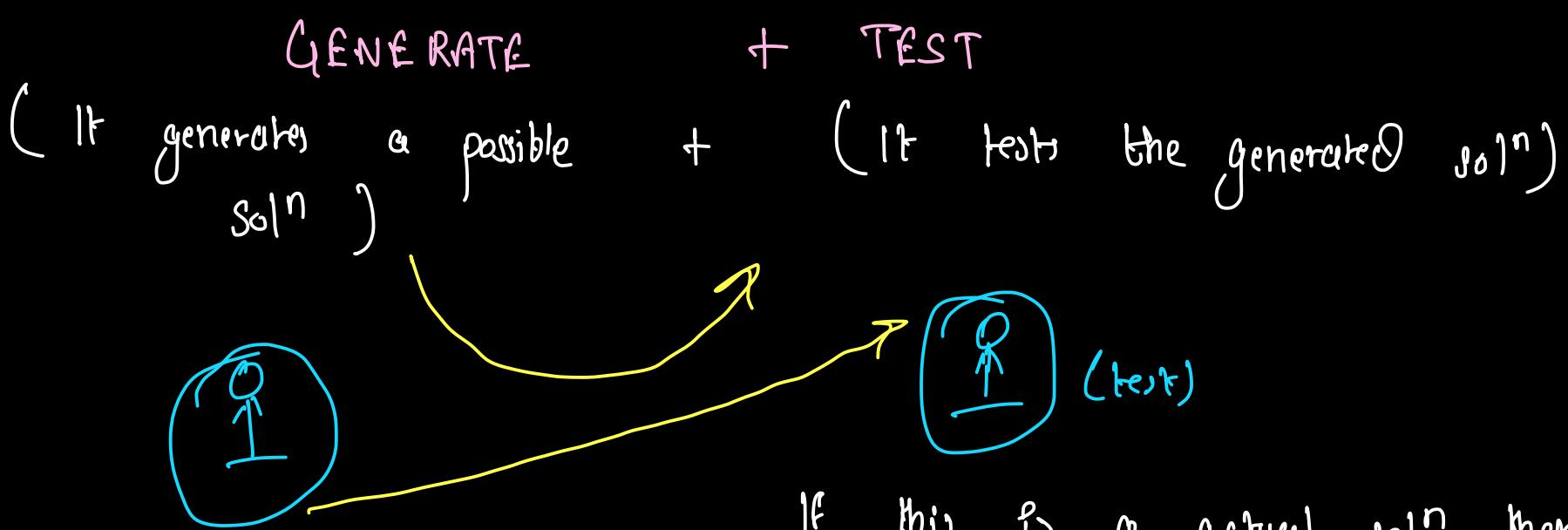
8 Puzzle Problem with Heuristic:



Difference b/w Blind Search and Heuristic Search in terms of T.C:

- * Blind Search explores four possible states without any Heuristic guidance leading to higher T.C. $O(b^d)$ (where $b \rightarrow$ branch factor, Depth).
- * Heuristic focuses on most promising state i.e. the state with the lowest heuristic value reaching 0 the search space and improving efficiency.

Generate and Test Algorithm: {Informed Search, DFS with backtracking}



If this is a actual soln then it quits otherwise generate a next possible soln.

- It is the simplest method than any other methods.

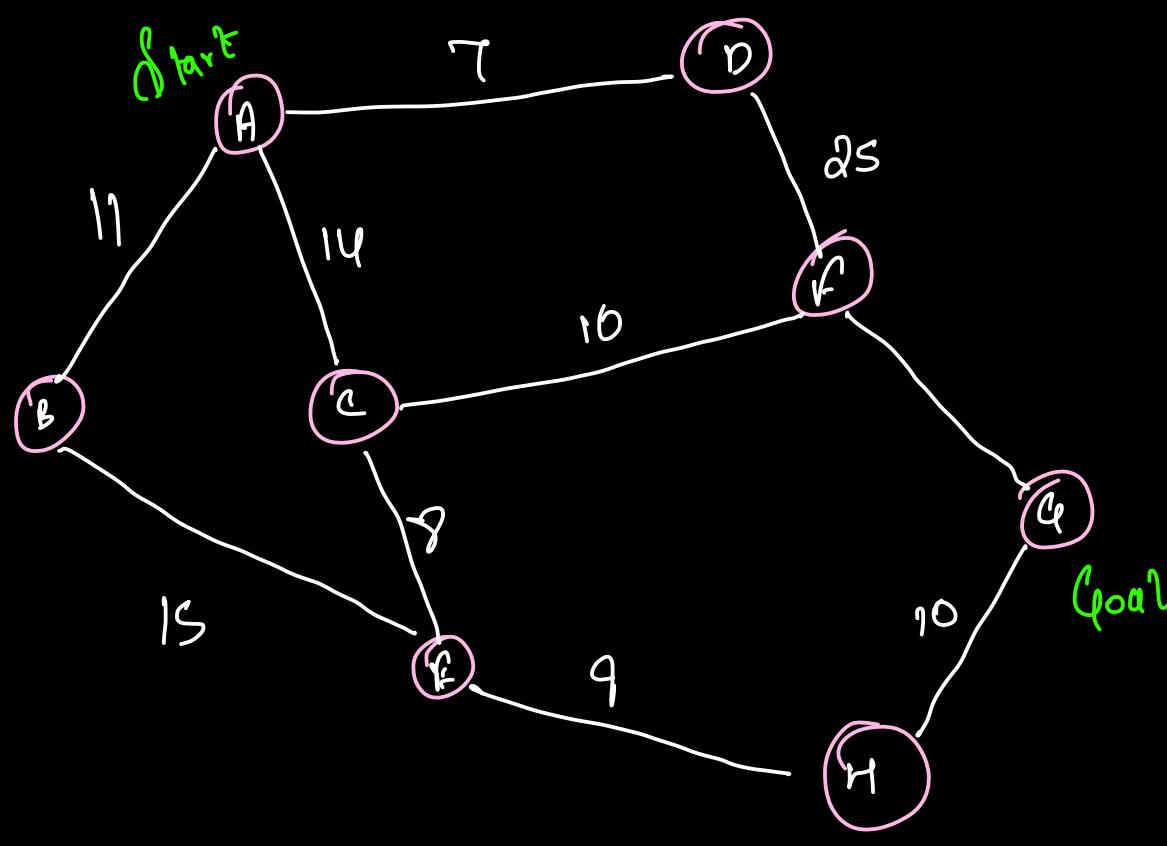
Algo:

1. Generate a possible solⁿ.
2. Test to see if it's an actual solⁿ.
3. If a solⁿ is found then it quits otherwise go to step 1.

Properties of Good generates:

1. Complete. (It gives the definite solⁿ)
2. Non-redundant
3. Informed search

Best first search Algo: {Informed Search, Heuristic}



$$\begin{aligned} A \rightarrow G &= 40 \\ B \rightarrow G &= 32 \\ C \rightarrow G &= 25 \\ D \rightarrow G &= 35 \\ E \rightarrow G &= 19 \\ F \rightarrow G &= 17 \\ H \rightarrow G &= 10 \\ G \rightarrow G &= 0 \end{aligned} \quad \left. \begin{array}{l} \\ \\ \\ \\ \\ \\ \\ \end{array} \right\} f$$

Algorithm:

let 'OPEN' be a priority queue containing initial state.

loop:

if OPEN is empty then return false

Node \leftarrow Remove \leftarrow first(Open)

If Node is a goal then return the path from initial to Node
else generate all successors of Node & put the newly generated
Node into OPEN according to their f values (heuristic value)

END LOOP.

Hill Climbing Algo:

- It is based on the greedy method.
- Best first search algo. greedy for the heuristic value.
- It has the guarantee for giving a good solⁿ but it may or may not give the optimal solⁿ.

Complexity:-

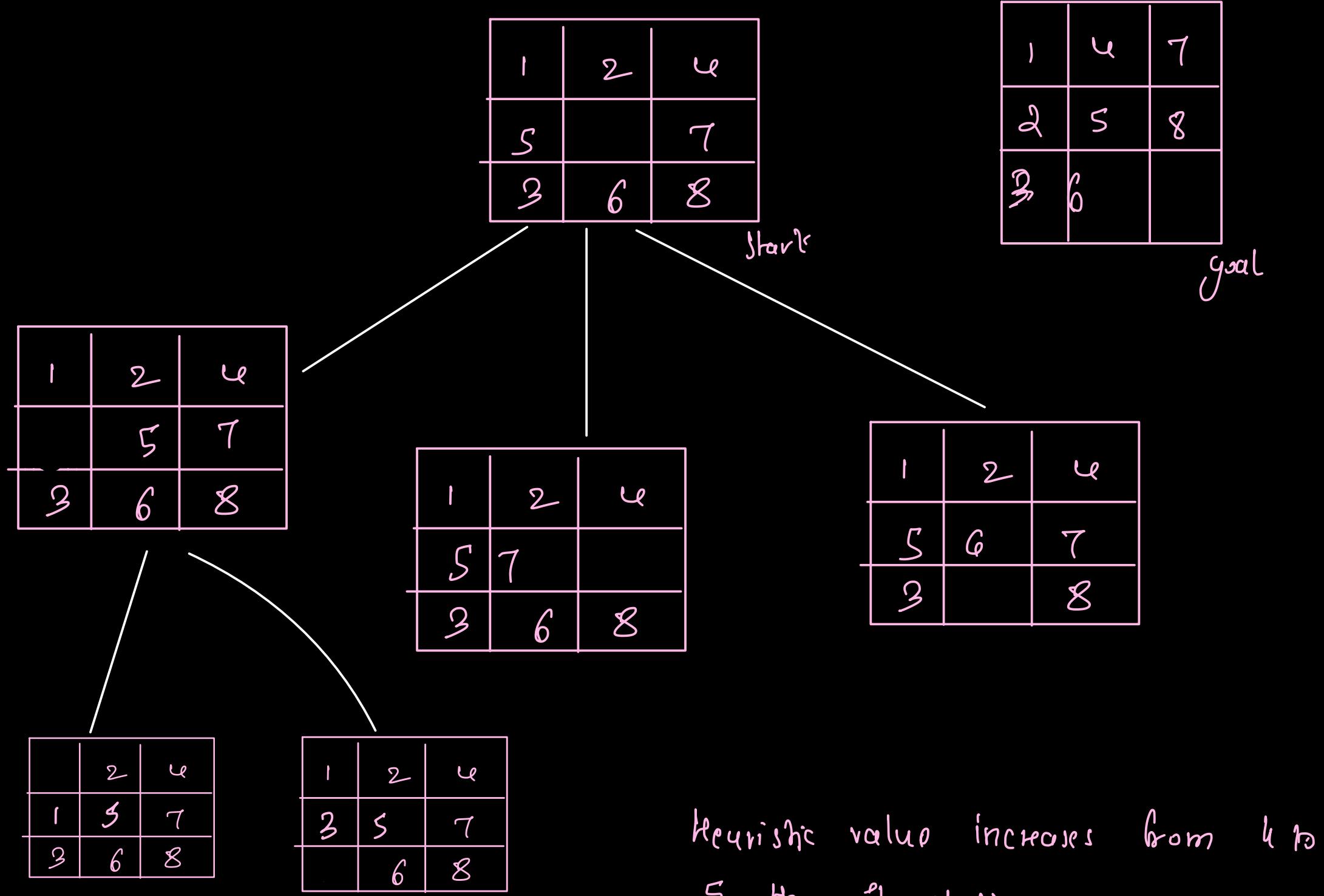
- Best Case or Avg Case or Nrm Case. \rightarrow It's time and space complexity performs much better than uninformed search algo.
- Worst Case \rightarrow It's same as uninformed search algo.

