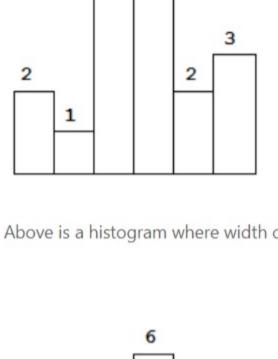
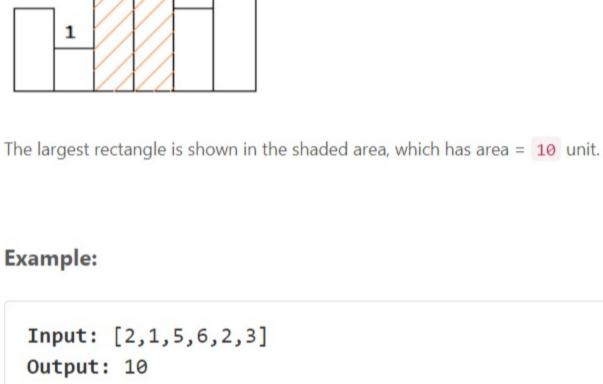
**LeetCode** 

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5

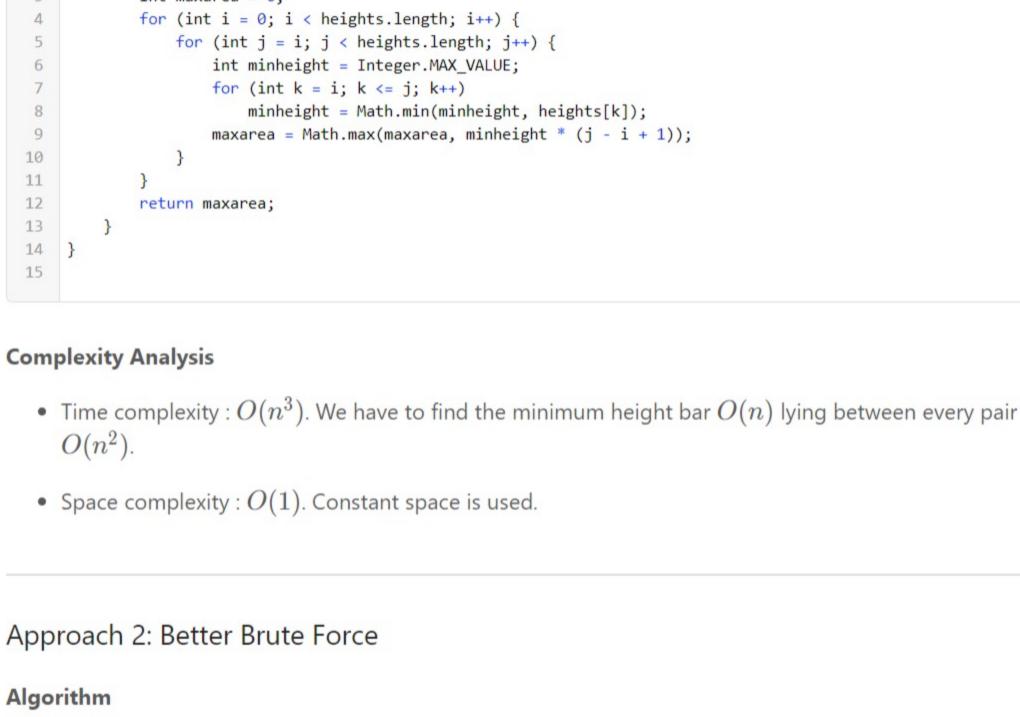


2

Approach 1: Brute Force

# 4

2 min. height 1



We can do one slight modification in the previous approach to optimize it to some extent. Instead of taking

every possible pair and then finding the bar of minimum height lying between them everytime, we can find

In mathematical terms,  $minheight = \min(minheight, heights(j))$ , where heights(j) refers to the

🔁 Сору

the bar of minimum height for current pair by using the minimum height bar of the previous pair.

### 7 8 9 }

height of the jth bar.

public class Solution {

int maxarea = 0;

return maxarea;

public int largestRectangleArea(int[] heights) {

for (int i = 0; i < heights.length; i++) {

int minheight = Integer.MAX\_VALUE;

• Space complexity : O(1). No extra space is used.

