f 💟 in

72. Edit Distance

**** Average Rating: 4.38 (56 votes)

You have the following 3 operations permitted on a word: 1. Insert a character 2. Delete a character

Given two words word1 and word2, find the minimum number of operations required to convert word1 to

3. Replace a character

- Example 1:
 - Input: word1 = "horse", word2 = "ros"

horse -> rorse (replace 'h' with 'r') rorse -> rose (remove 'r')

Output: 3

Explanation:

word2.

```
rose -> ros (remove 'e')
Example 2:
 Input: word1 = "intention", word2 = "execution"
 Output: 5
 Explanation:
 intention -> inention (remove 't')
```

```
Solution
Intuition
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The edit distance algorithm is very popular among the data scientists. It's one of the basic algorithms used

between. That would result in an exponential complexity and it's an overkill since we actually don't need to

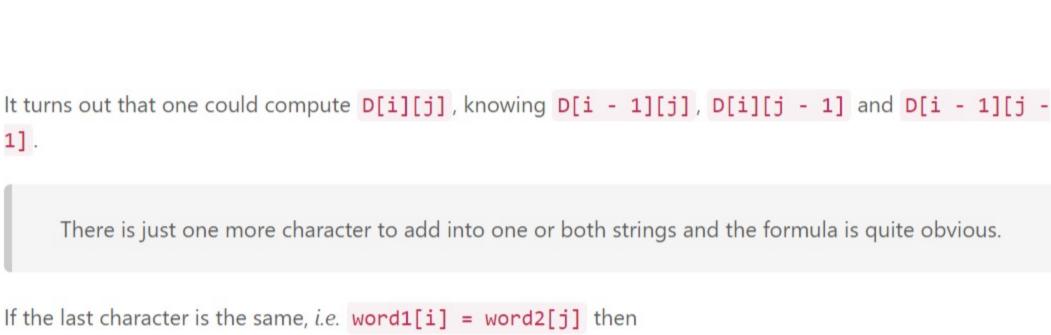
The naive approach would be to check for all possible edit sequences and choose the shortest one in-

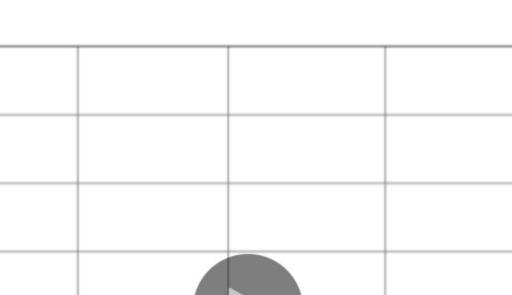
for evaluation of machine translation and speech recognition.

have all possible edit sequences but just the shortest one.

Approach 1: Dynamic Programming

The idea would be to reduce the problem to simple ones. For example, there are two words, horse and ros and we want to compute an edit distance D for them. One could notice that it seems to be more simple for short words and so it would be logical to relate an edit distance D[n][m] with the lengths n and





D[i][j] = ? the edit distance between HOR and RO D[i][j] = 1 + min(D[i - 1][j], D[i][j - 1], D[i - 1][j - 1]), since R! = 0



R s # 0 def minDistance(self, word1, word2): :type word1: str :type word2: str # if one of the strings is empty return n + m# array to store the convertion history $d = [0] * (m + 1) for _ in range(n + 1)]$ # init boundaries for i in range(n + 1):

🔁 Сору

149 A V C Share Reply **SHOW 3 REPLIES**



Plain English Description w/ JavaScript Solution:

9 A V C Share Reply fawadsuhail 🛊 6 🗿 February 1, 2020 5:39 AM 6 A V C Share Reply

> bykov * 16 • August 31, 2019 3:41 AM um, wouldn't it be easier to say: reduce the problem to find the LCS and max diff with it? 2 A V C Share Reply **SHOW 1 REPLY**

for i in range(1. len(word2) + 1): 2 A V C Share Reply

afung95014 * 0 • May 10, 2019 11:16 PM

(1 2 3)

inention -> enention (replace 'i' with 'e') enention -> exention (replace 'n' with 'x') exention -> exection (replace 'n' with 'c') exection -> execution (insert 'u')

1].

[0] = i and D[0][j] = j.

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Java Python

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Complexity Analysis

class Solution:

:rtype: int

n = len(word1)

m = len(word2)

if n * m == 0:

d[i][0] = i

d[0][j] = j

DP compute

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for j in range(m + 1):

for i in range(1, n + 1):

for j in range(1, m + 1):

left = d[i - 1][j] + 1

• Time complexity : $\mathcal{O}(mn)$ as it follows quite straightforward for the inserted loops.

• Space complexity : $\mathcal{O}(mn)$ since at each step we keep the results of all previous computations.

Now we have everything to actually proceed to the computations

m of input words.

Let's go further and introduce an edit distance D[i][j] which is an edit distance between the first i characters of word1 and the first j characters of word2.

D[i][j] = the edit distance between word1[1..i] and word2[1..j] i.e. between HOR and RO

word1[1..i] word2[1..j]

If the last character is the same, i.e. word1[i] = word2[j] then $D[i][j] = 1 + \min(D[i-1][j], D[i][j-1], D[i-1][j-1] - 1)$ and if not, i.e. word1[i] != word2[j] we have to take into account the replacement of the last character during the conversion. $D[i][j] = 1 + \min(D[i-1][j], D[i][j-1], D[i-1][j-1])$ So each step of the computation would be done based on the previous computation, as follows:

D[i-1][j] = 1 the edit distance between HO and RO D[i][j-1] = 2 the edit distance between HOR and R D[i-1][j-1]=2 the edit distance between HO and R

D[i][j] = 2

The obvious base case is an edit distance between the empty string and non-empty string that means D[i]

O Previous Next **1** Comments: 30 Sort By -Type comment here... (Markdown is supported) **Post** Preview tomasnovella 🛊 154 🗿 January 23, 2019 1:34 AM A Report Reaaaaally? You guys don't even mention in the solution that it's a good old Levenshtein distance? Please if you use some known algorithm, at least mention it! robta00 🛊 57 🗿 January 11, 2019 6:05 AM Thanks to the guy who contributes to this answer, but when word[i] == word[j], it's simply dp[i][j] = dp[i-1][j-1]. The way the answer is written might look more consistent in two cases but it's more confusing. **SHOW 8 REPLIES** ect582 * 78 ② January 10, 2019 6:41 AM A Report Please do not provide spaghetti code like this: if (n * m == 0)return n + m;

preceding inputs. One crucial step here is that the "base case" starts off with the empty String. Read More 32 A V C Share Reply SHOW 3 REPLIES

Effectively, what the solution above is describing is the creation of a matrix/table that has inputs for all

For all the people who want to have a better understanding of this problem I will refer to Algorithm

Because I have been trying to write solutions, I always wanted to make such a video to describe my

A Report

A Report

Best explanation of the algorithm https://medium.com/@ethannam/understanding-the-levenshteindistance-equation-for-beginners-c4285a5604f0 bupt_wc ★ 910 ② November 24, 2018 10:16 AM Hi, @andvary, I'm very curious about how the short video in this solution is made.

aramik 🛊 29 🗿 March 26, 2019 10:37 AM

Design Manual book by Steven Skiena page 282 or section 8.2.2.

A Report ruinart ★ 32 ② November 29, 2018 4:40 AM O(n)-space Python: n = len(word1)dp = [i for i in range(n + 1)]

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ideas. Can you tell me what the name of this video is, and it would be better if you could recommend a software for making this video. Read More 4 A V C Share Reply **SHOW 1 REPLY**