

DSA Notes from Stiver

Arrays

1) Kadane's algorithm

Problem Statement: Given an integer array arr,
find the contiguous subarray
(containing at least one number) which has
the largest sum and return its sum.

Approach: * Traverse through the array.

- * Have 2 variables, sum & maximum
- * Keep updating the sum as the sum of elements, and maximum as the maximum of sum.
- * But, when the sum < 0 , declare the sum as 0.
- * Return maximum

2) Sort an array of 0's, 1's and 2's

Problem statement: Given an array consisting of only 0's, 1's & 2's. Write a program to

in-place sort the array without using inbuilt sort functions (Expected : Single pass- $O(N)$ and constant space)

Eg ① Input: nums = [2, 0, 2, 1, 1, 0]
Output: [0, 0, 1, 1, 2, 2]

② Input: [2, 0, 0]

Output: [0, 0, 2]

③ Input: [0]

Output: [0]

Approach :-

Initialise low = 0, mid = 0, high = len(nums) - 1

while mid <= high:

 if nums[mid] == 0:

 nums[mid], nums[low] = nums[low], nums[mid]
 low += 1

 else if

 nums[mid] == 1:
 mid += 1

`if nums[mid] == 2:`
 `nums[mid], nums[high] = nums`
 `[high], nums[mid]`
 `high -= 1`

Eg. dry run

Initially: $[2, 0, 2, 1, 1, 0]$

\uparrow \uparrow
 low, high
 \downarrow mid

$$\text{mid} = 0$$

$[0, \cancel{0}, 2, 1, 1, 2] \rightarrow [0, 0, 2, 1, \cancel{1}, 2]$
 \uparrow \uparrow \downarrow
 low, high, mid

$[0, 0, 2, 1, 1, 2] \leftarrow [0, 0, 2, \cancel{1}, 1, 2]$
 \downarrow

$[0, 0, 1, 1, 2, 2]$
 \uparrow \uparrow \downarrow
 low, high, mid

$[0, 0, 1, \cancel{1}, 2, 2]$

\uparrow
 low,
 mid,
 high

3) Stock buy & sell

Problem statement: You are given an array of prices where $\text{prices}[i]$ is the price of a given stock on an i^{th} day.

You want to maximise your profit by choosing a single day to buy one stock and choosing a different day in the future to sell that stock. Return the max profit you can achieve from this transaction. If you cannot achieve any profit, return 0.

Examples

Example 1:

Input: $\text{prices} = [7, 1, 5, 3, 6, 4]$

Output: 5

Explanation: Buy on day 2 (price = 1) and sell on day 5 (price = 6), profit = $6 - 1 = 5$.

Note: That buying on day 2 and selling on day 1 is not allowed because you must buy before you sell.

Example 2:

Input: $\text{prices} = [7, 6, 4, 3, 1]$

Output: 0

Explanation: In this case, no transactions are done and the max profit = 0.

- Approach :-
- * Take min Price as a variable to store the minimum price
 - * Take max Prof as a variable to store the maximum Profit
 - * Traverse through the prices array, update min Price and maxProf (as current price - min Price)
 - * Return max Prof.

4) Merge overlapping subintervals

Problem Statement: Given an array of intervals, merge all the overlapping intervals and return an array of non-overlapping intervals.

Examples

Example 1:

Example 1:

Input: intervals=[[1,3],[2,6],[8,10],[15,18]]

Output: [[1,6],[8,10],[15,18]]

Explanation: Since intervals [1,3] and [2,6] are overlapping we can merge them to form [1,6] intervals.

Example 2:

Input: [[1,4],[4,5]]

Output: [[1,5]]

Explanation: Since intervals [1,4] and [4,5] are overlapping we can merge them to form [1,5].

Approach :- First sort the array of intervals. Then, create an empty list of intervals. Then,

$i = 0 \quad \rightarrow \quad res$

while $i < n$,

$j = i + 1$

while $j < n$ and intervals $[i][l] \geq$
intervals $[j][l]$
intervals $[i][l] \geq \max(\text{intervals } [j][l],$
intervals $[i][l])$
 $j^+ = l$
do append(intervals $[i]$)
 $i = j$

5) Merge 2 sorted arrays without extra space

Given two integer arrays **nums1** and **nums2**. Both arrays are sorted in **non-decreasing** order.