Hill Climb Algorithm:

1. Local Search Algorithm
2. Greedy Approach [Best Search]
3. No back track

* Algorithm:

1. Evaluate the initial state
2. Loop until a solⁿ is found or there are no operators left - delete and apply a new approach.
3. Evaluate the new state, if goal then quit.
4. If better than current stage then it is a new current stage.
5. It is blindfolded



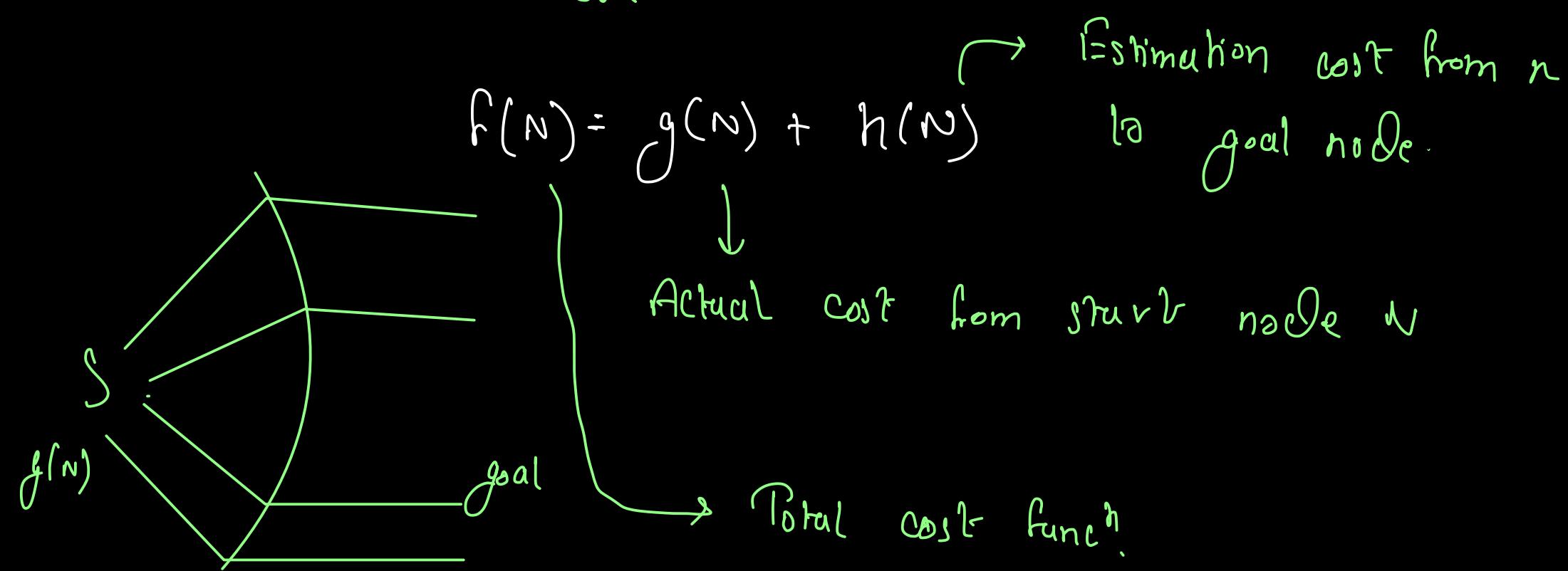
heuristic value increases from 4 to 5 then it stops.

Problems:

- 1. local minimum - Algo gets stuck at a peak which is not globally optimal. It thinks it has achieved a max value.
- All neighbor states have the same heuristic value.
- No clear dirⁿ to more algo hals.
- Higher value states exist but lies directly or indirectly
- Hill climbing can't reach it bcz if only explores one dirⁿ

A* Algorithm [Informed Searching]:

* → Admissible



$$f(A) = g(A) + h(A)$$

- A* Algorithm is a part of the Heuristic Search Techniques and informed search technique.
- Informed search means we already have some knowledge about the problem domain such as the goal state or how to reach it. This knowledge is called the heuristic value.
- It gives the guarantee for giving an optimal soln when it comes under the estimate.

Example:

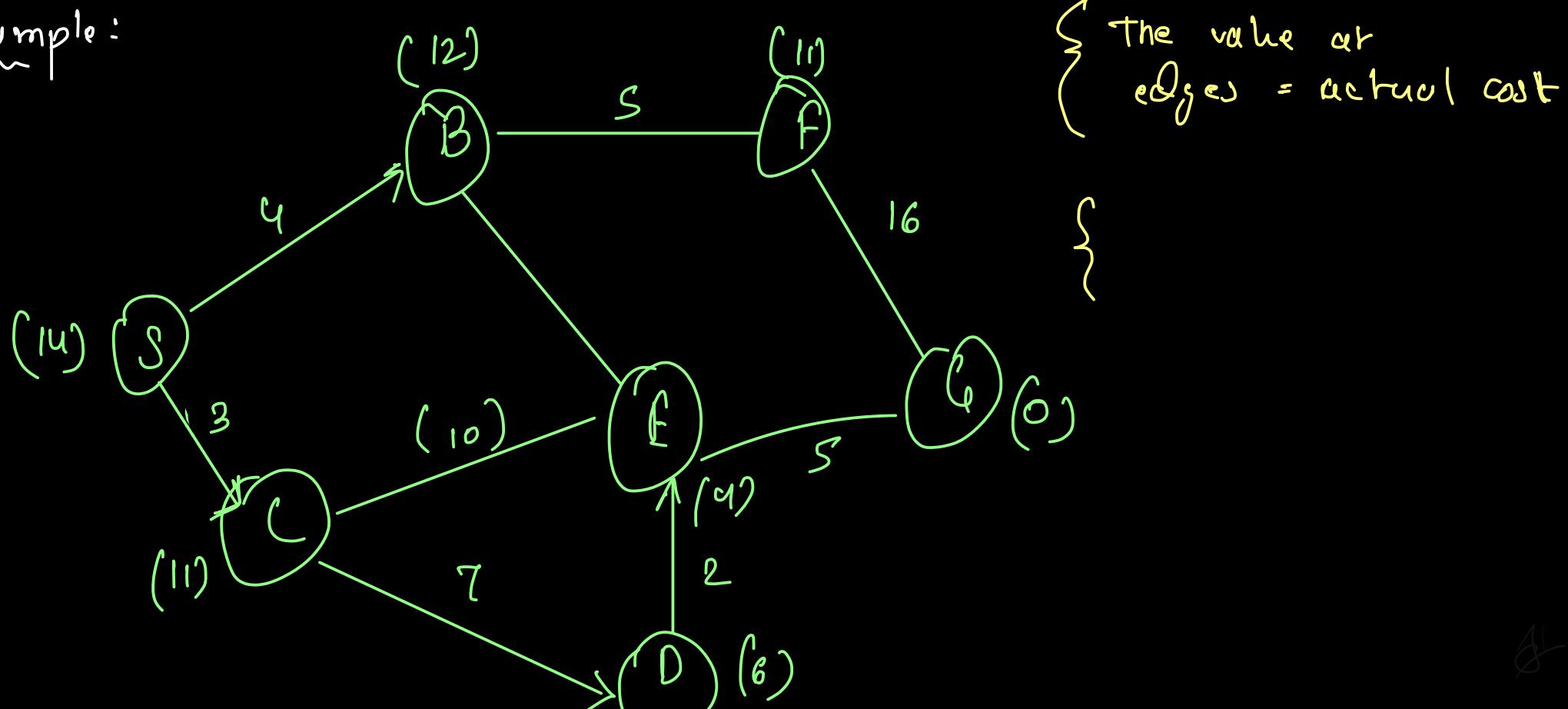


Table : $S \rightarrow G = 14$
 $B \rightarrow G = 12$
 $C \rightarrow G = 11$
 $E \rightarrow G = 4$
 $F \rightarrow G = 11$
 $D \rightarrow G = 6$
 $G \rightarrow G = 0$

S	14
B	12
C	11
E	4
F	11
D	6
G	0

* Step 1 \Rightarrow * $S \rightarrow B$

$$\begin{aligned}
 f(B) &= g(B) + h(B) \\
 &= 4 + 12 = 16 \rightarrow \text{Total cost} \\
 \bullet S \rightarrow C &\quad \downarrow \text{Actual} \quad \downarrow \text{Estimate} \\
 &
 \end{aligned}$$

$$\begin{aligned}
 f(C) &= g(C) + h(C) \\
 &= 3 + 11 = 14 \quad \left\{ \begin{array}{l} \text{Select the min Total} \\ \text{cost. i.e. } 14 \end{array} \right\}
 \end{aligned}$$

* Step 2 \Rightarrow $SC \rightarrow D$

$$\begin{aligned}
 f(D) &= g(D) + h(D) \\
 &= 7 + 3 + 6 = 16
 \end{aligned}$$

$SC \rightarrow E$

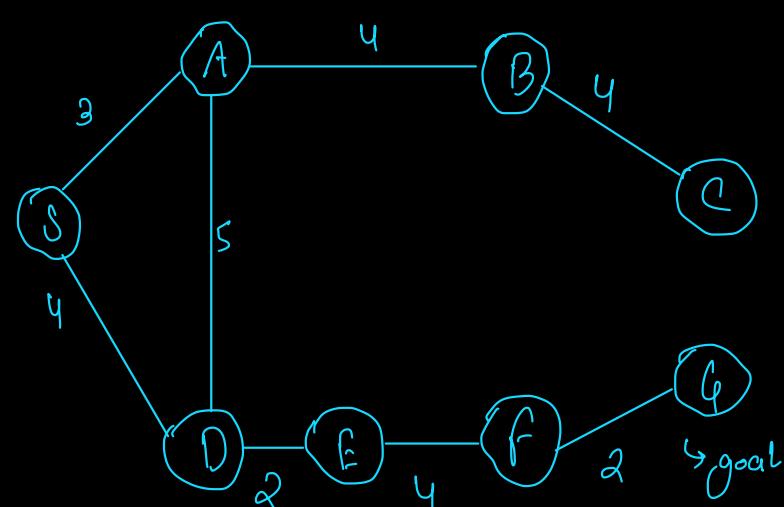
$$\begin{aligned}
 f(E) &= g(E) + h(E) \\
 &= 10 + 3 + 4 = 17
 \end{aligned}$$

Step 3 \Rightarrow SCD \rightarrow E

$$\begin{aligned} f(n) &= g(n) + h(n) \\ &= 12 + 4 = 16 \end{aligned}$$

Step 4 \Rightarrow SCD E \rightarrow C

$$\begin{aligned} f(n) &= g(n) + h(n) \\ &= 17 + 0 \\ &= 17 \end{aligned}$$



S	11.5
A	10.1
B	8.0
C	3.4
D	4.2
E	7.1
F	3.5
G	

Step 1 \Rightarrow J \rightarrow A

$$\begin{aligned} f(n) &= g(n) + h(n) \\ &= 3 + 10.1 \\ &= 13.1 \end{aligned}$$

J \rightarrow D

$$\begin{aligned} f(n) &= g(n) + h(n) \\ &= 4 + 9.2 = 13.2 \end{aligned}$$

Step 2: J A \rightarrow B

$$\begin{aligned} f(n) &= g(n) + h(n) \\ &= 3+4 + 8.0 \\ &= 15.0 \end{aligned}$$

J A \rightarrow D

$$\begin{aligned} f(n) &= g(n) + h(n) \\ &= 3 + 5 + 9.2 \\ &= 17.2 \end{aligned}$$

81

Step 3 \rightarrow SDF \rightarrow F

Step 4 \rightarrow SDEF \rightarrow G

$$f(n) = g(n) + h(n)$$

=

Final path \rightarrow S \rightarrow n, D \rightarrow E, F \rightarrow F, F \rightarrow G

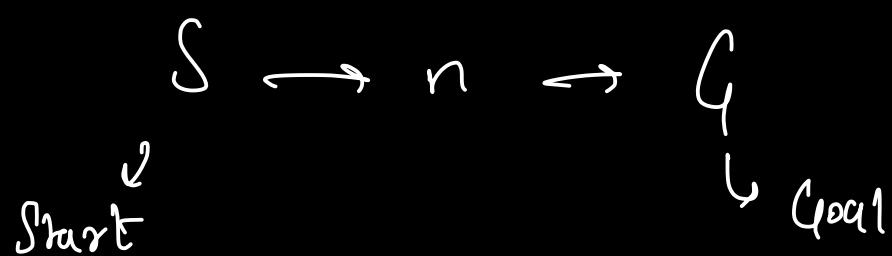
Total value = 12.

How to make base class Admissible:

$$h(n) \leq h^*(n) \longrightarrow \text{Underestimation}$$

$$h(n) \geq h^*(n) \longrightarrow \text{Overestimation}$$

Estimated value \rightarrow Actual value / optimal value



Underestimation:

If the heuristic value $h(n) \leq$ the actual cost to the goal node \therefore called underestimation.

