

# Visualization, Lecture

## Volume Visualization

### Part 2

## Direct Volume Visualization



# Overview: Current Lecture

## Contents of Current Lecture:

- introduction to direct volume visualization
- ray functions
- ray casting
- compositing

# Direct Volume Visualization

## Overview:

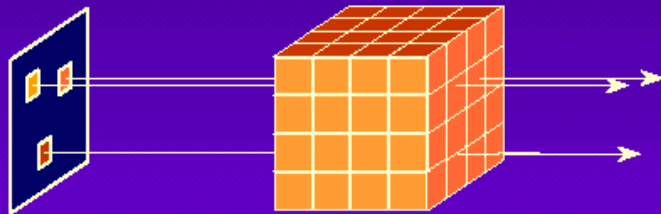
- No intermediate representation
- “Real 3D”
- Integration of so much information: difficult
- Object-order vs. image-order rendering
- Various techniques (ray casting, shear-warp, texture mapping, etc.)
- Various rendering techniques (compositing, MIP, first-hit, average, etc.)

# Direct Volume Visualization

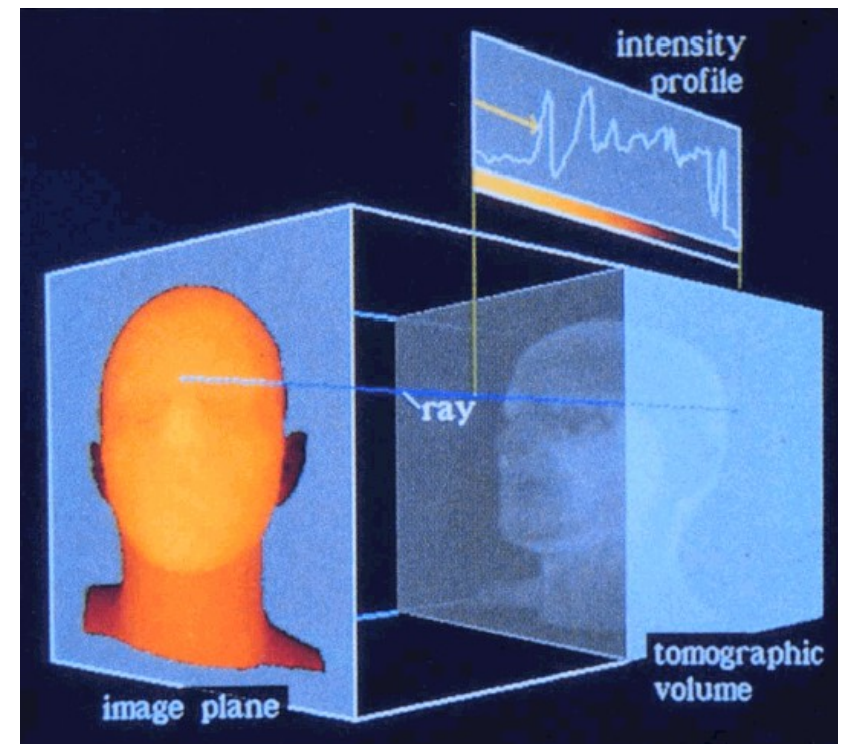
## Terminology:

- **Ray Casting:** the value of each pixel in the image is determined by sending a ray through the pixel into the scene (image order volume rendering)

Image-Order Approach: Traverse the image pixel-by-pixel and sample the volume.



Ray Casting



# Rendering Techniques: Ray Functions

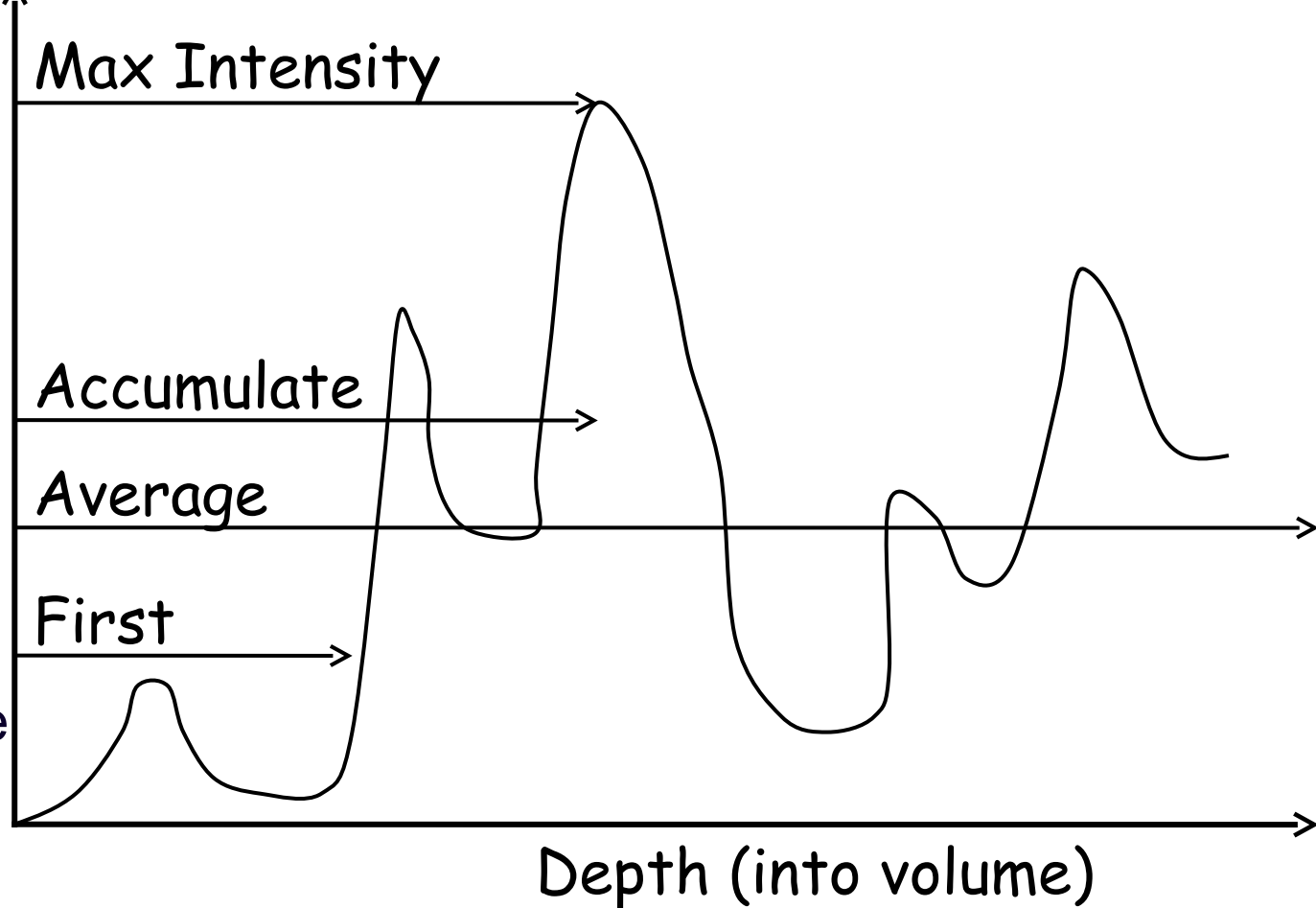
Ray Functions      Scalar

Overview:

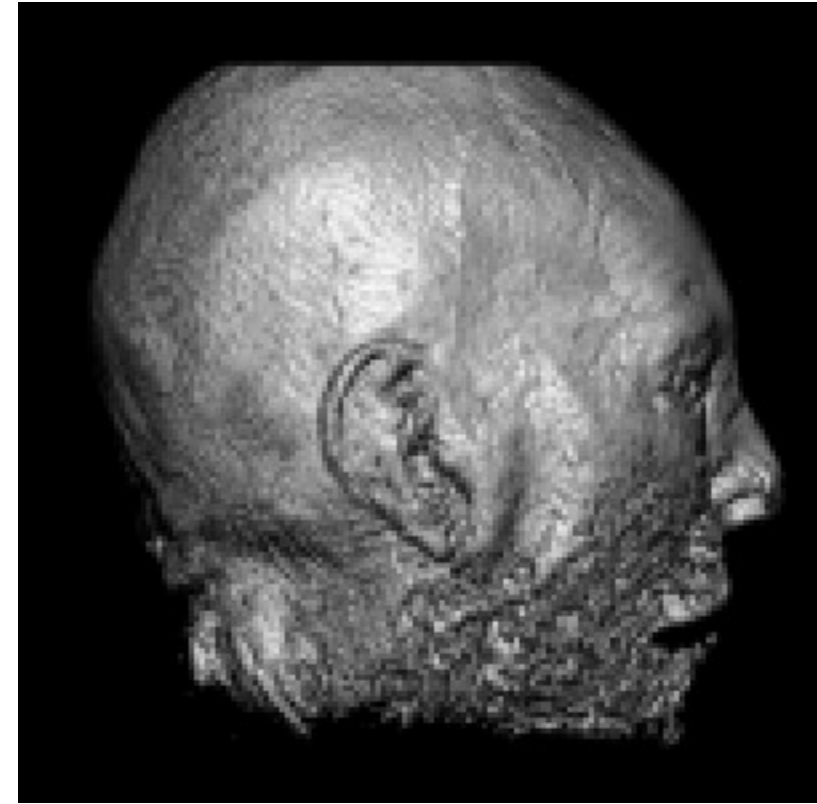
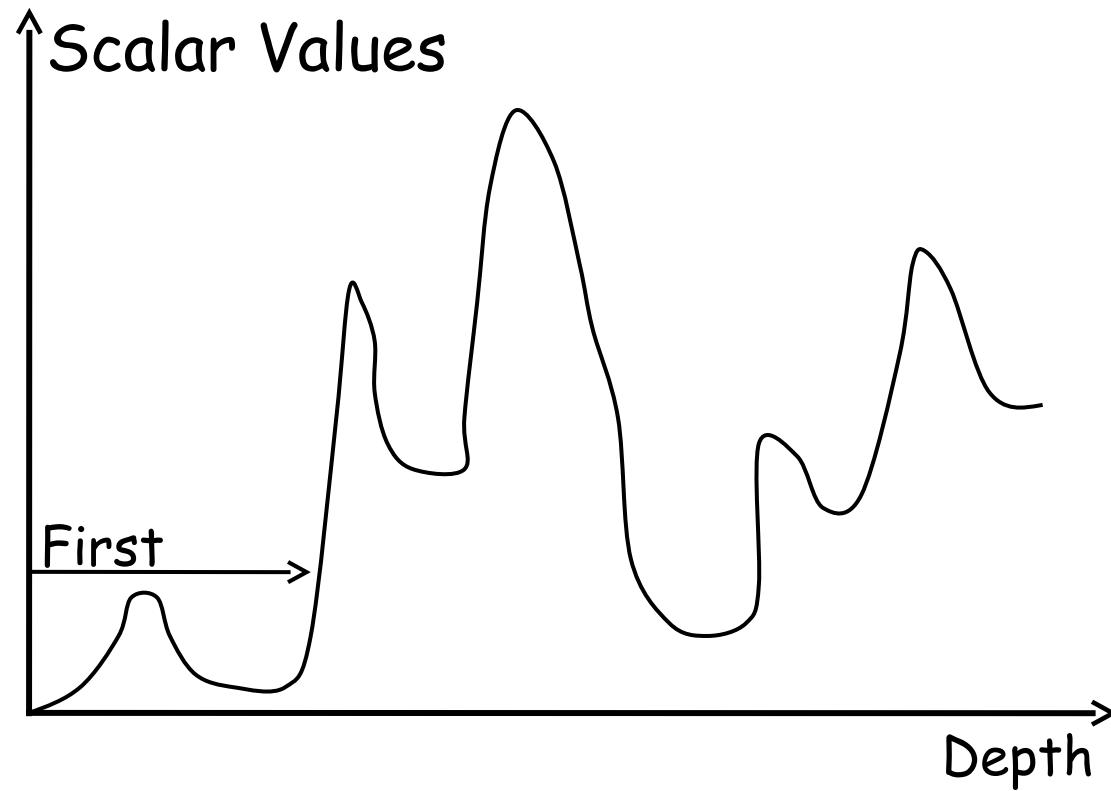
- MIP  
(Maximum Intensity Projection)
- Compositing
- X-Ray
- First Hit

Ray functions produce an *intensity profile*.