Merge both the arrays into a **single array sorted** in **non-decreasing** order.

- The **final** sorted array should be stored inside the array **nums1** and it should be done in-place.
- **nums1** has a length of **m + n**, where the first **m** elements denote the elements of **nums1** and rest are **0s**.
- **nums2** has a length of **n**.

Examples:

Input: $\text{nums1} = [-5, -2, 4, 5]$, $\text{nums2} = [-3, 1, 8]$

Output: $[-5, -3, -2, 1, 4, 5, 8]$

Explanation: The merged array is: $[-5, -3, -2, 1, 4, 5, 8]$, where $[-5, -2, 4, 5]$ are from nums1 and $[-3, 1, 8]$ are from nums2

Input: $\text{nums1} = [0, 2, 7, 8]$, $\text{nums2} = [-7, -3, -1]$

Output: $[-7, -3, -1, 0, 2, 7, 8]$

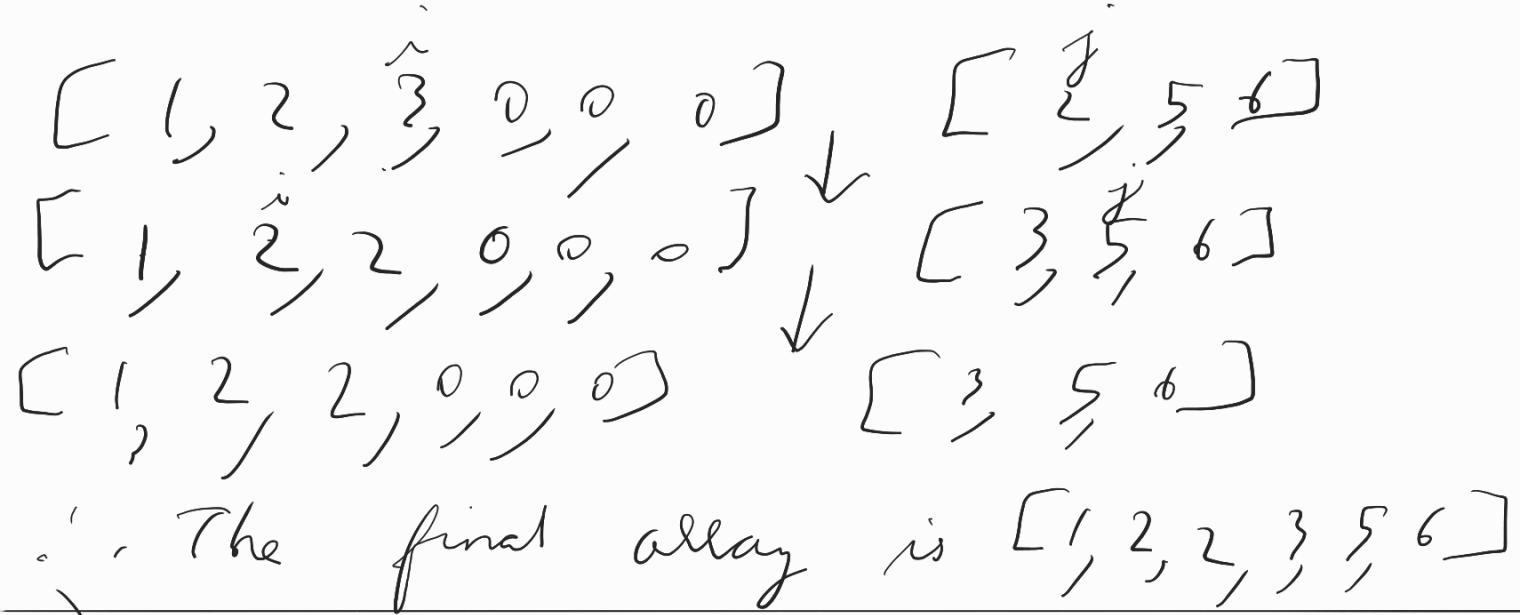
Explanation: The merged array is: $[-7, -3, -1, 0, 2, 7, 8]$, where $[0, 2, 7, 8]$ are from nums1 and $[-7, -3, -1]$ are from nums2

