Articles → 451. Sort Characters By Frequency ▼

# 451. Sort Characters By Frequency

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Given a string, sort it in decreasing order based on the frequency of characters.

Example 1:

```
Input:
"tree"
Output:
"eert"
Explanation:
'e' appears twice while 'r' and 't' both appear once.
So 'e' must appear before both 'r' and 't'. Therefore "eetr" is also a valid answer.
```

Input:

Example 2:

```
"cccaaa"
 Output:
 "cccaaa"
 Explanation:
 Both 'c' and 'a' appear three times, so "aaaccc" is also a valid answer.
 Note that "cacaca" is incorrect, as the same characters must be together.
Example 3:
```

```
Input:
"Aabb"
Output:
"bbAa"
Explanation:
```

## cannot modify it. We can only create a new String. Consider the following Java code.

## String a = "Hello "; a += "Leetcode";

This code creates a String called a with the value "Hello". It then sets a to be a new String, made

For the most part, we don't run into problems with String's being treated like this. But consider this code for reversing a String.

```
String reversedString = "";
 for (int i = s.length() - 1; i >= 0; i--) {
     reversedString += s.charAt(i);
 System.out.println(reversedString);
Each time a character is added to reverseString, a new String is created. Creating a new String has a
```

using a web search. The algorithms provided in the solutions here all do string building efficiently. Approach 1: Arrays and Sorting Intuition In order to sort the characters by frequency, we firstly need to know how many of each there are. One way to do this is to sort the characters by their numbers so that identical characters are side-by-side (all characters

by converting it from a String to an Array of characters.

Now that we have an Array , we can sort it, which will make all identical characters side-by-side.

Sorted

Group

['c', 'c', 'd', 'e', 'e', 'e', 'e', 'e', 'l', 'l', 'm', 'o', 'o', 'o', 't', 't', 'w']

["cc", "d", "eeeee", "ll", "m", "ooo", "tt", "w"]

["eeeee", "ooo", "cc", "II", "tt", "d", "m", "w"]

## There are a few different ways we can go from here. One easy-to-understand way is to create a new Array of String s. Each String in the list will consist of one of the unique characters from the sorted characters

Remember: do this process using StringBuilder s, not naïve String appending! (See the first section of

```
String build
                                                                 "eeeeeoooccllttdmw"
 ["eeeee", "ooo", "cc", "ll", "tt", "d", "m", "w"]
Algorithm
                                                                                                                   Сору
```

all\_strings = [] 11 12  $cur_sb = [s[\theta]]$ 13 for c in s[1:]: 14 # If the last character on string builder is different... 15 if cur\_sb[-1] != c: 16 all\_strings.append("".join(cur\_sb)) cur\_sb = []

### 24 # Convert to a single string to return. 25 # Converting a list of strings to a string is often done # using this rather strange looking python idiom. return "".join(all\_strings) Complexity Analysis Let n be the length of the input String.

# Make a list of strings, one for each unique char.

because we are adding n characters to the end of a List . The second part of the algorithm, sorting the List of characters, has a cost of  $O(n \log n)$ . The third part of the algorithm, grouping the characters into String's of similar characters, has a cost of O(n) because each character is being inserted once into a StringBuilder and once converted into a String. Finally, the fourth part of the algorithm, sorting the String's by length, has a worst case cost of O(n), which occurs when all the characters in the input String are unique. Because we drop constants and insignificant terms, we get  $O(n \log n) + 3 \cdot O(n) = O(n \log n)$ . Be careful with your own implementation—if you didn't do the string building process in a sensible way, then your solution could potentially be  $O(n^2)$ . Space Complexity: O(n).

W E L C O M T D Next, extract a copy of the keys from the HashMap and sort them by frequency using a Comparator that

Another approach is to use a HashMap to count how many times each character occurs in the String; the

## # Count up the occurances. counts = collections.Counter(s) # Build up the string builder. string\_builder = [] for letter, freq in counts.most\_common():

10 11

1 def frequencySort(self, s: str) -> str:

# e.g. "a" \* 4 -> "aaaa"

# letter \* freq makes freq copies of letter.

1. We can disregard k, and consider that in the worst case, k = n.

string\_builder.append(letter \* freq)

Approach 2: HashMap and Sort

keys are characters and the values are frequencies.

looks at the HashMap values to make its decisions.