Values



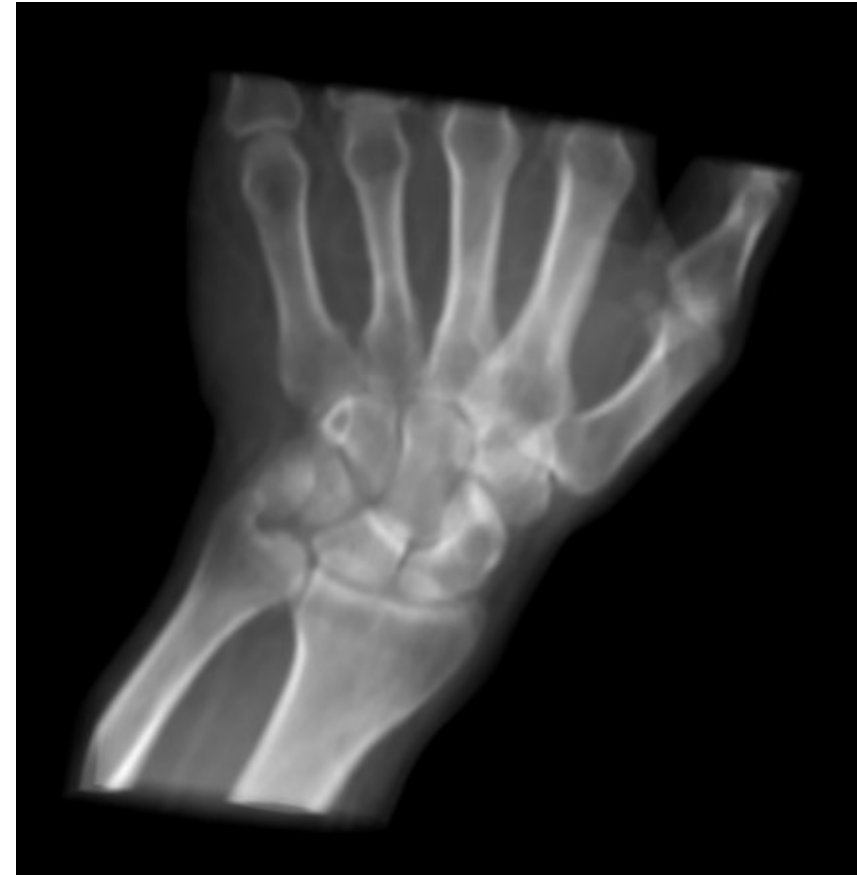
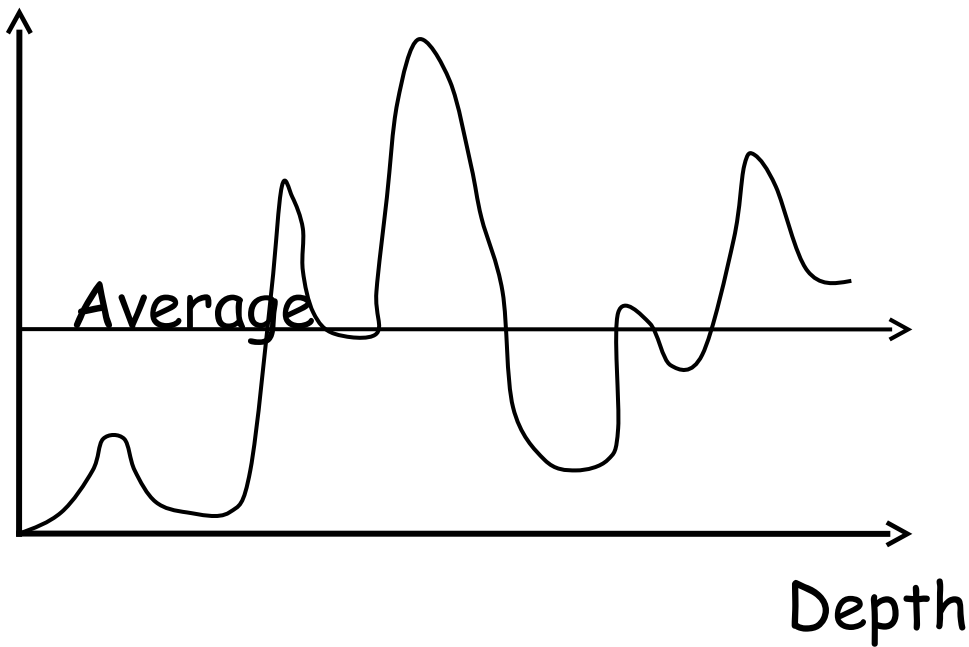
# First Hit: Iso-surface Extraction



**First Hit Ray Function:** Extracts iso-surfaces (again),  
done by Tuy&Tuy '84

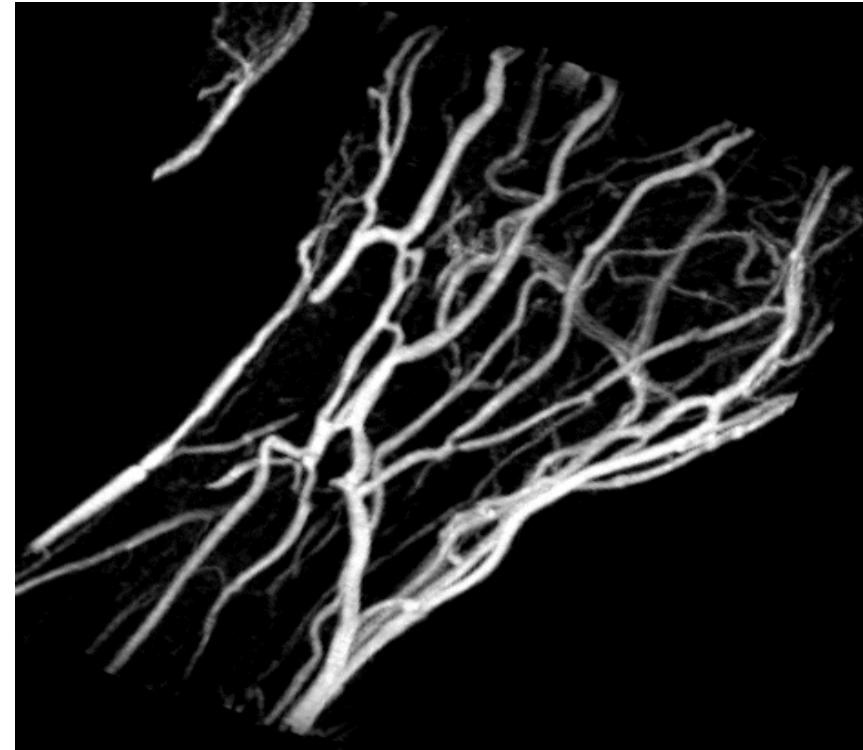
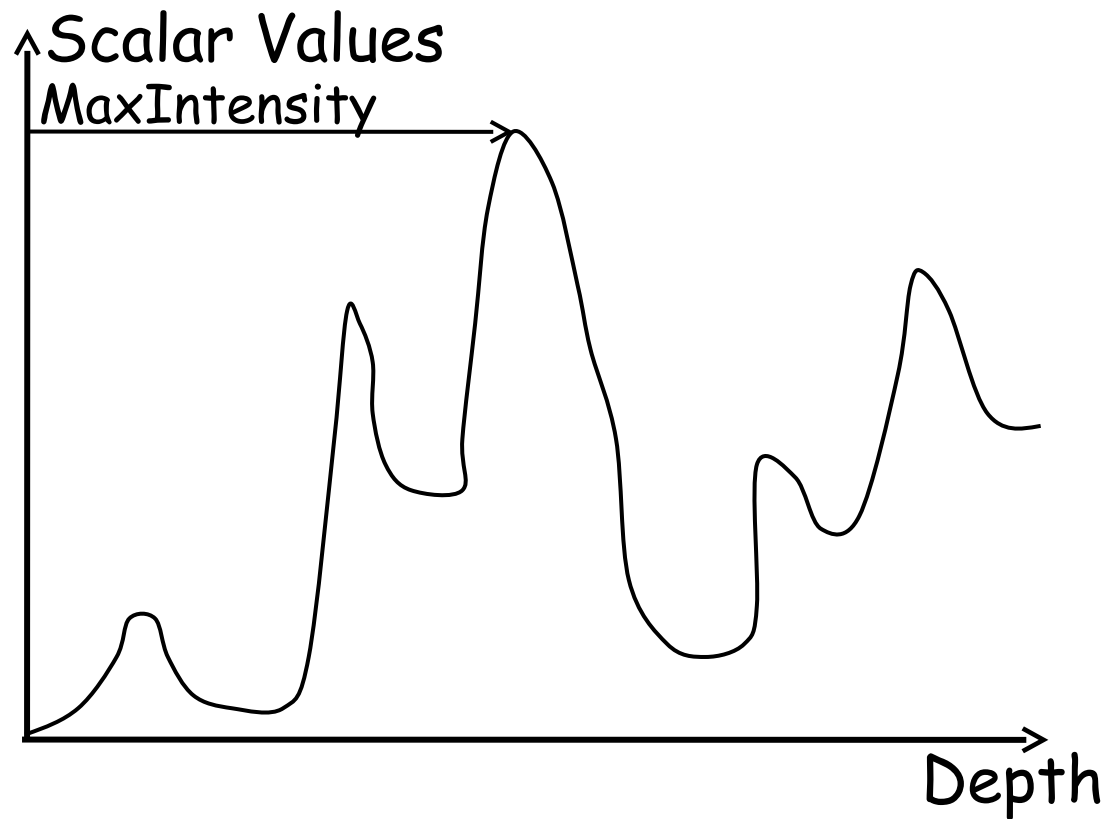
# Average: Like X-Rays

Scalar Field



**Average Ray Function:** Produces basically an X-ray picture

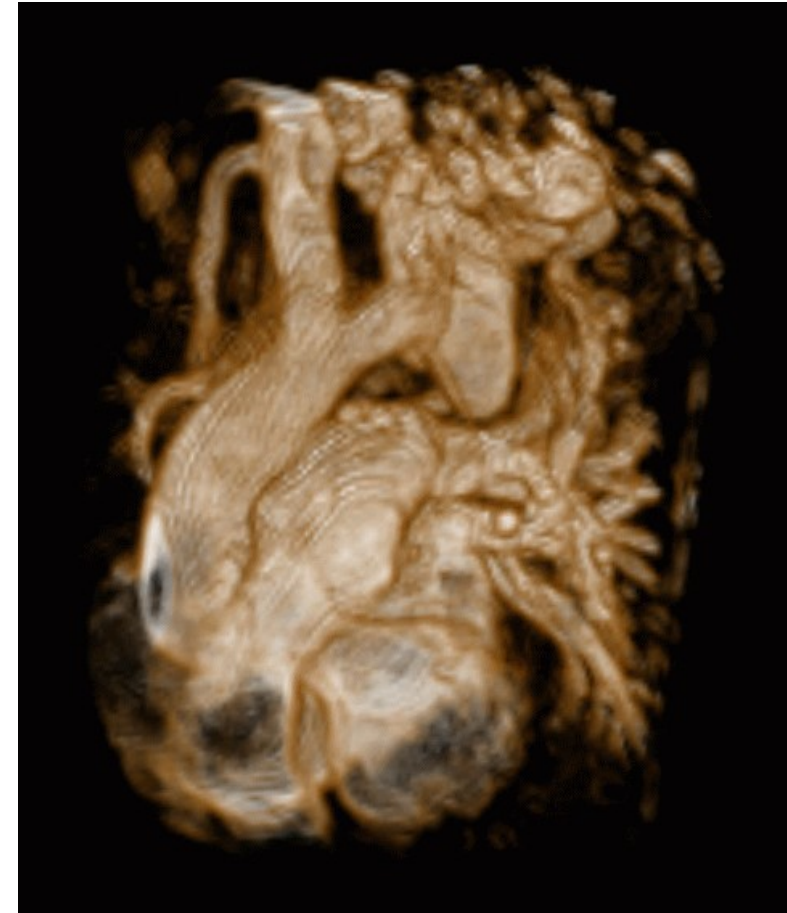
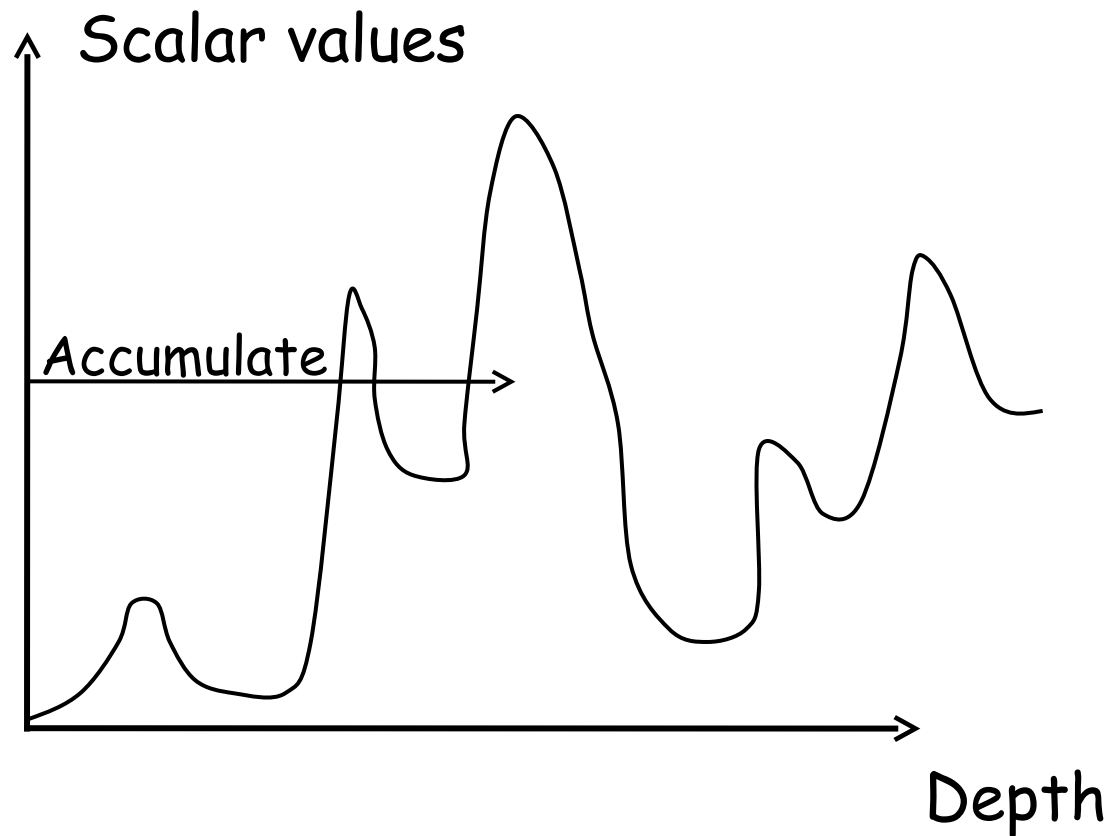
# MIP: maximum-intensity projection