Overestimation:

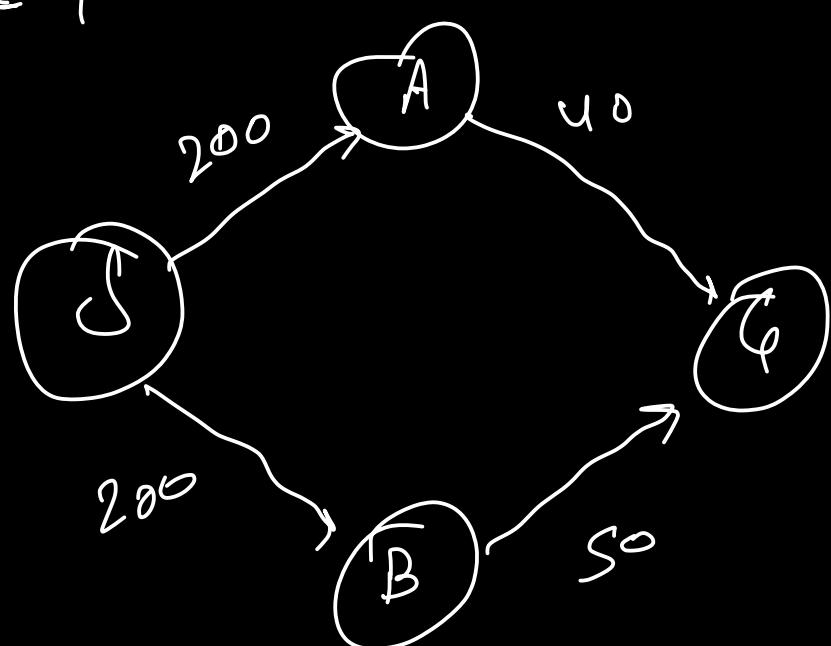
If the heuristic value $h(n) \geq$ the actual cost to the goal node \therefore called overestimation. Overestimation can lead to incorrect paths and suboptimal solⁿ. In this case, it may or may not give an optimal solⁿ. but in underestimation it

guarantees an optimal soln.

Real life example:

- Suppose the actual price of a laptop is 30k, but you had an expected price of 40k. You might quickly purchase if the shopkeeper offers it for 30k.

Graph:



$$h(A) = 80, h(B) = 70$$

$$A \rightarrow f(n) - g(n) + h(n)$$

$$\Rightarrow f(A) = 200 + 80 = 280$$

$$f(B) = 200 + 70 = 270$$

* Examples of :

Tic-tac-toe, Chess, 8 Puzzle Game

In game playing two major algos are used \rightarrow min-max algo,
 $\alpha-\beta$ _____

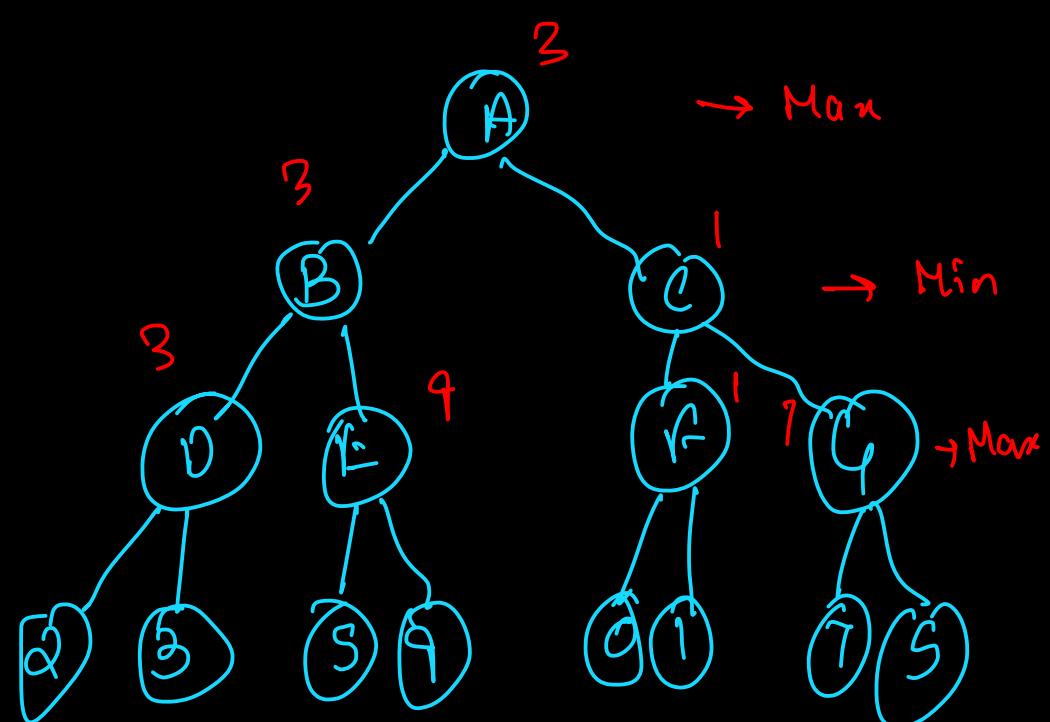
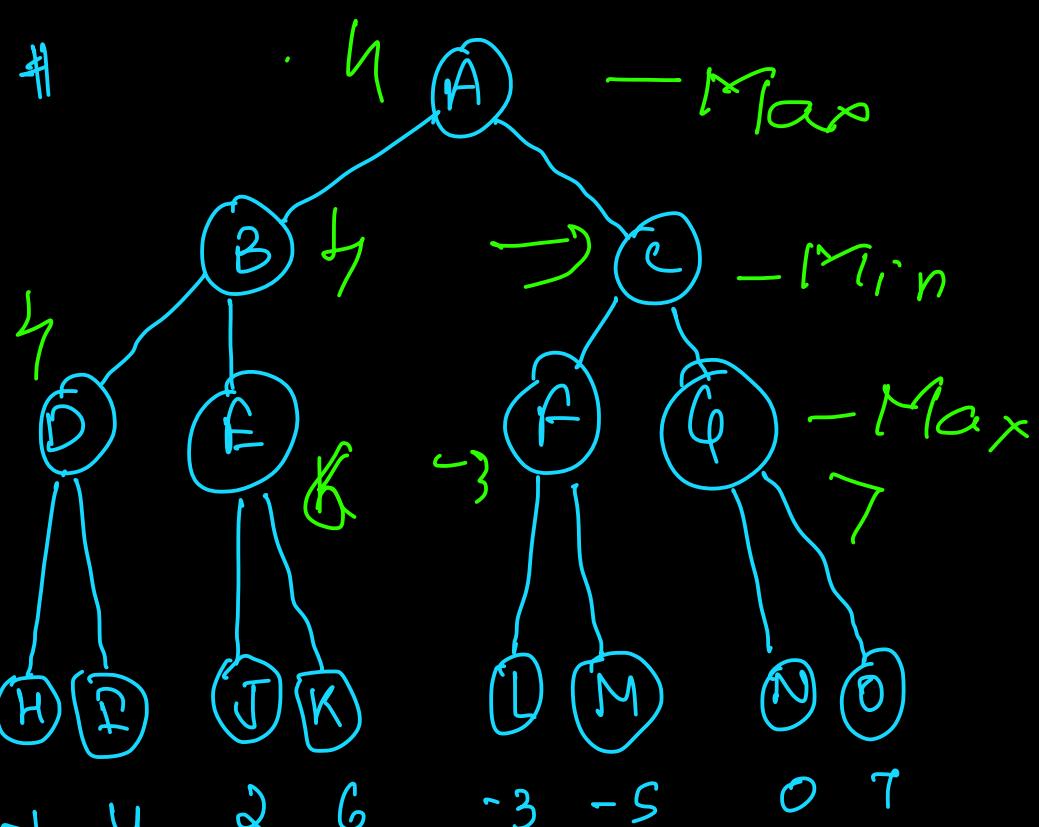
These algos work on a

Game tree Concepts:

- The tree shows all possible moves players can make.
- The player trying to maximise their chance of winning is called max.
- The opponent trying to minimise max chance of winning is called min.
- The game alternates b/w max and min moves at diff. levels of the tree.
- Complexity $\rightarrow O(b^d)$
 - $b \rightarrow$ branch factor
 - $d \rightarrow$ depth
- The algorithm goes from root node to the node.
calculates values and terminates and then propagates these values back to the best move.

Best Move Strategy:

- Two players compete max and min to make the best move to maximise the chance of winning.
- Min tries to minimise max chances and prevent



$A \rightarrow B \rightarrow D$

$A \rightarrow B \rightarrow D \rightarrow F$

$\alpha\text{-}\beta$ Pruning:

- It's an advanced version of min-max algo.
- It aims to improve the T.C. and performance of min-max by pruning unnecessary branches in the game tree.
- Min-max explores all nodes in the game tree leading to a T.C. of $O(b^d)$.
- Min-max evaluates every possible move which can be v. time consuming.
- But in $\alpha\text{-}\beta$ pruning, it cuts off the search fewer nodes (pruning).

- It reduces the no. of nodes explored and increases efficiency.
- If a best path is alr formed, remaining path

Alpha-Beta Algo:



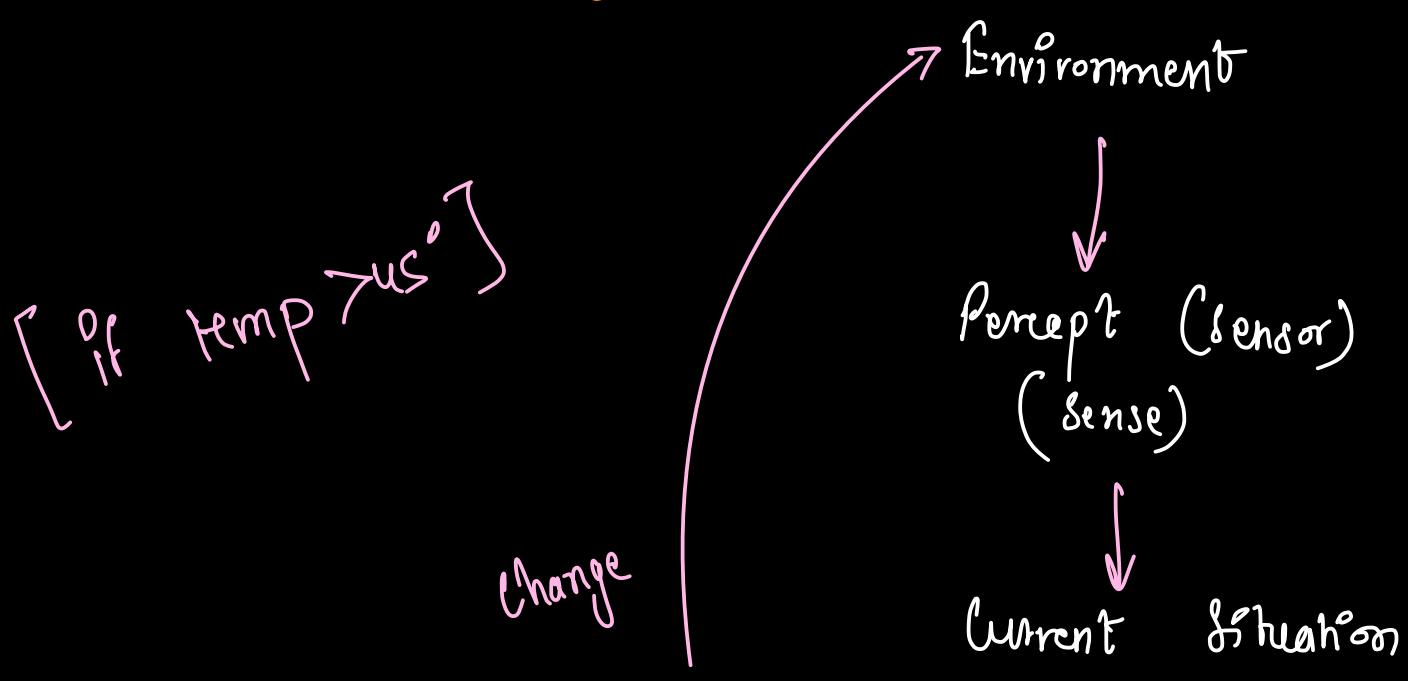
(2)	(3)	(5)	(9)	(0)	(1)	(7)	(5)
H	I	J	K	L	M	N	O

- P \rightarrow Performance
- E \rightarrow Environment-
- A \rightarrow Actions
- S \rightarrow Sensors.

