

ADBMSExp 2

8/10/22	Kartik Jolapara 60004200107	ADBMS Exp 2	Page No. 1 Date 8/10/22
Aim: Perform operation like searching, insertion, deletion on B-Tree and B+Tree			
Theory:			
<u>B-Tree</u>			
B-Tree is a self-balancing tree. B-Trees are useful when we are dealing with huge amounts of data that can't be fitted in main memory. When the number of keys is high, the data is read from the disk in form of blocks. Disk access time is very high compared to the main memory access time.			
The main idea of using B-Trees is to reduce the number of disk access. Most of the tree operations require $O(h)$ disk access where h is the height of the tree. B-Tree is a fat tree meaning, the height of B-Tree is kept low by putting maximum possible keys in a B-Tree node. Generally, the B-Tree node size is kept equal to disk block size since the height of the B-Tree is kept low so total disk access for most of the operations are reduced significantly compared to balanced Binary search tree like AVL Trees.			
<u>Properties of B-Tree</u>			
→ All leaves are at the same level			
→ B-Tree is defined by min minimum degree 't'. The value of 't' depends upon disk block size			
→ Every node except the root must contain atleast (t-1) keys. The root may contain minimum of 1 key.			

- 8 10 22
- All nodes may contain almost $(2^k - 1)$ keys.
 - No. of children of a node is equal to no. of keys in it plus 1.
 - All keys of a node are sorted in increasing order.
 - It grows & shrinks from root.
 - Insertion happens only at leaf node.

Time complexity of B-Tree:

search - $O(\log n)$

Insert - $O(\log n)$

Delete - $O(\log n)$

⊕ B+ Tree

B+ Tree is an extension of B-Tree which allows efficient insertion, deletion and search operations. In B-Tree, keys and records both can be stored in internal as well as leaf nodes. whereas, in B+ tree records can only be stored on leaf nodes and internal nodes can only store key values.

The leaf nodes of a B+ tree are linked together in the form of singly linked list to make search queries more efficient. B+ trees are used to store the large amount of data which can't be stored in main memory. Due to the fact that size of main memory is always limited, the internal nodes of B+ tree are stored in main memory whereas, leaf nodes are stored in secondary memory.

① Properties of B+ Tree

- All leaf nodes are at same level.
- The root has atleast two children
- Each node except root can have a maximum of m children and atleast $m/2$ children
- Each node can contain a maximum of $(m-1)$ keys and a maximum of $\lfloor m/2 \rfloor - 1$ keys
- Keys are used for indexing
- Data can be stored sequentially or directly

① Time Complexity

- search - $O(\log n)$
- Insert - $O(\log n)$
- delete - $O(\log n)$

② B-Tree v/s B+ Tree

B-Tree	B+ Tree
① Search keys cannot be repeatedly stored	① Redundant search keys can be present.
② Data ^{can} stored in the leaf node as well as internal nodes	② Data can only be stored on the leaf nodes
③ Searching for some data is slower process some data can be found on internal nodes as well as leaf nodes	③ Search is comparatively faster as data can only be found on the leaf nodes.
④ Deletion of internal nodes are complicated & time consuming	④ Deletion will never be a complex process since some elements will be deleted from leaf

B Tree	B+ Tree
③ Leaf nodes can't be linked together	③ Leaf nodes are linked together to make search operations more efficient.

Conclusion: Thus, we successfully studied & compared various operations in B Tree & B+ Tree.

B Tree Code:

```
class BTreeNode:
    def __init__(self, leaf=False):
        self.leaf = leaf
    self.keys = []    self.child
    = []

class BTree:
    def __init__(self, t):
        self.root = BTreeNode(True)
        self.t = t

    def insert(self, k):    root = self.root
    if len(root.keys) == (2 * self.t) - 1:
        temp = BTreeNode()
        self.root = temp
        temp.child.insert(0, root)
        self.split_child(temp, 0)
        self.insert_non_full(temp, k)
    else:
        self.insert_non_full(root, k)
```

```

def insert_non_full(self, x, k):
    i = len(x.keys) - 1
    if x.leaf:
        x.keys.append((None, None))
    while i >= 0 and k[0] < x.keys[i][0]:
        x.keys[i + 1] = x.keys[i]        i -= 1
        x.keys[i + 1] = k
    else:
        while i >= 0 and k[0] < x.keys[i][0]:
            i -= 1        i += 1
        if len(x.child[i].keys) == (2 * self.t) - 1:
            self.split_child(x, i)
    if k[0] > x.keys[i][0]:
        i += 1
    self.insert_non_full(x.child[i], k)

```

```

def split_child(self, x, i):
    t = self.t    y =
    x.child[i]    z =
    BTreeNode(y.leaf)
    x.child.insert(i + 1, z)
    x.keys.insert(i, y.keys[t - 1])
    z.keys = y.keys[t: (2 * t) - 1]
    y.keys = y.keys[0: t - 1]
    if not y.leaf:
        z.child = y.child[t: 2 * t]

