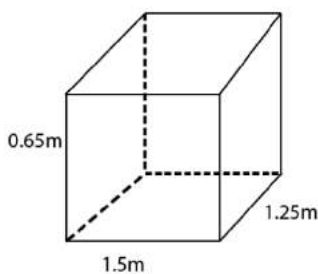


Exercise 13.1

Page No: 213

1. A plastic box 1.5 m long, 1.25 m wide and 65 cm deep, is to be made. It is to be open at the top. Ignoring the thickness of the plastic sheet, determine:
- The area of the sheet required for making the box.
 - The cost of sheet for it, if a sheet measuring 1m^2 costs Rs. 20.

Solution:



Given: length (l) of box = 1.5m

Breadth (b) of box = 1.25 m

Depth (h) of box = 0.65m

- (i) Box is to be open at top

Area of sheet required.

$$= 2lh + 2bh + lb$$

$$= [2 \times 1.5 \times 0.65 + 2 \times 1.25 \times 0.65 + 1.5 \times 1.25] \text{m}^2$$

$$= (1.95 + 1.625 + 1.875) \text{m}^2 = 5.45 \text{m}^2$$

- (ii) Cost of sheet per m^2 area = Rs.20.

$$\text{Cost of sheet of } 5.45 \text{ m}^2 \text{ area} = \text{Rs } (5.45 \times 20)$$

$$= \text{Rs.109.}$$

2. The length, breadth and height of a room are 5 m, 4 m and 3 m respectively. Find the cost of white washing the walls of the room and ceiling at the rate of Rs 7.50 per m^2 .

Solution:

Length (l) of room = 5m

Breadth (b) of room = 4m

Height (h) of room = 3m

It can be observed that four walls and the ceiling of the room are to be white washed.

Total area to be white washed = Area of walls + Area of ceiling of room

$$= 2lh + 2bh + lb$$

$$= [2 \times 5 \times 3 + 2 \times 4 \times 3 + 5 \times 4]$$

$$= (30+24+20)$$

$$= 74$$

$$\text{Area} = 74 \text{ m}^2$$

Also,

$$\text{Cost of white wash per m}^2 \text{ area} = \text{Rs. } 7.50 \text{ (Given)}$$

$$\begin{aligned} \text{Cost of white washing } 74 \text{ m}^2 \text{ area} &= \text{Rs. } (74 \times 7.50) \\ &= \text{Rs. } 555 \end{aligned}$$

3. The floor of a rectangular hall has a perimeter 250 m. If the cost of painting the four walls at the rate of Rs.10 per m² is Rs.15000, find the height of the hall.

[Hint: Area of the four walls = Lateral surface area.]

Solution:

Let length, breadth, and height of the rectangular hall be l, b, and h respectively.

$$\text{Area of four walls} = 2lh + 2bh$$

$$= 2(l+b)h$$

$$\text{Perimeter of the floor of hall} = 2(l+b)$$

$$= 250 \text{ m}$$

$$\text{Area of four walls} = 2(l+b)h = 250h \text{ m}^2$$

$$\text{Cost of painting per square meter area} = \text{Rs. } 10$$

$$\text{Cost of painting } 250h \text{ square meter area} = \text{Rs. } (250h \times 10) = \text{Rs. } 2500h$$

However, it is given that the cost of painting the walls is Rs. 15000.

$$15000 = 2500h$$

$$\text{Or } h = 6$$

Therefore, the height of the hall is 6 m.

4. The paint in a certain container is sufficient to paint an area equal to 9.375 m². How many bricks of dimensions 22.5 cm×10 cm×7.5 cm can be painted out of this container?

Solution:

$$\text{Total surface area of one brick} = 2(lb + bh + lb)$$

$$= [2(22.5 \times 10 + 10 \times 7.5 + 22.5 \times 7.5)] \text{ cm}^2$$

$$= 2(225 + 75 + 168.75) \text{ cm}^2$$

$$= (2 \times 468.75) \text{ cm}^2$$

$$= 937.5 \text{ cm}^2$$

Let n bricks can be painted out by the paint of the container

$$\text{Area of n bricks} = (n \times 937.5) \text{ cm}^2 = 937.5n \text{ cm}^2$$

$$\text{As per given instructions, area that can be painted by the paint of the container} = 9.375 \text{ m}^2 = 93750 \text{ cm}^2$$

$$\text{So, we have, } 93750 = 937.5n$$

$$n = 100$$

Therefore, 100 bricks can be painted out by the paint of the container.

5. A cubical box has each edge 10 cm and another cuboidal box is 12.5cm long, 10 cm wide and 8

cm high

(i) Which box has the greater lateral surface area and by how much?

(ii) Which box has the smaller total surface area and by how much?

Solution:

From the question statement, we have

Edge of a cube = 10cm

Length, $l = 12.5$ cm

Breadth, $b = 10$ cm

Height, $h = 8$ cm

(i) Find the lateral surface area for both the figures

Lateral surface area of cubical box = $4(\text{edge})^2$

$$= 4(10)^2$$

$$= 400 \text{ cm}^2 \dots(1)$$

Lateral surface area of cuboidal box = $2[lh+bh]$

$$= [2(12.5 \times 8 + 10 \times 8)]$$

$$= (2 \times 180) = 360$$

Therefore, Lateral surface area of cuboidal box is $360 \text{ cm}^2 \dots(2)$

From (1) and (2), lateral surface area of the cubical box is more than the lateral surface area of the cuboidal box. The difference between both the lateral surfaces is, 40 cm^2 .

(Lateral surface area of cubical box - Lateral surface area of cuboidal box = $400 \text{ cm}^2 - 360 \text{ cm}^2 = 40 \text{ cm}^2$)

(ii) Find the total surface area for both the figures

The total surface area of the cubical box = $6(\text{edge})^2 = 6(10 \text{ cm})^2 = 600 \text{ cm}^2 \dots(3)$

Total surface area of cuboidal box

$$= 2[lh+bh+lb]$$

$$= [2(12.5 \times 8 + 10 \times 8 + 12.5 \times 10)]$$

$$= 610$$

This implies, Total surface area of cuboidal box is $610 \text{ cm}^2 \dots(4)$

From (3) and (4), the total surface area of the cubical box is smaller than that of the cuboidal box. And their difference is 10 cm^2 .

Therefore, the total surface area of the cubical box is smaller than that of the cuboidal box by 10 cm^2

6. A small indoor greenhouse (herbarium) is made entirely of glass panes (including base) held together with tape. It is 30cm long, 25 cm wide and 25 cm high.

(i) What is the area of the glass?

(ii) How much of tape is needed for all the 12 edges?

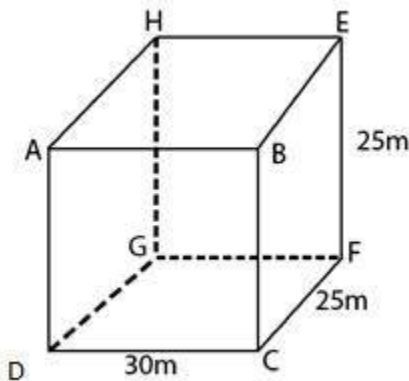
Solution:

Length of greenhouse, say $l = 30$ cm

Breadth of greenhouse, say $b = 25$ cm
Height of greenhouse, say $h = 25$ cm

(i) Total surface area of greenhouse = Area of the glass = $2[lb+lh+bh]$
 $= [2(30 \times 25 + 30 \times 25 + 25 \times 25)]$
 $= [2(750 + 750 + 625)]$
 $= (2 \times 2125) = 4250$
 Total surface area of the glass is 4250 cm^2

(ii)



From figure, tape is required along sides AB, BC, CD, DA, EF, FG, GH, HE, AH, BE, DG, and CF.

Total length of tape = $4(l+b+h)$
 $= [4(30+25+25)]$ (after substituting the values)
 $= 320$

Therefore, 320 cm tape is required for all the 12 edges.

7. Shanti Sweets Stall was placing an order for making cardboard boxes for packing their sweets. Two sizes of boxes were required. The bigger of dimensions $25 \text{ cm} \times 20 \text{ cm} \times 5 \text{ cm}$ and the smaller of dimension $15 \text{ cm} \times 12 \text{ cm} \times 5 \text{ cm}$. For all the overlaps, 5% of the total surface area is required extra. If the cost of the cardboard is Rs. 4 for 1000 cm^2 , find the cost of cardboard required for supplying 250 boxes of each kind.

Solution:

Let l , b and h be the length, breadth and height of the box.

Bigger Box:

$l = 25 \text{ cm}$

$b = 20 \text{ cm}$

$h = 5 \text{ cm}$

Total surface area of bigger box = $2(lb+lh+bh)$
 $= [2(25 \times 20 + 25 \times 5 + 20 \times 5)]$

$$= [2(500+125+100)]$$

$$= 1450 \text{ cm}^2$$

Extra area required for overlapping $1450 \times 5/100 \text{ cm}^2$

$$= 72.5 \text{ cm}^2$$

While considering all over laps, total surface area of bigger box

$$= (1450+72.5) \text{ cm}^2 = 1522.5 \text{ cm}^2$$

Area of cardboard sheet required for 250 such bigger boxes

$$= (1522.5 \times 250) \text{ cm}^2 = 380625 \text{ cm}^2$$

Smaller Box:

Similarly, total surface area of smaller box = $[2(15 \times 12 + 15 \times 5 + 12 \times 5)] \text{ cm}^2$

$$= [2(180+75+60)] \text{ cm}^2$$

$$= (2 \times 315) \text{ cm}^2$$

$$= 630 \text{ cm}^2$$

Therefore, extra area required for overlapping $630 \times 5/100 \text{ cm}^2 = 31.5 \text{ cm}^2$

Total surface area of 1 smaller box while considering all overlaps

$$= (630+31.5) \text{ cm}^2 = 661.5 \text{ cm}^2$$

Area of cardboard sheet required for 250 smaller boxes = $(250 \times 661.5) \text{ cm}^2 = 165375 \text{ cm}^2$

In Short:

Box	Dimensions (in cm)	Total surface area (in cm^2)	Extra area required for overlapping (in cm^2)	Total surface area for all overlaps (in cm^2)	Area for 250 such boxes (in cm^2)
Bigger Box	$l = 25$ $b = 20$ $c = 5$	1450	$1450 \times 5/100$ $= 72.5$	$(1450+72.5) =$ 1522.5	$(1522.5 \times 250) =$ 380625
Smaller Box	$l = 15$ $b = 12$ $h = 5$	630	$630 \times 5/100 =$ 31.5	$(630+31.5) =$ 661.5	$(250 \times 661.5) =$ 165375

Now, Total cardboard sheet required = $(380625+165375) \text{ cm}^2$

$$= 546000 \text{ cm}^2$$

Given: Cost of 1000 cm^2 cardboard sheet = Rs. 4

Therefore, Cost of 546000 cm^2 cardboard sheet = Rs. $(546000 \times 4)/1000 = \text{Rs. } 2184$

Therefore, the cost of cardboard required for supplying 250 boxes of each kind will be Rs. 2184.