Approach :- Consider $i = m - 1$, $j = 0$
while $i \geq 0$ and $j \leq n$ and $\text{nums1}[i] \geq \text{nums2}[j]$:
 $\text{nums1}[i] < \text{nums2}[j]$:
 $\text{nums1}[i] = \text{nums2}[j]$
 $i = i - 1$
 $j = j + 1$

Take nums1 as $\text{nums1}[i:m]$ and sort

2 arrays. Then join nums1 with
nums2.

Eg:- $\text{nums1} = [1, 2, 3, 0, 0]$, $m = 3$
 $\text{nums2} = [2, 5, 6, 0, 0]$, $n = 3$



6) Search in a sorted 2D matrix

Problem Statement: You have been given a 2-D array 'mat' of size ' $N \times M$ ' where 'N' and 'M' denote the number of rows and columns, respectively. The elements of each row are sorted in non-decreasing order. Moreover, the first element of a row is greater than the last element of the previous row (if it exists). You are given an integer 'target', and your task is to find if it exists in the given 'mat' or not.

Examples:

Example 1:

Input Format: $N = 3, M = 4, \text{target} = 8$,

$\text{mat}[] =$

1 2 3 4

5 6 7 8

9 10 11 12

Result: true

Explanation: The 'target' = 8 exists in the 'mat' at index (1, 3).

Example 2:

Input Format: N = 3, M = 3, target = 78,

mat[] =

1 2 4

6 7 8

9 10 34

Result: false

Explanation: The 'target' = 78 does not exist in the 'mat'. Therefore in the output, we see 'false'.

Approach

- * Convert 2 D array into 1 D array
- * Perform binary search on the 1 D array.

7) Unique path

Problem Statement: Given a matrix $m \times n$, count paths from left-top to the right bottom of a matrix with the constraints that from each cell you can either only move to the rightward direction or the downward direction.

Examples:

Example 1:

Input Format: m = 2, n= 2

Output: 2

Explanation: From the top left corner there are total 2 ways to reach the bottom right corner:

Step 1: Right -> Down

Step 2: Down -> Right

Example 2:

Input Format: m = 2, n= 3

Output: 3

Explanation: From the top left corner there is a total of 3 ways to reach the bottom right corner.

Step 1: Right -> Right -> Down

Step 2: Right -> Down -> Right

Step 3: Down -> Right-> Right

Approach: Finding combinations using DP

8) Reverse Pairs

Problem Statement: Given an array of numbers, you need to return the count of reverse pairs. **Reverse Pairs** are those pairs where $i < j$ and $\text{arr}[i] > 2 * \text{arr}[j]$.

Examples

Example 1:

Input: N = 5, array[] = {1,3,2,3,1}

Output: 2

Explanation: The pairs are (3, 1) and (3, 1) as from both the pairs the condition $\text{arr}[i] > 2 * \text{arr}[j]$ is satisfied.

Example 2:

Input: $N = 4$, $\text{array}[] = \{3, 2, 1, 4\}$

Output: 1

Explanation: There is only 1 pair (3, 1) that satisfy the condition $\text{arr}[i] > 2 * \text{arr}[j]$

Approach :- This approach is similar to mergesort.

* Once we divide the array into subchunks, before merging, we have to call this function.

```
def countPairs(A, l, r):
    count = 0
    j = m + 1
    for i in range(l, m + 1):
        while j <= r and A[i] >
            2 * A[j]:
            j += 1
        count += (j - (m + 1))
    return count
```