**Max Ray Function: Maximum Intensity Projection (MIP)** used for Magnetic Resonance Angiogram (MRA)



# Compositing: Semi-transparency



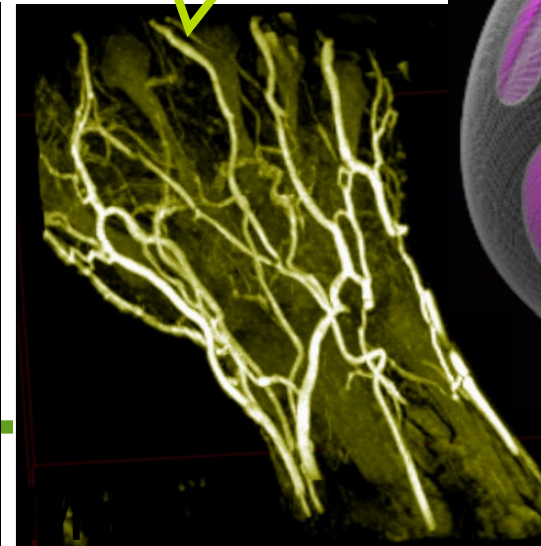
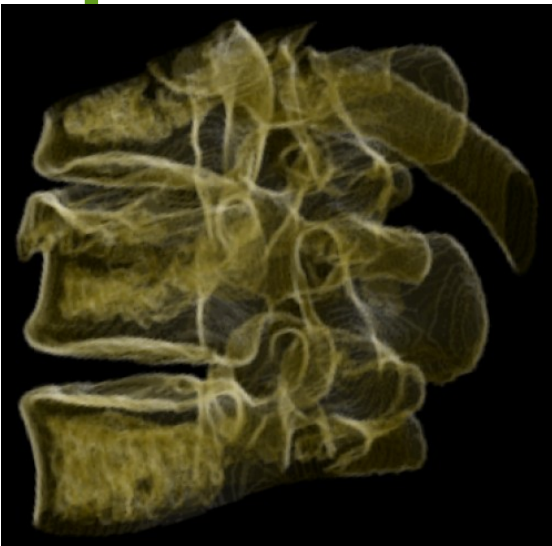
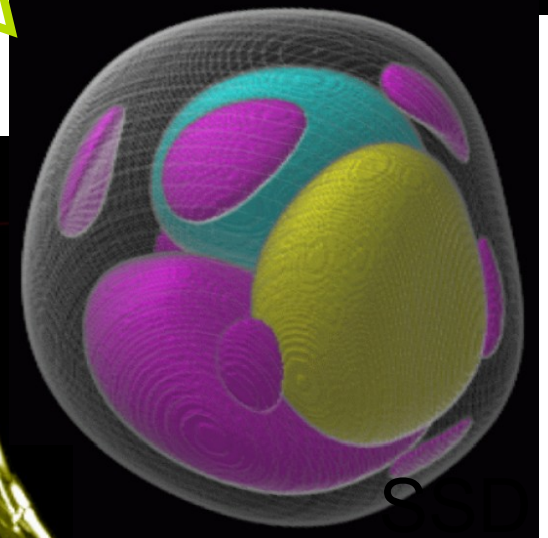
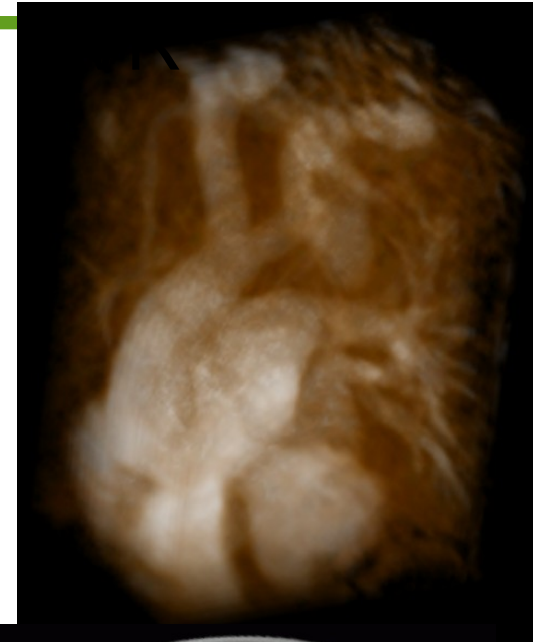
**Accumulate:** Make transparent layers visible.

Levoy '88

# Combining Ray Functions

## Some Possibilities:

- $\alpha$ -compositing
- shaded surface display
- maximum-intensity projection
- x-ray simulation
- contour rendering



# The Ray Casting Pipeline

## Classical Image-Order Method

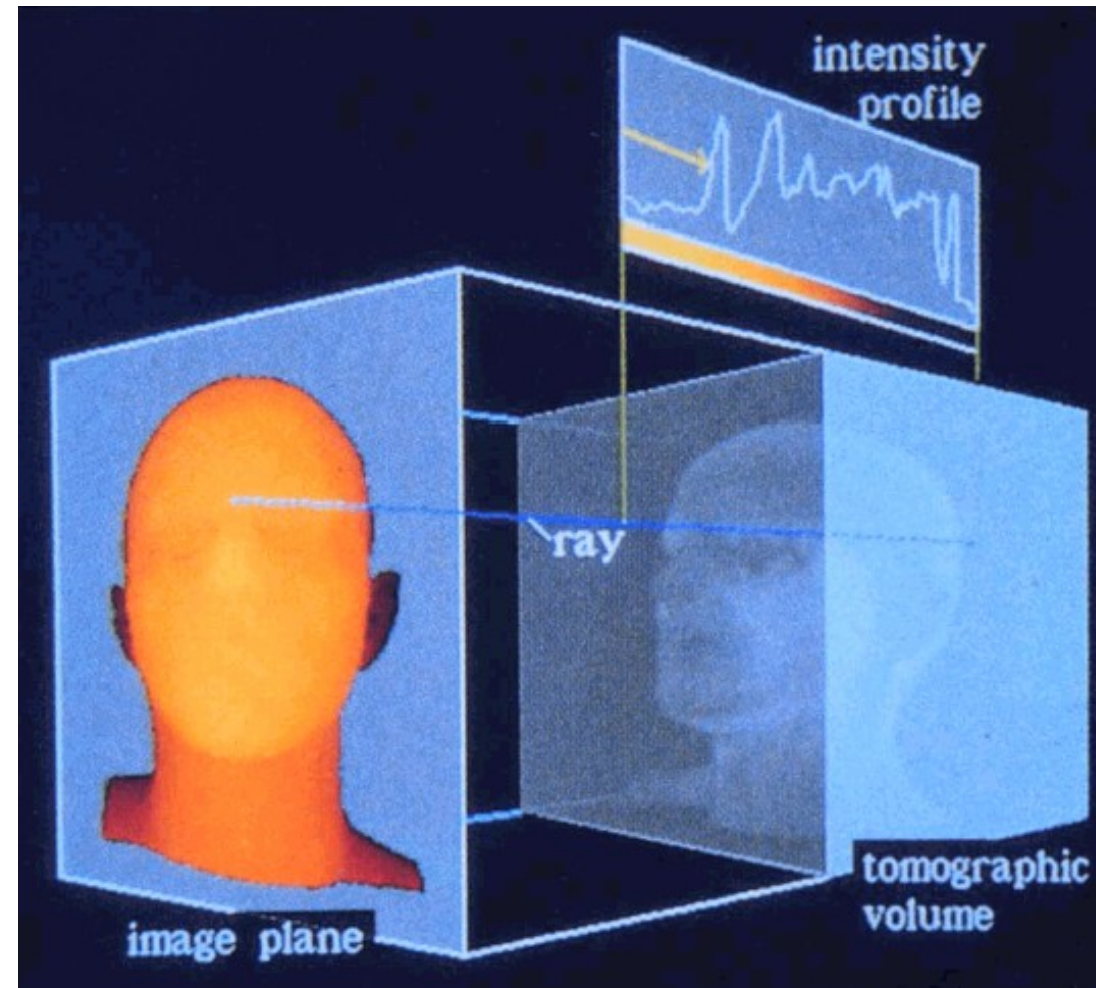
# Ray Tracing vs. Ray Casting

- Ray Tracing: image generation method
- In volume rendering: only primary light scattering --> thus Ray Casting
- Classical image-order method
- Ray tracing: radiate object surface or slices  
Ray casting: no objects, just scalar (e.g. density) values in 3D
- Theory: consider all density values  
Practice: traverse volume slice by slice
- Interpolation necessary per slice

# Ray Through Volume Data

## Overview:

- Volume Data: 1D values defined in 3D,  $f(\mathbf{x}) \in \mathbb{R}^1$ ,  $\mathbf{x} \in \mathbb{R}^3$
- Ray defined as half of a line:  $\mathbf{r}(t) \in \mathbb{R}^3$ ,  $t \in \mathbb{R}^1_{>0}$
- Values along Ray:  
 $f(\mathbf{r}(t)) \in \mathbb{R}^1$ ,  $t \in \mathbb{R}^1_{>0}$   
(intensity profile)





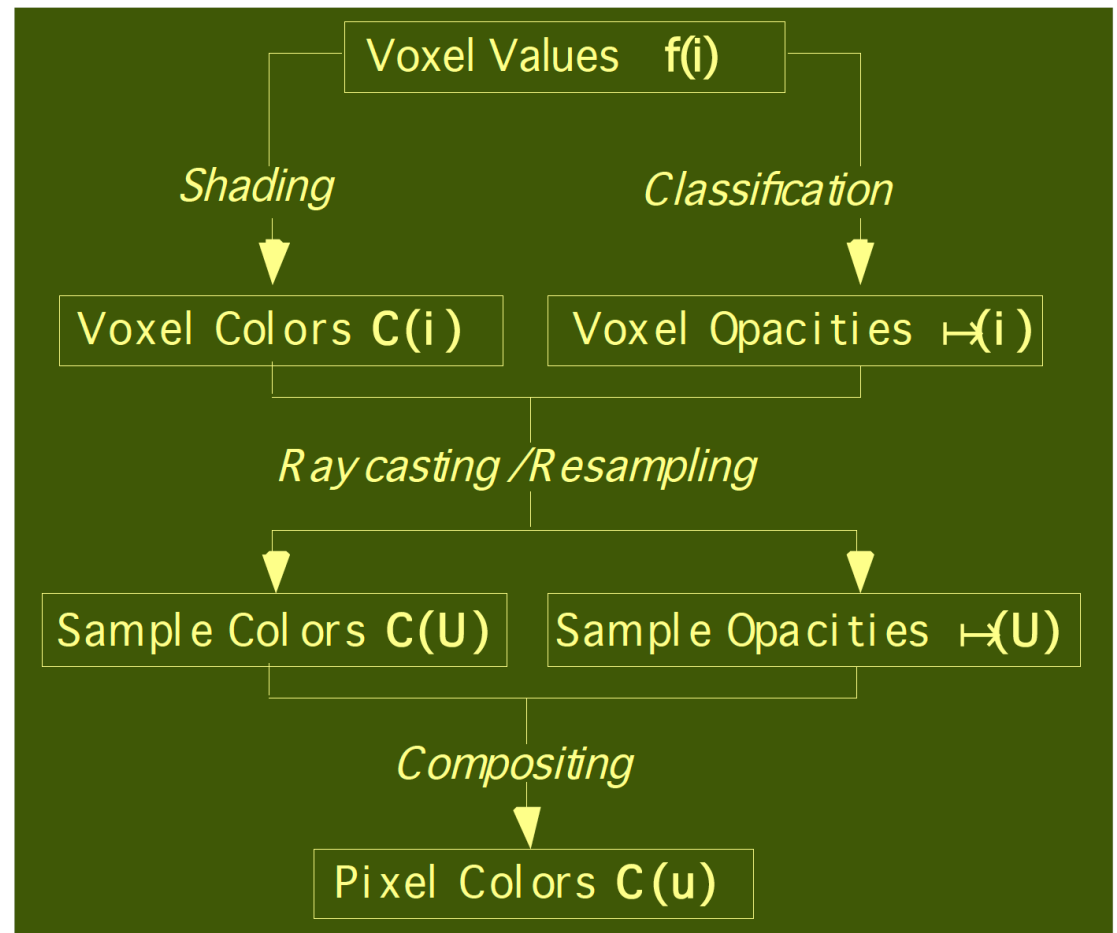
# The Ray Casting Pipeline

Levoy '88:

1. set color and alpha (using transfer function)