8. Praveen wanted to make a temporary shelter for her car, by making a box – like structure with tarpaulin that covers all the four sides and the top of the car (with the front face as a flap which can be rolled up). Assuming that the stitching margins are very small, and therefore negligible, how much tarpaulin would be required to make the shelter of height 2.5m, with base dimensions $4\text{m} \times 3\text{m}$?

Solution:

Let l , b and h be the length, breadth and height of the shelter.

Given:

$$l = 4\text{m}$$

$$b = 3\text{m}$$

$$h = 2.5\text{m}$$

Tarpaulin will be required for the top and four wall sides of the shelter.

Using formula, Area of tarpaulin required $= 2(lh+bh)+lb$

On putting the values of l , b and h , we get

$$= [2(4 \times 2.5 + 3 \times 2.5) + 4 \times 3] \text{ m}^2$$

$$= [2(10 + 7.5) + 12] \text{ m}^2$$

$$= 47 \text{ m}^2$$

Therefore, 47 m^2 tarpaulin will be required.



Exercise 13.2

Page No: 216

1. The curved surface area of a right circular cylinder of height 14 cm is 88 cm^2 . Find the diameter of the base of the cylinder. (Assume $\pi = 22/7$)

Solution:

Height of cylinder, $h = 14 \text{ cm}$

Let the diameter of the cylinder be d

Curved surface area of cylinder = 88 cm^2

We know that, formula to find Curved surface area of cylinder is $2\pi rh$.

So $2\pi rh = 88 \text{ cm}^2$ (r is the radius of the base of the cylinder)

$$2 \times (22/7) \times r \times 14 = 88 \text{ cm}^2$$

$$2r = 2 \text{ cm}$$

$$d = 2 \text{ cm}$$

Therefore, the diameter of the base of the cylinder is 2 cm.

2. It is required to make a closed cylindrical tank of height 1m and base diameter 140cm from a metal sheet. How many square meters of the sheet are required for the same? Assume $\pi = 22/7$

Solution:

Let h be the height and r be the radius of a cylindrical tank.

Height of cylindrical tank, $h = 1 \text{ m}$

Radius = half of diameter = $(140/2) \text{ cm} = 70 \text{ cm} = 0.7 \text{ m}$

$$\begin{aligned} \text{Area of sheet required} &= \text{Total surface area of tank} = 2\pi r(r+h) \text{ unit square} \\ &= [2 \times (22/7) \times 0.7(0.7+1)] \\ &= 7.48 \end{aligned}$$

Therefore, 7.48 square meters of the sheet are required.

3. A metal pipe is 77 cm long. The inner diameter of a cross section is 4 cm, the outer diameter being 4.4cm. (see fig. 13.11). Find its

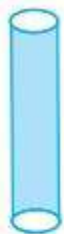


Fig. 13.11

- (i) inner curved surface area,
- (ii) outer curved surface area
- (iii) total surface area

(Assume $\pi=22/7$)

Solution:

Let r_1 and r_2 Inner and outer radii of cylindrical pipe

$$r_1 = 4/2 \text{ cm} = 2 \text{ cm}$$

$$r_2 = 4.4/2 \text{ cm} = 2.2 \text{ cm}$$

Height of cylindrical pipe, h = length of cylindrical pipe = 77 cm

$$\begin{aligned} \text{(i) curved surface area of outer surface of pipe} &= 2\pi r_1 h \\ &= 2 \times (22/7) \times 2 \times 77 \text{ cm}^2 \\ &= 968 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{(ii) curved surface area of inner surface of pipe} &= 2\pi r_2 h \\ &= 2 \times (22/7) \times 2.2 \times 77 \text{ cm}^2 \\ &= (22 \times 22 \times 2.2) \text{ cm}^2 \\ &= 1064.8 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{(iii) Total surface area of pipe} &= \text{inner curved surface area} + \text{outer curved surface area} + \text{Area of both circular ends of pipe.} \\ &= 2\pi r_1 h + 2\pi r_2 h + (\pi r_1^2 - \pi r_2^2) \\ &= 968 + 1064.8 + 2\pi(2.2^2 - 2^2) \\ &= 2031.8 + 5.28 \\ &= 2038.08 \text{ cm}^2 \end{aligned}$$

Therefore, the total surface area of the cylindrical pipe is 2038.08 cm².

4. The diameter of a roller is 84 cm and its length is 120 cm. It takes 500 complete revolutions to move once over to level a playground. Find the area of the playground in m²? (Assume $\pi = 22/7$)

Solution:

A roller is shaped like a cylinder.

Let h be the height of the roller and r be the radius.

$$h = \text{Length of roller} = 120 \text{ cm}$$

$$\text{Radius of the circular end of roller} = r = (84/2) \text{ cm} = 42 \text{ cm}$$

Now, CSA of roller = $2\pi rh$

$$= 2 \times (22/7) \times 42 \times 120$$

$$= 31680 \text{ cm}^2$$

$$\begin{aligned}\text{Area of field} &= 500 \times \text{CSA of roller} \\ &= (500 \times 31680) \text{ cm}^2 \\ &= 15840000 \text{ cm}^2 \\ &= 1584 \text{ m}^2.\end{aligned}$$

Therefore, area of playground is 1584 m^2 . Answer!

5. A cylindrical pillar is 50 cm in diameter and 3.5 m in height. Find the cost of painting the curved surface of the pillar at the rate of Rs. 12.50 per m^2 . (Assume $\pi = 22/7$)

Solution:

Let h be the height of a cylindrical pillar and r be the radius.

Given:

$$\text{Height cylindrical pillar} = h = 3.5 \text{ m}$$

$$\text{Radius of the circular end of pillar} = r = \text{diameter}/2 = 50/2 = 25\text{cm} = 0.25\text{m}$$

$$\text{CSA of pillar} = 2\pi rh$$

$$= 2 \times (22/7) \times 0.25 \times 3.5$$

$$= 5.5 \text{ m}^2$$

$$\text{Cost of painting } 1 \text{ m}^2 \text{ area} = \text{Rs. } 12.50$$

$$\text{Cost of painting } 5.5 \text{ m}^2 \text{ area} = \text{Rs. } (5.5 \times 12.50)$$

$$= \text{Rs. } 68.75$$

Therefore, the cost of painting the curved surface of the pillar at the rate of Rs. 12.50 per m^2 is Rs 68.75.

6. Curved surface area of a right circular cylinder is 4.4 m^2 . If the radius of the base of the cylinder is 0.7 m , find its height. (Assume $\pi = 22/7$)

Solution:

Let h be the height of the circular cylinder and r be the radius.

$$\text{Radius of the base of cylinder, } r = 0.7\text{m}$$

$$\text{CSA of cylinder} = 2\pi rh$$

$$\text{CSA of cylinder} = 4.4\text{m}^2$$

Equating both the equations, we have

$$2 \times (22/7) \times 0.7 \times h = 4.4$$

$$\text{Or } h = 1$$

Therefore, the height of the cylinder is 1 m .

7. The inner diameter of a circular well is 3.5m . It is 10m deep. Find

(i) its inner curved surface area,

(ii) the cost of plastering this curved surface at the rate of Rs. 40 per m^2 .

(Assume $\pi = 22/7$)

Solution:

Inner radius of circular well, $r = 3.5/2\text{m} = 1.75\text{m}$

Depth of circular well, say $h = 10\text{m}$

(i) Inner curved surface area $= 2\pi rh$

$$= (2 \times (22/7) \times 1.75 \times 10)$$

$$= 110$$

Therefore, the inner curved surface area of the circular well is 110 m^2 .

(ii) Cost of plastering 1 m^2 area = Rs.40

Cost of plastering 110 m^2 area = Rs (110×40)

$$= \text{Rs.}4400$$

Therefore, the cost of plastering the curved surface of the well is Rs. 4400.

8. In a hot water heating system, there is cylindrical pipe of length 28 m and diameter 5 cm. Find the total radiating surface in the system. (Assume $\pi = 22/7$)

Solution:

Height of cylindrical pipe = Length of cylindrical pipe = 28m

Radius of circular end of pipe = diameter/ 2 = $5/2\text{ cm} = 2.5\text{cm} = 0.025\text{m}$

Now, CSA of cylindrical pipe $= 2\pi rh$, where r = radius and h = height of the cylinder

$$= 2 \times (22/7) \times 0.025 \times 28\text{ m}^2$$

$$= 4.4\text{m}^2$$

The area of the radiating surface of the system is 4.4m^2 .

9. Find

(i) the lateral or curved surface area of a closed cylindrical petrol storage tank that is 4.2 m in diameter and 4.5m high.