Types of Agents:

1. Simple Reflex Agents.
2. Model Based ..
3. Goal ..
4. Utility Based Agent.
5. Learning Agents.

Simple Reflex Agent:



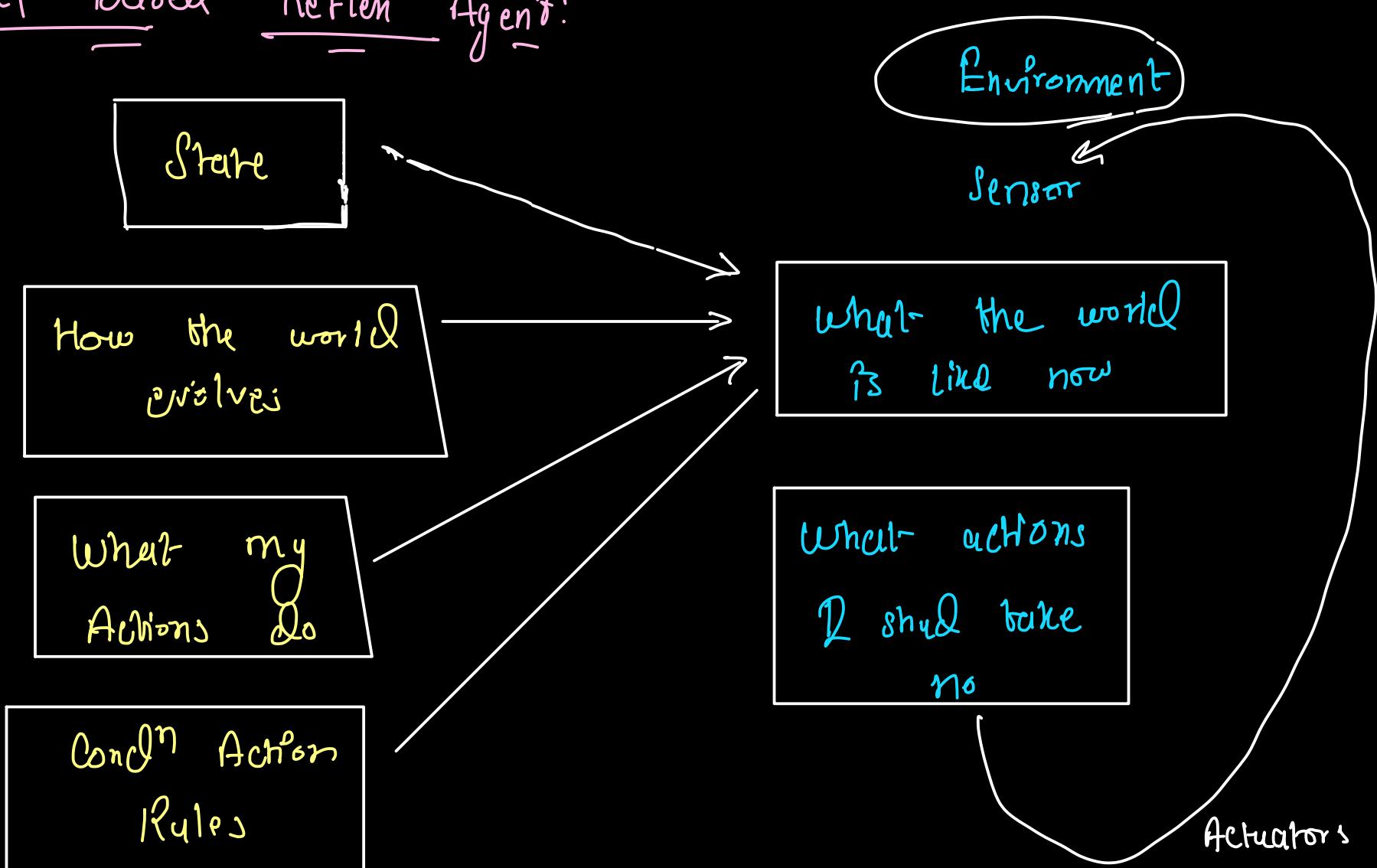
(What the world is like now)

If-then (condn)

Action

- Act on the basis of current perception.
- Ignores the rest of percept history.
- Based on if-then rules.
- Environment should be fully observable.

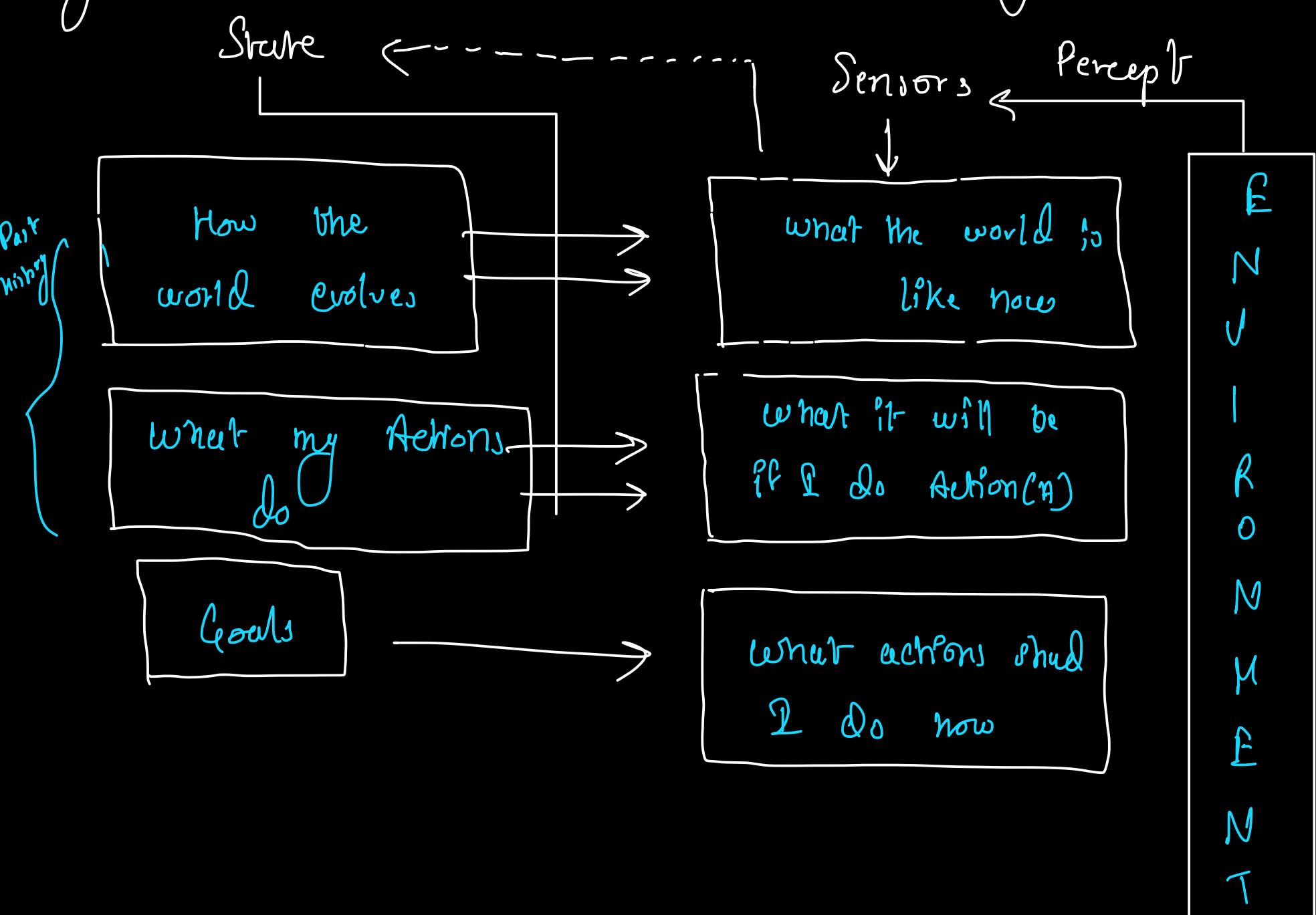
Model Based Reflec^t Agent:



- Model based means knowledge based made by historical or past cond'n then it makes the decision.
- The environment should be partially observable environment.
- Stores percept history (internal model).
- It works on the modelling.

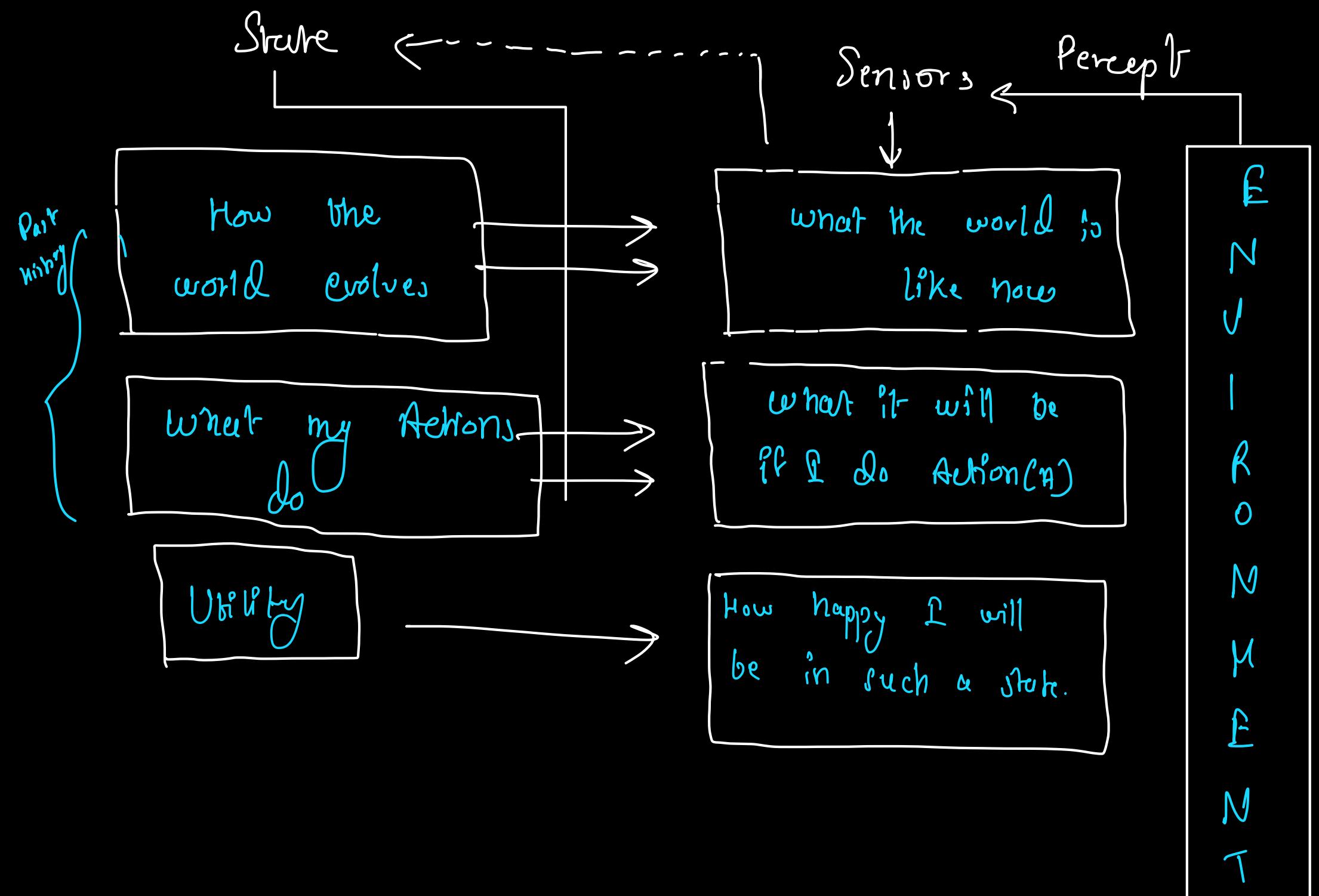
Goal Based Agent:

- It is an expansion of model based reflec agent.
- It is based on desirable situation (goal).
- Searching and planning
- We know the start state and goal state then we go to the goal state with the help of past history. and according to this history we do planning and searching.
- Fig →