E O C L T D M W

return "".join(string\_builder) 12

We know that  $k \leq n$ , because there can't be more unique characters than there are characters in the String. We also know that k is somewhat bounded by the fact that there's only a finite number of

2. We can consider k, recognising that the number of unique characters is not infinite. This is more

```
because it made no difference there.
  • Time Complexity : O(n \log n) OR O(n + k \log k).
     Putting the characterss into the HashMap has a cost of O(n), because each of the n characterss must
     be put in, and putting each in is an O(1) operation.
     Sorting the HashMap keys has a cost of O(k \log k), because there are k keys, and this is the
     standard cost for sorting. If only using n, then it's O(n \log n). For the previous question, the sort was
     carried out on n items, not k, so was possibly a lot worse.
     Traversing over the sorted keys and building the String has a cost of O(n), as n characters must be
     inserted.
     Therefore, if we're only considering n, then the final cost is O(n \log n).
     Considering k as well gives us O(n + k \log k), because we don't know which is largest out of n and
     k \log k. We do, however, know that in total this is less than or equal to O(n \log n).
```

frequency for any one character is n. This means that once we've determined all the letter frequencies using a HashMap, we can sort them in O(n) time using **Bucket Sort**. Recall that for our previous approaches, we used comparison-based sorts, which have a cost of  $O(n \log n)$ . This was the HashMap from earlier.

Recall that Bucket Sort is the sorting algorithm where items are placed at Array indexes based on their values (the indexes are called "buckets"). For this problem, we'll need to have a List of characters at each

While we could simply make our bucket  $\frac{1}{2}$  length n, we're best to just look for the maximum value (frequency) in the HashMap. That way, we only use as much space as we need, and won't need to iterate

Finally, we need to iterate over the buckets, starting with the largest and ending with the smallest, building

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Sort By \*

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While the second approach is probably adequate for an interview, there is actually a way of solving this

Firstly, observe that because all of the characters came out of a String of length n, the maximum

### string\_builder = [] 15 for i in range(len(buckets) - 1, 0, -1): 16 for c in buckets[i]: 17 string\_builder.append(c \* i) 19 return "".join(string\_builder)

over heaps of empty buckets during the next phase.

up the string in much the same way as we did before.

# Bucket sort the characters by frequency. buckets = [[] for \_ in range(max\_freq + 1)]

considered for the last approach makes no difference this time).