(ii) How much steel was actually used, if $1/12$ of the steel actually used was wasted in making the tank. (Assume $\pi = 22/7$)

Solution:

Height of cylindrical tank, $h = 4.5\text{m}$

Radius of the circular end, $r = (4.2/2)\text{m} = 2.1\text{m}$

(i) the lateral or curved surface area of cylindrical tank is $2\pi rh$

$$= 2 \times (22/7) \times 2.1 \times 4.5\text{ m}^2$$

$$= (44 \times 0.3 \times 4.5)\text{ m}^2$$

$$= 59.4\text{ m}^2$$

Therefore, CSA of tank is 59.4 m^2 .

(ii) Total surface area of tank $= 2\pi r(r+h)$

$$= 2 \times (22/7) \times (2.1+4.5)$$

$$= 44 \times 0.3 \times 6.6$$

$$= 87.12\text{ m}^2$$

Now, Let $S\text{ m}^2$ steel sheet be actually used in making the tank.

$$S(1 - 1/12) = 87.12 \text{ m}^2$$

This implies, $S = 95.04 \text{ m}^2$

Therefore, 95.04 m^2 steel was used in actual while making such a tank.

10. In fig. 13.12, you see the frame of a lampshade. It is to be covered with a decorative cloth. The frame has a base diameter of 20 cm and height of 30 cm. A margin of 2.5 cm is to be given for folding it over the top and bottom of the frame. Find how much cloth is required for covering the lampshade. (Assume $\pi = 22/7$)



Fig. 13.12

Solution:

Say h = height of the frame of lampshade, looks like cylindrical shape

r = radius

Total height is $h = (2.5 + 30 + 2.5) \text{ cm} = 35 \text{ cm}$ and

$r = (20/2) \text{ cm} = 10 \text{ cm}$

Use curved surface area formula to find the cloth required for covering the lampshade which is $2\pi rh$

$$= (2 \times (22/7) \times 10 \times 35) \text{ cm}^2$$

$$= 2200 \text{ cm}^2$$

Hence, 2200 cm^2 cloth is required for covering the lampshade.

11. The students of Vidyalaya were asked to participate in a competition for making and decorating penholders in the shape of a cylinder with a base, using cardboard. Each penholder was to be of radius 3 cm and height 10.5 cm. The Vidyalaya was to supply the competitors with cardboard. If there were 35 competitors, how much cardboard was required to be bought for the competition? (Assume $\pi = 22/7$)

Solution:

Radius of the circular end of cylindrical penholder, $r = 3 \text{ cm}$

Height of penholder, $h = 10.5 \text{ cm}$

Surface area of a penholder = CSA of pen holder + Area of base of penholder

$$= 2\pi rh + \pi r^2$$

$$= 2 \times (22/7) \times 3 \times 10.5 + (22/7) \times 3^2 = 1584/7$$

Therefore, Area of cardboard sheet used by one competitor is $1584/7 \text{ cm}^2$

So, Area of cardboard sheet used by 35 competitors = $35 \times 1584/7 = 7920 \text{ cm}^2$

Therefore, 7920 cm^2 cardboard sheet will be needed for the competition.



Exercise 13.3

Page No: 221

1. Diameter of the base of a cone is 10.5 cm and its slant height is 10 cm. Find its curved surface area (Assume $\pi=22/7$)

Solution:

Radius of the base of cone = diameter/ 2 = $(10.5/2)\text{cm} = 5.25\text{cm}$

Slant height of cone, say $l = 10\text{ cm}$

CSA of cone is $= \pi rl$

$$= (22/7) \times 5.25 \times 10 = 165$$

Therefore, the curved surface area of the cone is 165 cm^2 .

2. Find the total surface area of a cone, if its slant height is 21 m and diameter of its base is 24 m. (Assume $\pi = 22/7$)

Solution:

Radius of cone, $r = 24/2\text{ m} = 12\text{m}$

Slant height, $l = 21\text{ m}$

Formula: Total Surface area of the cone $= \pi r(l+r)$

$$\begin{aligned}\text{Total Surface area of the cone} &= (22/7) \times 12 \times (21+12)\text{ m}^2 \\ &= 1244.57\text{m}^2\end{aligned}$$

3. Curved surface area of a cone is 308 cm^2 and its slant height is 14 cm. Find

(i) radius of the base and (ii) total surface area of the cone.

(Assume $\pi = 22/7$)

Solution:

Slant height of cone, $l = 14\text{ cm}$

Let the radius of the cone be r .

(i) We know, CSA of cone $= \pi rl$

Given: Curved surface area of a cone is 308 cm^2

$$(308) = (22/7) \times r \times 14$$

$$308 = 44r$$

$$r = 308/44 = 7$$

Radius of a cone base is 7 cm .

(ii) Total surface area of cone = CSA of cone + Area of base (πr^2)

$$\text{Total surface area of cone} = 308 + (22/7) \times 7^2 = 308 + 154$$

Therefore, the total surface area of the cone is 462 cm^2 .

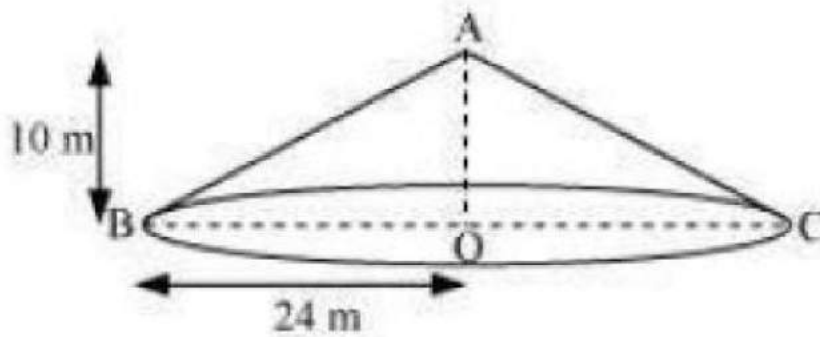
4. A conical tent is 10 m high and the radius of its base is 24 m. Find

(i) slant height of the tent.

(ii) cost of the canvas required to make the tent, if the cost of 1 m² canvas is Rs 70.

(Assume $\pi=22/7$)

Solution:



Let ABC be a conical tent

Height of conical tent, $h = 10$ m

Radius of conical tent, $r = 24$ m

Let the slant height of the tent be l .

(i) In right triangle ABO, we have

$$AB^2 = AO^2 + BO^2 \text{ (using Pythagoras theorem)}$$

$$l^2 = h^2 + r^2$$

$$= (10)^2 + (24)^2$$

$$= 676$$

$$l = 26$$

Therefore, the slant height of the tent is 26 m.

(ii) CSA of tent $= \pi rl$

$$= (22/7) \times 24 \times 26 \text{ m}^2$$

Cost of 1 m² canvas = Rs 70

Cost of $(13728/7)$ m² canvas is equal to Rs $(13728/7) \times 70 = \text{Rs } 137280$

Therefore, the cost of the canvas required to make such a tent is Rs 137280.

5. What length of tarpaulin 3 m wide will be required to make conical tent of height 8 m and base radius 6m? Assume that the extra length of material that will be required for stitching margins and wastage in cutting is approximately 20 cm. [Use $\pi=3.14$]

Solution:

Height of conical tent, $h = 8\text{m}$
Radius of base of tent, $r = 6\text{m}$
Slant height of tent, $l^2 = (r^2 + h^2)$
 $l^2 = (6^2 + 8^2) = (36 + 64) = (100)$
or $l = 10$

Again, CSA of conical tent $= \pi rl$
 $= (3.14 \times 6 \times 10) \text{ m}^2$
 $= 188.4 \text{ m}^2$

Let the length of tarpaulin sheet required be L
As 20 cm will be wasted, therefore,
Effective length will be $(L - 0.2\text{m})$.
Breadth of tarpaulin $= 3\text{m}$ (given)
Area of sheet $= \text{CSA of tent}$
 $[(L - 0.2) \times 3] = 188.4$
 $L - 0.2 = 62.8$
 $L = 63$
Therefore, the length of the required tarpaulin sheet will be 63 m.

6. The slant height and base diameter of conical tomb are 25m and 14 m respectively. Find the cost of white-washing its curved surface at the rate of Rs. 210 per 100 m². (Assume $\pi = 22/7$)

Solution:

Slant height of conical tomb, $l = 25\text{m}$
Base radius, $r = \text{diameter}/2 = 14/2 \text{ m} = 7\text{m}$
CSA of conical tomb $= \pi rl$
 $= (22/7) \times 7 \times 25 = 550$

CSA of conical tomb $= 550 \text{ m}^2$
Cost of white-washing 550 m² area, which is Rs $(210 \times 550)/100$
 $= \text{Rs. } 1155$
Therefore, cost will be Rs. 1155 while white-washing tomb.

7. A joker's cap is in the form of right circular cone of base radius 7 cm and height 24cm. Find the area of the sheet required to make 10 such caps. (Assume $\pi = 22/7$)

Solution:

Radius of conical cap, $r = 7 \text{ cm}$
Height of conical cap, $h = 24\text{cm}$
Slant height, $l^2 = (r^2 + h^2)$
 $= (7^2 + 24^2)$
 $= (49 + 576)$

$$= (625)$$

$$\text{Or } l = 25 \text{ cm}$$

$$\text{CSA of 1 conical cap} = \pi r l$$

$$= (22/7) \times 7 \times 25$$

$$= 550$$

$$\text{CSA of 10 caps} = (10 \times 550) \text{ cm}^2 = 5500 \text{ cm}^2$$

Therefore, the area of the sheet required to make 10 such caps is 5500 cm^2 .