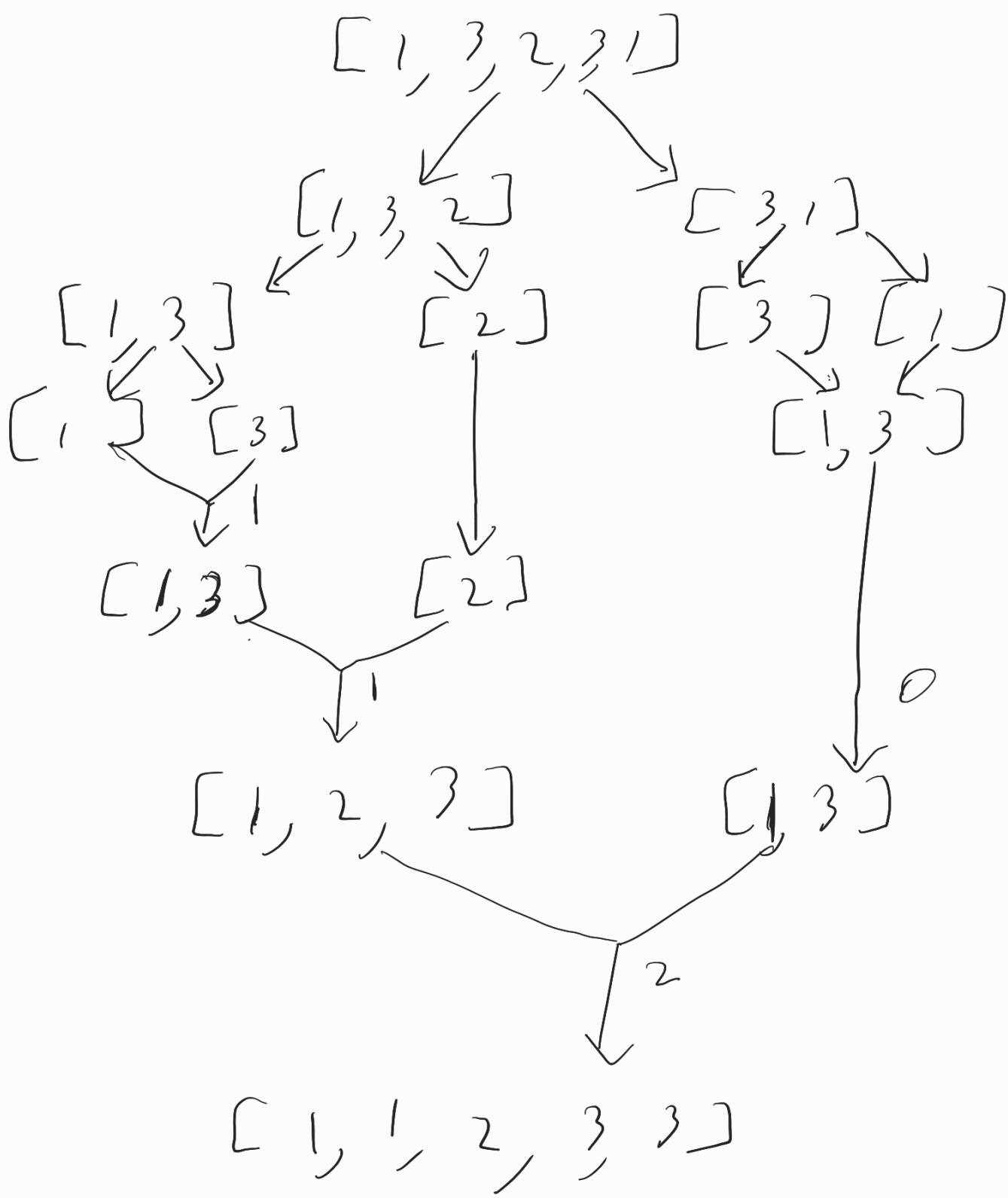
The main mergesort (A, l, r):

```
cnt = 0
if l < r:
    m = (l + r) // 2
    cnt += mergesort(A, l, m)
```

$\text{cnt } t = \text{mergesort}(A, m+1, r)$
 $\text{cnt } t = \text{mergesort}(A, l, m, r)$
 $\text{merge}(A, l, m, r)$
 returns cnt

Example dry run :-

$$A = [1, 3, 2, 3, 1]$$



∴ The final answer is 2.

9) 4-sum problem

Problem Statement: Given an array of N integers, your task is to find unique quads that add up to give a target value. In short, you need to return an array of all the unique quadruplets [arr[a], arr[b], arr[c], arr[d]] such that their sum is equal to a given target.