2. Ray casting, interpolation

3. Compositing



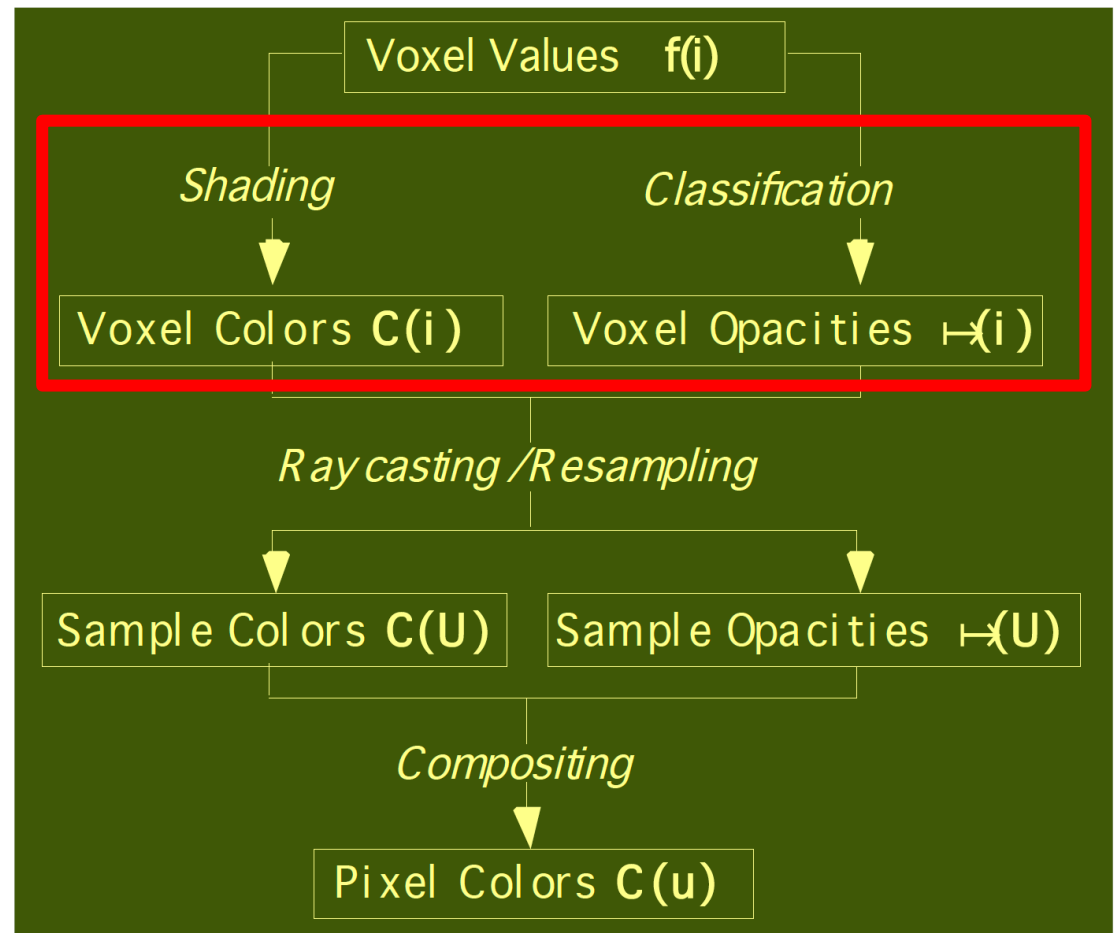
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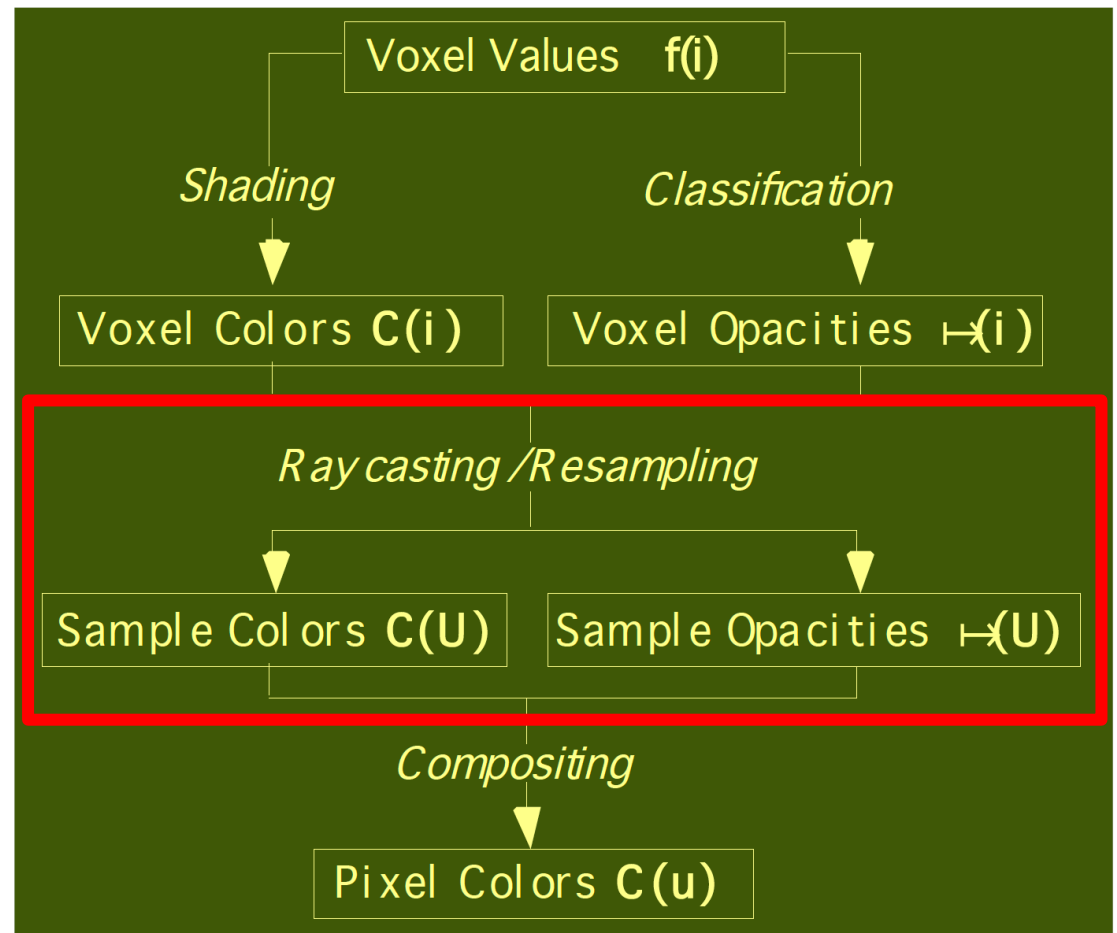
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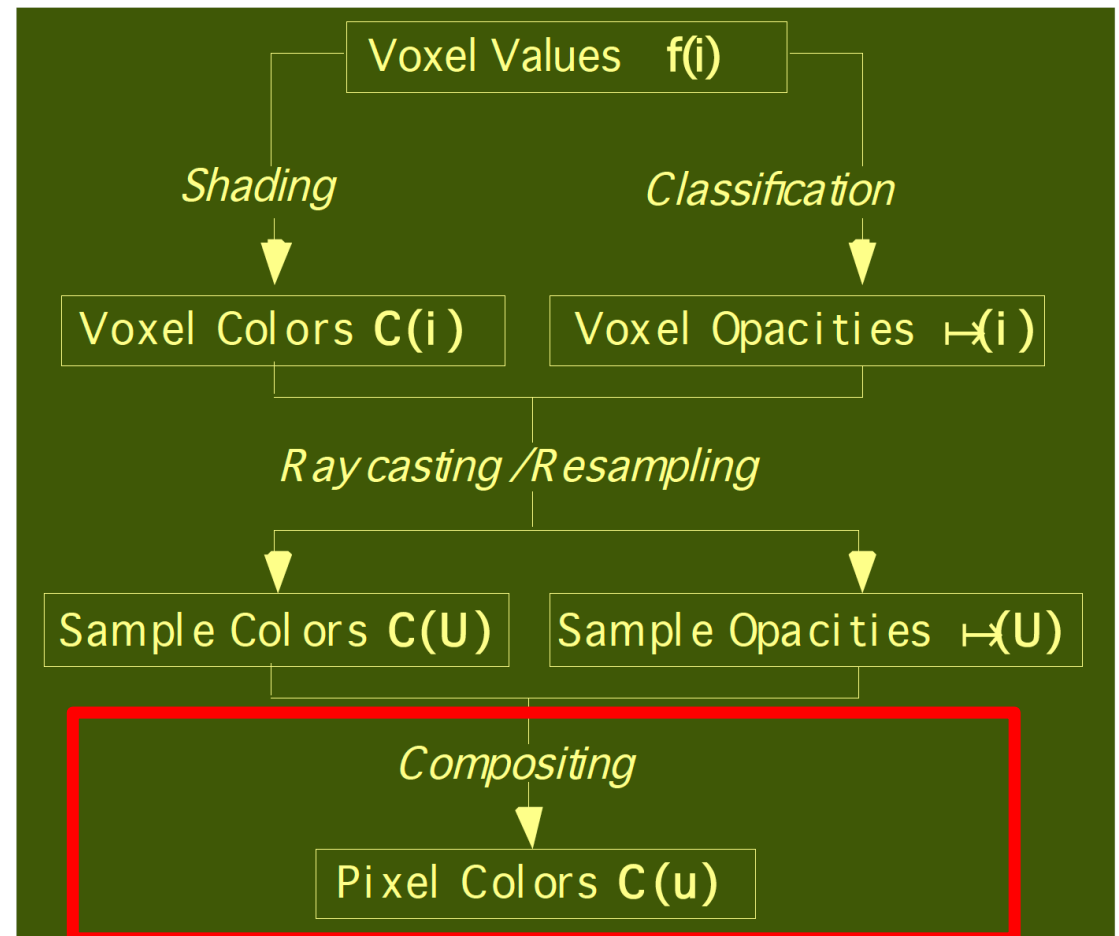
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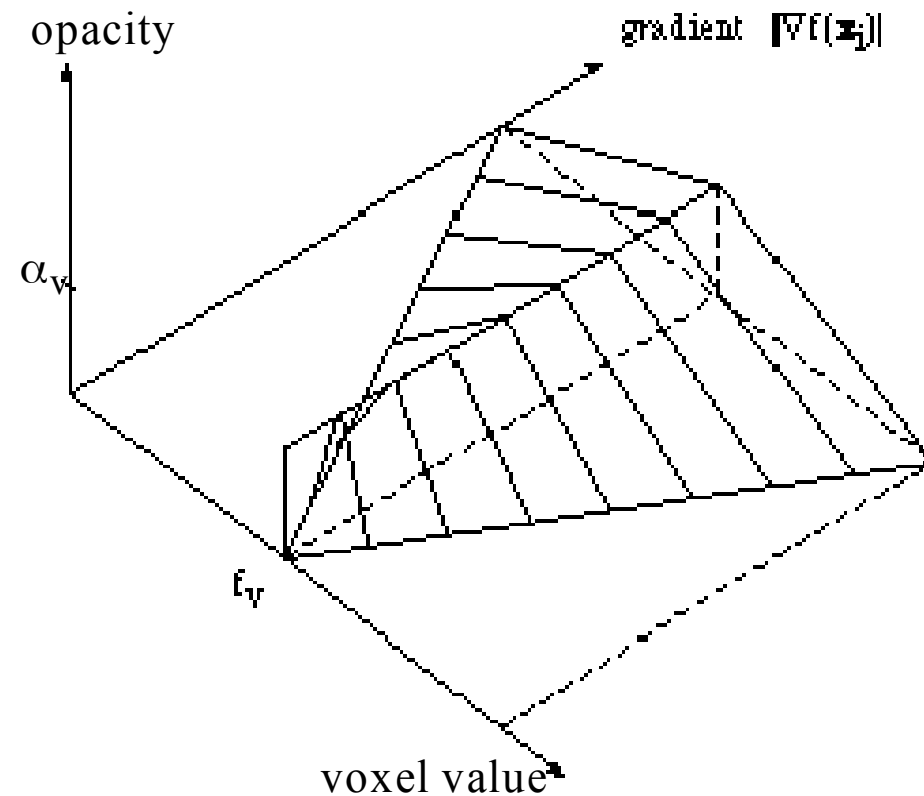
# 1. Shading and Classification of Voxel Values

voxel shading according to transfer function

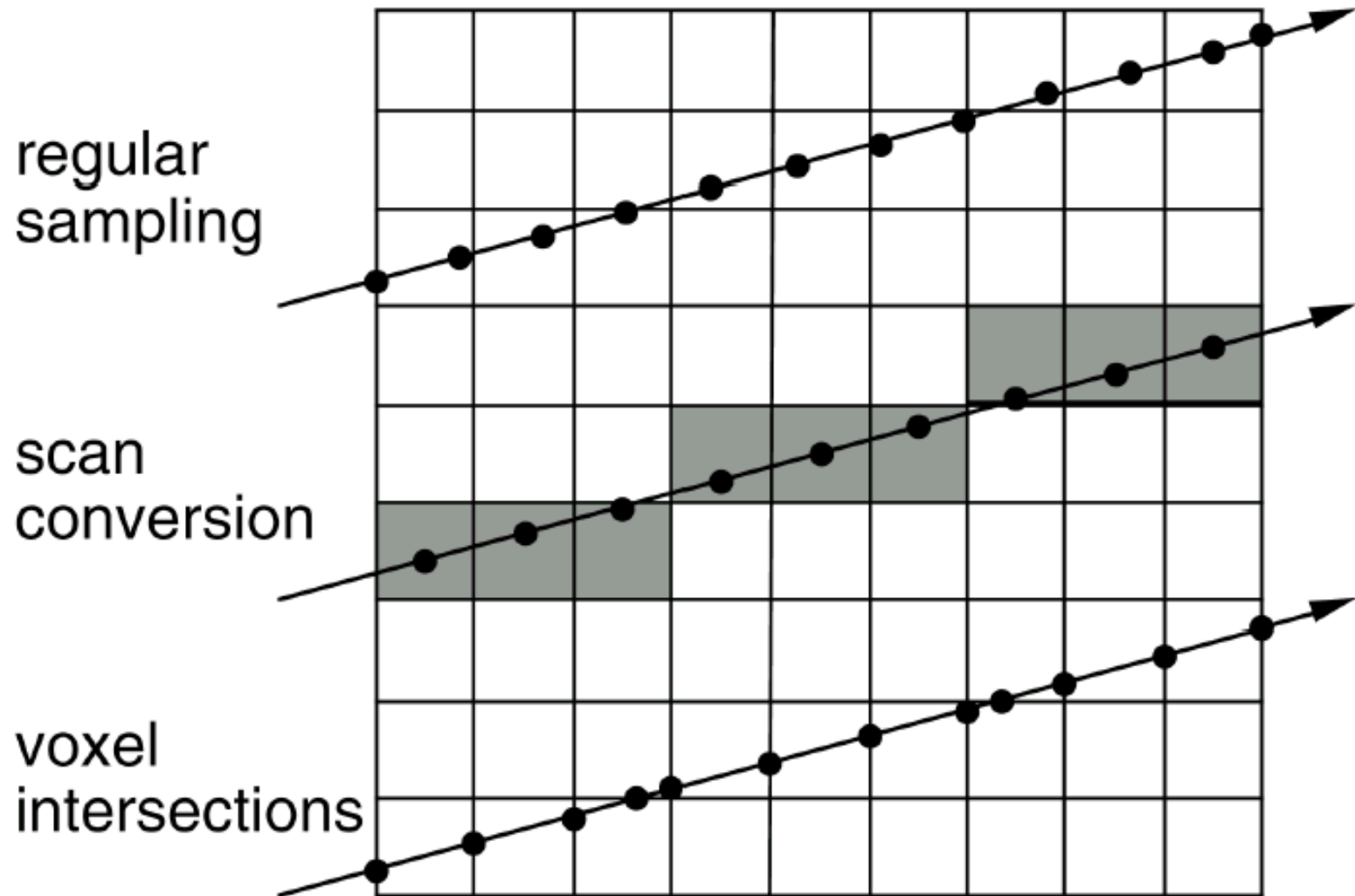
- diffuse shading (Phong), gradient used to derive normals

voxel classification,  $f(i) \rightarrow \alpha(i)$ :