8. A bus stop is barricaded from the remaining part of the road, by using 50 hollow cones made of recycled cardboard. Each cone has a base diameter of 40 cm and height 1 m. If the outer side of each of the cones is to be painted and the cost of painting is Rs. 12 per m^2 , what will be the cost of painting all these cones? (Use $\pi = 3.14$ and take $\sqrt{1.04} = 1.02$)

Solution:

Given:

$$\text{Radius of cone, } r = \text{diameter}/2 = 40/2 \text{ cm} = 20 \text{ cm} = 0.2 \text{ m}$$

$$\text{Height of cone, } h = 1 \text{ m}$$

$$\text{Slant height of cone is } l, \text{ and } l^2 = (r^2 + h^2)$$

$$\text{Using given values, } l^2 = (0.2^2 + 1^2)$$

$$= (1.04)$$

$$\text{Or } l = 1.02$$

$$\text{Slant height of the cone is } 1.02 \text{ m}$$

Now,

$$\text{CSA of each cone} = \pi r l$$

$$= (3.14 \times 0.2 \times 1.02)$$

$$= 0.64056$$

$$\text{CSA of 50 such cones} = (50 \times 0.64056) = 32.028$$

$$\text{CSA of 50 such cones} = 32.028 \text{ m}^2$$

Again,

$$\text{Cost of painting } 1 \text{ m}^2 \text{ area} = \text{Rs } 12 \text{ (given)}$$

$$\text{Cost of painting } 32.028 \text{ m}^2 \text{ area} = \text{Rs } (32.028 \times 12)$$

$$= \text{Rs. } 384.336$$

$$= \text{Rs. } 384.34 \text{ (approximately)}$$

Therefore, the cost of painting all these cones is Rs. 384.34.

Exercise 13.4

Page No: 225

1. Find the surface area of a sphere of radius:

(i) 10.5cm (ii) 5.6cm (iii) 14cm

(Assume $\pi=22/7$)

Solution:

Formula: Surface area of sphere (SA) = $4\pi r^2$

(i) Radius of sphere, $r = 10.5$ cm

$$SA = 4 \times (22/7) \times 10.5^2 = 1386$$

Surface area of sphere is 1386 cm^2

(ii) Radius of sphere, $r = 5.6$ cm

$$\text{Using formula, } SA = 4 \times (22/7) \times 5.6^2 = 394.24$$

Surface area of sphere is 394.24 cm^2

(iii) Radius of sphere, $r = 14$ cm

$$SA = 4\pi r^2$$

$$= 4 \times (22/7) \times (14)^2$$

$$= 2464$$

Surface area of sphere is 2464 cm^2

2. Find the surface area of a sphere of diameter:

(i) 14cm (ii) 21cm (iii) 3.5cm

(Assume $\pi = 22/7$)

Solution:

Radius of sphere, $r = \text{diameter}/2 = 14/2 \text{ cm} = 7 \text{ cm}$

Formula for Surface area of sphere = $4\pi r^2$

$$= 4 \times (22/7) \times 7^2 = 616$$

Surface area of a sphere is 616 cm^2

(ii) Radius (r) of sphere = $21/2 = 10.5$ cm

$$\text{Surface area of sphere} = 4\pi r^2$$

$$= 4 \times (22/7) \times 10.5^2 = 1386$$

Surface area of a sphere is 1386 cm^2

Therefore, the surface area of a sphere having diameter 21cm is 1386 cm^2

(iii) Radius(r) of sphere = $3.5/2 = 1.75$ cm

Surface area of sphere = $4\pi r^2$
 $= 4 \times (22/7) \times 1.75^2 = 38.5$
Surface area of a sphere is 38.5 cm^2

3. Find the total surface area of a hemisphere of radius 10 cm. [Use $\pi=3.14$]

Solution:

Radius of hemisphere, $r = 10\text{cm}$
Formula: Total surface area of hemisphere = $3\pi r^2$
 $= 3 \times 3.14 \times 10^2 = 942$
The total surface area of given hemisphere is 942 cm^2 .

4. The radius of a spherical balloon increases from 7cm to 14cm as air is being pumped into it. Find the ratio of surface areas of the balloon in the two cases.

Solution:

Let r_1 and r_2 be the radii of spherical balloon and spherical balloon when air is pumped into it respectively. So

$r_1 = 7\text{cm}$
 $r_2 = 14 \text{ cm}$

Now, Required ratio = (initial surface area)/(Surface area after pumping air into balloon)
 $= 4\pi r_1^2 / 4\pi r_2^2$
 $= (r_1/r_2)^2$
 $= (7/14)^2 = (1/2)^2 = 1/4$

Therefore, the ratio between the surface areas is 1:4.

5. A hemispherical bowl made of brass has inner diameter 10.5cm. Find the cost of tin-plating it on the inside at the rate of Rs 16 per 100 cm^2 . (Assume $\pi = 22/7$)

Solution:

Inner radius of hemispherical bowl, say $r = \text{diameter}/2 = (10.5)/2 \text{ cm} = 5.25 \text{ cm}$
Formula for Surface area of hemispherical bowl = $2\pi r^2$
 $= 2 \times (22/7) \times (5.25)^2 = 173.25$

Surface area of hemispherical bowl is 173.25 cm^2

Cost of tin-plating 100 cm^2 area = Rs 16

Cost of tin-plating 1 cm^2 area = Rs $16/100$

Cost of tin-plating 173.25 cm^2 area = Rs. $(16 \times 173.25)/100 = \text{Rs } 27.72$

Therefore, the cost of tin-plating the inner side of the hemispherical bowl at the rate of Rs 16 per 100 cm^2 is Rs **27.72**.

6. Find the radius of a sphere whose surface area is 154 cm^2 . (Assume $\pi = 22/7$)

Solution:

Let the radius of the sphere be r .

Surface area of sphere = 154 (given)

Now,

$$4\pi r^2 = 154$$

$$r^2 = (154 \times 7) / (4 \times 22) = (49/4)$$

$$r = (7/2) = 3.5$$

The radius of the sphere is 3.5 cm .

7. The diameter of the moon is approximately one fourth of the diameter of the earth. Find the ratio of their surface areas.

Solution:

If diameter of earth is said d , then the diameter of moon will be $d/4$ (as per given statement)

Radius of earth = $d/2$

Radius of moon = $\frac{1}{2} \times d/4 = d/8$

Surface area of moon = $4\pi(d/8)^2$

Surface area of earth = $4\pi(d/2)^2$

$$\text{Ratio of their Surface areas} = \frac{4\pi \left(\frac{d}{8}\right)^2}{4\pi \left(\frac{d}{2}\right)^2} = \frac{4}{64} = 1/16$$

The ratio between their surface areas is $1:16$.

8. A hemispherical bowl is made of steel, 0.25 cm thick. The inner radius of the bowl is 5 cm . Find the outer curved surface of the bowl. (Assume $\pi = 22/7$)

Solution:

Given:

Inner radius of hemispherical bowl = 5 cm

Thickness of the bowl = 0.25 cm

Outer radius of hemispherical bowl = $(5 + 0.25) \text{ cm} = 5.25 \text{ cm}$

Formula for outer CSA of hemispherical bowl = $2\pi r^2$, where r is radius of hemisphere
 $= 2 \times (22/7) \times (5.25)^2 = 173.25$

Therefore, the outer curved surface area of the bowl is 173.25 cm^2 .

9. A right circular cylinder just encloses a sphere of radius r (see fig. 13.22). Find
- (i) surface area of the sphere,
 - (ii) curved surface area of the cylinder,
 - (iii) ratio of the areas obtained in (i) and (ii).



Fig. 13.22

Solution:

(i) Surface area of sphere = $4\pi r^2$, where r is the radius of sphere

(ii) Height of cylinder, $h = r + r = 2r$

Radius of cylinder = r

CSA of cylinder formula = $2\pi rh = 2\pi r(2r)$ (using value of h)
 $= 4\pi r^2$

(iii) Ratio between areas = (Surface area of sphere)/CSA of Cylinder
 $= 4\pi r^2 / 4\pi r^2 = 1/1$

Ratio of the areas obtained in (i) and (ii) is 1:1.

Exercise 13.5

Page No: 228

1. A matchbox measures 4 cm×2.5cm×1.5cm. What will be the volume of a packet containing 12 such boxes?

Solution:

Dimensions of a matchbox (a cuboid) are $l \times b \times h = 4 \text{ cm} \times 2.5 \text{ cm} \times 1.5 \text{ cm}$ respectively

Formula to find the volume of matchbox = $l \times b \times h = (4 \times 2.5 \times 1.5) = 15$

Volume of matchbox = 15 cm^3

Now, volume of 12 such matchboxes = $(15 \times 12) \text{ cm}^3 = 180 \text{ cm}^3$

Therefore, the volume of 12 matchboxes is 180 cm^3 .

2. A cuboidal water tank is 6m long, 5m wide and 4.5m deep. How many litres of water can it hold? ($1 \text{ m}^3 = 1000 \text{ l}$)

Solution:

Dimensions of a cuboidal water tank are: $l = 6 \text{ m}$ and $b = 5 \text{ m}$ and $h = 4.5 \text{ m}$

Formula to find volume of tank, $V = l \times b \times h$

Put the values, we get

$V = (6 \times 5 \times 4.5) = 135$

Volume of water tank is 135 m^3

Again,

We are given that, amount of water that 1 m^3 volume can hold = 1000 l

Amount of water, 135 m^3 volume hold = $(135 \times 1000) \text{ litres} = 135000 \text{ litres}$

Therefore, given cuboidal water tank can hold up to 135000 litres of water.

3. A cuboidal vessel is 10m long and 8m wide. How high must it be made to hold 380 cubic metres of a liquid?

Solution:

Given:

Length of cuboidal vessel, $l = 10 \text{ m}$

Width of cuboidal vessel, $b = 8 \text{ m}$

Volume of cuboidal vessel, $V = 380 \text{ m}^3$

Let the height of the given vessel be h .

Formula for Volume of a cuboid, $V = l \times b \times h$

Using formula, we have

$$l \times b \times h = 380$$

$$10 \times 8 \times h = 380$$

$$\text{Or } h = 4.75$$

Therefore, the height of the vessels is 4.75 m.