Note:

$0 \leq a, b, c, d < n$

a, b, c, and d are distinct.

$\text{arr}[a] + \text{arr}[b] + \text{arr}[c] + \text{arr}[d] == \text{target}$

Examples

Example 1:

Input Format: $\text{arr}[] = [1, 0, -1, 0, -2, 2]$, target = 0

Result: $[[-2, -1, 1, 2], [-2, 0, 0, 2], [-1, 0, 0, 1]]$

Explanation: We have to find unique quadruplets from the array such that the sum of those elements is equal to the target sum given that is 0. The result obtained is such that the sum of the quadruplets yields 0.

Example 2:

Input Format: $\text{arr}[] = [4, 3, 3, 4, 4, 2, 1, 2, 1, 1]$, target = 9

Result: $[[1, 1, 3, 4], [1, 2, 2, 4], [1, 2, 3, 3]]$

Explanation: The sum of all the quadruplets is equal to the target i.e. 9.

Approach :

- * We need 4 pointers, i, j, l, r , sort the arrays.
- * Traverse i from 0 to $n-1$
- * If $i > 0$ & $\text{nums}[i] = \text{nums}[i-1]$, then continue.
- * Else, run j from $i+1$ to n .
- * Again, if $j > i+1$ & $\text{nums}[j] = \text{nums}[j-1]$, then continue.
- * Later, initialise l as $j+1$ & r as $n-1$.
- * While $l < r$, do the following instructions.
 - If the sum of the numbers at the 4 pointers is equal to the target, then increment l such that the next number is not the current number, and decrement r such that the previous number is not the current number.
 - If the sum of the numbers at the 4 pointers is less than the target, increment l .
 - If the sum of the numbers at the 4 pointers is more than the target, decrement r .

Eg dry run:

$$arr = [1, 0, -1, 0, -2, 2]$$

$$\text{Sorted arr} = [-2, -1, 0, 0, 1, 2]$$

$$i = 0$$

$$j=1 \\ l=2, r=5$$

$$\text{sum} = -2 - 1 + 0 + 2 = -1 \quad (l+r=1)$$

$$l=3, r=5$$

$$\text{sum} = -2 - 1 + 0 + 2 = -1 \quad (l+r=1)$$

$$l=4, r=5$$

$$\text{sum} = -2 - 1 + 1 + 2 = 0 \quad \checkmark$$

$$j=2$$

$$l=3, r=5$$

$$\text{sum} = -2 + 0 + 0 + 2 = 0$$

$$j=3$$

$$l=4, r=5$$

$$\text{sum} = -2 + 0 + 1 + 2 = 1$$

$$i=1$$

$$j=2$$

$$l=3, r=5$$

$$\text{sum} = -1 + 0 + 0 + 2 = 1$$

$$l=3, r=4$$

$$\text{sum} = -1 + 0 + 0 + 1 = 0 \quad \checkmark$$

$$j=3$$

$$l=4, r=5$$

$$\text{sum} = -1 + 0 + 1 + 2 = 2$$

$$i=2$$

$$\begin{aligned}
 j &= 3 \\
 i &= \{, s = 5 \\
 \text{sum} &= 0 + 0 + 1 + 2 = 3
 \end{aligned}$$

\therefore The total number of quadruplets are ?.

(10) Longest Consecutive Sequence

Problem Statement: You are given an array of 'N' integers. You need to find the length of the longest sequence which contains the consecutive elements.

Examples:

Example 1: Input: [100, 200, 1, 3, 2, 4]

Output: 4

Explanation: The longest consecutive subsequence is 1, 2, 3, and 4.

Input: [3, 8, 5, 7, 6]

Output: 4

Explanation: The longest consecutive subsequence is 5, 6, 7, and 8.

Approach * First reduce the list of numbers to a set (by not having duplicate entries)

* Traverse through the elements in st.

* Check if the number one less than

the current element is not there in the set, then initialise the counter as 1. Then, increase the counter if the next number is there in the set.

* Then after incrementing the counter, then update the largest number variable as the max of the current variable value and the counter's value.

Eg:- nums = [100, 4, 200, 1, 3, 2]

st = [100, 4, 200, 1, 3, 2]

i = 100

The next number does not exist.

i = 4

3 is there.

i = 200.

