# 351. Android Unlock Patterns 4

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**6 0 0** 

number of unlock patterns of the Android lock screen, which consist of minimum of **m** keys and maximum **n** keys.

Given an Android **3x3** key lock screen and two integers **m** and **n**, where  $1 \le m \le n \le 9$ , count the total

## Each pattern must connect at least m keys and at most n keys. 2. All the keys must be distinct.

Rules for a valid pattern:

- 3. If the line connecting two consecutive keys in the pattern passes through any other keys, the other keys
- must have previously selected in the pattern. No jumps through non selected key is allowed.
- The order of keys used matters.



4 5 6 7 8 9

```
Invalid move: 4 - 1 - 3 - 6
Line 1 - 3 passes through key 2 which had not been selected in the pattern.
Invalid move: 4 - 1 - 9 - 2
Line 1 - 9 passes through key 5 which had not been selected in the pattern.
```

Valid move: 2 - 4 - 1 - 3 - 6

Line 1 - 3 is valid because it passes through key 2, which had been selected in the pattern

Valid move: 6 - 5 - 4 - 1 - 9 - 2 Line 1 - 9 is valid because it passes through key 5, which had been selected in the pattern.

Example:

Input: m = 1, n = 1Output: 9

## Summary

Arrays.

Solution

The algorithm uses backtracking technique to enumerate all possible k combinations of numbers  $[1 \dots 9]$ 

ullet Select a digit i which is not used in the pattern till this moment. This is done with the help of a used

ullet We need to keep last inserted digit last. The algorithm makes a check whether one of the following

After Android launched its "unlock pattern" system to protect our smart phones from unauthorized access, the most common question that comes to one's mind is: How secure exactly are these patterns? The current article gives an answer to this question, as presenting an algorithm, which computes the number of all valid pattern combinations. It is intended for intermediate users and introduces the following ideas: Backtracking,

### where $m \leq k \leq n$ . During the generation of the recursive solution tree, the algorithm cuts all the branches which lead to patterns which doesn't satisfy the rules and counts only the valid patterns. In order to compute

Algorithm

Approach #1: (Backtracking) [Accepted]

array which stores all available digits.

selected.

Java

}

}

return res;

if (used[index])

return false;

// first digit of the pattern

private boolean isValid(int index, int last) {

a valid pattern, the algorithm performs the following steps:

conditions is valid.  $\circ$  There is a knight move (as in chess) from last towards i or last and i are adjacent digits in a row, in a column. In this case the sum of both digits should be an odd number.

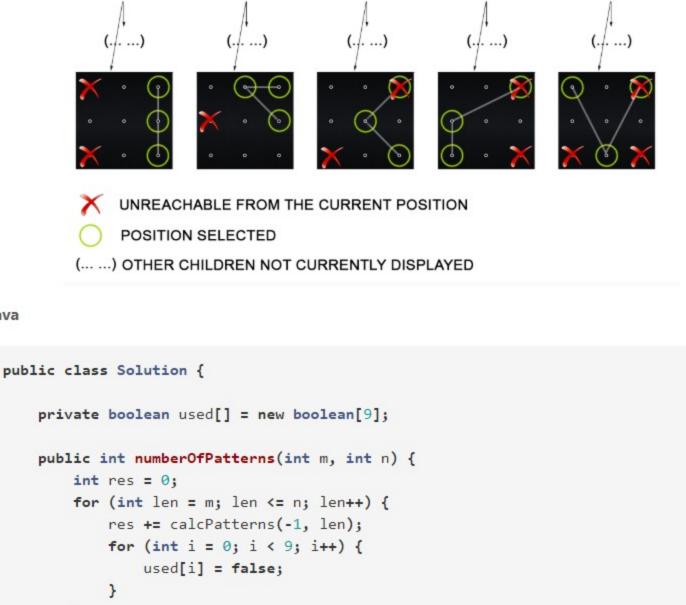
 $\circ \; last \; {
m and} \; i \; {
m are} \; {
m adjacent} \; {
m digits} \; {
m in} \; {
m a} \; {
m diagonal}$ In case one of the conditions above is satisfied, digit i becomes part of partially generated valid pattern and the algorithm continues with the next candidate digit till the pattern is fully generated. Then it counts it. In

case none of the conditions are satisfied, the algorithm rejects the current digit i, backtracks and continues