4. Find the cost of digging a cuboidal pit 8m long, 6m broad and 3m deep at the rate of Rs 30 per m^3 .

Solution:

The given pit has its length(l) as 8m, width (b) as 6m and depth (h) as 3 m.

Volume of cuboidal pit = $l \times b \times h = (8 \times 6 \times 3) = 144$ (using formula)

Required Volume is 144 m^3

Now,

Cost of digging per m^3 volume = Rs 30

Cost of digging 144 m^3 volume = Rs $(144 \times 30) = \text{Rs } 4320$

5. The capacity of a cuboidal tank is 50000 litres of water. Find the breadth of the tank, if its length and depth are respectively 2.5 m and 10 m.

Solution:

Length (l) and depth (h) of tank is 2.5 m and 10 m respectively.

To find: The value of breadth, say b .

Formula to find the volume of a tank = $l \times b \times h = (2.5 \times b \times 10) \text{ m}^3 = 25b \text{ m}^3$

Capacity of tank = $25b \text{ m}^3$, which is equal to $25000b$ litres

Also, capacity of a cuboidal tank is 50000 litres of water (Given)

Therefore, $25000b = 50000$

This implies, $b = 2$

Therefore, the breadth of the tank is 2 m.

6. A village, having a population of 4000, requires 150 litres of water per head per day. It has a tank measuring $20 \text{ m} \times 15 \text{ m} \times 6 \text{ m}$. For how many days will the water of this tank last?

Solution:

Length of the tank = $l = 20 \text{ m}$

Breadth of the tank = $b = 15 \text{ m}$

Height of the tank = $h = 6 \text{ m}$

Total population of a village = 4000

Consumption of the water per head per day = 150 litres

Water consumed by the people in 1 day = (4000×150) litres = 600000 litres ...(1)

Formula to find the capacity of tank, $C = l \times b \times h$

Using given data, we have

$$C = (20 \times 15 \times 6) \text{ m}^3 = 1800 \text{ m}^3$$

Or $C = 1800000$ litres

Let water in this tank last for d days.

Water consumed by all people in d days = Capacity of tank (using equation (1))

$$600000 d = 1800000$$

$$d = 3$$

Therefore, the water of this tank will last for 3 days. **Answer**

7. A godown measures $40 \text{ m} \times 25 \text{ m} \times 15 \text{ m}$. Find the maximum number of wooden crates each measuring $1.5 \text{ m} \times 1.25 \text{ m} \times 0.5 \text{ m}$ that can be stored in the godown.

Solution:

From statement, we have

Length of the godown = 40 m

Breadth = 25 m

Height = 15 m

Whereas,

Length of the wooden crate = 1.5 m

Breadth = 1.25 m

Height = 0.5 m

Since godown and wooden crate are in cuboidal shape. Find the volume of each using formula, $V = l b h$.

Now,

$$\text{Volume of godown} = (40 \times 25 \times 15) \text{ m}^3 = 10000 \text{ m}^3$$

$$\text{Volume of a wooden crate} = (1.5 \times 1.25 \times 0.5) \text{ m}^3 = 0.9375 \text{ m}^3$$

Let us consider that, n wooden crates can be stored in the godown, then

Volume of n wooden crates = Volume of godown

$$0.9375 \times n = 10000$$

$$\text{Or } n = 10000 / 0.9375 = 10666.66$$

Hence, the number of wooden crates can be stored in a godown are 10666.

8. A solid cube of side 12 cm is cut into eight cubes of equal volume. What will be the side of the new cube? Also, find the ratio between their surface areas.

Solution:

Side of a cube = 12 cm (Given)

Find the volume of cube:

Volume of cube = (Side)³ = (12)³cm³ = 1728cm³

Surface area of a cube with side 12 cm = $6a^2 = 6(12)^2$ cm² ... (1)

Cube is cut into eight small cubes of equal volume, say side of each cube is p.

Volume of a small cube = p³

Surface area = $6p^2$... (2)

Volume of each small cube = (1728/8) cm³ = 216 cm³

Or (p)³ = 216 cm³

Or p = 6 cm

Now, Surface areas of the cubes ratios = (Surface area of bigger cube)/(Surface area of smaller cubes)

From equation (1) and (2), we get

Surface areas of the cubes ratios = $(6a^2)/(6p^2) = a^2/p^2 = 12^2/6^2 = 4$

Therefore, the required ratio is 4 : 1.

9. A river 3m deep and 40m wide is flowing at the rate of 2km per hour. How much water will fall into the sea in a minute?

Solution:

Given:

Depth of river, h = 3 m

Width of river, b = 40 m

Rate of water flow = 2km per hour = 2000m/60min = 100/3 m/min

Now, Volume of water flowed in 1 min = $(100/3) \times 40 \times 3 = 4000$ m³

Therefore, 4000 m³ water will fall into the sea in a minute.

Exercise 13.6

Page No: 230

1. The circumference of the base of cylindrical vessel is 132cm and its height is 25cm. How many litres of water can it hold? ($1000 \text{ cm}^3 = 1\text{L}$) (Assume $\pi = 22/7$)

Solution:

Circumference of the base of cylindrical vessel = 132 cm

Height of vessel, $h = 25 \text{ cm}$

Let r be the radius of the cylindrical vessel.

Step 1: Find the radius of vessel

We know that, circumference of base = $2\pi r$, so

$$2\pi r = 132 \text{ (given)}$$

$$r = (132/(2\pi))$$

$$r = 66 \times 7/22 = 21$$

Radius is 21 cm

Step 2: Find the volume of vessel

Formula: Volume of cylindrical vessel = $\pi r^2 h$

$$= (22/7) \times 21^2 \times 25$$

$$= 34650$$

Therefore, volume is 34650 cm^3

Since, $1000 \text{ cm}^3 = 1\text{L}$

So, Volume = $34650/1000 \text{ L} = 34.65\text{L}$

Therefore, vessel can hold 34.65 litres of water.

2. The inner diameter of a cylindrical wooden pipe is 24cm and its outer diameter is 28 cm. The length of the pipe is 35cm. Find the mass of the pipe, if 1 cm^3 of wood has a mass of 0.6g. (Assume $\pi = 22/7$)

Solution:

Inner radius of cylindrical pipe, say $r_1 = \text{diameter}_1/2 = 24/2 \text{ cm} = 12\text{cm}$

Outer radius of cylindrical pipe, say $r_2 = \text{diameter}_2/2 = 28/2 \text{ cm} = 14 \text{ cm}$

Height of pipe, $h = \text{Length of pipe} = 35\text{cm}$

Now, the Volume of pipe = $\pi(r_2^2 - r_1^2)h \text{ cm}^3$

Substitute the values.

$$\text{Volume of pipe} = 110 \times 52 \text{ cm}^3 = 5720 \text{ cm}^3$$

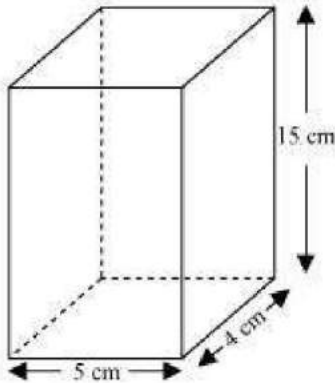
Since, **Mass of 1 cm^3 wood = 0.6 g**

Mass of 5720 cm^3 wood = $(5720 \times 0.6) \text{ g} = 3432 \text{ g}$ or 3.432 kg. Answer!

3. A soft drink is available in two packs - (i) a tin can with a rectangular base of length 5cm and width 4cm, having a height of 15 cm and (ii) a plastic cylinder with circular base of diameter 7cm and height 10cm. Which container has greater capacity and by how much? (Assume $\pi=22/7$)

Solution:

(i) tin can will be cuboidal in shape



Dimensions of tin can are

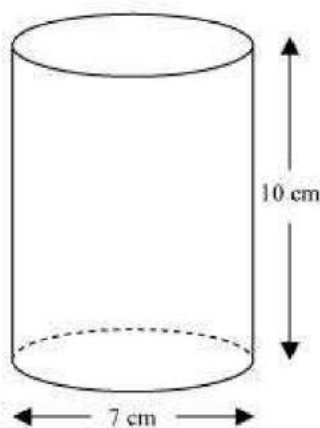
Length, $l = 5$ cm

Breadth, $b = 4$ cm

Height, $h = 15$ cm

Capacity of tin can $= l \times b \times h = (5 \times 4 \times 15) \text{ cm}^3 = 300 \text{ cm}^3$

(ii) Plastic cylinder will be cylindrical in shape.



Dimensions of plastic can are:

Radius of circular end of plastic cylinder, $r = 3.5\text{cm}$

Height, $H = 10\text{ cm}$

Capacity of plastic cylinder $= \pi r^2 H$

Capacity of plastic cylinder $= (22/7) \times (3.5)^2 \times 10 = 385$

Capacity of plastic cylinder is 385 cm^3

From results of (i) and (ii), plastic cylinder has more capacity.

Difference in capacity $= (385 - 300)\text{ cm}^3 = 85\text{ cm}^3$

4. If the lateral surface of a cylinder is 94.2 cm^2 and its height is 5 cm , then find

(i) radius of its base (ii) its volume. [Use $\pi = 3.14$]

Solution:

CSA of cylinder $= 94.2\text{ cm}^2$

Height of cylinder, $h = 5\text{ cm}$

(i) Let radius of cylinder be r .

Using CSA of cylinder, we get

$$2\pi rh = 94.2$$

$$2 \times 3.14 \times r \times 5 = 94.2$$

$$r = 3$$

radius is 3 cm

(ii) Volume of cylinder

Formula for volume of cylinder $= \pi r^2 h$

Now, $\pi r^2 h = (3.14 \times (3)^2 \times 5)$ (using value of r from (i))

$$= 141.3$$

Volume is 141.3 cm^3

5. It costs Rs 2200 to paint the inner curved surface of a cylindrical vessel 10 m deep. If the cost of painting is at the rate of Rs 20 per m^2 , find

(i) inner curved surface area of the vessel

(ii) radius of the base

(iii) capacity of the vessel

(Assume $\pi = 22/7$)

Solution:

(i) Rs 20 is the cost of painting 1 m^2 area.