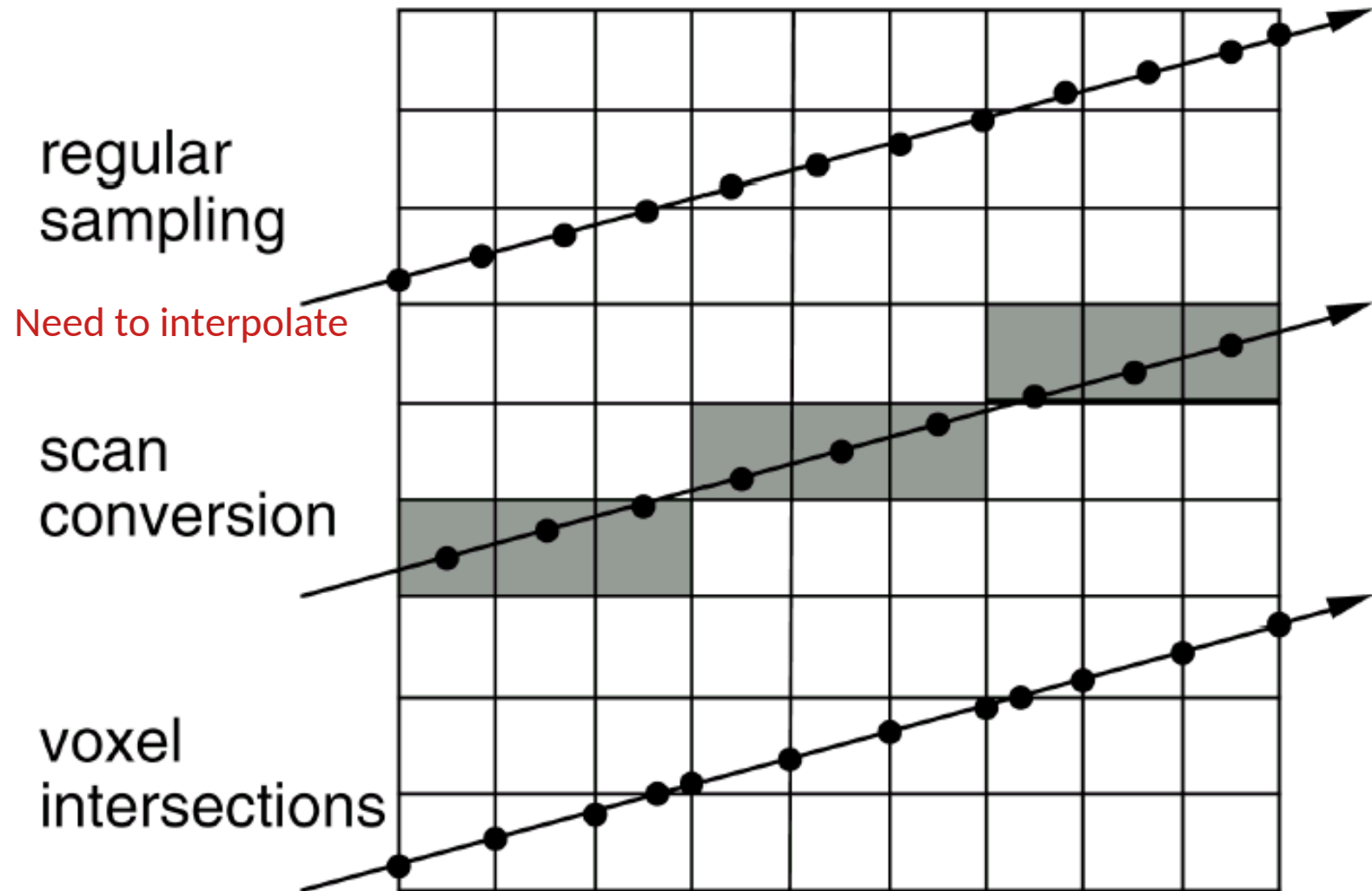
- according to gradients
- emphasizes transitions/boundaries



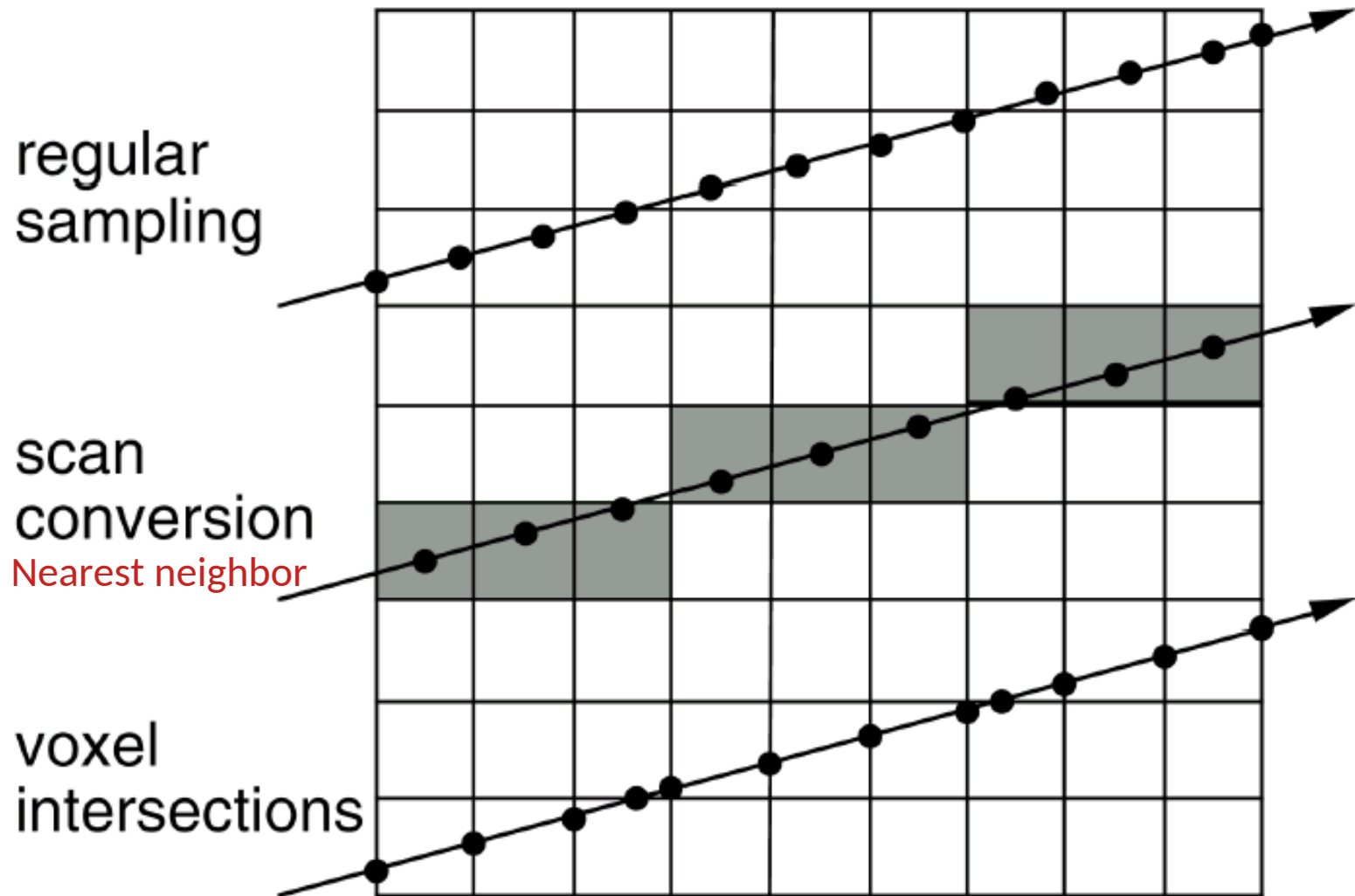
## 2. Ray traversal – Three Approaches



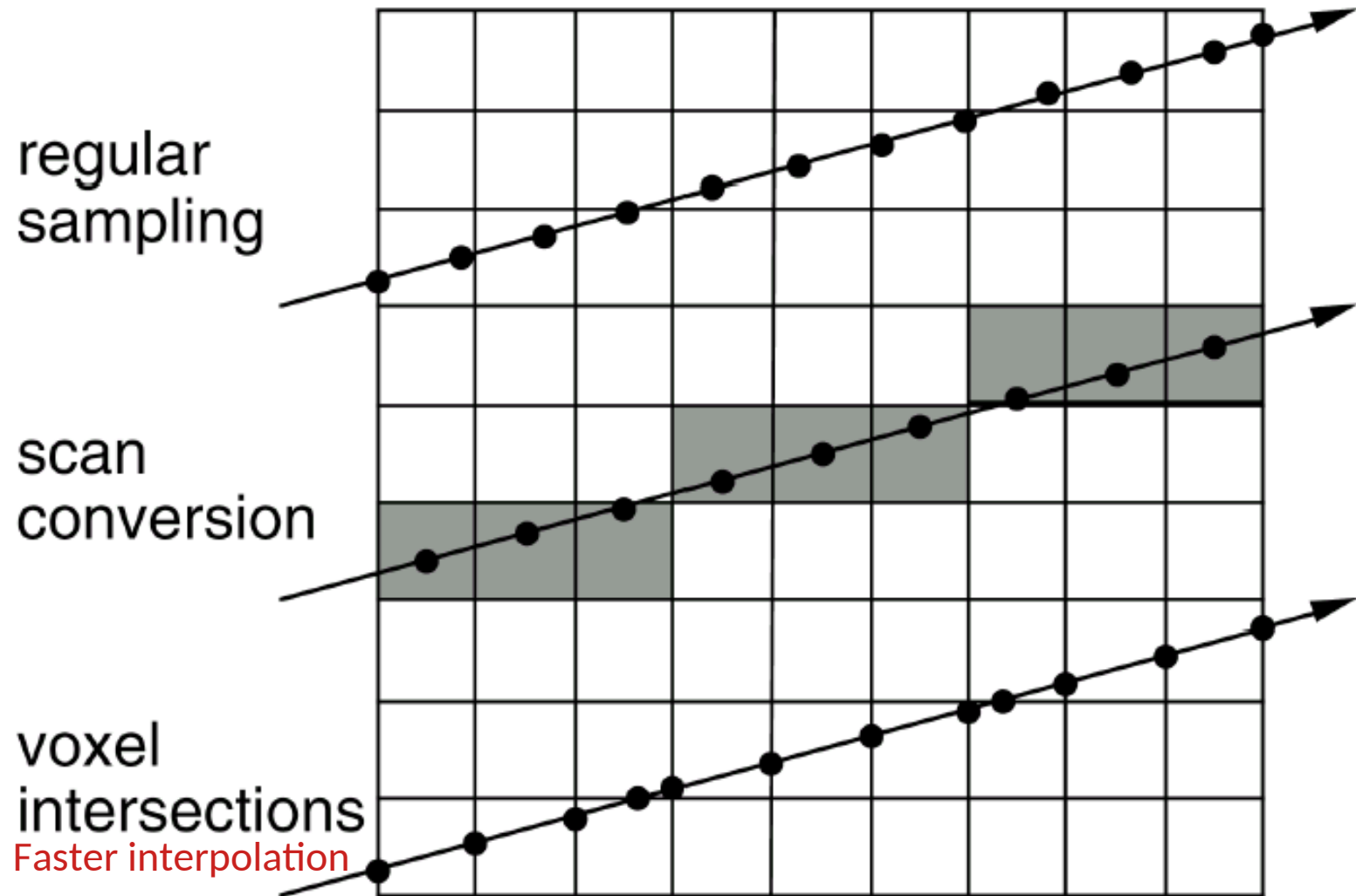
## 2. Ray traversal – Three Approaches



## 2. Ray traversal – Three Approaches



## 2. Ray traversal – Three Approaches



## 2. Ray Traversal, Interpolation

- Voxel-based vs. cell-based ray traversal
- Tri-linear (interpolation within the cell)  
vs. Bi-linear (interpolation along cell edges)
- Tri-linear:
  - first 4\* in z-Direction (Quadratic interpolation),
  - then 2\* in y-Direction (Linear interpolation),
  - then 1\* in x-Direction (value interpolation)

# 3. Compositing

## Terminology

**compositing:** the sample-by-sample accumulation of color and opacity values along a ray as it traverses volume data. –bob

