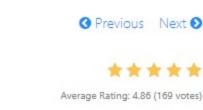
221. Maximal Square 💆

July 14, 2016 | 196.1K views



(1) (2) (3)

Given a 2D binary matrix filled with 0's and 1's, find the largest square containing only 1's and return its area. Example:

```
Input:
10100
10111
1 1 1 1 1
10010
Output: 4
```

Solution

within the matrix. The question now is - how to go for it?

of the current, both initialized to 0. Starting from the left uppermost point in the matrix, we search for a 1. No operation needs to be done for a 0. Whenever a 1 is found, we try to find out the largest square that can be

and column index temporarily and then check whether all the elements of that row and column are 1 or not. If all the elements happen to be 1, we move diagonally further as previously. If even one element turns out to be 0, we stop this diagonal movement and update the size of the largest square. Now we, continue the traversal of the matrix from the element next to the initial 1 found, till all the elements of the matrix have been traversed. Java public class Solution { public int maximalSquare(char[][] matrix) {

```
for (int j = 0; j < cols; j++) {
                 if (matrix[i][j] == '1') {
                     int sqlen = 1;
                     boolean flag = true;
                     while (sqlen + i < rows && sqlen + j < cols && flag) {
                          for (int k = j; k <= sqlen + j; k++) {
                              if (matrix[i + sqlen][k] == '0') {
                                  flag = false;
                                  break;
                              }
                         for (int k = i; k <= sqlen + i; k++) {
                              if (matrix[k][j + sqlen] == '0') {
                                  flag = false;
                                  break;
                              }
                         }
                         if (flag)
                              sqlen++;
                     }
                     if (maxsqlen < sqlen) {</pre>
                         maxsqlen = sqlen;
                     }
                 }
             }
        }
        return maxsqlen * maxsqlen;
    }
}
• Time complexity : O((mn)^2). In worst case, we need to traverse the complete matrix for every 1.
```

We initialize another matrix (dp) with the same dimensions as the original one initialized with all 0's.

0 1 1 1 1 00111

Original Matrix 2

}

return maxsqlen * maxsqlen;

}

public class Solution {

}

}

}

Complexity Analysis

}

}

Java

0 1 1 1 1

in the original matrix.

as

```
dp(i, j) = min (dp(i-1, j), dp(i-1, j-1), dp(i, j-1)) + 1.
We also remember the size of the largest square found so far. In this way, we traverse the original matrix
once and find out the required maximum size. This gives the side length of the square (say maxsqlen). The
```

dp(i,j) represents the side length of the maximum square whose bottom right corner is the cell with index (i,j)

Starting from index (0,0), for every 1 found in the original matrix, we update the value of the current element

1 1 1 1 0 1 1 0 1 1 1 0 1 0 1 1 1 1 1 3 1 0 0 1 1 **(1**) 3 0 2

```
An entry 2 at (1,3) implies that we have a square of side 2 up to that index in the original matrix. Similarly, a
2 at (1,2) and (2,2) implies that a square of side 2 exists up to that index in the original matrix. Now to
make a square of side 3, only a single entry of 1 is pending at (2,3). So, we enter a 3 corresponding to that
position in the dp array.
Now consider the case for the index (3,4). Here, the entries at index (3,3) and (2,3) imply that a square of
side 3 is possible up to their indices. But, the entry 1 at index (2,4) indicates that a square of side 1 only can
be formed up to its index. Therefore, while making an entry at the index (3,4), this element obstructs the
formation of a square having a side larger than 2. Thus, the maximum sized square that can be formed up to
this index is of size 2 \times 2.
```

int rows = matrix.length, cols = rows > 0 ? matrix[0].length : 0; int[][] dp = new int[rows + 1][cols + 1]; int maxsqlen = 0; for (int i = 1; i <= rows; i++) { for (int j = 1; j <= cols; j++) { if (matrix[i-1][j-1] == '1'){

maxsqlen = Math.max(maxsqlen, dp[i][j]);

dp[i][j] = Math.min(Math.min(dp[i][j - 1], dp[i - 1][j]), dp[i - 1

```
}
Complexity Analysis
  • Time complexity : O(mn). Single pass.
  • Space complexity : O(mn). Another matrix of same size is used for dp.
Approach #3 (Better Dynamic Programming) [Accepted]
```

min(prev,dp[i-1],dp[i]) java

public int maximalSquare(char[][] matrix) {

int[] dp = new int[cols + 1]; int maxsqlen = 0, prev = 0;

for (int i = 1; i <= rows; i++) {

int temp = dp[j];

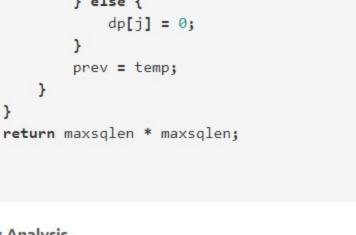
} else {

for (int j = 1; j <= cols; j++) {

if (matrix[i - 1][j - 1] == '1') {

prev

dp[i-1]



Analysis written by: @vinod23 Rate this article: * * * * *

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How can one come up with this solution during an interview......