The next number does not exist.

i = 1

cnt = 1

i = 2

cnt = 2

i = 3

cnt = 3

i = 4

cnt = 4

4 is the longest length.

11) 3 sum

Problem Statement: Given an array of N integers, your task is to find unique triplets that add up to give a sum of zero. In short, you need to return an array of all the unique triplets [arr[a], arr[b], arr[c]] such that $i \neq j$, $j \neq k$, $k \neq i$, and their sum is equal to zero.

Examples

Example 1:

Input: nums = [-1,0,1,2,-1,-4]

Output: [[-1,-1,2],[-1,0,1]]

Explanation: Out of all possible unique triplets possible, [-1,-1,2] and [-1,0,1] satisfy the condition of summing up to zero with $i \neq j \neq k$

Example 2:

Input: nums=[-1,0,1,0]

Output: Output: [[-1,0,1],[-1,1,0]]

Explanation: Out of all possible unique triplets possible, [-1,0,1] and [-1,1,0] satisfy the condition of summing up to zero with $i \neq j \neq k$

Approach : * Sort the numbers

- * Take 3 pointers, i, j, k .
- * Traverse through i from 0 to $n-1$.
- * Check if the previous number is not same as the current number
- * Take j as $i+1$ & k as $n-1$.
- * While $j < k$, calculate the sum of

nums[i], nums[j], nums[k]

- * If the sum is equal to 0, then append the triplet in to the anslist, then increment j till the current number is not equal to the previous number, and decrement k till the current number is not equal to the next number.
- * If the sum is less than 0, then increment j
- * If the sum is more than 0, then decrement k.

Eg Dry run.

$$\text{nums} = [-1, 0, 1, 2, -1, -4]$$

$$\text{sorted nums array: } [-4, \overset{0}{-1}, \overset{1}{-1}, \overset{2}{0}, \overset{3}{1}, \overset{4}{2}, \overset{5}{5}]$$

$$i = 0$$

$$j = 1, k = 5 \\ \text{sum} = -4 - 1 + 2 = -3 \quad (j+1)$$

$$j = 2, k = 5 \\ \text{sum} = -4 - 1 + 2 = -3 \quad (j+1)$$

$$j = 3, k = 5 \\ \text{sum} = -4 + 0 + 2 = -2 \quad (j+1)$$

$$j = 4, k = 5$$

$$\text{sum} = -4 + 1 + 2 = -1$$

$$i = 1$$

$$j = 2, k = 5$$

$$\text{sum} = -1 - 1 + 2 = 0$$

$$j = 3, k = 4$$

$$\text{sum} = -1 + 0 + 4 = 3$$

$$i = 2$$

$$j = 3, k = 5$$

$$\text{sum} = -1 + 0 + 2 = 1 \quad (k -= 1)$$

$$j = 3, k = 4$$

$$\text{sum} = -1 + 0 + 1 = 0$$

$$\therefore \text{anslist} = [[-1, -1, 2], [-1, 0, 1]]$$

12) Remove duplicates from sorted array

Problem Statement: Given an integer array sorted in non-decreasing order, remove the duplicates in place such that each unique element appears only once. The relative order of the elements should be kept the same.

If there are k elements after removing the duplicates, then the first k elements of the array should hold the final result. It does not matter what you leave beyond the first k elements.

Note: Return k after placing the final result in the first k slots of the array.

Examples

Example 1:

Input: arr[1,1,2,2,2,3,3]

Output: arr[1,2,3,_,_,_,_]

Explanation: Total number of unique elements are 3, i.e [1,2,3] and Therefore return 3 after assigning [1,2,3] in the beginning of the array.

Example 2:

Input: arr[1,1,1,2,2,3,3,3,3,4,4]

Output: arr[1,2,3,4,_,_,_,_,_,_]

Explanation: Total number of unique elements are 4, i.e [1,2,3,4] and Therefore return 4 after assigning [1,2,3,4] in the beginning of the array.