**kernel:** (a.k.a. convolution kernel a.k.a. convolution filter) “one or two dimensional images that are used for computing the weighted average of pixel images”  
–The OpenGL Programming Guide



# 3. Compositing: F2B vs. B2F

## Back-to-Front (B2F):

- $c = c(1 - \alpha(i\Delta s)) + C(i\Delta s)$
- $\alpha = \alpha(1 - \alpha(i\Delta s)) + \alpha(i\Delta s)$

## Front-to-Back (F2B):

- $c = C(i\Delta s) \alpha(i\Delta s) (1 - \alpha) + c$
- $\alpha = \alpha(i\Delta s)(1 - \alpha) + \alpha$

$c$  = current color

$\alpha$  = opacity (inverse of transparency)

$i$  = sample index

$s$  = sample

$\Delta s$  = distance between samples

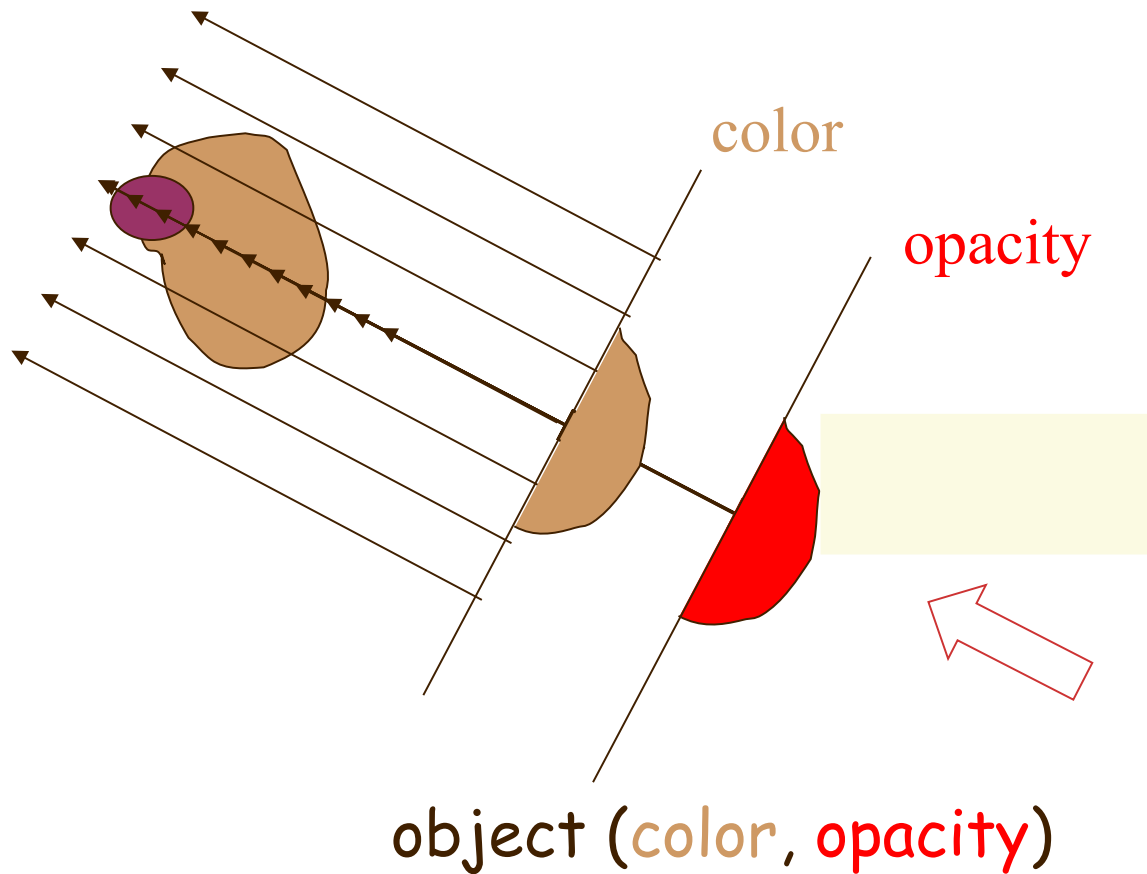
$C$  = color at sample

# Compositing: F2B vs. B2F

F2B: a ray can be stopped once opacity approaches 1.0 -early ray termination.

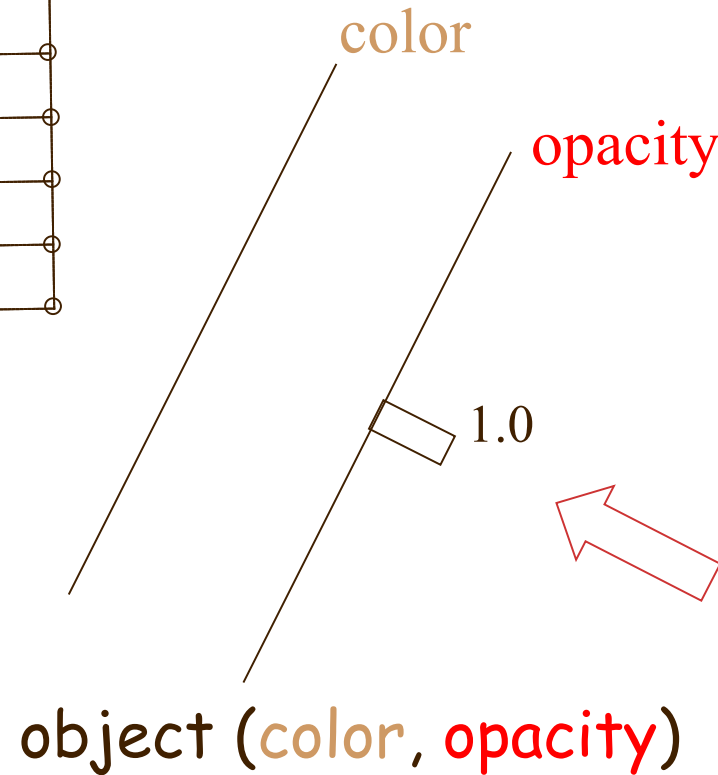
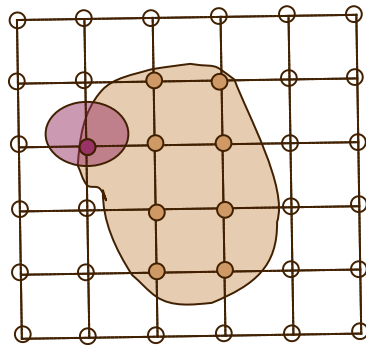
B2F: a generalization of the Painter's algorithm –less frequently used.