```

```
y.child = y.child[0: t - 1]
```

```
def print_tree(self, x, l=0):  
    print("Level ", l, " ", len(x.keys), end=":")  
    for i in x.keys:    print(i, end=" ")    print()  
    l += 1    if len(x.child) > 0:    for i in  
x.child:        self.print_tree(i, l)
```

```
def search_key(self, k, x=None):  
if x is not None:  
    i = 0    while i < len(x.keys) and k >  
x.keys[i][0]:    i += 1    if i < len(x.keys)  
and k == x.keys[i][0]:  
        return (x, i)  
elif x.leaf:  
return None  
else:  
    return self.search_key(k, x.child[i])  
  
else:  
    return self.search_key(k, self.root)
```

```
def main(): B  
= BTree(3)
```

```

    for i in range(10):
        B.insert((i, 2 * i))

    B.print_tree(B.root)

    if B.search_key(8) is not None:
        print("\nFound")
    else:
        print("\nNot Found")

if __name__ == '__main__':
    main()

```

Output:

```

Level 1    2: (3, 6) (4, 8)
Level 1    4: (6, 12) (7, 14) (8, 16) (9, 18)

Found

```

B+ Tree

Code:

```

import math

class Node:
    def __init__(self, order):

```



```

        self.order = order
self.values = []      self.keys
= []      self.nextKey =
None      self.parent =
None      self.check_leaf =
False

```

```

def insert_at_leaf(self, leaf, value, key):
    if (self.values):
        temp1 = self.values
for i in range(len(temp1)):
    if (value == temp1[i]):
        self.keys[i].append(key)
break      elif (value <
temp1[i]):
        self.values = self.values[:i] + [value] + self.values[i:]
self.keys = self.keys[:i] + [[key]] + self.keys[i:]
break      elif (i + 1 == len(temp1)):
self.values.append(value)      self.keys.append([key])
break      else:
        self.values = [value]
self.keys = [[key]]

```

```

class BplusTree:

```

```

def __init__(self, order):
self.root = Node(order)
self.root.check_leaf = True

def insert(self, value, key):
    value = str(value)
old_node = self.search(value)
old_node.insert_at_leaf(old_node,
value, key)

    if (len(old_node.values) == old_node.order):
        node1 = Node(old_node.order)
node1.check_leaf = True        node1.parent =
old_node.parent        mid = int(math.ceil(old_node.order /
2)) - 1        node1.values = old_node.values[mid + 1:]
node1.keys = old_node.keys[mid + 1:]        node1.nextKey
= old_node.nextKey        old_node.values =
old_node.values[:mid + 1]        old_node.keys =
old_node.keys[:mid + 1]        old_node.nextKey = node1
self.insert_in_parent(old_node, node1.values[0], node1)

def search(self, value):    current_node =
self.root    while(current_node.check_leaf
== False):
        temp2 = current_node.values
for i in range(len(temp2)):
    if (value == temp2[i]):

```

```

        current_node = current_node.keys[i + 1]
break        elif (value < temp2[i]):
        current_node = current_node.keys[i]
break        elif (i + 1 ==
len(current_node.values)):
current_node = current_node.keys[i + 1]
break
    return current_node

```

```

def find(self, value, key):    l =
self.search(value)    for i, item in
enumerate(l.values):        if item ==
value:            if key in l.keys[i]:
return True        else:
return False    return False

```

```

def insert_in_parent(self, n, value, ndash):
if (self.root == n):
    rootNode = Node(n.order)
rootNode.values = [value]
rootNode.keys = [n, ndash]
self.root = rootNode        n.parent
= rootNode        ndash.parent =
rootNode        return

```

```

    parentNode = n.parent
temp3 = parentNode.keys    for

```

```

i in range(len(temp3)):      if
(temp3[i] == n):

    parentNode.values = parentNode.values[:i] + \
        [value] + parentNode.values[i:]
    parentNode.keys = parentNode.keys[:i +
        1] + [ndash] + parentNode.keys[i + 1:]
    if (len(parentNode.keys) > parentNode.order):
        parentdash = Node(parentNode.order)
        parentdash.parent = parentNode.parent      mid =
        int(math.ceil(parentNode.order / 2)) - 1
        parentdash.values = parentNode.values[mid + 1:]
        parentdash.keys = parentNode.keys[mid + 1:]
        value_ = parentNode.values[mid]      if (mid == 0):
            parentNode.values = parentNode.values[:mid + 1]
        else:
            parentNode.values = parentNode.values[:mid]
        parentNode.keys = parentNode.keys[:mid + 1]      for j
        in parentNode.keys:      j.parent = parentNode
        for j in parentdash.keys:      j.parent = parentdash
        self.insert_in_parent(parentNode, value_, parentdash)

    def delete(self, value, key):
        node_ = self.search(value)

        temp = 0
        for i, item in enumerate(node_.values):
            if item == value:

```

```

        temp = 1

        if key in node_.keys[i]:
            if len(node_.keys[i]) > 1:

                node_.keys[i].pop(node_.keys[i].index(key))
            elif node_ == self.root:
                node_.values.pop(i)
            node_.keys.pop(i)
            else:
                node_.keys[i].pop(node_.keys[i].index(key))
            del node_.keys[i]
            node_.values.pop(node_.values.index(value))
            self.deleteEntry(node_, value, key)
            else:
                print("Value not in Key")
            return
            if temp == 0:
                print("Value not in Tree")
            return

