

32. Longest Valid Parentheses 🛂 Dec. 23, 2016 | 186.9K views

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parentheses substring. Example 1:

Given a string containing just the characters '(' and ')', find the length of the longest valid (well-formed)

Input: "(()" Output: 2 Explanation: The longest valid parentheses substring is "()"

```
Example 2:
  Input: ")()())"
 Output: 4
```

Explanation: The longest valid parentheses substring is "()()"

Solution

Method.

Every time we encounter a '(', we push it onto the stack. For every ')' encountered, we pop a '(' from the stack. If '(' isn't available on the stack for popping at anytime or if stack contains some elements after

((--> invalid

() --> valid, length=2

processing complete substring, the substring of parentheses is invalid. In this way, we repeat the process for every possible substring and we keep on storing the length of the longest valid string found so far.

Example: "((())" ((--> invalid

)) --> invalid ((()--> invalid)(())--> valid, length=4 maxlength=4 Copy

```
for (int i = 0; i < s.length(); i++) {</pre>
   4
   5
                   if (s.charAt(i) == '(') {
   6
                       stack.push('(');
                  } else if (!stack.empty() && stack.peek() == '(') {
   7
   8
                       stack.pop();
  9
                  } else {
                       return false;
  10
  11
  12
  13
               return stack.empty();
  14
           public int longestValidParentheses(String s) {
  15
               int maxlen = 0;
  16
               for (int i = 0; i < s.length(); i++) {
  17
                   for (int j = i + 2; j \le s.length(); j+=2) {
  18
  19
                       if (isValid(s.substring(i, j))) {
  20
                           maxlen = Math.max(maxlen, j - i);
  21
  22
  23
               return maxlen;
  24
  25
           }
  26
Complexity Analysis
```

- To fill dp array we will check every two consecutive characters of the string and if
- if s[i dp[i 1] 1] = '(') then dp[i] = dp[i-1] + dp[i-dp[i-1] - 2] + 2

The reason behind this is that if the 2nd last ')' was a part of a valid substring (say sub_s), for the last ')' to

substring of which the 2nd last ')' is a part (i.e. before sub_s). Thus, if the character before sub_s happens to

be '(', we update the ${
m dp}[i]$ as an addition of 2 in the length of sub_s which is ${
m dp}[i-1]$. To this, we also add

be a part of a larger substring, there must be a corresponding starting '(' which lies before the valid

the length of the valid substring just before the term "(,sub_s,)" , i.e. ${
m dp}[i-{
m dp}[i-1]-2]$.

Maxlength=0

1/8

• Time complexity : $O(n^3)$. Generating every possible substring from a string of length n requires $O(n^2)$. Checking validity of a string of length n requires O(n). • Space complexity : O(n). A stack of depth n will be required for the longest substring.

For better understanding of this method, see this example:

```
2
)
```

```
-1
    public class Solution {
2
        public int longestValidParentheses(String s) {
             int maxans = 0;
5
            Stack<Integer> stack = new Stack<>();
6
             stack.push(-1);
7
            for (int i = 0; i < s.length(); i++) {
                 if (s.charAt(i) == '(') {
8
9
                     stack.push(i);
10
                } else {
11
                     stack.pop();
12
                     if (stack.empty()) {
13
                         stack.push(i);
14
15
                         maxans = Math.max(maxans, i - stack.peek());
16
                     }
17
                }
```

18 19

20

21 }

Algorithm

Complexity Analysis

O Previous

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Preview

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second loop.

SHOW 1 REPLY

SHOW 2 REPLIES

right. (*)

michalhr # 29 ② June 7, 2018 3:57 PM

I have to admit this is too hard for me..

wanders * 33 • November 22, 2018 9:00 PM

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• Time complexity : O(n). Two traversals of the string.

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Complexity Analysis

return maxans;

Approach 4: Without extra space

• Time complexity : O(n). n is the length of the given string..

• Space complexity : O(n). The size of stack can go up to n.

becomes greater than left we reset left and right to 0.

Example of this approach: M **С**ору Java public class Solution {

In this approach, we make use of two counters left and right. First, we start traversing the string from the

encountered, we increment the right counter. Whenever left becomes equal to right, we calculate the

left towards the right and for every '(' encountered, we increment the left counter and for every ')'

length of the current valid string and keep track of maximum length substring found so far. If right

Next, we start traversing the string from right to left and similar procedure is applied.

lostandfoundii ★ 181 ② May 29, 2018 11:09 AM Solution 4 is super smart!! 117 A V Share Reply **SHOW 2 REPLIES** Minghao2017 * 107 • April 3, 2019 4:25 PM I can hardly write a workable one. So sad... 107 ∧ ∨ ♂ Share → Reply

In the solution #4: "else if (right > = left)" can be simplified to "else if (right > left)". Similarly in the

• Space complexity : O(1). Only two extra variables left and right are needed.