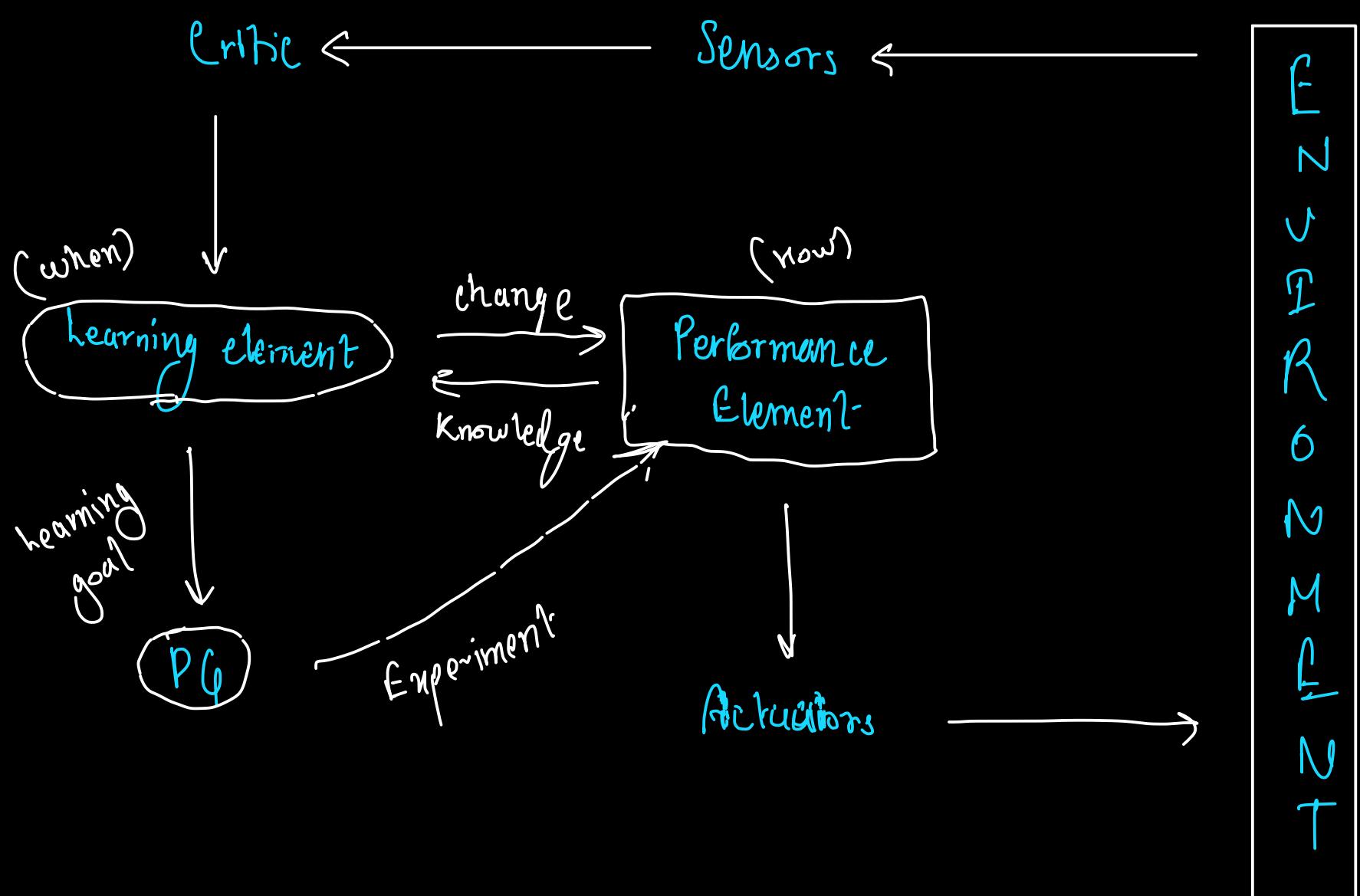


Utility Based Agent:

- Focus on utility not goal.
- Defined the utility function.
- Deals with happy and unhappy state.



Learning Agent → It learns overtime from experience.

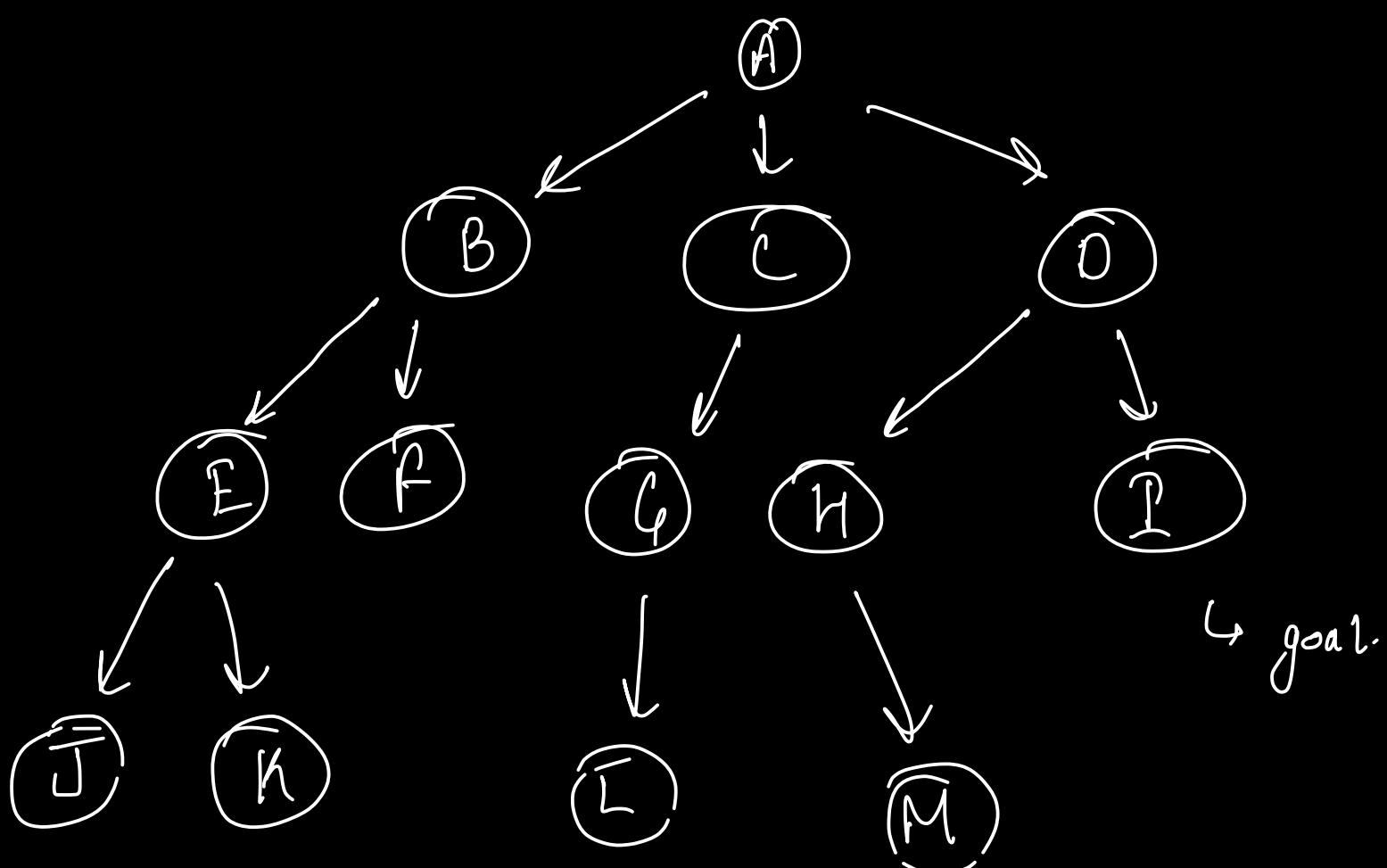


- Learning agent is a type of intelligent agent that learns over time from experience.
- Critic \Rightarrow It takes input from env and then pass the feedback to the learning element. It observes the environment.
- Learner \Rightarrow Stands for learning element. It focuses on when to use.
- Planner \Rightarrow " performance ". It focuses on how to do anything.
- Problem Generator \Rightarrow Problem Generator. It generates the problem. Ex: takes new route again and again.
- Actuators \Rightarrow Those who perform actions.

Iterative Deepening Search:

↳ Iterative Deepening Depth First Search (IDDFS)

- It combines both the benefits of DFS (Depth) & BFS (Breadth).
- It ensures completeness & optimality.
- Searches to a limited depth increasing the limit with each iteration.
- Ensures exploration of all nodes at each depth before going deeper.
- Ex:

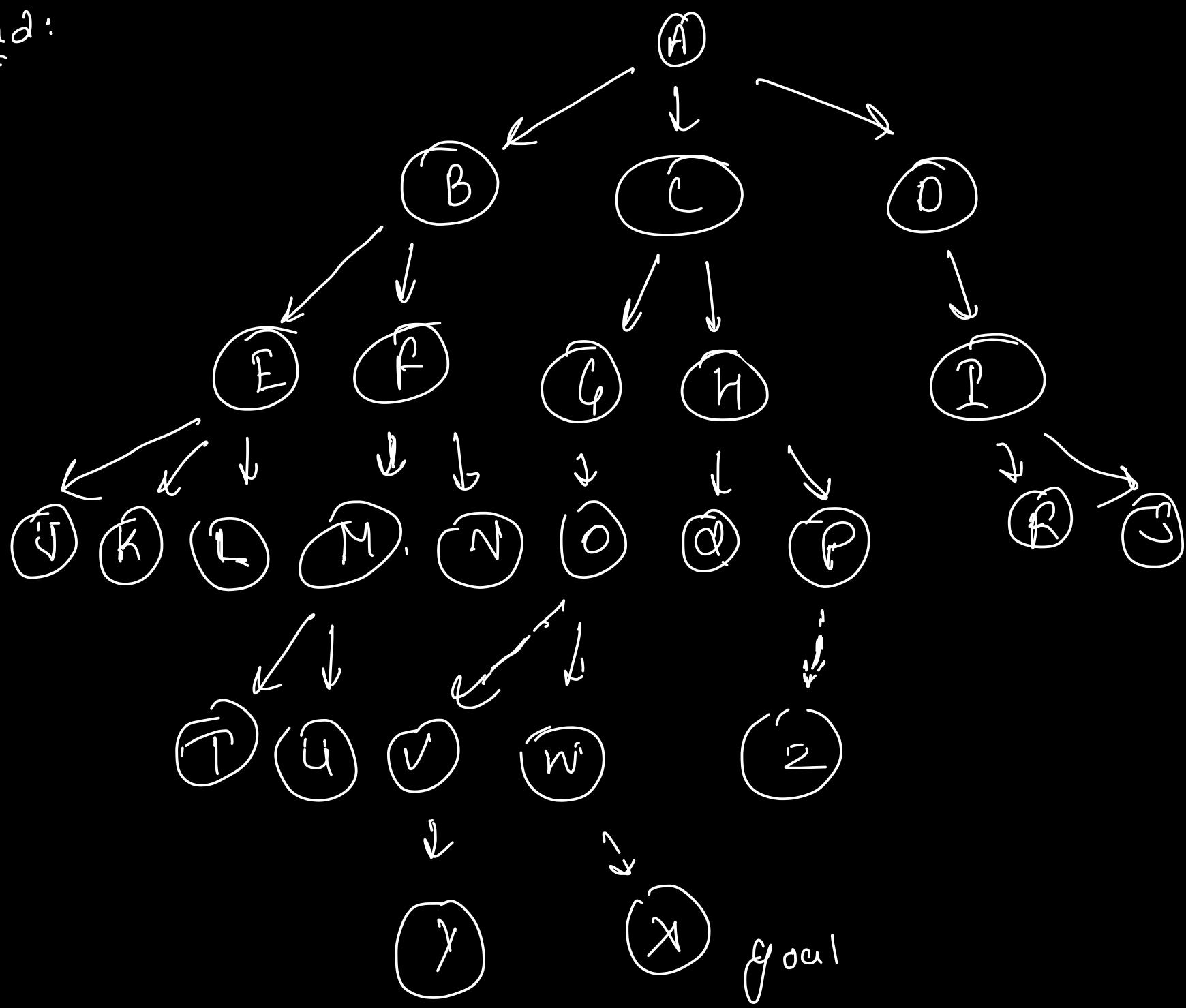


$$\mathcal{T} = A$$

$$P_1 = A \rightarrow B \rightarrow C \rightarrow D$$

$$\mathbb{I}_2 = A \rightarrow B \rightarrow C \rightarrow D \rightarrow E \rightarrow F \rightarrow G \rightarrow H \rightarrow I$$

End:
=



$I_0 = A$

$I_1 = A \rightarrow B \rightarrow C \rightarrow D$

$I_2 = A \rightarrow B \rightarrow E \rightarrow F \rightarrow C \rightarrow G \rightarrow H \rightarrow D \rightarrow I$

$I_3 = A \rightarrow B \rightarrow E \rightarrow J \rightarrow K \rightarrow L \rightarrow F \rightarrow M \rightarrow T \rightarrow N \rightarrow G \rightarrow O \rightarrow H \rightarrow Q \rightarrow P \rightarrow I$
 $\rightarrow R \rightarrow S$

$I_4 = A \rightarrow B \rightarrow E \rightarrow J \rightarrow K \rightarrow L \rightarrow F \rightarrow M \rightarrow T \rightarrow U \rightarrow N \rightarrow C \rightarrow G \rightarrow O$
 $\rightarrow V \rightarrow W \rightarrow H \rightarrow Q \rightarrow P \rightarrow Z \rightarrow D \rightarrow R \rightarrow Q \rightarrow J$

$I_5 = A \rightarrow B \rightarrow E \rightarrow J \rightarrow K \rightarrow L \rightarrow F \rightarrow M \rightarrow T \rightarrow U \rightarrow N \rightarrow C \rightarrow G \rightarrow O \rightarrow V$
 $\rightarrow Y \rightarrow W \rightarrow X$
 \downarrow
goal.