 $\circ$  The middle element mid in the line which connects i and last was previously selected. In case i

and last are positioned at both ends of the diagonal, digit mid = 5 should be previously

- to search for other valid digits among the unused ones. RECURSIVE TREE FOR ANDROID UNLOCK PATTERN COMPUTATION



```
if (last == -1)
               return true;
           // knight moves or adjacent cells (in a row or in a column)
           if ((index + last) % 2 == 1)
               return true;
           // indexes are at both end of the diagonals for example 0,0, and 8,8
           int mid = (index + last)/2;
           if (mid == 4)
               return used[mid];
           // adjacent cells on diagonal - for example 0,0 and 1,0 or 2,0 and //1,1
           if ((index%3 != last%3) && (index/3 != last/3)) {
               return true;
           // all other cells which are not adjacent
           return used[mid];
      }
      private int calcPatterns(int last, int len) {
           if (len == 0)
               return 1;
           int sum = 0;
           for (int i = 0; i < 9; i++) {
               if (isValid(i, last)) {
                    used[i] = true;
                    sum += calcPatterns(i, len - 1);
                    used[i] = false;
               }
           }
           return sum;
      }
  }
Complexity Analysis
  • Time complexity : O(n!), where n is maximum pattern length
     The algorithm computes each pattern once and no element can appear in the pattern twice. The time
     complexity is proportional to the number of the computed patterns. One upper bound of the number
     of all possible combinations is:
                                     \sum_{i=m}^{n} {}_{9}P_{i} = \sum_{i=m}^{n} \frac{9!}{(9-i)!}
  • Space complexity : O(n), where n is maximum pattern length In the worst case the maximum depth of
     recursion is n. Therefore we need O(n) space used by the system recursive stack
Further Thoughts
The algorithm above could be optimized if we consider the symmetry property of the problem. We notice
that the number of valid patterns with first digit 1, 3, 7, 9 are the same. A similar observation is true for
patterns which starts with digit 2, 4, 6, 8. Hence we only need to calculate one among each group and
multiply by 4.
You can find the optimized solution here.
Analysis written by: @elmirap.
Rate this article: * * * * *
```

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## ArizonaTea ★ 313 ② February 2, 2019 12:43 AM Knight jump is condition free....wow... Look at the problem description and its examples, so misleading. 47 A V C Share Share

Preview

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s961206 # 619 / July 31, 2019 3:07 AM I think the three line code is useless?

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What do the examples mean ?? I don't get it.

logical\_paradox ★ 237 ② November 22, 2018 12:07 AM

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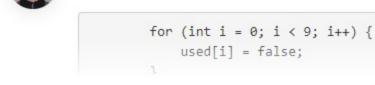
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the 8,8 in the comment is so confusing, please change it to (2,2)

indexes are at both end of the diagonals for example 0,0, and 8,8 adjacent cells on diagonal - for example 0,0 and 1,0 or 2,0 and //1,1

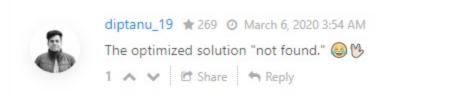
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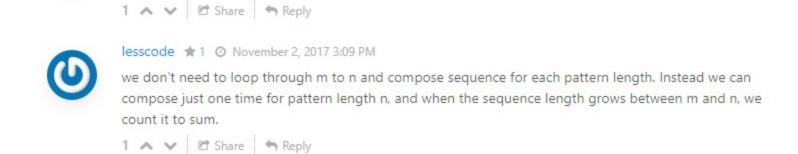


bigonze 🛊 1 🗿 December 13, 2019 10:53 PM

to have already been visited!! Please clarify it.

ambareeshsrja16 🖈 110 🗿 May 7, 2019 9:51 AM

Dead link for optimized solution code, please change?



When looking at the problem description this is not clear that the move 1 -> 8 does not need 4 and 5

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