16 ∧ ∨ ☑ Share ¬ Reply **SHOW 7 REPLIES** interviewrecipes 🖈 1385 🗿 September 17, 2018 5:35 AM I am finding it little difficult to digest the second part of 4th approach. I am convinced that it is required

Brute Force **Optimization**, Time complexity: **O (n²)** and Space complexity: **O (1)**

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public int longestValidParentheses(String s) { int count = 0; int max = 0: s961206 ★ 733 ② February 28, 2019 12:22 PM

thinking and wondering, finally solved it.:)

zhengzhicong 🖈 294 🗿 November 16, 2018 5:21 PM

(1 2 3 4 5 6 ... 9 10 >

8 🔨 🔀 Share 🦘 Reply

python3:

A Report Damn, the feeling you get when your intuition solves the problem is ineffable.. Solved using stack approach..Thought I wouldn't be able to solve it without looking at the solution..But after 1 day of

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Summary We need to determine the length of the largest valid substring of parentheses from a given string. Approach 1: Brute Force **Algorithm** In this approach, we consider every possible non-empty even length substring from the given string and check whether it's a valid string of parentheses or not. In order to check the validity, we use the Stack's

Java public class Solution { 2 public boolean isValid(String s) { 3 Stack<Character> stack = new Stack<Character>();

Approach 2: Using Dynamic Programming **Algorithm** This problem can be solved by using Dynamic Programming. We make use of a ${
m d}{
m p}$ array where ith element of ${
m d}{
m p}$ represents the length of the longest valid substring ending at ith index. We initialize the complete ${
m d}{
m p}$ array with 0's. Now, it's obvious that the valid substrings must end with ')'. This further leads to the

conclusion that the substrings ending with '(' will always contain '0' at their corresponding ${ m d}{ m p}$ indices. Thus, we update the dp array only when ')' is encountered. 1. $\mathbf{s}[i]=\text{`})\text{'}$ and $\mathbf{s}[i-1]=\text{`}(\text{'}, \text{i.e. string looks like ``.....()"} <math>\Rightarrow$ dp[i] = dp[i-2] + 2We do so because the ending "()" portion is a valid substring anyhow and leads to an increment of 2 in the length of the just previous valid substring's length. 2. $\mathrm{s}[i]=$ ')' and $\mathrm{s}[i-1]=$ ')', i.e. string looks like "......)" \Rightarrow

Copy Java public class Solution { 2 public int longestValidParentheses(String s) { 3 int maxans = 0; 4 int dp[] = new int[s.length()]; for (int i = 1; i < s.length(); i++) { 5 6 if (s.charAt(i) == ')') { 7 if (s.charAt(i - 1) == '(') { 8 $dp[i] = (i \ge 2 ? dp[i - 2] : 0) + 2;$ 9 } else if $(i - dp[i - 1] > 0 && s.charAt(i - dp[i - 1] - 1) == '(') {$ dp[i] = dp[i - 1] + ((i - dp[i - 1]) >= 2 ? dp[i - dp[i - 1] - 2] : 0) + 2;10 11 maxans = Math.max(maxans, dp[i]); 12 } 13 14 15 return maxans; 16 17 **Complexity Analysis** • Time complexity : O(n). Single traversal of string to fill dp array is done. • Space complexity : O(n). dp array of size n is used. Approach 3: Using Stack **Algorithm** Instead of finding every possible string and checking its validity, we can make use of stack while scanning the given string to check if the string scanned so far is valid, and also the length of the longest valid string. In order to do so, we start by pushing -1 onto the stack. For every '(' encountered, we push its index onto the stack. For every ')' encountered, we pop the topmost element and subtract the current element's index from the top element of the stack, which gives the length of the currently encountered valid string of parentheses. If while popping the element, the stack becomes empty, we push the current element's index onto the stack. In this way, we keep on calculating the lengths of the valid substrings, and return the length of the longest valid string at the end. See this example for better understanding. Push -1 Maxlength=0 Copy Copy Java 3 4

public int longestValidParentheses(String s) { 2 int left = 0, right = 0, maxlength = 0; 3 4 for (int i = 0; i < s.length(); i++) { if (s.charAt(i) == '(') { 5 left++; 6 } else { 7 8 right++; 9 if (left == right) { 10 maxlength = Math.max(maxlength, 2 * right); 11 12 } else if (right >= left) { left = right = 0; 13 14 } 15 left = right = 0; 16 17 for (int i = s.length() - 1; i >= 0; i--) { if (s.charAt(i) == '(') { 18 19 left++; } else { 20 21 right++; 22 23 if (left == right) { 24 maxlength = Math.max(maxlength, 2 * left); } else if (left >= right) { 25 left = right = 0; 26 } 27

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Proof of validity for approach 4: Let i and j denote the starting and ending indices of the longest valid subsequence. Note that in the forward pass after (fully) processing each character, it's always the case that left > =

appenthused0418 ★ 66 ② October 5, 2018 5:33 PM

and I get it up to certain extent, but still not getting the precise intuition behind that. Could someone please explain? 22 A V C Share Reply **SHOW 8 REPLIES**

windliang * 1002 • November 30, 2018 1:40 PM

why solution 4 works? Could anybody explain for us? 10 ∧ ∨ ♂ Share ★ Reply SHOW 1 REPLY itachi_2019 ★9 ② October 14, 2017 10:34 PM

class Solution: def longestValidParentheses(self, s): Read More 7 A V Share Seply