```

```

def deleteEntry(self, node_, value, key):

    if not node_.check_leaf:
        for i, item in enumerate(node_.keys):
            if item == key:
                node_.keys.pop(i)
            break
        for i, item in
            enumerate(node_.values):
                if item
                    == value:

```

```

        node_.values.pop(i)
break

    if self.root == node_ and len(node_.keys) == 1:
        self.root = node_.keys[0]
node_.keys[0].parent = None
del node_        return

    elif (len(node_.keys) < int(math.ceil(node_.order / 2)) and node_.check_leaf
== False) or (len(node_.values) < int(math.ceil((node_.order - 1) / 2)) and
node_.check_leaf == True):

        is_predecessor = 0
parentNode = node_.parent

        PrevNode = -1
        NextNode = -1

        PrevK = -1        PostK = -1        for
i, item in enumerate(parentNode.keys):

            if item == node_:

if i > 0:

                PrevNode = parentNode.keys[i - 1]
                PrevK = parentNode.values[i - 1]

            if i < len(parentNode.keys) - 1:
NextNode = parentNode.keys[i + 1]
                PostK = parentNode.values[i]

```



```

        if PrevNode == -1:            ndash = NextNode
value_ = PostK            elif NextNode == -1:            is_predecessor
= 1            ndash = PrevNode            value_ = PrevK
else:            if len(node_.values) + len(NextNode.values) <
node_.order:
            ndash = NextNode
value_ = PostK            else:
            is_predecessor = 1
ndash = PrevNode
value_ = PrevK

        if len(node_.values) + len(ndash.values) < node_.order:
if is_predecessor == 0:            node_, ndash = ndash,
node_            ndash.keys += node_.keys            if not
node_.check_leaf:
            ndash.values.append(value_)
        else:
            ndash.nextKey = node_.nextKey
ndash.values += node_.values

        if not ndash.check_leaf:
for j in ndash.keys:
j.parent = ndash
            self.deleteEntry(node_.parent, value_, node_)
del node_            else:            if is_predecessor ==
1:            if not node_.check_leaf:

```

```

        ndashpm = ndash.keys.pop(-1)
ndashkm_1 = ndash.values.pop(-1)
node_.keys = [ndashpm] + node_.keys
node_.values = [value_] + node_.values
parentNode = node_.parent          for i, item in
enumerate(parentNode.values):
    if item == value_:
        p.values[i] = ndashkm_1
break                               else:
        ndashpm = ndash.keys.pop(-1)
ndashkm = ndash.values.pop(-1)
node_.keys = [ndashpm] + node_.keys
node_.values = [ndashkm] + node_.values
parentNode = node_.parent          for i, item in
enumerate(p.values):              if item == value_:
        parentNode.values[i] = ndashkm
break                             else:          if not
node_.check_leaf:
        ndashp0 = ndash.keys.pop(0)
ndashk0 = ndash.values.pop(0)      node_.keys
= node_.keys + [ndashp0]          node_.values =
node_.values + [value_]          parentNode =
node_.parent                      for i, item in
enumerate(parentNode.values):    if item ==
value_:
        parentNode.values[i] = ndashk0
break                             else:

```

```

        ndashp0 = ndash.keys.pop(0)
    ndashk0 = ndash.values.pop(0)
    node_.keys
    = node_.keys + [ndashp0]
    node_.values =
    node_.values + [ndashk0]
    parentNode =
    node_.parent
    for i, item in
    enumerate(parentNode.values):
        if item ==
    value_:
        parentNode.values[i] = ndash.values[0]
    break

```

```

        if not ndash.check_leaf:
    for j in ndash.keys:
        j.parent = ndash
        if not
    node_.check_leaf:
        for j in
    node_.keys:
        j.parent =
    node_
        if not
    parentNode.check_leaf:
    for j in parentNode.keys:
        j.parent = parentNode

```

```

def printTree(tree):
    lst = [tree.root]
    level = [0]
    leaf
    = None
    flag = 0
    lev_leaf = 0

```

```
node1 = Node(str(level[0]) + str(tree.root.values))
```

```
while (len(lst) != 0):      x =  
lst.pop(0)      lev = level.pop(0)  
if (x.check_leaf == False):      for i,  
item in enumerate(x.keys):  
    print(item.values)  
else:  
    for i, item in enumerate(x.keys):  
        print(item.values)  
if (flag == 0):  
lev_leaf = lev  
leaf = x      flag = 1
```

```
record_len = 3 bplustree =  
BplusTree(record_len)  
bplustree.insert('5', '33')  
bplustree.insert('15', '21')  
bplustree.insert('25', '31')  
bplustree.insert('35', '41')  
bplustree.insert('45', '10')
```

```
printTree(bplustree)
```

```
if(bplustree.find('45', '10')):  
    print("Found") else:
```

print("Not found") **Output:**

```
['15', '25']  
['35', '45']  
['5']  
Found
```