

18/April/22

Analysis Of Algorithms.

Eg. Problem : Sum of n natural numbers

Input : $n=3$

Output : 6 // $1+2+3$

Solⁿ 1 :

```
int fun1 (int n)
{
    return  $n * (n+1) / 2$ ;
}
```

Solⁿ 2 :

```
int fun2 (int n)
{
    int sum = 0;
    for (int i = 0; i <= n; i++)
        sum = sum + i;
    return sum;
}
```

Solⁿ 3 :

```
int fun3 (int n)
{
    int sum = 0;
    for (int i = 1; i <= n; i++)
        for (int j = 1; j <= i; j++)
            sum++;
    return sum;
}
```

Asymptotic Analysis

- The idea is to measure order of growth.
- Does not depend upon machine, programming language etc.
- No need to implement, we can analyze algorithms.

Time taken by Solution 1 → C_1

Time taken by Solution 2 → $C_2n + C_3$

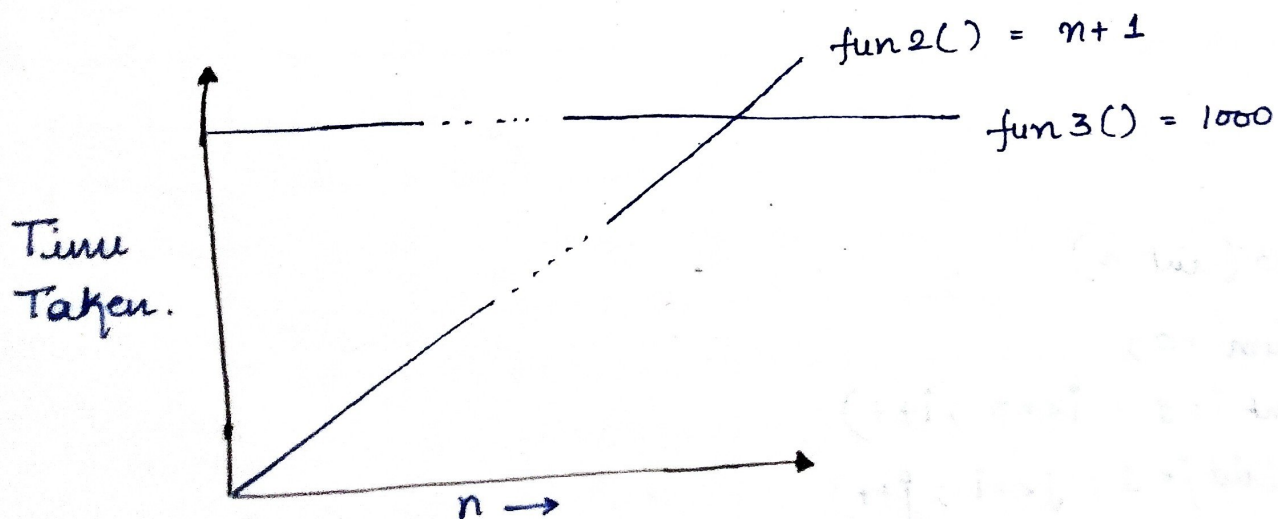
Time taken by Solution 3 → $C_4n^2 + C_5n + C_6$

Order of growth.

- We can simply ignore the lower order terms and take the higher order term into consideration.

For example:

$C_2n + C_3 \rightarrow \text{linear}$



fun 2() → linear

fun 3() → constant

* After certain value of n $\text{fun2}()$ will always take more time than $\text{fun3}()$.