- Approach :- * Keep 2 pointers, i & j
- * $i = 0, j$ from 1 to $n - 1$
 - * If $\text{nums}[i] \neq \text{nums}[j]$, then keep on incrementing i .
 - * After finding that $\text{nums}[i] = \text{nums}[j]$, deduce that $\text{nums}[i] = \text{nums}[j]$
 - * Return $i + 1$

Ex: dry run

arr = [1, 1, 2, 2, 3, 3, 3, 3, 4, 4]

$i = 0, j = 1$
 $j = 2$
 $j = 3$
 $i = 1 \quad arr = [1, 2, 1, 2, 2, 3, 4, 5, 6, 7, 8, 9]$
 $j = 4$
 $j = 5$
 $i = 2 \quad arr = [1, 2, 3, 2, 2, 3, 3, 3, 4, 4]$
 $j = 6$
 $j = 7$
 $j = 8$
 $i = 3 \quad arr = [1, 2, 3, 4, 2, 3, 3, 3, 4, 4]$
 $j = 9$

Return $i + 1$

13) Max consecutive ones

Problem Statement: Given an array that contains **only 1 and 0** return the count of **maximum consecutive ones** in the array.

Examples:

Example 1:

Input: prices = {1, 1, 0, 1, 1, 1}

Output: 3

Explanation: There are two consecutive 1's and three consecutive 1's in the array out of which maximum is 3.

Input: prices = {1, 0, 1, 1, 0, 1}

Output: 2

Explanation: There are two consecutive 1's in the array.

Approach:- Declare a variable called maxi (to store the max number of ones)

- * Traverse through the array.
- * If the number is 1, then declare & initialize c as 0, and check if the next numbers are 1. If they are 1, then increment c.
- * Finally, when the number is 0 again, update maxi as the max of c and prev_max.

Eg dry run

$$\text{nums} = [0, 1, 2, 3, 4, 5]$$

$$i = 0, \text{maxi} = 0$$

$$c = 0$$

$$c = 1$$

$$i = 1$$

$$c = 2$$

$$i = 2$$

$$\text{maxi} = 2$$

$$i = 3$$

$$c = 0$$

$c = 1$
 $i = 4$
 $c = 2$
 $i = 5$
 $c = 3$

$\boxed{\max i = 3}$

14) Largest subarray with K sum

Problem Statement: Given an array containing both positive and negative integers, we have to find the length of the longest subarray with the sum of all elements equal to zero.

Examples

Example 1: Input Format: $N = 6$, $\text{array}[] = \{9, -3, 3, -1, 6, -5\}$ **Result:** 5

Explanation: The following subarrays sum to zero: $\{-3, 3\}$, $\{-1, 6, -5\}$, $\{-3, 3, -1, 6, -5\}$ Since we require the length of the longest subarray, our answer is 5!

Example 2: Input Format: $N = 8$, $\text{array}[] = \{6, -2, 2, -8, 1, 7, 4, -10\}$

Result: 8 Subarrays with sum 0 : $\{-2, 2\}$, $\{-8, 1, 7\}$, $\{-2, 2, -8, 1, 7\}$, $\{6, -2, 2, -8, 1, 7, 4, -10\}$ Length of longest subarray = 8

Example 3: Input Format: $N = 3$, $\text{array}[] = \{1, 0, -5\}$ **Result:** 1

Subarray : $\{0\}$ Length of longest subarray = 1

Example 4: Input Format: $N = 5$, $\text{array}[] = \{1, 3, -5, 6, -2\}$ **Result:** 0

Subarray: There is no subarray that sums to zero

Approach :- * Initialise sum as 0. Create a hashmap

* Traverse through the array

- * sum += arr[i]
- * If the sum is 0, max length = i + 1
- * Else,
 - If sum in hash, max length = max(maxLength, i - hash[sum]).
 - Else, add the [sum, i] into the hashmap
- * Returns maxLength

15) Count number of subarrays with given XOR k

Problem Statement: Given an array of integers A and an integer B. Find the total number of subarrays having bitwise XOR of all elements equal to k.