A* Algorithm in 8 puzzle Problem:

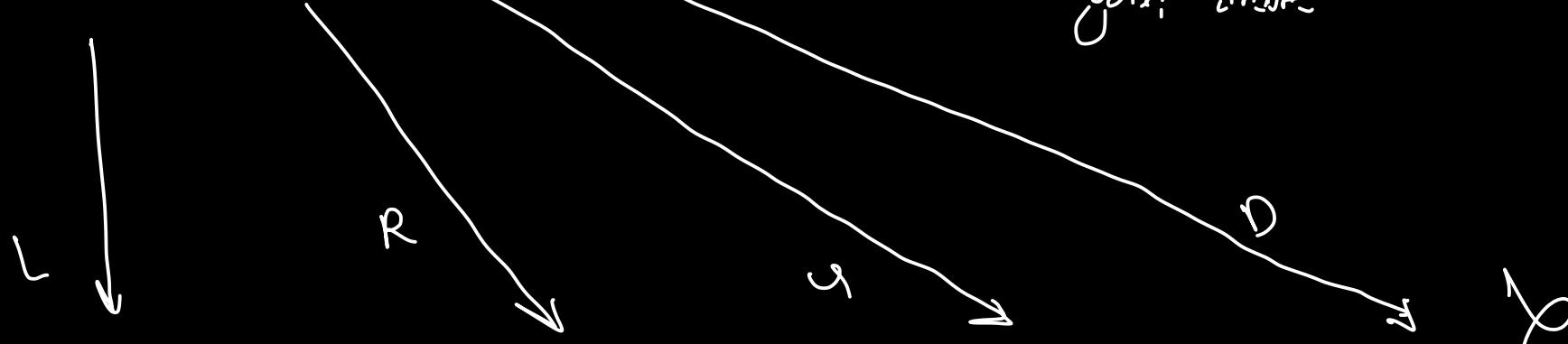
- The main aim is to find the most cost effective path to reach the goal state.

2	8	3
1	6	4
7		5

initial state

1	2	3
8		4
7	6	5

goal state



2	8	3
1	6	4
7	5	

2	8	3
1	6	4
7	5	

2	8	3
1	6	4
7	6	5

$$f(n) = g(n) + h(n)$$

$$= S + ;$$

$$= 6$$

L

R

C

D

X

2	8	3
1	4	
7	6	5

2	8	3
1	4	
7	6	5

2		3
1	8	4
7	6	5

f(8)

f(6)

f(5)

L L

R

C

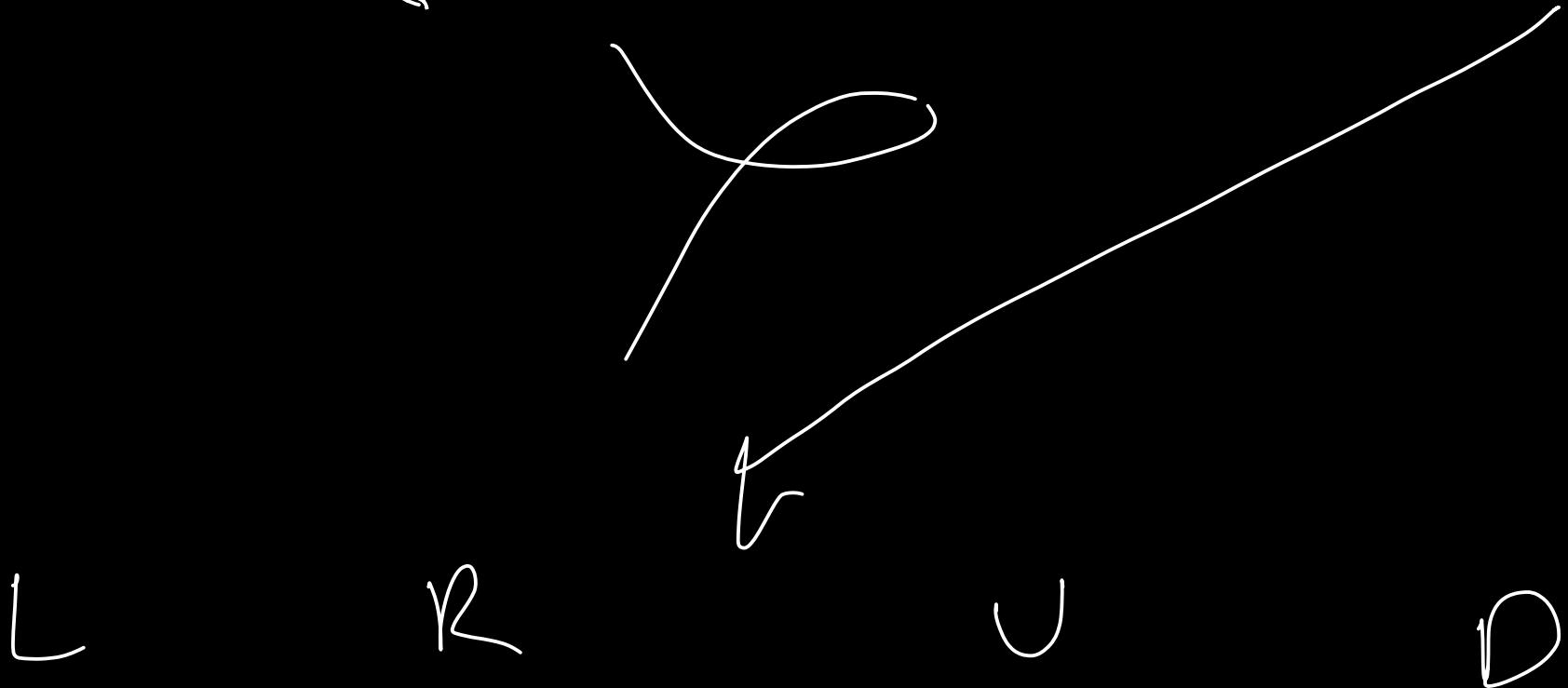
D

2	8	3
1	4	
7	6	5

	8	3
2	1	4
7	6	5

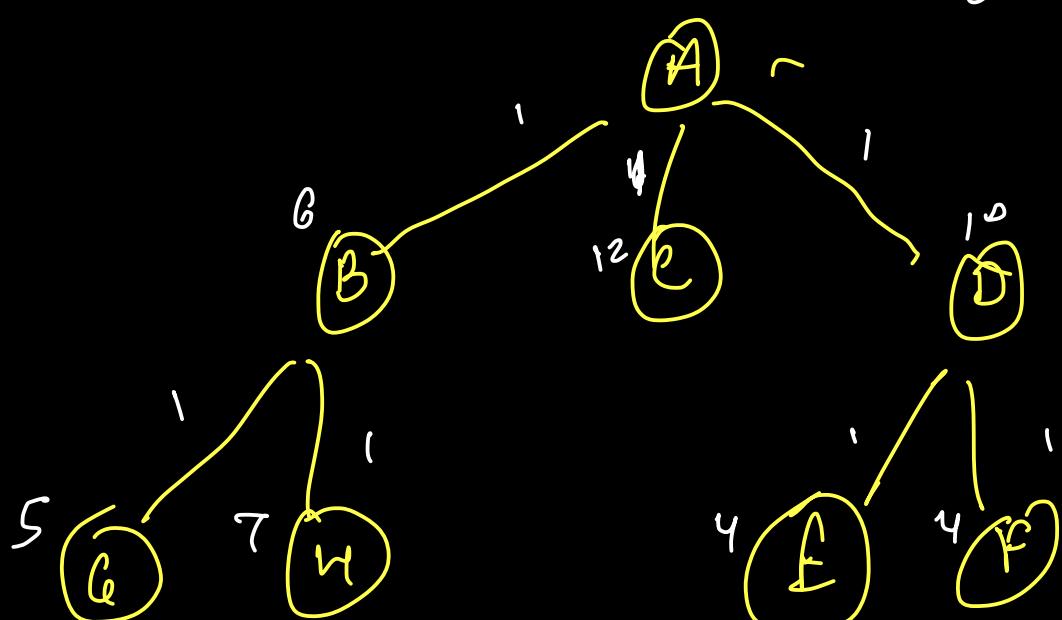
2	8	3
7	1	4
6		5

8

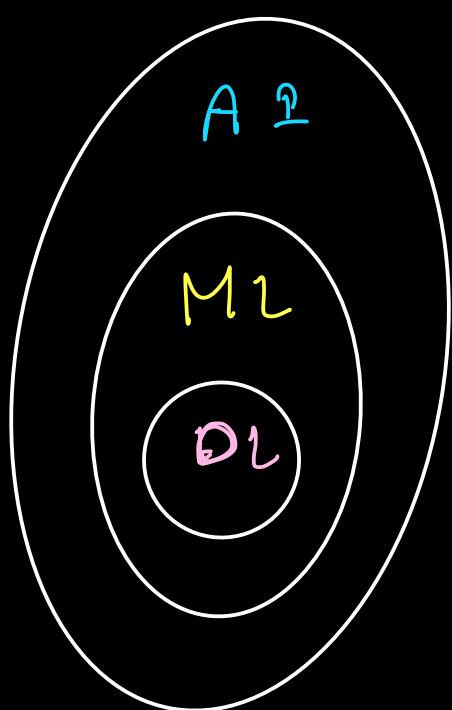


* In this complex prob. is broken down into smaller pieces and the a solⁿ is found.

- * A* and AO* both work on Best First Search. Both are informed searching.
- On the basis of heuristic value we find the solⁿ
- A* gives optimal solⁿ if we work on underestimate.
- AO* will always give optimal solⁿ, there is no guarantee
- " explore all paths once it get a solⁿ.

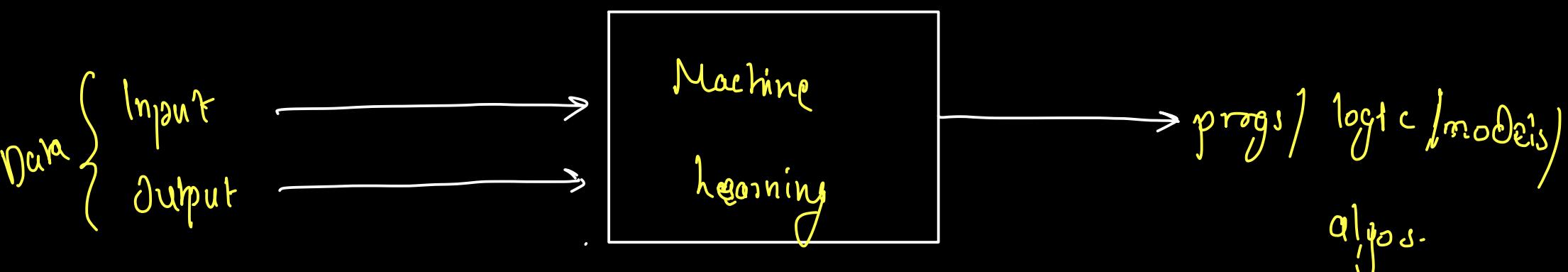


Machine learning



- ML is a branch of AI that focuses on developing models and algos that let computers learn from data without being explicitly programmed for every task.
- In simple words, ML teaches the systems to think and understand like humans while learning from the data.