Approach 3: Divide and Conquer Approach

for (int j = i; j < heights.length; j++) {</pre>

minheight = Math.min(minheight, heights[j]);

maxarea = Math.max(maxarea, minheight \* (j - i + 1));

Java

1 2

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12 13

**Algorithm** 

- **Complexity Analysis** • Time complexity :  $O(n^2)$ . Every possible pair is considered
- 3. The largest rectangle confined to the right of the shortest bar(subproblem). Let's take an example:

Here, the shortest bar is of height 2. The area of the widest rectangle using this bar as height is 2x8=16. Now,

we need to look for cases 2 and 3 mentioned above. Thus, we repeat the same process to the left and right

6x1=6 and 5x1=5 exist in its left and right respectively. Similarly we find an area of 3x3=9, 4x1=4 and 9x1=9

2

2

**С**ору

to the left of 2. Thus, we get 16 as the correct maximum area. See the figure below for further clarification:

of 2. In the left of 2, 4 is the minimum, forming an area of rectangle 4x3=12. Further, rectangles of area

## 4 2

3

2

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**Complexity Analysis** 

conquer.

• Time complexity:

Average Case:  $O(n \log n)$ .

public class Solution { public int calculateArea(int[] heights, int start, int end) { 3 if (start > end) 4 return 0; 5 int minindex = start; 6 for (int i = start; i <= end; i++)

return Math.max(heights[minindex] \* (end - start + 1), Math.max(calculateArea(heights, start,

Worst Case:  $O(n^2)$ . If the numbers in the array are sorted, we don't gain the advantage of divide and

```
You can observe that in the Divide and Conquer Approach, we gain the advantage, since the large problem is
divided into substantially smaller subproblems. But, we won't gain much advantage with that approach if the
array happens to be sorted in either ascending or descending order, since every time we need to find the
minimum number in a large subarray O(n). Thus, the overall complexity becomes O(n^2) in the worst case.
We can reduce the time complexity by using a Segment Tree to find the minimum every time which can be
done in O(\log n) time.
For implementation, click here.
Complexity Analysis
   • Time complexity : O(n \log n). Segment tree takes \log n for a total of n times.
   • Space complexity : O(n). Space required for Segment Tree.
Approach 5: Using Stack
Algorithm
In this approach, we maintain a stack. Initially, we push a -1 onto the stack to mark the end. We start with the
leftmost bar and keep pushing the current bar's index onto the stack until we get two successive numbers in
```

descending order, i.e. until we get a[i]. Now, we start popping the numbers from the stack until we hit a

number stack[j] on the stack such that  $aigl[stack[j]igr] \le a[i]$ . Every time we pop, we find out the area of

rectangle formed using the current element as the height of the rectangle and the difference between the

width i.e. if we pop an element stack[top] and i is the current index to which we are pointing in the original

 $(i - stack[top - 1] - 1) \times a[stack[top]].$ 

Further, if we reach the end of the array, we pop all the elements of the stack and at every pop, this time we

stack[top] refers to the element just popped. Thus, we can get the area of the of the largest rectangle by

3]

maxarea = Math.max(maxarea, heights[stack.pop()] \* (i - stack.peek() - 1));

M

M

while (stack.peek() != -1 && heights[stack.peek()] >= heights[i])

Max Area=0

1/18

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A Report

A Report

-1

Stack

use the following equation to find the area: (stack[top] - stack[top-1]) imes a ig[ stack[top] ig] , where

The following example will clarify the process further: [6, 7, 5, 2, 4, 5, 9, 3]

the current element's index pointed to in the original array and the element stack[top-1]-1 as the

array, the current area of the rectangle will be considered as:

# [6, 0

Java

1

2

3

4

6

7 8

9

10

**Complexity Analysis** 

O Previous

Comments: 37

• Space complexity : O(n). Stack is used. Rate this article: \* \* \* \* \*

33 A V Share Reply go2ready 🛊 13 🗿 February 22, 2018 1:43 PM I guess there is a typo in the description of the algorithm. The second equation used to find area when

it is a typo? Or I have misunderstood sth.

dance-henry ★ 22 ② September 12, 2019 12:22 PM

1. the stack is used to stored the index.

There are 3 critical points to understand the stack approach.

13 A V Share Seply

SHOW 3 REPLIES

laaptu 🛊 42 🧿 March 12, 2019 6:09 AM

solution of this problem using stack based approach.

argest Rectangle in

**SHOW 1 REPLY** 

nxn \* 70 • September 15, 2018 8:39 AM What's the intuition behind the stack approach? Like why does this: (i-stack[top-1]-1)xa[stack[top]] work? What I mean is what's the relationship between a[stack[top]] and stack[top-1] as an index? I have seen several explanations of this solution from different sources but nobody has an intuitive explanation of why it works.

and paste the Java solution it works..