Rs 1 is the cost to paint $1/20\text{ m}^2$ area

$$\begin{aligned}\text{So, Rs 2200 is the cost of painting} &= (1/20 \times 2200)\text{ m}^2 \\ &= 110\text{ m}^2 \text{ area}\end{aligned}$$

The inner surface area of the vessel is 110 m^2 .

(ii) Radius of the base of the vessel, let us say r .

Height (h) = 10 m and

Surface area formula = $2\pi rh$

Using result of (i)

$$2\pi rh = 110 \text{ m}^2$$

$$2 \times \frac{22}{7} \times r \times 10 = 110$$

$$r = 1.75$$

Radius is 1.75 m.

(iii) Volume of vessel formula = $\pi r^2 h$

Here $r = 1.75$ and $h = 10$

$$\text{Volume} = \left(\frac{22}{7}\right) \times (1.75)^2 \times 10 = 96.25$$

Volume of vessel is 96.25 m^3

Therefore, the capacity of the vessel is 96.25 m^3 or 96250 litres.

6. The capacity of a closed cylindrical vessel of height 1m is 15.4 liters. How many square meters of metal sheet would be needed to make it? (Assume $\pi = \frac{22}{7}$)

Solution:

Height of cylindrical vessel, $h = 1 \text{ m}$

Capacity of cylindrical vessel = 15.4 litres = 0.0154 m^3

Let r be the radius of the circular end.

Now,

$$\text{Capacity of cylindrical vessel} = \left(\frac{22}{7}\right) \times r^2 \times 1 = 0.0154$$

After simplifying, we get, $r = 0.07 \text{ m}$

Again, total surface area of vessel = $2\pi r(r+h)$

$$= \left(2 \times \frac{22}{7} \times 0.07(0.07+1)\right)$$

$$= 0.44 \times 1.07$$

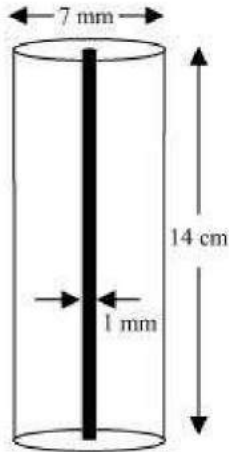
$$= 0.4708$$

Total surface area of vessel is 0.4708 m^2

Therefore, 0.4708 m^2 of the metal sheet would be required to make the cylindrical vessel.

7. A lead pencil consists of a cylinder of wood with solid cylinder of graphite filled in the interior. The diameter of the pencil is 7 mm and the diameter of the graphite is 1 mm. If the length of the pencil is 14 cm, find the volume of the wood and that of the graphite. (Assume $\pi = \frac{22}{7}$)

Solution:



Radius of pencil, $r_1 = 7/2 \text{ mm} = 0.7/2 \text{ cm} = 0.35 \text{ cm}$

Radius of graphite, $r_2 = 1/2 \text{ mm} = 0.1/2 \text{ cm} = 0.05 \text{ cm}$

Height of pencil, $h = 14 \text{ cm}$

Formula to find, volume of wood in pencil $= \pi(r_1^2 - r_2^2)h$ cubic units

Substitute the values, we have

$$= [(22/7) \times (0.35^2 - 0.05^2) \times 14]$$

$$= 44 \times 0.12$$

$$= 5.28$$

This implies, volume of wood in pencil $= 5.28 \text{ cm}^3$

Again,

Volume of graphite $= \pi r_2^2 h$ cubic units

Substitute the values, we have

$$= (22/7) \times 0.05^2 \times 14$$

$$= 44 \times 0.0025$$

$$= 0.11$$

So, the volume of graphite is 0.11 cm^3 .

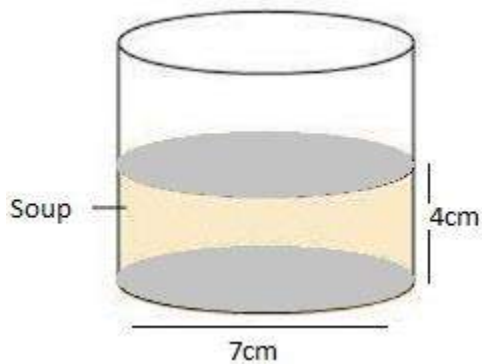
8. A patient in a hospital is given soup daily in a cylindrical bowl of diameter 7cm. If the bowl is filled with soup to a height of 4cm, how much soup the hospital has to prepare daily to serve 250 patients? (Assume $\pi = 22/7$)

Solution:

Diameter of cylindrical bowl $= 7 \text{ cm}$

Radius of cylindrical bowl, $r = 7/2 \text{ cm} = 3.5 \text{ cm}$

Bowl is filled with soup to a height of 4cm, so $h = 4 \text{ cm}$



Volume of soup in one bowl = $\pi r^2 h$
 $(22/7) \times 3.5^2 \times 4 = 154$

Volume of soup in one bowl is 154 cm^3

Therefore,

Volume of soup given to 250 patients = $(250 \times 154) \text{ cm}^3 = 38500 \text{ cm}^3$
 $= 38.5 \text{ litres}$. Answer!

Exercise 13.7

Page No: 233

1. Find the volume of the right circular cone with

(i) radius 6cm, height 7 cm (ii) radius 3.5 cm, height 12 cm (Assume $\pi = 22/7$)

Solution:

Volume of cone = $(1/3) \pi r^2 h$ cube units

Where r be radius and h be the height of the cone

(i) Radius of cone, $r = 6$ cm

Height of cone, $h = 7$ cm

Say, V be the volume of the cone, we have

$$V = (1/3) \times (22/7) \times 36 \times 7$$

$$= (12 \times 22)$$

$$= 264$$

The volume of the cone is 264 cm^3 .

(ii) Radius of cone, $r = 3.5$ cm

Height of cone, $h = 12$ cm

$$\text{Volume of cone} = (1/3) \times (22/7) \times 3.5^2 \times 12 = 154$$

Hence,

The volume of the cone is 154 cm^3 .

2. Find the capacity in litres of a conical vessel with

(i) radius 7cm, slant height 25 cm (ii) height 12 cm, slant height 12 cm

(Assume $\pi = 22/7$)

Solution:

(i) Radius of cone, $r = 7$ cm

Slant height of cone, $l = 25$ cm

$$\text{Height of cone, } h = \sqrt{l^2 - r^2}$$

$$h = \sqrt{25^2 - 7^2}$$

$$h = \sqrt{625 - 49}$$

or $h = 24$

Height of the cone is 24 cm

Now,

Volume of cone, $V = (1/3) \pi r^2 h$ (formula)

$$V = (1/3) \times (22/7) \times 7^2 \times 24$$

$$= (154 \times 8)$$

$$= 1232$$

So, the volume of the vessel is 1232 cm^3

Therefore, capacity of the conical vessel = $(1232/1000)$ liters (because $1\text{L} = 1000 \text{ cm}^3$)
= 1.232 Liters.

(ii) Height of cone, $h = 12 \text{ cm}$

Slant height of cone, $l = 13 \text{ cm}$

$$\text{Radius of cone, } r = \sqrt{l^2 - h^2}$$

$$r = \sqrt{13^2 - 12^2}$$

$$r = \sqrt{169 - 144}$$

$$r = 5$$

Hence, the radius of cone is 5 cm.

Now, Volume of cone, $V = (1/3)\pi r^2 h$

$$V = (1/3) \times (22/7) \times 5^2 \times 12 \text{ cm}^3$$
$$= 2200/7$$

Volume of cone is $2200/7 \text{ cm}^3$

Now, Capacity of the conical vessel = $2200/7000$ litres ($1\text{L} = 1000 \text{ cm}^3$)
= $11/35$ litres

3. The height of a cone is 15cm. If its volume is 1570cm^3 , find the diameter of its base. (Use $\pi = 3.14$)

Solution:

Height of the cone, $h = 15 \text{ cm}$

Volume of cone = 1570 cm^3

Let r be the radius of the cone

As we know: Volume of cone, $V = (1/3) \pi r^2 h$

So, $(1/3) \pi r^2 h = 1570$

$$(1/3) \times 3.14 \times r^2 \times 15 = 1570$$

$$r^2 = 100$$

$$r = 10$$

Radius of the base of cone 10 cm.

4. If the volume of a right circular cone of height 9cm is $48\pi\text{cm}^3$, find the diameter of its base.

Solution:

Height of cone, $h = 9\text{cm}$

Volume of cone $= 48\pi \text{ cm}^3$

Let r be the radius of the cone.

As we know: Volume of cone, $V = (1/3) \pi r^2 h$

So, $1/3 \pi r^2(9) = 48 \pi$

$r^2 = 16$

$r = 4$

Radius of cone is 4 cm.

So, diameter $= 2 \times \text{Radius} = 8$

Thus, diameter of base is 8cm.

**5. A conical pit of top diameter 3.5m is 12m deep. What is its capacity in kiloliters?
(Assume $\pi = 22/7$)**

Solution:

Diameter of conical pit $= 3.5 \text{ m}$

Radius of conical pit, $r = \text{diameter} / 2 = (3.5/2) \text{ m} = 1.75 \text{ m}$

Height of pit, $h = \text{Depth of pit} = 12 \text{ m}$

Volume of cone, $V = (1/3) \pi r^2 h$

$V = (1/3) \times (22/7) \times (1.75)^2 \times 12 = 38.5$

Volume of cone is 38.5 m^3

Hence, capacity of the pit $= (38.5 \times 1) \text{ kiloliters} = 38.5 \text{ kiloliters}$.