How ML is diff from traditional programming:



- ML learns with the help of Data

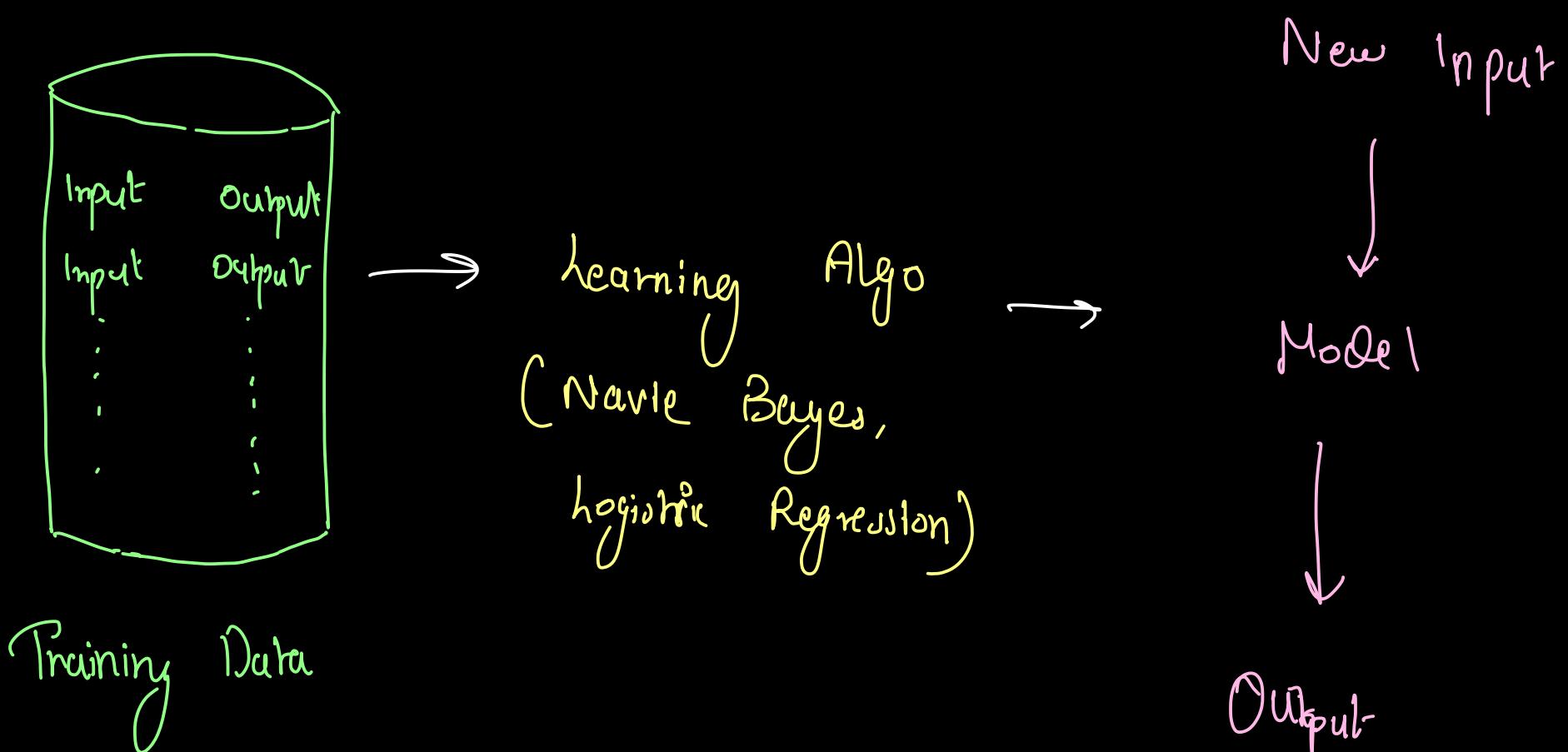
How ML Works?

- Problem Statement
- Data Collection
- Data Cleaning
- " Analyse & Exploration
- " Modelling
- Optimisation and Deployment
- The main of ML is to reduce the error margin

$$E.M. = \frac{\text{Desired output} - \text{Actual output}}{(\text{Expected})}$$

Types of ML:

- Supervised Learning

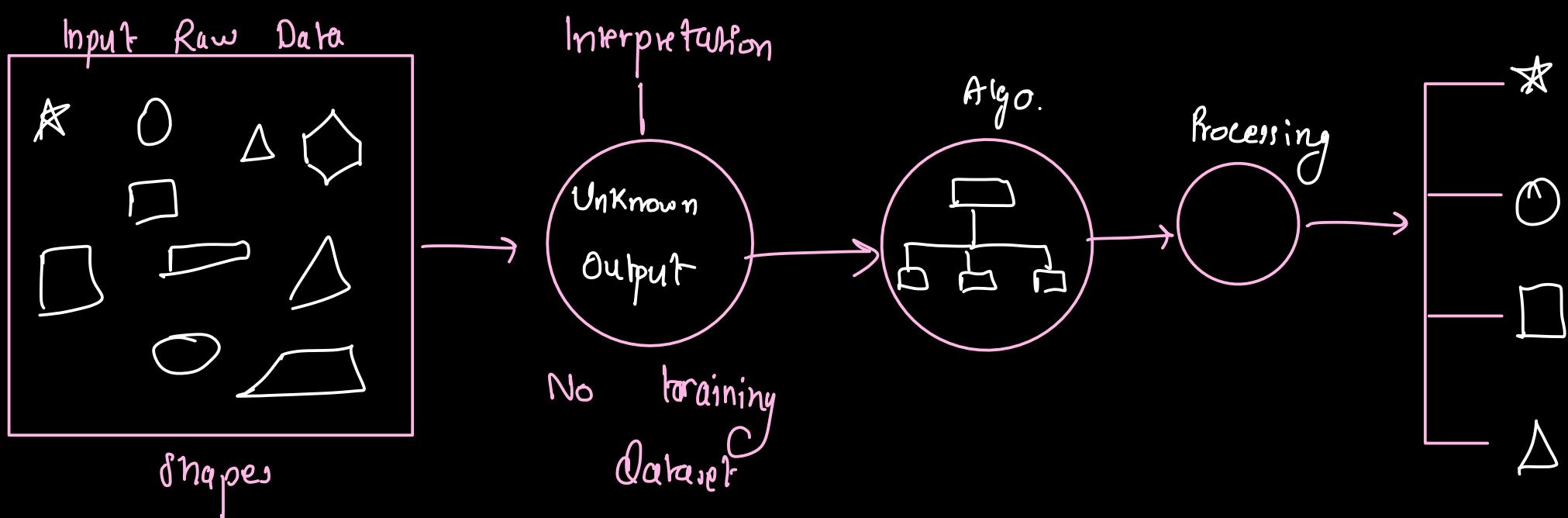


- Training Data
- Both input and output

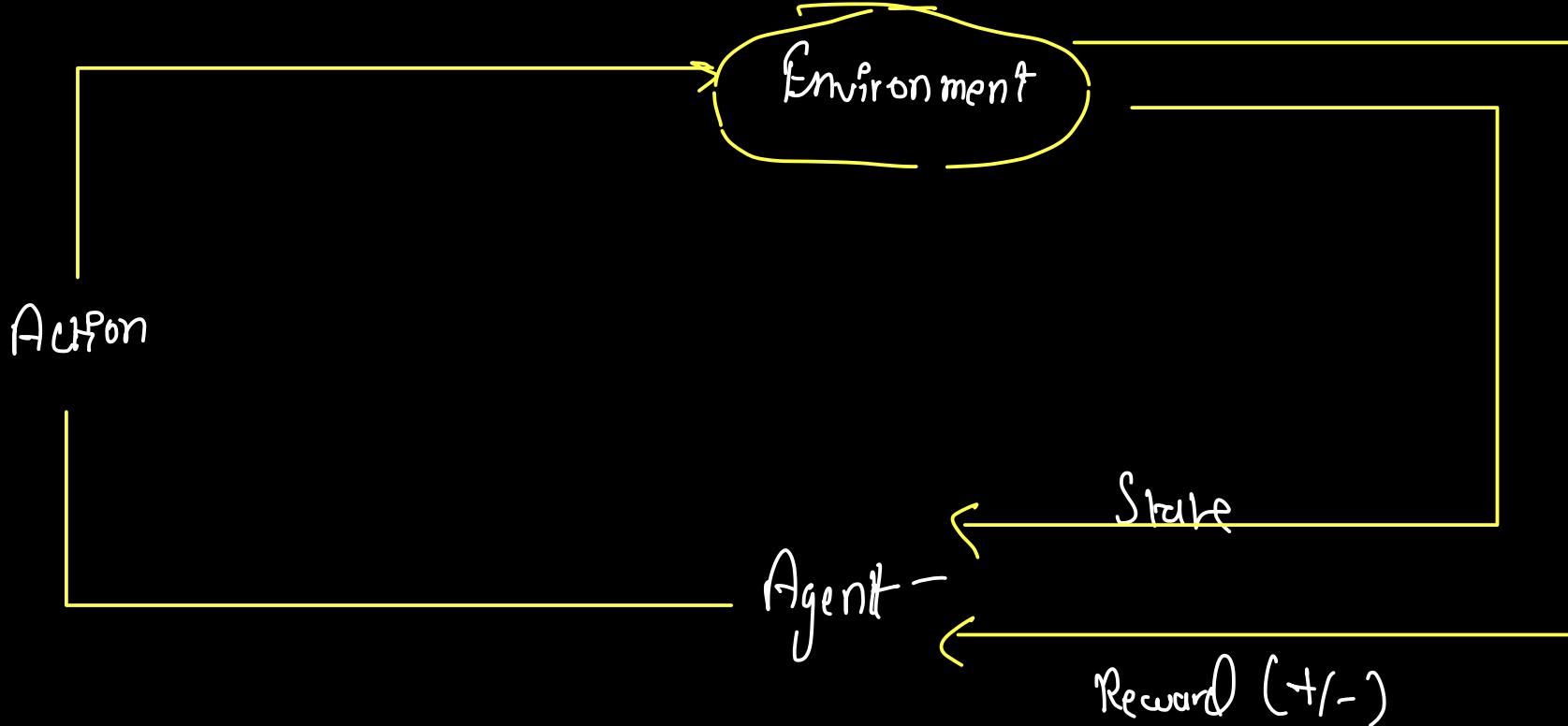
- It performs classification.
- In Supervised learning, models are trained on labelled data to predict or classify new, unseen data.
- A supervisor (teacher) provides both input and output, helping the machine learn from this data.

Unsupervised learning:

- Learning based only on an input dataset without labelled outputs.
- The machine has no prior knowledge only input and fit groups data into clusters.
- Algos: K Mean Clustering
- In unsupervised learning no supervisor is present



Reinforcement learning:



- It is a feedback based ML approach. Here an agent learns to which action to perform by looking at the env. and the results of actions.
- It is related to semi-supervised learning.
- For each current action, the agent gets the feedback and for incorrect action the agent gets -ve feedback or penalty.
- The agent interacts with the env and identifies the possible action it can perform.
- The primary goal of an agent is to perform actions by looking at the env and get the max. the rewards.
- In RL, the agent learns automatically using feedbacks without any labelled data unlike supervised learning.
- RL is used to solve specific type of problems where decision making is sequential. And the goal is long term.

Types of RL: → +ve feedback
→ -ve feedback

a) Where do we use RL?

↳ Its used in designing robots or in games.

• It is not suitable for env where complete info is present.

For eg: The problems like obj. detection, hand detection can be better solved using a classifier than by RL.

Steps of Feature Engineering:

1. EDA { Exploring Data Analysts }

↳ ① Analysis → ① How many numerical features may be there.

② How many categorical features may be there;

③ Missing values

④ Outliers.

Step 2 → Handling the missing values

→ Mean
→ Median
→ Mode.

Step 3 → Handling Imbalanced Dataset.

↳ Imbalanced Dataset always gives poor accuracy so it's essential to convert imbalanced Dataset into balanced Dataset to improve the accuracy.

Step 4 → Treating the outliers

Step 5 → Scaling the data.

(a) Standardization

Normalization.

Converting the categorical features into numerical features.

Feature Selection:

- We select only those features that are important.
1. Correlation
 2. K-Neighbours
 3. Chi-Squared Test.
 4. Genetic Algorithm
 5. Feature Importance {Extra tree classifier}.

Handling Missing Values:

1. Delete the records which has missing values.
2. Create a separate model to handle missing values.
3. Statistical methods → mean, median, pofnt.

Deleting records which has missing values:

f_1	f_2	f_3	f_4	O/P
1	200	100	70	
2	300	-	80	
-	400	-	-	
4	600	20	10	
5	800	10	15	

↳ In this most of the features have empty.

- When we have a huge dataset like millions of records then only it's applicable. But if we have a smaller dataset, we never follow this step.

Create a separate Model:

- It takes much more time for large dataset to fit it is only applicable for small dataset.

	f_1	f_2	f_3	f_4	O/P
test dataset	{ -	20	30	40	100
	100	150	60	40	200
Training dataset	{ 50	80	90	100	360
	70	20	10	40	100

f_2, f_3, f_4

↳ model (training model) \rightarrow O/P.

- ↳ Whenever we have a missing value in a feature, then we have to consider our test dataset and remaining all the datasets are training dataset.

Statistical Techniques (Best technique):

Mean.

10

20

30

40

30

• Mean

• Median

Dealing with Categorical Feature:

- 1> Nominal feature (No rank) [eg, States]
- 2> Ordinal " (Rank given) [eg, Grades]

Techniques for Handling the Categorical Feature:

1. Label Encoding
2. Count or Frequency Encoding.
3. Ordinal Encoding {Ordinal Dataset}.
4. One Hot Encoding {Nominal Dataset}.