# Volumetric Ray Integration

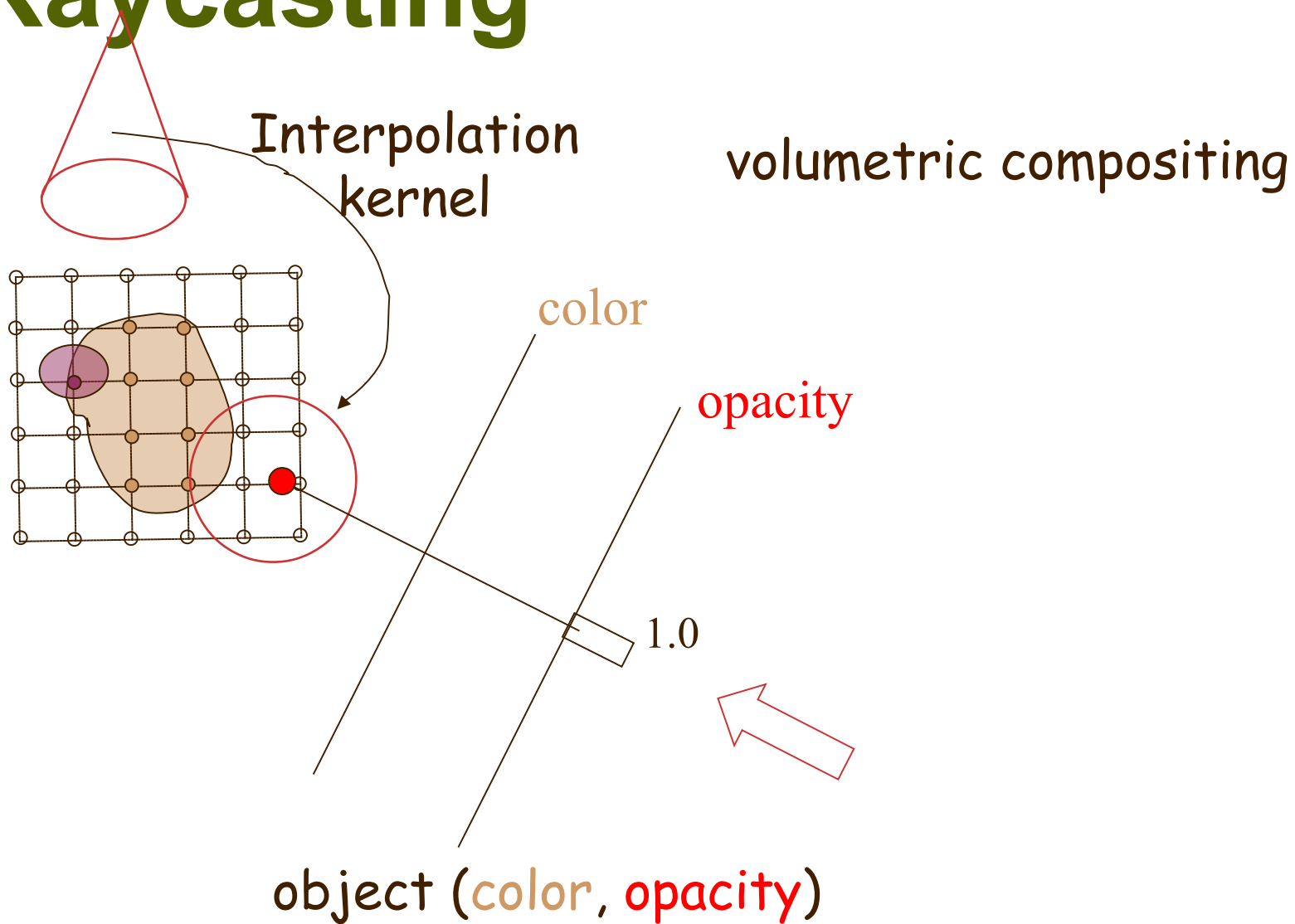


# Raycasting

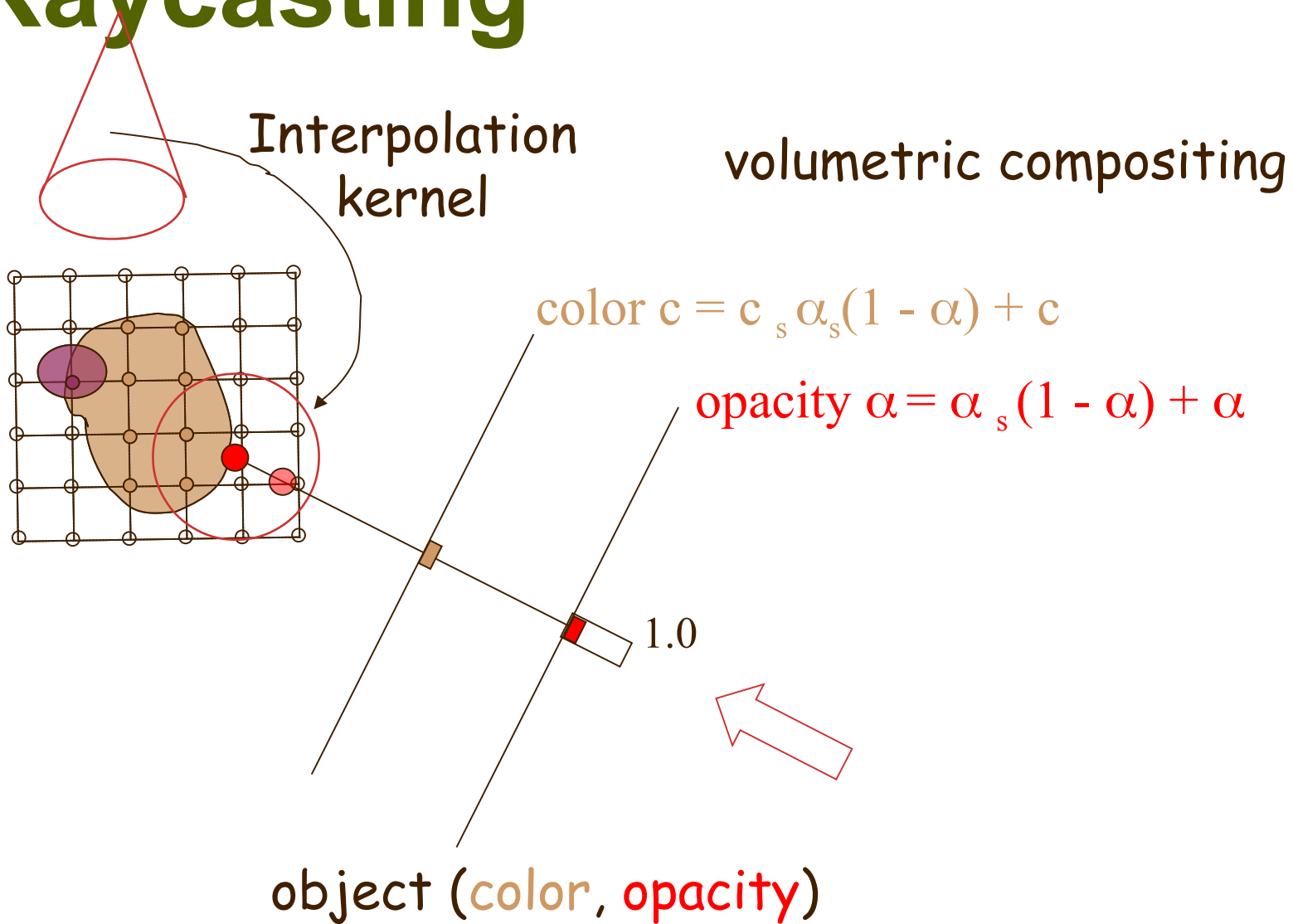
volumetric compositing



# Raycasting

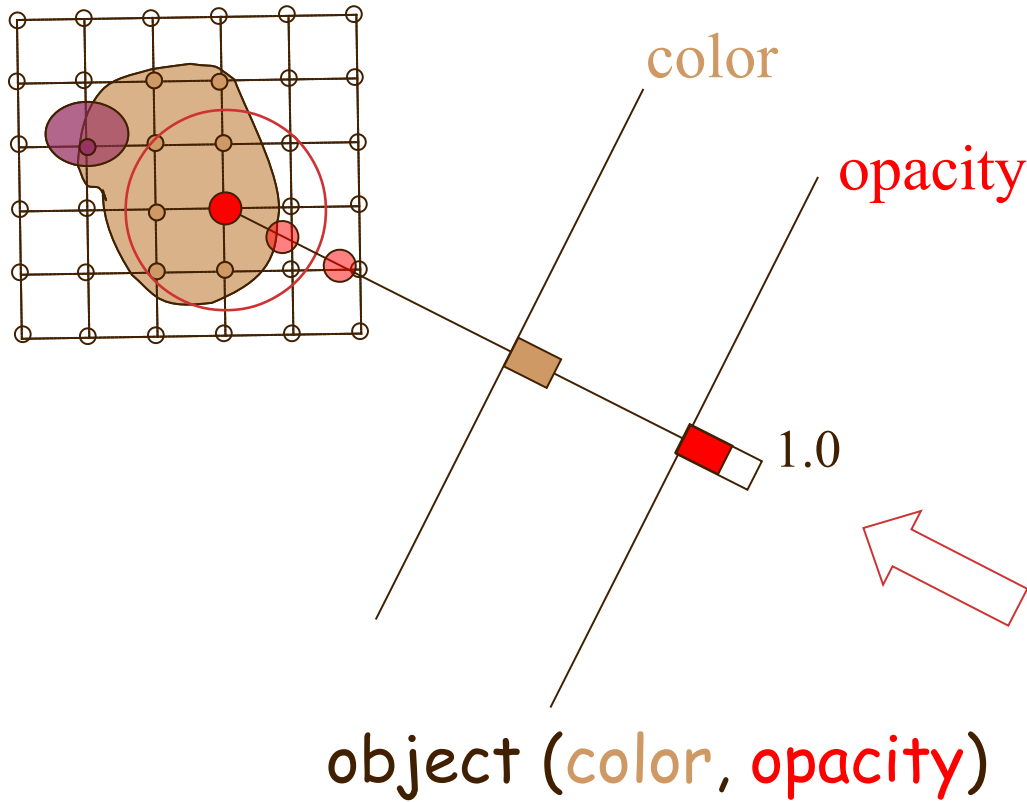


# Raycasting



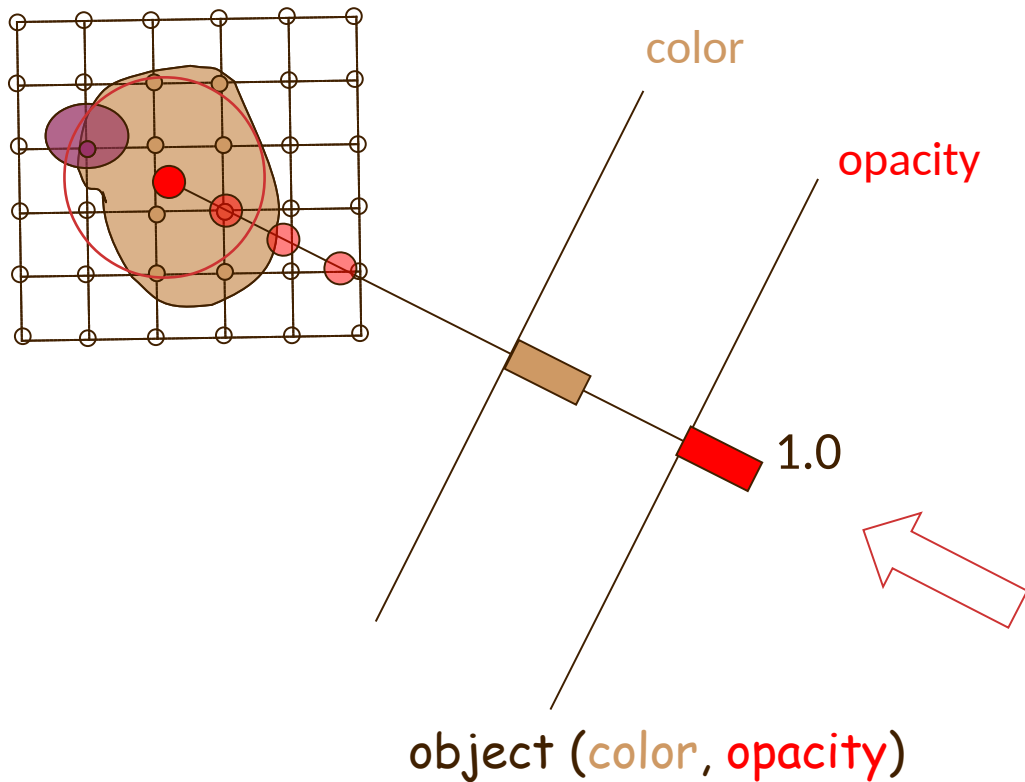
# Raycasting

volumetric compositing



# Raycasting

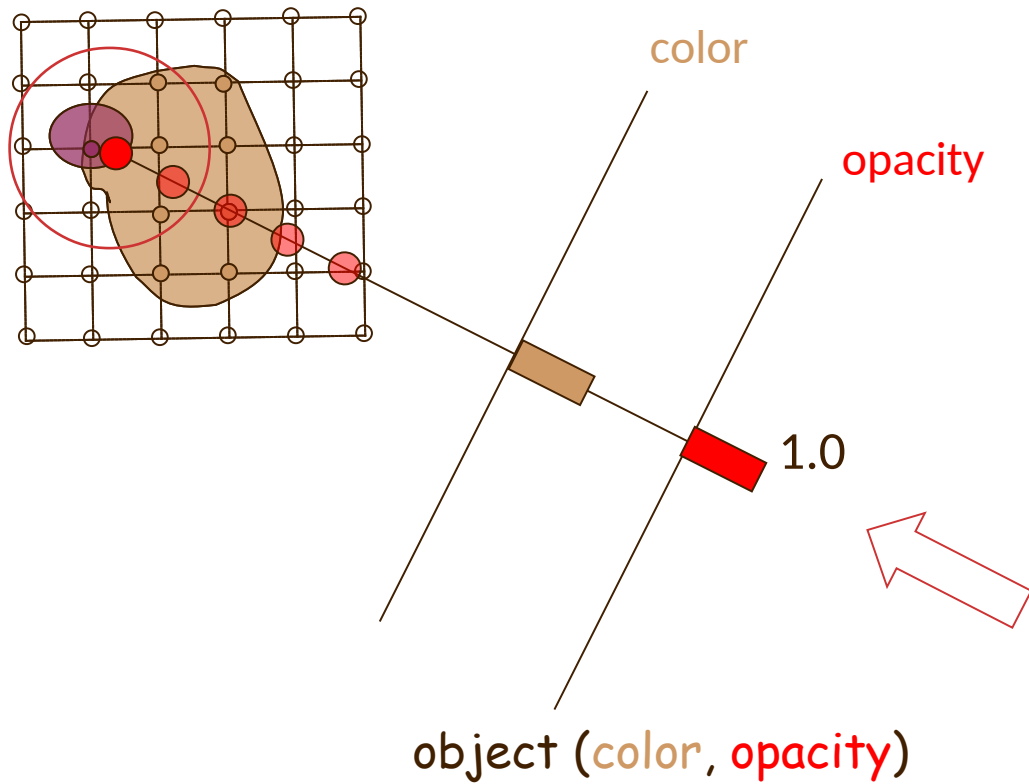
volumetric compositing





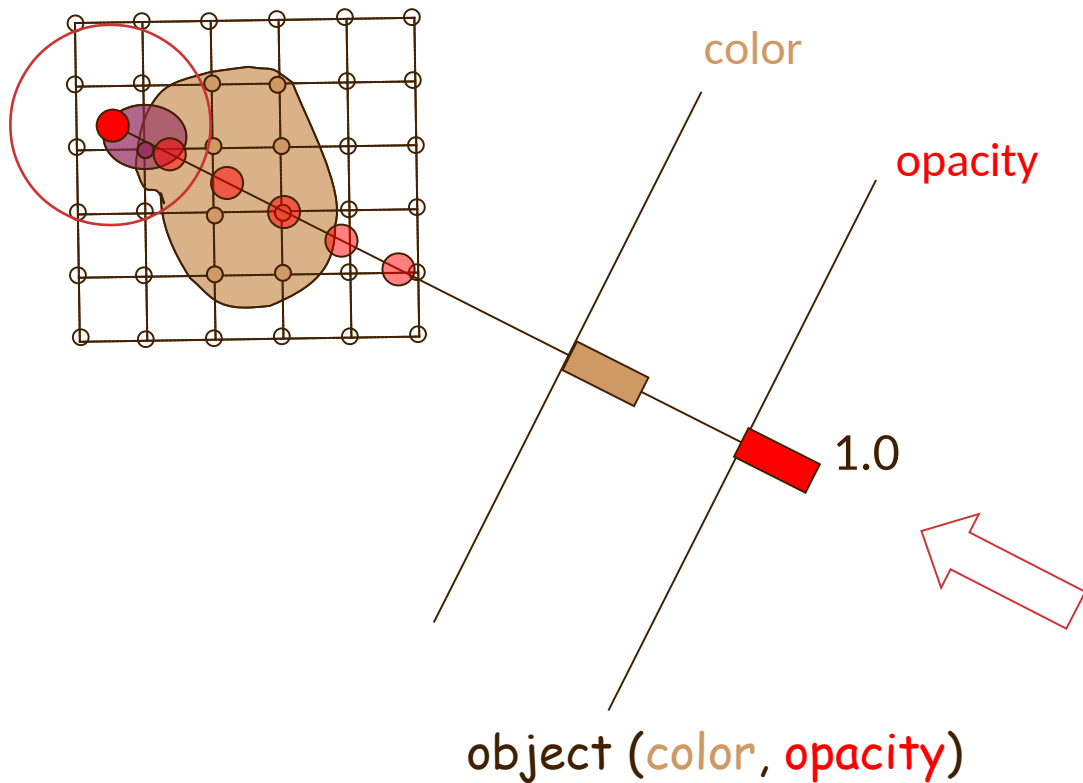
# Raycasting

volumetric compositing



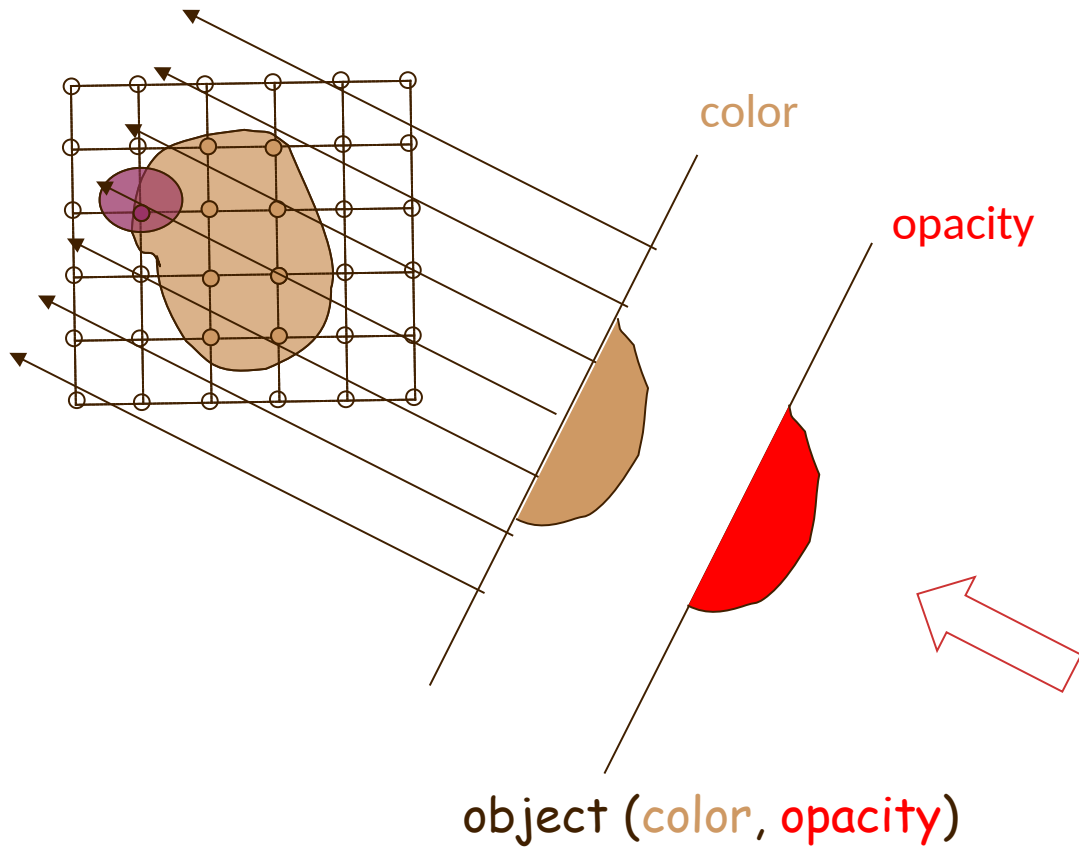
# Raycasting

volumetric compositing



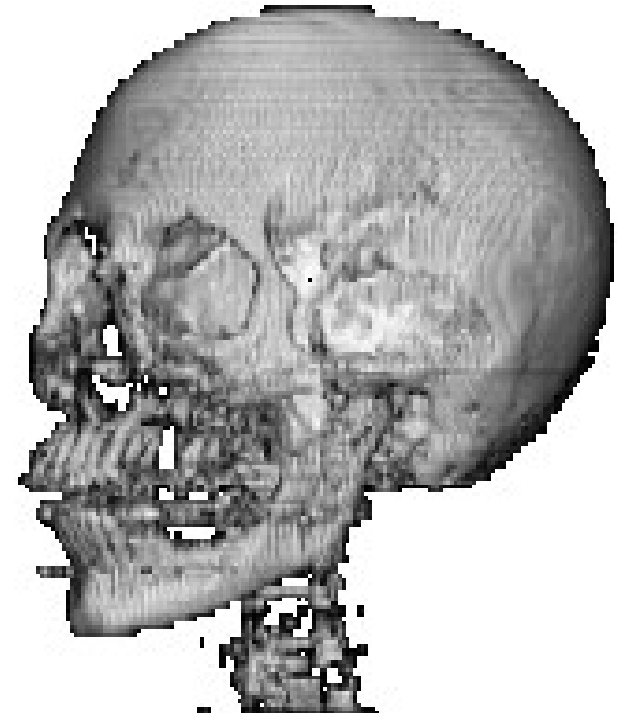
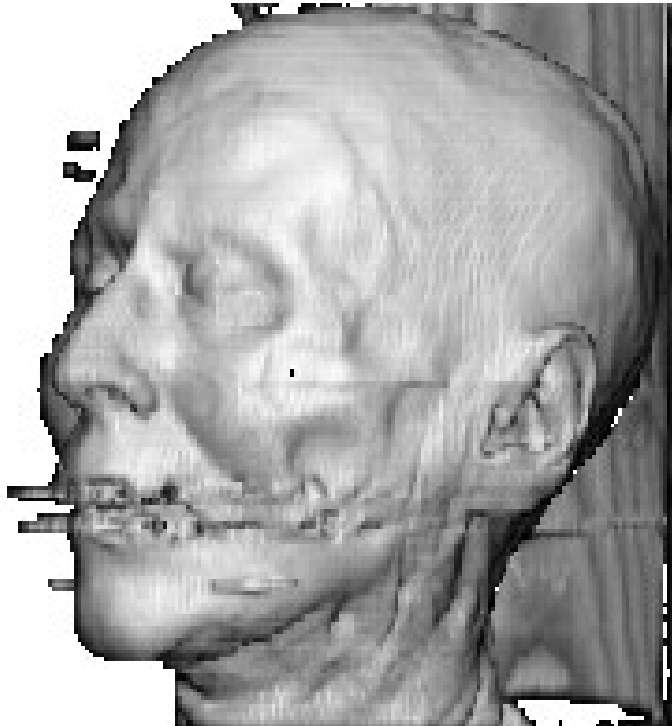
# Raycasting

volumetric compositing



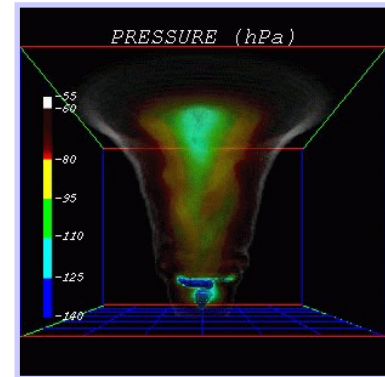
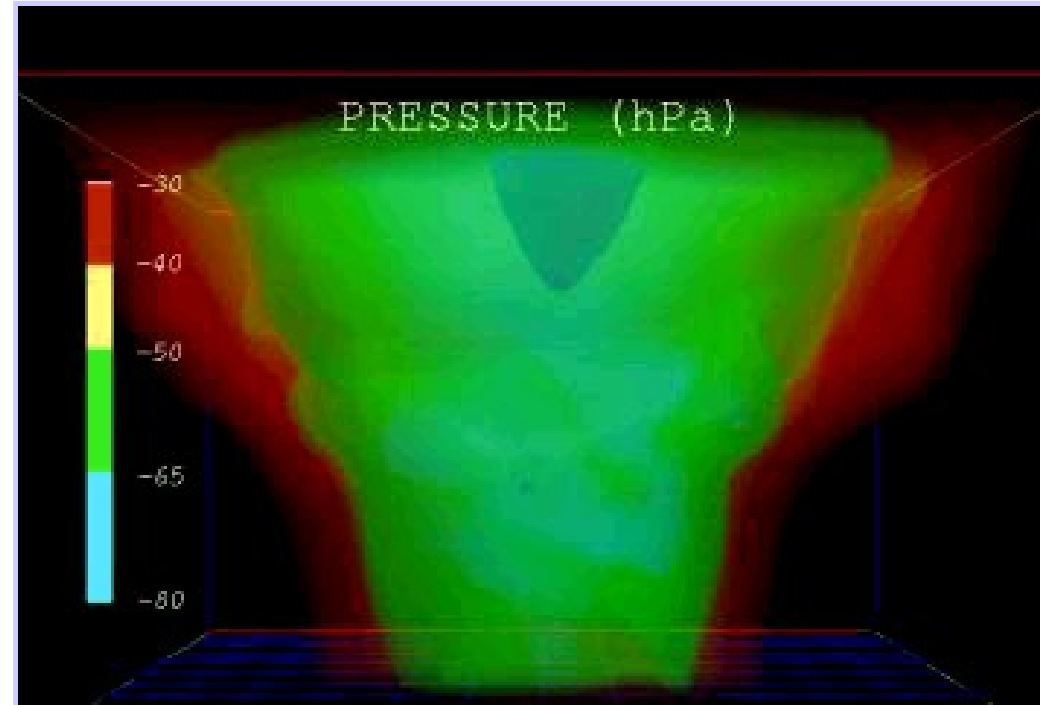