Like before, the HashMap building has a cost of O(n).

```
Same as above. The bucket Array also uses O(n) space, because its length is at most n, and there
     are k items across all the buckets.
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```

public String frequencySort(String s) { PriorityOueuecMan.EntrycCharacter. Read More 2 A V & Share A Reply **SHOW 5 REPLIES** 

PS: PriorityQueue is the first thing that came to my mind when I did the "May LeetCoding Challenge". It

my3m ★ 558 ② March 15, 2020 7:13 AM Approach 1 last section can be simplified to return String.join("", charStrings); 1 A V E Share A Reply jingjing\_334 ★ 76 ② May 22, 2020 3:11 PM Wow thank you! I never thought there could be an O(n) solution. For years I thought O(nlogn) is the best possible solution. Thank you! I learned so much. geralt\_ # 28 @ June 2, 2020 9:49 PM With time complexity : O(n) Space complexity: O(1) coz at max its 256 chars

Read More 0 A V E Share Share SHOW 1 REPLY sea0920 \* 176 May 31, 2020 5:39 AM This bucket sort solution takes longer than a solution using generic sort. I think there is overhead in getting max freq, creating/iterating empty buckets. 0 ∧ ∨ Ø Share ♠ Reply

**6** 🖸 🗓

Average Rating: 4.95 (41 votes)

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with the letters from the old a and the additional letters "Leetcode". It then assigns this new String to

String s = "Hello There";

The solution is to use a StringBuilder. A StringBuilder collects up the characters that will be converted into a String so that only one String needs to be created—once all the characters are ready to go. Recall that inserting an item at the end of an f Array has a cost of O(1), and so the total cost of inserting the n characters into the StringBuilder is O(n), and it is also O(n) to then convert that StringBuilder into a String, giving a total of O(n). String s = "Hello There"; StringBuilder sb = new StringBuilder(); for (int i = s.length() - 1; i >= 0; i--) { sb.append(s.charAt(i)); String reversedString = sb.toString();

in a programming language are identified by a unique number). Then, knowing how many times each appears will be a lot easier. Because String s are immutable though, we cannot sort the String directly. Therefore, we'll need to start "welcometoleetcode" ['w', 'e', 'l', 'c', 'o', 'm', 'e', 't', 'o', 'l', 'e', 'e', 't', 'c', 'o', 'd', 'e']

this article if you're confused). The next step is to sort this Array of String's by length. To do this, we'll need to implement a suitable Comparator. Recall that there is no requirement for characters of the same frequency to appear in a specific order.

Length sort

if not s: return s # Convert s to a list. s = list(s) # Sort the characters in s. s.sort()

 Time Complexity: O(n log n). The first part of the algorithm, converting the String to a List of characters, has a cost of O(n),

It is impossible to do better with the space complexity, because String's are immutable. The List of characters, List of Strings, and the final output String, are all of length n, so we have a space complexity of O(n).

Finally, initialise a new StringBuilder and then iterate over the list of sorted characters (sorted by frequency). Look up the values in the HashMap to know how many of each character to append to the StringBuilder. Algorithm

Copy

## **Complexity Analysis** Let n be the length of the input String and k be the number of unique characters in the String.

accurate for real world purposes.

The HashMap uses O(k) space.

better with the space complexity here.

Approach 3: Multiset and Bucket Sort

problem with a time complexity of O(n).

Intuition

Space Complexity: O(n).

However, the StringBuilder at the end dominates the space complexity, pushing it up to O(n), as every character from the input String must go into it. Like was said above, it's impossible to do

W E L C O M T D

index. For example, here is how our **string** from before goes into the buckets.

for c, i in counts.items():

buckets[i].append(c)

# Build up the string.

It'd be impossible to do better than this, because we need to look at each of the n characters in the input String at least once. Space Complexity: O(n).

Let n be the length of the input String . The k (number of unique characters in the input String that we

The bucket sorting is O(n), because inserting items has a cost of O(k) (each entry from the

HashMap ), and building the buckets initially has a worst case of O(n) (which occurs when k=1).

NeosDeus ★ 278 ② March 6, 2020 9:19 AM Super clean written article! Looking forward to your next one @Hai\_dee! 19 ∧ ∨ E Share → Reply SHOW 2 REPLIES

ztztzt8888 🛊 55 ② May 22, 2020 10:33 PM

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class Solution {

"bbaA" is also a valid answer, but "Aabb" is incorrect. Note that 'A' and 'a' are treated as two different characters. Solution Remember, Strings are Immutable! The input type for this question is a String. When dealing with Strings, we need to be careful to not inadvertently convert what should have been an O(n) algorithm into an  $O(n^2)$  one. String s in most programming languages are immutable. This means that once a String is created, we

# the variable a , throwing away the reference to the old one. It does NOT actually "modify" a .

cost of n, where n is the length of the String. The result? Simply reversing a String has a cost of  $O(n^2)$ using the above algorithm.

If you're unsure what to do for your particular programming language, it shouldn't be too difficult to find

System.out.println(reversedString);

['w', 'e', 'l', 'c', 'o', 'm', 'e', 't', 'o', 'l', 'e', 'e', 't', 'c', 'o', 'd', 'e'] Array.

['c', 'c', 'd', 'e', 'e', 'e', 'e', 'e', 'l', 'l', 'm', 'o', 'o', 'o', 't', 't', 'w']

["cc", "d", "eeeee", "ll", "m", "ooo", "tt", "w"] Finally, we can convert this Array of Strings into a single String. In Java, this can be done by passing the Array into a StringBuilder and then calling .toString(...) on it.

Java Python

1 def frequencySort(self, s: str) -> str:

17 18 cur\_sb.append(c) 19 all\_strings.append("".join(cur\_sb)) 20 21 # Sort the strings by length from \*longest\* to shortest. 22 all\_strings.sort(key=lambda string : len(string), reverse=True) 23

10

Intuition

characters in Unicode (or ASCII, which I suspect is all we need to worry about for this question). There are two ways of approaching the complexity analysis for this question. I've provided analysis for both ways of approaching it. I choose not to bring it up for the previous approach,

What's interesting here is that if we only consider n, the time complexity is the same as the previous approach. But by considering k, we can see that the difference is potentially substantial.

> Java Python 1 def frequencySort(self, s: str) -> str: if not s: return s # Determine the frequency of each character. counts = collections.Counter(s) max\_freq = max(counts.values())

11

13

**Complexity Analysis** 

Time Complexity: O(n).

Because  $k \leq n$ , we're left with O(n).

So in total, we have O(n).

Algorithm

0 1 2 3 4

W L 0

М C

D Т

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@ Preview

ChaoWan\_2020 ★ 46 ② April 14, 2020 7:34 PM This should be easy level



(12)

very clean and informative 0 ∧ ∨ Ø Share ♠ Reply absolut\_red # 6 @ May 23, 2020 8:35 AM Very well written article @Hai\_dee! all the characters in the input String are unique. 0 A V & Share + Reply meyerhot 🖈 21 🗿 May 22, 2020 10:26 PM

Finally, the fourth part of the algorithm, sorting the Strings by length, has a worst case cost of O(n), which occurs when Read More This is a medium yet pairs of songs divisible by 60 is easy...yeaaaalriiiight. 0 ∧ ∨ ₾ Share ♠ Reply