6. The volume of a right circular cone is 9856 cm^3 . If the diameter of the base is 28cm, find

(i) height of the cone

(ii) slant height of the cone

(iii) curved surface area of the cone

(Assume $\pi = 22/7$)

Solution:

Volume of a right circular cone $= 9856 \text{ cm}^3$

Diameter of the base $= 28 \text{ cm}$

(i) Radius of cone, $r = (28/2) \text{ cm} = 14 \text{ cm}$

Let the height of the cone be h

Volume of cone, $V = (1/3) \pi r^2 h$

$(1/3) \pi r^2 h = 9856$

$(1/3) \times (22/7) \times 14 \times 14 \times h = 9856$

$h = 48$

The height of the cone is 48 cm.

(ii) Slant height of cone, $l = \sqrt{r^2 + h^2}$

$$l = \sqrt{14^2 + 48^2} = \sqrt{196 + 2304} = 50$$

Slant height of the cone is 50 cm.

(iii) curved surface area of cone = πrl

$$= (22/7) \times 14 \times 50$$

$$= 2200$$

curved surface area of the cone is 2200 cm^2 .

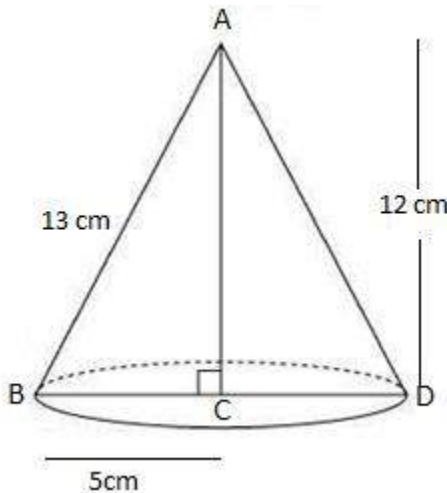
7. A right triangle ABC with sides 5cm, 12cm and 13cm is revolved about the side 12 cm. Find the volume of the solid so obtained.

Solution:

Height (h) = 12 cm

Radius (r) = 5 cm, and

Slant height (l) = 13 cm



Volume of cone, $V = (1/3) \pi r^2 h$

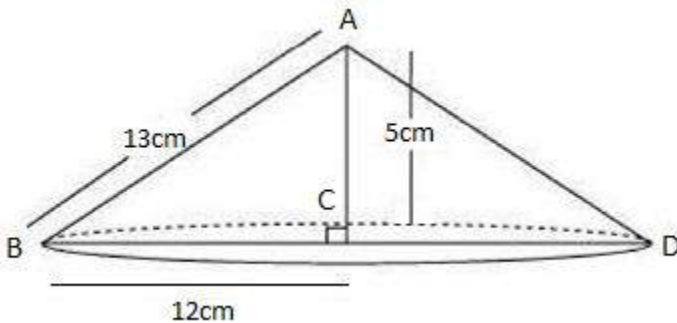
$$V = (1/3) \times \pi \times 5^2 \times 12$$

$$= 100\pi$$

Volume of the cone so formed is $100\pi \text{ cm}^3$.

8. If the triangle ABC in the Question 7 is revolved about the side 5cm, then find the volume of the solids so obtained. Find also the ratio of the volumes of the two solids obtained in Questions 7 and 8.

Solution:



A right-angled $\triangle ABC$ is revolved about its side 5cm, a cone will be formed of radius as 12 cm, height as 5 cm, and slant height as 13 cm.

$$\begin{aligned}\text{Volume of cone} &= \frac{1}{3} \pi r^2 h; \text{ where } r \text{ is the radius and } h \text{ be the height of cone} \\ &= \frac{1}{3} \times \pi \times 12 \times 12 \times 5 \\ &= 240 \pi\end{aligned}$$

The volume of the cones of formed is $240\pi \text{ cm}^3$.

So, required ratio = (result of question 7) / (result of question 8) = $(100\pi)/(240\pi) = 5/12 = 5:12$.

9. A heap of wheat is in the form of a cone whose diameter is 10.5 m and height is 3 m. Find its volume. The heap is to be covered by canvas to protect it from rain. Find the area of the canvas. (Assume $\pi = 22/7$)

Solution:

$$\text{Radius (r) of heap} = (10.5/2) \text{ m} = 5.25$$

$$\text{Height (h) of heap} = 3\text{m}$$

$$\begin{aligned}\text{Volume of heap} &= \frac{1}{3} \pi r^2 h \\ &= \frac{1}{3} \times \left(\frac{22}{7}\right) \times 5.25 \times 5.25 \times 3 \\ &= 86.625\end{aligned}$$

The volume of the heap of wheat is 86.625 m^3 .

Again,

$$\text{Area of canvas required} = \text{CSA of cone} = \pi r l, \text{ where } l = \sqrt{r^2 + h^2}$$

After substituting the values, we have

$$\text{CSA of cone} = \left[\frac{22}{7} \times 5.25 \times \sqrt{(5.25)^2 + 3^2}\right]$$

$$= (22/7) \times 5.25 \times 6.05$$

$$= 99.825$$

Therefore, the area of the canvas is 99.825 m².



Exercise 13.8

Page No: 236

1. Find the volume of a sphere whose radius is

(i) 7 cm (ii) 0.63 m

(Assume $\pi = 22/7$)

Solution:

(i) Radius of sphere, $r = 7$ cm

Using, Volume of sphere $= (4/3) \pi r^3$

$$= (4/3) \times (22/7) \times 7^3$$

$$= 4312/3$$

Hence, volume of the sphere is $4312/3 \text{ cm}^3$

(ii) Radius of sphere, $r = 0.63$ m

Using, volume of sphere $= (4/3) \pi r^3$

$$= (4/3) \times (22/7) \times 0.63^3$$

$$= 1.0478$$

Hence, volume of the sphere is 1.05 m^3 (approx).

2. Find the amount of water displaced by a solid spherical ball of diameter

(i) 28 cm (ii) 0.21 m

(Assume $\pi = 22/7$)

Solution:

(i) Diameter = 28 cm

Radius, $r = 28/2 \text{ cm} = 14 \text{ cm}$

Volume of the solid spherical ball $= (4/3) \pi r^3$

$$\text{Volume of the ball} = (4/3) \times (22/7) \times 14^3 = 34496/3$$

Hence, volume of the ball is $34496/3 \text{ cm}^3$

(ii) Diameter = 0.21 m

Radius of the ball $= 0.21/2 \text{ m} = 0.105 \text{ m}$

Volume of the ball $= (4/3) \pi r^3$

$$\text{Volume of the ball} = (4/3) \times (22/7) \times 0.105^3 \text{ m}^3$$

Hence, volume of the ball $= 0.004851 \text{ m}^3$

3. The diameter of a metallic ball is 4.2 cm. What is the mass of the ball, if the density of the metal is 8.9 g per cm^3 ? (Assume $\pi = 22/7$)

Solution:

Given,

Diameter of a metallic ball = 4.2 cm

Radius(r) of the metallic ball, $r = 4.2/2 \text{ cm} = 2.1 \text{ cm}$

Volume formula = $\frac{4}{3} \pi r^3$

Volume of the metallic ball = $(\frac{4}{3}) \times (\frac{22}{7}) \times 2.1 \text{ cm}^3$

Volume of the metallic ball = 38.808 cm^3

Now, using relationship between, density, mass and volume,

Density = Mass/Volume

Mass = Density \times volume

= $(8.9 \times 38.808) \text{ g}$

= 345.3912 g

Mass of the ball is 345.39 g (approx).

4. The diameter of the moon is approximately one-fourth of the diameter of the earth. What fraction of the volume of the earth is the volume of the moon?

Solution:

Let the diameter of earth be “d”. Therefore, the radius of earth will be $d/2$

Diameter of moon will be $d/4$ and the radius of moon will be $d/8$

Find the volume of the moon :

Volume of the moon = $(\frac{4}{3}) \pi r^3 = (\frac{4}{3}) \pi (d/8)^3 = \frac{4}{3} \pi (d^3/512)$

Find the volume of the earth :

Volume of the earth = $(\frac{4}{3}) \pi r^3 = (\frac{4}{3}) \pi (d/2)^3 = \frac{4}{3} \pi (d^3/8)$

Fraction of the volume of the earth is the volume of the moon

$$\text{Volume of the moon/ volume of the earth} = \frac{\frac{4}{3} \pi (\frac{d^3}{512})}{\frac{4}{3} \pi (\frac{d^3}{8})} = \frac{8}{512} = \frac{1}{64}$$

Answer: Volume of moon is of the $1/64$ volume of earth.

5. How many litres of milk can a hemispherical bowl of diameter 10.5cm hold? (Assume $\pi = 22/7$)

Solution:

Diameter of hemispherical bowl = 10.5 cm

Radius of hemispherical bowl, $r = 10.5/2 \text{ cm} = 5.25 \text{ cm}$

Formula for volume of the hemispherical bowl = $(\frac{2}{3}) \pi r^3$

Volume of the hemispherical bowl = $(\frac{2}{3}) \times (\frac{22}{7}) \times 5.25^3 = 303.1875$

Volume of the hemispherical bowl is 303.1875 cm^3

Capacity of the bowl = $(303.1875)/1000 \text{ L} = 0.303 \text{ litres (approx.)}$

Therefore, hemispherical bowl can hold 0.303 litres of milk.

6. A hemi spherical tank is made up of an iron sheet 1cm thick. If the inner radius is 1 m, then find the volume of the iron used to make the tank. (Assume $\pi = \frac{22}{7}$)

Solution:

Inner Radius of the tank, (r) = 1m

Outer Radius (R) = 1.01m

Volume of the iron used in the tank = $(\frac{2}{3}) \pi (R^3 - r^3)$

Put values,

Volume of the iron used in the hemispherical tank = $(\frac{2}{3}) \times (\frac{22}{7}) \times (1.01^3 - 1^3) = 0.06348$

So, volume of the iron used in the hemispherical tank is 0.06348 m^3 .