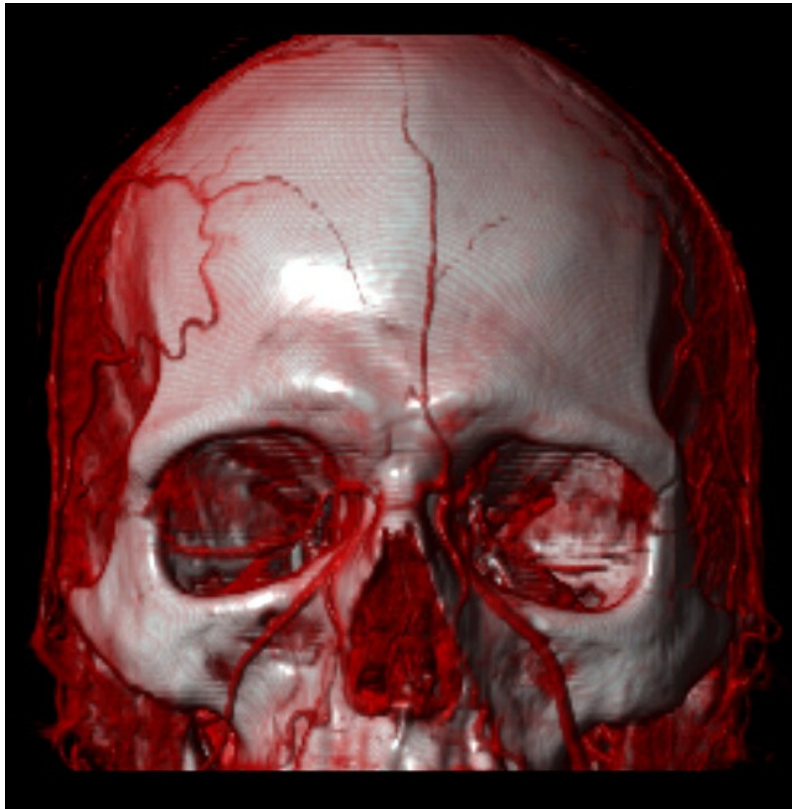
# Ray Casting – Examples

Different transfer functions (quasi-surface rend.),  
256 x 256 x 113 CT data



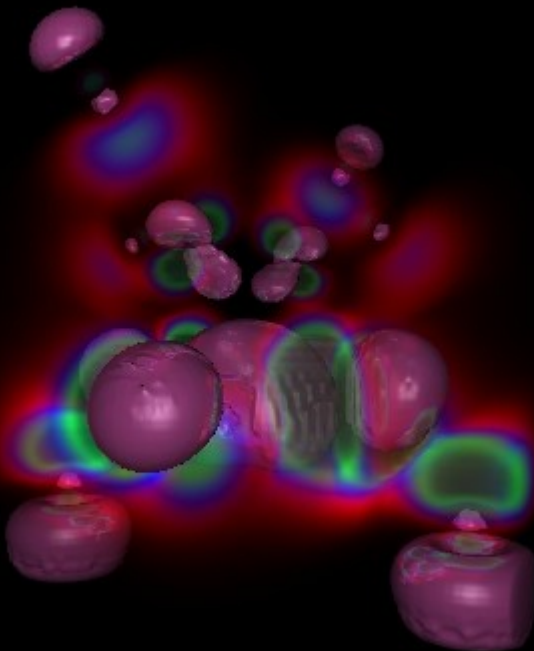
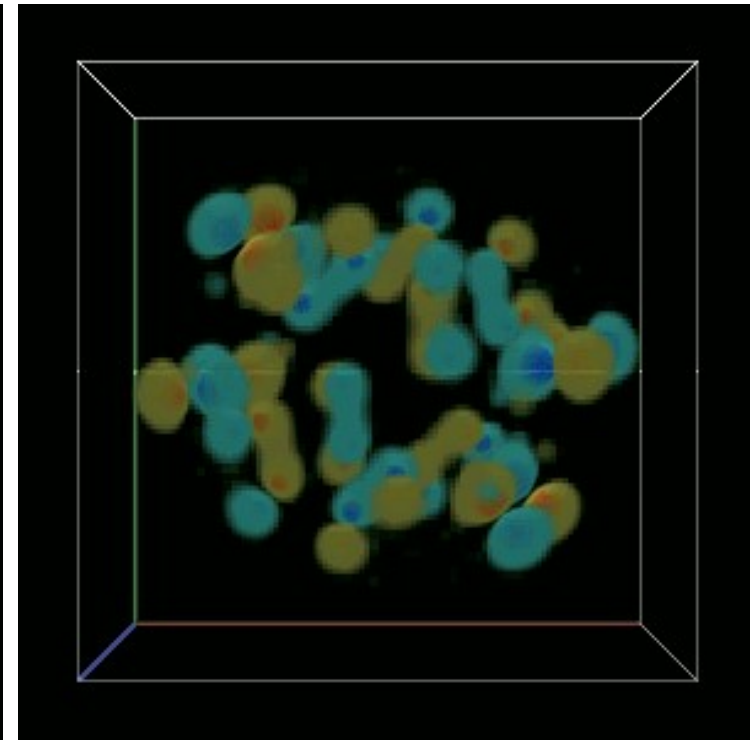
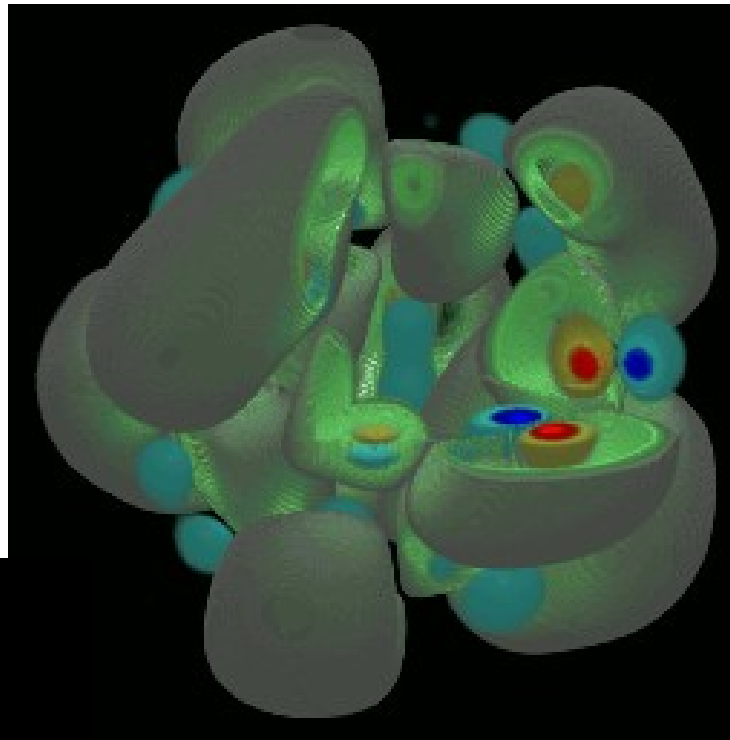
# Ray Casting – More Examples

- Tornado Viz:
- Head data:



# Ray Casting – more Examples

Molecular  
data:



# Literature

## Paper (more details):

- Marc Levoy: “**Display of Surfaces from Volume Data**” in *IEEE Computer Graphics & Applications*, Vol. 8, No. 3, June 1988

## For more, see also

- **Data Visualization, Principles and Practice, Chapter 10 Volume Visualization**, by A. Telea, AK Peters, 2008

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■ Torsten Möller

■ M. Eduard Gröller

■ Helwig Hauser