Image Noise Reduction

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- Common types of image noise include:
 - ▶ Salt and pepper noise: contains random occurrences of black & white pixels
 - ▶ Impulse noise: contains random occurrences of white pixels
 - ▶ Gaussian noise: variations in intensity drawn from a Gaussian normal distribution

Noise Model

▶ We can consider a noisy image to be modelled as follows:

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If we can estimate the noise model we can figure out how to restore the image

Filtering to Remove Noise

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This is implemented as the simple smoothing filter

It blurs the image.

Median Filter

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Median Filter

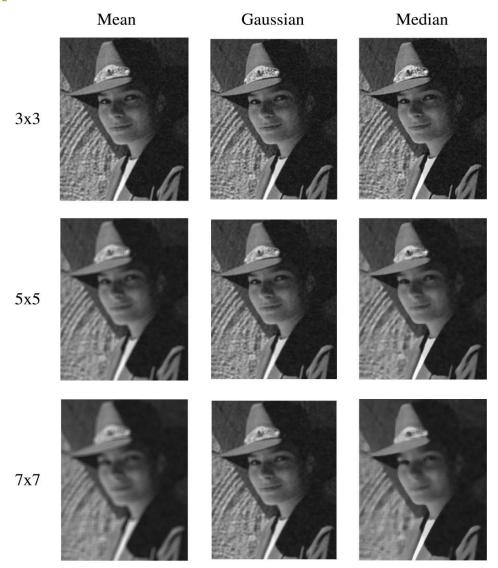
Median Filter:

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- Excellent at noise removal, without the smoothing effects that can occur with other smoothing filters
- Particularly good when salt and pepper noise is present

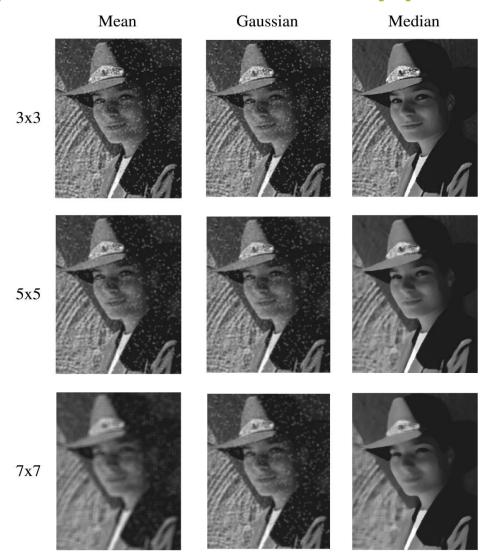
Comparison: Gaussian noise

Comparison: Gaussian noise



Comparison: Salt & Pepper Noise

Comparison: Salt & Pepper Noise



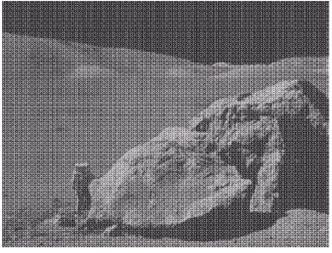
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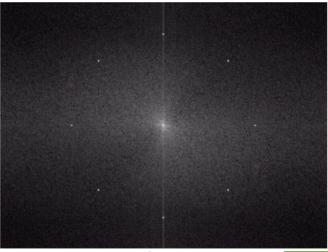
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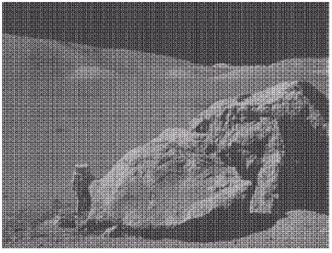
- Typically arises due to electrical or electromagnetic interference
- Gives rise to regular noise patterns in an image

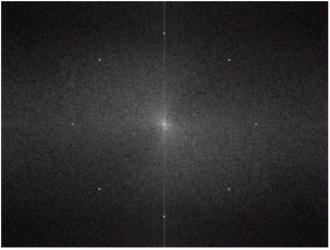
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- Frequency domain techniques in the Fourier domain are most effective at removing periodic noise





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- Band reject filters can be used for this purpose
- An ideal band reject filter is given as follows:

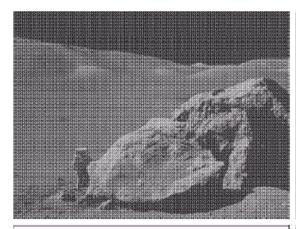
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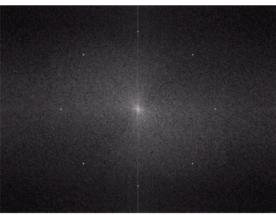
$$H(u,v) = \begin{cases} 1 & \text{if } D(u,v) < D_0 - \frac{W}{2} \\ 0 & \text{if } D_0 - \frac{W}{2} \le D(u,v) \le D_0 + \frac{W}{2} \\ 1 & \text{if } D(u,v) > D_0 + \frac{W}{2} \end{cases}$$

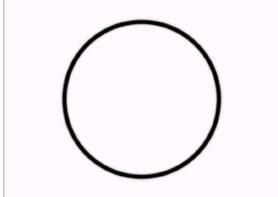
Band Reject Filter Example

Image corrupted by sinusoidal noise

Fourier spectrum of corrupted image







Butterworth band reject filter

Filtered image