2 A V C Share Reply

( 1 2 3 4 )

7 A V Share Share Reply

lh19900702 ★94 ② May 25, 2017 8:14 AM

The last step of animation is wrong. The final result 16 comes from (the minimum height 2 \* the number of column 8). This is because, the last stop of i is 7. 2 \* (7 - (-1)) = 16 as well. The algorithm for ending is incorrect. 4 ^ V Share Reply SHOW 1 REPLY boy27910231 🛊 98 🗿 April 5, 2017 9:53 AM

def largestRectangleArea(self, heights: List[int]) -> int:

0 Right pointer Left pointer area. Java public class Solution { 1 public int largestRectangleArea(int[] heights) { 2 3 int maxarea = 0;

This approach relies on the observation that the rectangle with maximum area will be the maximum of: 1. The widest possible rectangle with height equal to the height of the shortest bar. 2. The largest rectangle confined to the left of the shortest bar(subproblem).

[6, 4, 5, 2, 4, 3, 9]

10

6

4

Divide and Conquer Java

if (heights[minindex] > heights[i])

minindex - 1), calculateArea(heights, minindex + 1, end)));

return calculateArea(heights, 0, heights.length - 1);

public int largestRectangleArea(int[] heights) {

minindex = i;

• Space complexity : O(n). Recursion with worst case depth n. Approach 4: Better Divide and Conquer **Algorithm** 

### 7 6 5

10

8

4

3

2

1

7,

public class Solution {

stack.push(-1);

int maxarea = 0;

stack.push(i);

5,

2

public int largestRectangleArea(int[] heights) {

Stack < Integer > stack = new Stack < > ();

for (int i = 0; i < heights.length; ++i) {

• Time complexity : O(n). n numbers are pushed and popped.

Type comment here... (Markdown is supported)

comparing the new area found everytime.

11 while (stack.peek() != -1) maxarea = Math.max(maxarea, heights[stack.pop()] \* (heights.length - stack.peek() -1)); 12 13 return maxarea; 14 15 }

Preview Post TravellingSalesman \* 122 March 8, 2019 5:18 PM A Report Let me try to give my thought process behind using stack, hope it helps: 1. Idea is, we will consider every element a[i] to be a candidate for the area calculation. That is, if a[i] is the minimum element then what is the maximum area possible for all such rectangles? We can easily figure out that it's a[i]\*(R-L+1-2) or a[i] \* (R-L-1), where a[R] is first subsequent Read More 116 ∧ ∨ ♂ Share ★ Reply **SHOW 8 REPLIES** Kaiyubo ★ 92 ② November 14, 2018 2:52 AM I think there is a typo in Divide and Conquer example. It should be  $2 \times 7 = 14$ . 70 A V Share Reply

This video https://www.youtube.com/watch?v=RVIh0snn4Qc, helped me understand the logic for

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for loop ends seems differ from the Java implementation down below. In the implementation, the

formula used is: (len(a) - stack[top-1] - 1) \* a[stack[top]]. Can anyone else confirm this for me? Whether

Read More

2. when we pop the stack, the heights[stack.pop()] is monotonically decreasing, and therefore we can treat the original index (i - 1) as one anchor point to calculate the width. 8 A V C Share Reply

SHOW 1 REPLY

**SHOW 7 REPLIES** XiangkunYe ★ 69 ② January 13, 2019 12:20 PM About Approach 5 I think there's a mistake that we should use (len(a)-1-stack[top-1]) × a[stack[top]] instead of  $(stack[top]-stack[top-1]) \times a[stack[top]]$ . 6 ∧ ∨ ♂ Share → Reply SHOW 1 REPLY

A Report for the last solution, we can add a 0 at the end of heights and "force pop" all the remaining elements in the stack. That way we can save the last while loop 4 ^ V C Share Reply kevinhynes # 286 ② July 2, 2019 6:54 PM A Report

Is Solution 3 (vanilla Divide and Conquer) supposed to pass? I am getting TLE in Python but if I copy

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Above is a histogram where width of each bar is 1, given height = [2,1,5,6,2,3].

Summary We need to find the rectangle of largest area that can be formed by using the given bars of histogram.

Solution Firstly, we need to take into account the fact that the height of the rectangle formed between any two bars will always be limited by the height of the shortest bar lying between them which can be understood by looking at the figure below: Area=2x7

7 6 5 3

Thus, we can simply start off by considering every possible pair of bars and finding the area of the rectangle formed between them using the height of the shortest bar lying between them as the height and the spacing between them as the width of the rectangle. We can thus, find the required rectangle with the maximum **Сору** 

84. Largest Rectangle In Histogram 💆 Dec. 7, 2016 | 61.9K views Given n non-negative integers representing the histogram's bar height where the width of each bar is 1, find the area of largest rectangle in the histogram.