Examples

Example 1:

Input Format: A = [4, 2, 2, 6, 4], k = 6

Result: 4

Explanation: The subarrays having XOR of their elements as 6 are [4, 2], [4, 2, 2, 6, 4], [2, 2, 6], [6]

Example 2:

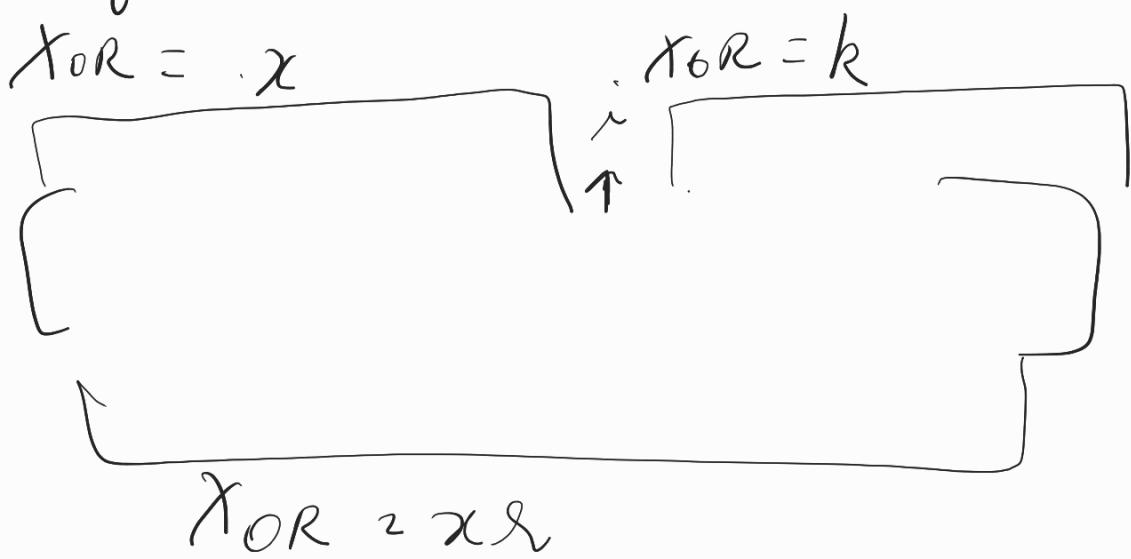
Input Format: A = [5, 6, 7, 8, 9], k = 5

Result: 2

Explanation: The subarrays having XOR of their elements as 5 are

[5] and [5, 6, 7, 8, 9]

Approach * Imagine that there is an endpoint. The prefix XOR is x_r , the prefix index of the elements before any index i is x_c and that after the index is k .



$$\begin{aligned} \text{So, } x_r &= x^r \\ x^r \cdot R &= x^r k^r \\ \Rightarrow x &= x^r k \end{aligned}$$

- * So, our approach should be that for $k=6$, we need to see whether there is x_r .
- * We need to create a hashmap having x_r as 0, and an element $[x_r : 1]$.
- * As we traverse the array, we need to update x_r as $x_r \cdot arr[i]$.
- * Later, we need to compute x as $x^r \cdot k$.

- * If x already exists in the hash,
count $\leftarrow \text{hash}[x]$
- * We have to add x to the hash
- * Finally, returns the count

Eg dry run

$$\text{arr} = [4, 2, 2, 6, 4]$$

$$xr = 0, \text{hash} = \{0:1\}$$

$$i = 0$$

$$xr = 4, x = 4^1 6 = 2, \text{hash} = \{0:1, 4:1\}$$

$$xr = 4^1 2 = 6, x = 6^1 6 = 0, \text{cnt} = 1,$$

$$\text{hash} = \{0:1, 4:1, 6:1\}$$

$$xr = 6^1 2 = 4, x = 4^1 6 = 2, \text{cnt} = 1$$

$$\text{hash} = \{0:1, 4:2, 6:1\}$$

$$xr = 4^1 6 = 2, x = 2^1 6 = 4, \text{cnt} = 1 + 2 = 3$$

$$\text{hash} = \{0:1, 4:2, 6:1, 2:1\}$$

$$xr = 2^1 4 = 6, x = 0, \text{cnt} = 3 + 1 = 4$$

$$\text{hash} = \{0:2, 4:2, 6:1, 2:1\}$$

$$\therefore \text{Final count} = 4$$