Preview

Type comment here... (Markdown is supported)

leetcodefan ★ 1942 ② February 1, 2019 2:06 AM The DP approach is brilliant! I love this problem.

34 A V C Share A Reply

SHOW 1 REPLY

StefanPochmann * 50877 July 19, 2016 7:04 AM Btw, something about the title, more precisely the word "maximal": In math/compsci, that roughly speaking means something that can't be made larger by adding something to it. For example, in the

I think code should be like below to follow the first image. It created a col * row size dp matrix, but

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13 A V C Share Reply SHOW 1 REPLY

PepperGo ★ 178 ② November 11, 2018 10:20 PM

SHOW 3 REPLIES HelloImLiXin 🛊 9 🗿 March 6, 2020 12:43 AM

def maximalSquare(self, matrix: List[List[str]]) -> int: if not matrix: 5 A V Share Share Reply

class Solution:

(1 2 3 4 5 6 7)

Summary We need to find the largest square comprising of all ones in the given m imes n matrix. In other words we need to find the largest set of connected ones in the given matrix that forms a square. Approach #1 Brute Force [Accepted] The simplest approach consists of trying to find out every possible square of 1's that can be formed from

We use a variable to contain the size of the largest square found so far and another variable to store the size formed including that 1. For this, we move diagonally (right and downwards), i.e. we increment the row index

int rows = matrix.length, cols = rows > 0 ? matrix[0].length : 0; int maxsqlen = 0; for (int i = 0; i < rows; i++) {

Complexity Analysis Space complexity: O(1). No extra space is used. Approach #2 (Dynamic Programming) [Accepted] Algorithm

We will explain this approach with the help of an example. 01110 11111

required result is the area $maxsqlen^2$. To understand how this solution works, see the figure below.

0 1 1 1 0 1

dp

public class Solution { public int maximalSquare(char[][] matrix) {

Algorithm In the previous approach for calculating dp of i^{th} row we are using only the previous element and the (i- $1)^{th}$ row. Therefore, we don't need 2D dp matrix as 1D dp array will be sufficient for this. Initially the dp array contains all 0's. As we scan the elements of the original matrix across a row, we keep on updating the dp array as per the equation dp[j] = min(dp[j-1], dp[j], prev), where prev refers to the old dp[j-1]. For every row, we repeat the same process and update in the same dp array.

dp[i]

new_dp[i]

int rows = matrix.length, cols = rows > 0 ? matrix[0].length : 0;

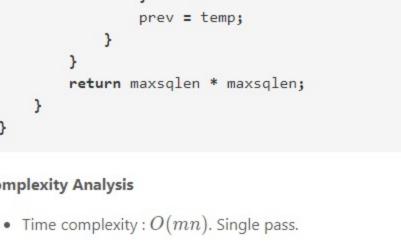
maxsqlen = Math.max(maxsqlen, dp[j]);

dp[j] = Math.min(Math.min(dp[j - 1], prev), dp[j]) + 1;

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• Space complexity : O(n). Another array which stores elements in a row is used for dp.

302 A V C Share Share SHOW 17 REPLIES eefiasfira 🛊 595 🗿 September 26, 2019 1:44 PM For all people wondering how you'd solve this in an interview in 30 mins - this is a fairly easy DP problem. If you're confused its because the explanation jumps into the bottom-up DP solution without explaining how it got there. You can never figure out a bottom-up DP solution without first figuring out a top down recursive approach. If during the recursion you find you're solving the same 241 A V C Share Reply **SHOW 16 REPLIES**

10100 Read More 33 A V 🗹 Share 🦘 Reply SHOW 2 REPLIES djy0 🛊 21 🗿 August 6, 2017 9:08 PM @keitaito You are right. The picture and depiction in article isn't consistent with its code.

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jeremyasm ★ 206 ② August 3, 2019 7:49 PM After hours, I finally undertand that in Approach 3 the 'prev' stores the dp[j - 1] of the previous row. At first the code really puzzled me (although the pic is clear). What a brilliant solution!

t4sk 🛊 9 🗿 January 20, 2018 9:06 AM

added judgement for i != 0 && j != 0.

when iterating the first row or first column, the formula for dp(i, j) is checking for values out of bounds. By shifting the whole dp to the right and bottom by 1 and adding a padding of 0's to the 1st row and 1st column, it makes the formula work without checking for boundaries. 9 A V Share Share Reply

for solution 2, what are the benefits to set dp[][] size as rows + 1 and cols + 1 instead of rows and cols? 6 A V C Share Share Here's a Python3 version of the approach #2 discussed in the article:

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brian37 ★ 79 ② April 17, 2019 9:51 PM Dp is awesome! 5 A V C Share Reply