7. Find the volume of a sphere whose surface area is 154 cm^2 . (Assume $\pi = \frac{22}{7}$)

Solution:

Let r be the radius of a sphere.

Surface area of sphere = $4\pi r^2$

$4\pi r^2 = 154 \text{ cm}^2$ (given)

$r^2 = (154 \times 7) / (4 \times 22)$

$r = 7/2$

Radius is $7/2 \text{ cm}$

Now,

Volume of the sphere = $(\frac{4}{3}) \pi r^3$

Volume of the sphere = $(\frac{4}{3}) \times (\frac{22}{7}) \times (\frac{7}{2})^3 = 179 \frac{2}{3}$

Volume of the sphere is $179 \frac{2}{3} \text{ cm}^3$

8. A dome of a building is in the form of a hemi sphere. From inside, it was white-washed at the cost of Rs. 4989.60. If the cost of white-washing is Rs 20 per square meter, find the

(i) inside surface area of the dome (ii) volume of the air inside the dome

(Assume $\pi = \frac{22}{7}$)

Solution:

(i) Cost of white-washing the dome from inside = Rs 4989.60

Cost of white-washing 1 m^2 area = Rs 20

CSA of the inner side

$$\text{of dome} = 498.96/2 \text{ m}^2 = 249.48 \text{ m}^2$$

(ii) Let the inner radius of the hemispherical dome be r .

$$\text{CSA of inner side of dome} = 249.48 \text{ m}^2 \text{ (from (i))}$$

$$\text{Formula to find CSA of a hemi sphere} = 2\pi r^2$$

$$2\pi r^2 = 249.48$$

$$2 \times (22/7) \times r^2 = 249.48$$

$$r^2 = (249.48 \times 7) / (2 \times 22)$$

$$r^2 = 39.69$$

$$r = 6.3$$

So, radius is 6.3 m

Volume of air inside the dome = Volume of hemispherical dome

$$\text{Using formula, volume of the hemisphere} = \frac{2}{3} \pi r^3$$

$$= \frac{2}{3} \times (22/7) \times 6.3 \times 6.3 \times 6.3$$

$$= 523.908$$

$$= 523.9 \text{ (approx.)}$$

Answer: Volume of air inside the dome is 523.9 m³.

9. Twenty-seven solid iron spheres, each of radius r and surface area S are melted to form a sphere with surface area S' . Find the

(i) radius r' of the new sphere,

(ii) ratio of S and S' .

Solution:

$$\text{Volume of the solid sphere} = \frac{4}{3} \pi r^3$$

$$\text{Volume of twenty seven solid sphere} = 27 \times \frac{4}{3} \pi r^3 = 36 \pi r^3$$

(i) New solid iron sphere radius = r'

$$\text{Volume of this new sphere} = \frac{4}{3} \pi (r')^3$$

$$\frac{4}{3} \pi (r')^3 = 36 \pi r^3$$

$$(r')^3 = 27r^3$$

$$r' = 3r$$

Radius of new sphere will be $3r$ (thrice the radius of original sphere)

ii) Surface area of iron sphere of radius r , $S = 4\pi r^2$

$$\text{Surface area of iron sphere of radius } r' = 4\pi (r')^2$$

Now

$$S/S' = (4\pi r^2) / (4\pi (r')^2)$$

$$S/S' = r^2 / (3r)^2 = 1/9$$

The ratio of S and S' is 1: 9.

10. A capsule of medicine is in the shape of a sphere of diameter 3.5mm. How much medicine (in mm³) is needed to fill this capsule? (Assume $\pi = 22/7$)

Solution:

Diameter of capsule = 3.5 mm

Radius of capsule, say $r = \text{diameter} / 2 = (3.5/2) \text{ mm} = 1.75 \text{ mm}$

Volume of spherical capsule = $\frac{4}{3} \pi r^3$

Volume of spherical capsule = $(\frac{4}{3}) \times (\frac{22}{7}) \times (1.75)^3 = 22.458$

Answer: The volume of the spherical capsule is 22.46 mm^3 .



Exercise 13.9

Page No: 236

1. A wooden bookshelf has external dimensions as follows: Height = 110cm, Depth = 25cm, Breadth = 85cm (see fig. 13.31). The thickness of the plank is 5cm everywhere. The external faces are to be polished and the inner faces are to be painted. If the rate of polishing is 20 paise per cm^2 and the rate of painting is 10 paise per cm^2 , find the total expenses required for polishing and painting the surface of the bookshelf.

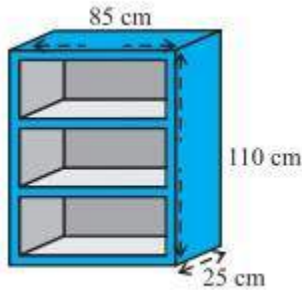


Fig. 13.31

Solution:

External dimensions of book self,

Length, $l = 85\text{cm}$

Breadth, $b = 25\text{ cm}$

Height, $h = 110\text{ cm}$

External surface area of shelf while leaving out the front face of the shelf

$$= lh + 2(lb + bh)$$

$$= [85 \times 110 + 2(85 \times 25 + 25 \times 110)] = (9350 + 9750) = 19100$$

External surface area of shelf is 19100 cm^2

$$\text{Area of front face} = [85 \times 110 - 75 \times 100 + 2(75 \times 5)] = 1850 + 750$$

So, area is 2600 cm^2

$$\text{Area to be polished} = (19100 + 2600)\text{ cm}^2 = 21700\text{ cm}^2.$$

Cost of polishing 1 cm^2 area = Rs 0.20

$$\text{Cost of polishing } 21700\text{ cm}^2 \text{ area Rs. } (21700 \times 0.20) = \text{Rs } 4340$$

Dimensions of row of the book shelf

Length(l) = 75 cm

Breadth (b) = 20 cm and

Height(h) = 30 cm

$$\text{Area to be painted in one row} = 2(l+h)b + lh = [2(75+30) \times 20 + 75 \times 30] = (4200 + 2250) = 6450$$

So, area is 6450 cm^2 .

Area to be painted in

$$3 \text{ rows} = (3 \times 6450) \text{ cm}^2 = 19350 \text{ cm}^2.$$

Cost of painting 1 cm^2 area = Rs. 0.10

$$\text{Cost of painting } 19350 \text{ cm}^2 \text{ area} = \text{Rs } (19350 \times 0.1) = \text{Rs } 1935$$

Total expense required for polishing and painting = Rs. $(4340 + 1935) = \text{Rs. } 6275$

Answer: The cost for polishing and painting the surface of the book shelf is Rs. 6275.

2. The front compound wall of a house is decorated by wooden spheres of diameter 21 cm, placed on small supports as shown in fig. 13.32. Eight such spheres are used for this purpose, and are to be painted silver. Each support is a cylinder of radius 1.5 cm and height 7 cm and is to be painted black. Find the cost of paint required if silver paint costs 25 paise per cm^2 and black paint costs 5 paise per cm^2 .

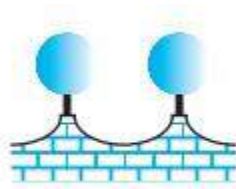


Fig. 13.32

Solution:

Diameter of wooden sphere = 21 cm

Radius of wooden sphere, $r = \text{diameter} / 2 = (21/2) \text{ cm} = 10.5 \text{ cm}$

$$\begin{aligned} \text{Formula: Surface area of wooden sphere} &= 4\pi r^2 \\ &= 4 \times (22/7) \times (10.5)^2 = 1386 \end{aligned}$$

So, surface area is 1386 cm^2

Radius of the circular end of cylindrical support = 1.5 cm

Height of cylindrical support = 7 cm

$$\begin{aligned} \text{Curved surface area} &= 2\pi rh \\ &= 2 \times (22/7) \times 1.5 \times 7 = 66 \end{aligned}$$

So, CSA is 66 cm^2

Now,

$$\begin{aligned} \text{Area of the circular end of cylindrical support} &= \pi r^2 \\ &= (22/7) \times 1.5^2 \\ &= 7.07 \end{aligned}$$

Area of the circular end is 7.07 cm^2

Again,

$$\text{Area to be painted silver} = [8 \times (1386 - 7.07)] = 8 \times 1378.93 = 11031.44$$

Area to be painted is 11031.44 cm^2

Cost for painting with silver colour = Rs $(11031.44 \times 0.25) = \text{Rs } 2757.86$

Area to be painted black = $(8 \times 66) \text{ cm}^2 = 528 \text{ cm}^2$

Cost for painting with black colour = Rs (528×0.05) = Rs 26.40

Therefore, the total painting cost is:

$$= \text{Rs}(2757.86 + 26.40)$$

$$= \text{Rs } 2784.26$$

3. The diameter of a sphere is decreased by 25%. By what percent does its curved surface area decrease?

Solution:

Let the diameter of the sphere be “d”.

Radius of sphere, $r_1 = d/2$

New radius of sphere, say $r_2 = (d/2) \times (1 - 25/100) = 3d/8$

Curved surface area of sphere, $(CSA)_1 = 4\pi r_1^2 = 4\pi \times (d/2)^2 = \pi d^2 \dots (1)$

Curved surface area of sphere when radius is decreased $(CSA)_2 = 4\pi r_2^2 = 4\pi \times (3d/8)^2 = (9/16)\pi d^2 \dots (2)$

From equation (1) and (2), we have

Decrease in surface area of sphere = $(CSA)_1 - (CSA)_2$

$$= \pi d^2 - (9/16)\pi d^2$$

$$= (7/16)\pi d^2$$

$$\text{Percentage decrease in surface area of sphere} = \frac{(CSA)_1 - (CSA)_2}{(CSA)_1} \times 100$$

$$= (7\pi d^2 / 16\pi d^2) \times 100 = 700/16 = 43.75\%$$

Therefore, the percentage decrease in the surface area of the sphere is 43.75% .