

CSCM37: Data Visualisation

Coursework 3

05/05/20

Andy Gray 445348

Paper Title: Time-Dependent Flow seen through Approximate Observer Killing Fields

1 Summary of Concept (or Problem Statement)

Flow fields usually are visualised in relative to a global observer, or a single frame of reference. Objective criteria for detecting features such as vortices, also has a similar issue, as it relies on the use of a global reference point or separate references for each point in space and time. However, the authors claim that no global frame can show all flow features well equally. Therefore the authors propose a framework that allows a smooth trade-off between the two extremes. A novel notion of observation has been developed to observe the time derivative. This development restricts individual movements to rigid motions, while overall computing the killing field approximately, in a matching rigid like motion. Instead of focusing on flow features, the framework enables continuous transition between the observers visualising how all observers jointly perceive the input field. In order to do this, a concept of observation time is introduced. Observation time creates a visualisation by using the corresponding stream, path, streak and timelines. These characteristics are computed using standard techniques, but the input field must be transformed as accordingly. Therefore, derived flow features, such as vortices and input flow that are perceived by the observer, get classed as objective.

2 Contributions

One observer and its rigid motion are not flexible enough [17, 19], so the authors propose to use an approximate killing field instead of an exact one, observer field u . However, for this to be meaningful with respect to a general observer field u , we have to define a suitably generalised concept of an observer-relative time derivative of the input field v with respect to u . We call this the observed time derivative that we construct by building on the general concept of the Lie derivative from differential geometry [16, 29, 32].

The main contributions are split into two key stages. Stage one introduces a generalisation of the standard streamlines, pathlines, streak lines, and timelines by introducing the concept of observation time. Which involves computing a visualisation of a relative observer field, as at the observers move as well an observer related visualisation will be different. While aiming to approximate killing fields, the generalisations work for any general observer field as well. Stage two is applying the observer velocity field to the objective computation of vortices, which is enabled as the optimisation is guaranteed to find the same unique observed field for any given input flow, for a chosen optimisation parameter.

3 Related Work Summary

The paper related work references five related topics. These topics are Euclidean observers; Multiple observers; Flow decomposition; Vortex detection; Killing fields.

The concept of a Euclidean observer within space is vital in fluid mechanics [20] and within flow visualisation [17]. The author reference Truesdell and Noll

[46] in regards to their work with continuum mechanics. With further references to Holzapfel and Ogden [22, 35] for their more detailed work, all about defining a transformation between two observers.

A Galilean-invariant vortex detection method first proposed by Weinkauff et al. [50]. This multiple observer, which was not originally presented as such, computes at each point in time and space a different constant velocity observer. While each method is not objective, they compute each observer separately. The author states that Gunther et al. [17] use optimisation to compute different rigid-motion observers. Again all observations are computed individually. They are optimised over a large constant-size neighbourhood. With additional references to Bujack et al. [10], who consider multiple observers via a weighted average of vector fields seen from a finite number of certain Galileaninvariant critical points.

HelmholtzHodge decomposition [7, 8], flow decomposition can also be used to remove background flow, corresponding to the harmonic component [9]. While also referencing Sujudi and Haines [44], LAVD criterion of Haller et al. [21]. However, Gunther et al. [17, 18] work on vortex detection, is the main style being used based on its ability to compute an objective's velocity field and its derivatives, which will make all the criteria computed from the properties automatically.

The final related work is Killing fields. These are vector fields that induce flow that preserves the distance, infinitesimal isometries. These correspond to the derivatives, in the euclidean space, of all the rigid motions. Approximate Killing fields have been used in shape deformation [33], shape space exploration [28], planar as-Killing-as-possible vector fields [43], on curved surfaces [6], and for designing approximate Killing fields on meshes [3, 4]. Approximate Killing fields have also been used for the decomposition of 2-tensors in a compact region of 2D Euclidean space [14], and for non-rigid image registration [13].

4 Summary of Implementation

5 Summary of Results

While using MATLAB for the implementation, a solution for the sparse linear system with a pre-conditioned incomplete Cholesky conjugate gradient solver, which illustrated the observer field-relative visualisation and objective vortex detection by using standard vortex measures. The author achieved this by using the optimisation as well as the computation of w_r (observation time field). The authors were able to pinpoint the vortex cores for four centers with object core lines with a grid resolution of 64x64, time steps of 64, $u(x, t)$ 2:15 min and $w_r(x, t)$ 47 sec; Observer-related visualisation of core lines and swirling particles with a grid resolution of 390x210, time steps of 14, $u(x, t)$ 3 min and $w_r(x, t)$ 67 sec; 2D time-dependent vortex street with a grid resolution of 400x50, time steps of 1001, $u(x, t)$ 2:24 min and $w_r(x, t)$ 1:00 hrs; 3D time-dependent vortex street with a grid resolution of 192x64x48, time steps of 102, $u(x, t)$ 7:12 hrs.

6 Analysis and Discussion

The initial proof-of-concept provided benefits, but it could be optimised even further. A limitation is that computation time goes up as the time sequence gets longer. It was also observed, initially, that rigid body rotation had a velocity magnitude profile modulated by a horizontal wave function which created an unsteady input field v .

The authors have been able to make their framework work globally, but implicitly still adapts locally. Unlike the approach of Gunther et al. [17] depends on a fixed neighbourhood size that is not adapted, showing that the framework is a significant benefit.

References