Label Encoding:

20	News	Title	X12	ABC.	P

Label Feature

↳ Output

- Output is having labels, it means labels are available in classification problem then we have to apply label encoding.

↳ Ordinal Encoding:

- If we have ordinal dataset means the dataset having only order the O.E. is applied.

* $PQ > UG > HS > 10$

$$\begin{array}{ll}
 HS \rightarrow 0 & HS \rightarrow 0 \\
 UG \rightarrow 1 & UG \rightarrow 1 \\
 PQ \rightarrow 2 & PQ \rightarrow 2 \\
 PQ \rightarrow 2 & \\
 UG \rightarrow 1 & \\
 HS \rightarrow 0 & \\
 UG \rightarrow 1 &
 \end{array}$$

*

Age	Gender	Review	Education	Purchase	
10	Female	Good	$UG \rightarrow 0$	Yes	→ 1
24	"	Avg	$PQ \rightarrow 1$	Yes	→ 1
26	"	Poor	$PQ \rightarrow 1$	No	→ 0
27	"	Poor	$PQ \rightarrow 1$	No	→ 0
44	"	Avg	$UG \rightarrow 0$	No	→ 0

Good → 2

Avg → 1

Poor → 0

One Hot Encoding:

↳ It is applied only for nominal data.

↳ No rank in this

↳ Ex: \rightarrow Gender \rightarrow Male
 \rightarrow Female

Gender	Male	Female
Male	1	0
Female	0	1
Male	1	0
Male	1	0
Male	1	0

Freq. Encoding:

- If any features having more categories, it means bimodal features.
- Replace each category with count of how often it appears in data.

Target Encoding:

- It replaces each category with mean of target variable (only for classification)

Categorical Feature	label	ONE	LE	FE	Target Enc (Label Freq.)
A	No	A B C 1 0 0	0	u	0.5
A	Yes	A B C 1 0 0	1	u	"
A	No	A B C 1 0 0	0	u	"
B	Yes	A B C 0 1 0	1	2	1

A: 4

4

A	Yes	1 0 0	1	4	0.5
C	No	0 0 1	0	2	1
B	Yes	0 1 0	1	2	"
C	Yes	0 0 1	1	2	"

$\sum x_i^2$

Categorical Feature	Label	OHE		FB		TE	LE
		M	F	4	5		
Male	N	1	0	4	2/4	0	
Female	Y	0	1	5	2/3	1	
"	Y	0	1	5	"	1	
Male	N	1	0	4	2/4	0	
Female	N	0	1	5	4/5	0	
"	N	0	1	5	"	1	
Male	Y	0	1	5	"	1	
"	Y	0	1	5	"	1	
Male	N	1	0	4	2/4	0	
"	N	1	6	4	"	0	

Feature Scaling:

Male Height in feet (h_1)	Female Height in cm (h_2)	Hire Span in Year (h_3)
8.0	150	30
8.5	165	40
7.9	170	36
8.2	140	41

- It's a method to scale numeric features in the same scale or range { -1 to 1, 0 to 1, 0 to 10 and so on...? }.
It is also called as Data normalization.
- It's involved in last step of Data pre-processing and before ML Model training. We apply feature scaling on independent variables. We fit feature scaling with trained data and transform on train and test data.

Q.) Why do we use feature Scaling?

- The scale of raw feature is different acc. to its units. ML algos can't understand feature's units, it understands only nos.
- If height 140cm and 8.2feet. ML algos understand only nos. Then it assumes that $140 > 8.2$

Q.) Which ML algo requires feature scaling?

- K-Nearest Neighbour (KNN).
 - K-Means
 - Support Vector Machine
 - PCA (Principle Component Analysis).
 - LDA (Linear Discriminant Analysis).
 - Linear Regression.
 - Logistic Regression.
- Linear Base & Algo

• Neural Networks

* Tree based algos don't require feature scaling

Types of feature scaling:

- Min - Max Scaler
- Std Scaler
- Man Abs Scaler
- Robust Scaler
- Quantile Transformer Scaler
- Power Transformer Scaler

PCA:

* Calculate Eigen values & Eigen Vectors.

$$\begin{bmatrix} 12.67 & 16.33 \\ 16.33 & 22 \end{bmatrix}$$

$$* \begin{bmatrix} S - \lambda I \end{bmatrix} = 0$$

$$\Rightarrow \begin{bmatrix} 12.67 - \lambda & 16.33 \\ 16.33 & 22 - \lambda \end{bmatrix} = 0$$

$$\therefore (12.67 - \lambda)(22 - \lambda) - (16.33)^2 = 0$$

$$\therefore 278.74 - 12.67\lambda - 22\lambda + \lambda^2 - (16.33)^2 = 0$$

$$\Rightarrow \lambda^2 - 34.67\lambda + 12.072 = 0$$

$$\Rightarrow \lambda = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= 34.31, 0.35. \quad \left\{ \text{Picking the larger value?} \right.$$

Step 4:

$$\begin{bmatrix} 12.67 - \lambda & 16.33 \\ 16.33 & 22 - \lambda \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} -21.64 & 16.33 \\ 16.33 & -12.31 \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$\therefore -21.64u_1 + 16.33u_2 = 0$$

$$16.33u_1 - 12.31u_2 = 0$$

$$\rightarrow \frac{u_2}{u_1} = \frac{21.64}{16.33} = 1.328$$

$$\rightarrow \frac{u_1}{u_2} = \frac{16.33}{21.64} = 0.7546$$

Step 5: Project Data onto principle component.

x_1	x_2	PCA
5	10	16.625
3	7	10.475
10	15	28.256
2	4	

$$* \begin{bmatrix} 5 & 10 \end{bmatrix} \begin{bmatrix} 1.32S_6 \\ 1 \end{bmatrix} \quad \left\{ \begin{bmatrix} 2 & 4 \end{bmatrix} \begin{bmatrix} 1.32S_6 \\ 1 \end{bmatrix} \right.$$

$\hookrightarrow 5x_1 \cdot 1.32S_6 + 10x_1 = 16.628$

Feature Selection:

* Need for Feature Selection:

- Student Database:

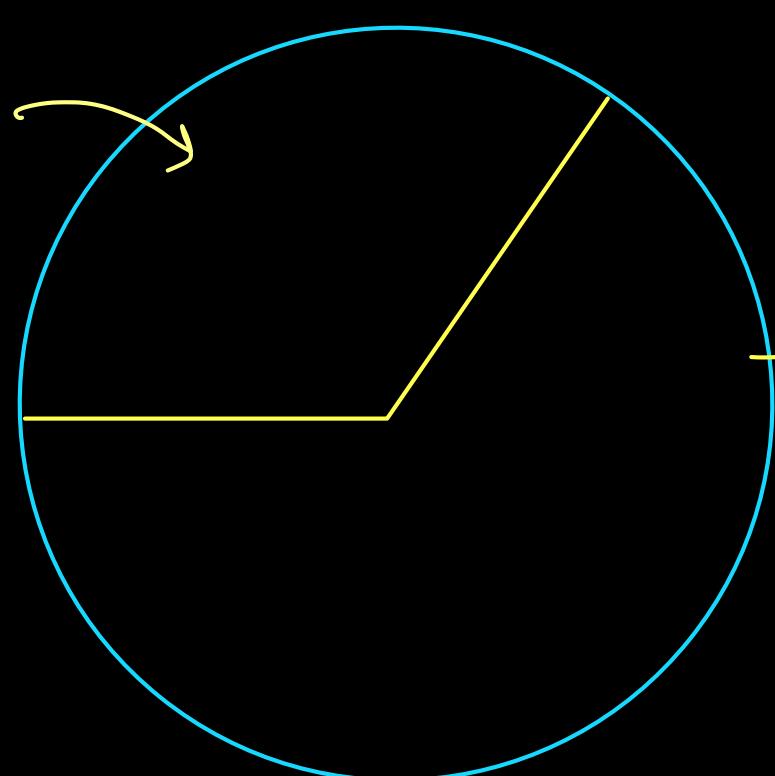
Name	Marks	Address	Race	Religion	Attendance
				X	

- All the features the model does not give goal accuracy. If gives 60% accuracy.
- With relevant and best features, the model performs well. It gives above 60% accuracy.

What is Feature Selection?:

Selecting optimal
4 best features

for M.L. Models



Removing irrelevant
or partially relevant
features from the
data.

Importance of Feature Selection:

- Reduces the curse of dimensionality.
- It works on the relevance and importance of feature.
- It minimizes the cost of computation.
- It helps in learning the model by providing the best features for training the ML Model.
- It helps in achieving very good accuracy.

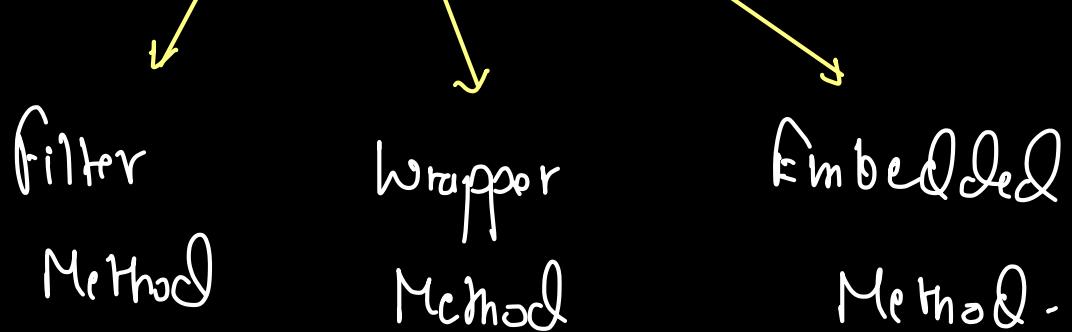
Feature Selection Techniques:

↓
Supervised Feature selection

(We require the target or output variable)

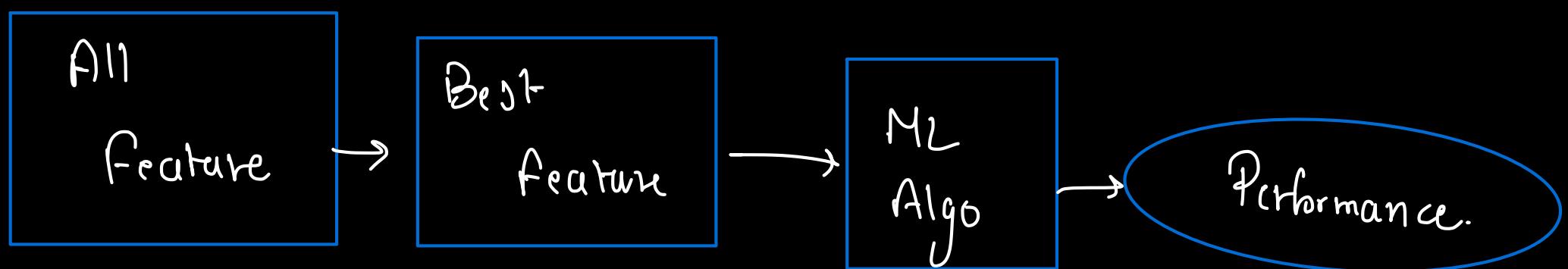
↓
Unsupervised Feature Selection

(We do not require the target or output variable)



I. Filter Method

- Information gain → Determines Reduction in Entropy
- Chi squared Test → Determines the rs b/w categorical variable
- Fisher's Score → Returns the rank of the feature in descending order.
- Missing value Ratio → Evaluate the features at against threshold value.



Advantages of filter Method:

- Better Computational Complexity.
- Fast and Scalable
- Independent of Classifier

Disadvantages of filter Method:

- Ignores Interaction with Classifier
- " Feature Dependencies.

Wrapper Method:

All
features

Feature
subset
ML
Algo

Performance

- Forward Selection: Begins with empty set of features, with each iteration keeps adding one feature and evaluates.
- Backward Elimination: Begins with all the features, with each iteration removes the least significant feature.
- Exhaustive Feature Selection: Evaluation is based on Brute-Force Method.
- Recursive Feature Elimination: It is recursive, greedy optimisation approach.

Advantages:

- Interacts with classifier
- Minimises Computational cost
- Model is feature dependent

Disadvantages:

- High Risk of Overfitting.
- Computationally intensive.
- Lower Discriminative power

H. Embedded Method:

- Regularization techniques like L1, L2 and Elastic Nets.
- Random Forest , Decision Tree , Trees Based Methods, for Feature Selection.