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518. Coin Change II

Nov. 16, 2019 | 27.9K views

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You are given coins of different denominations and a total amount of money. Write a function to compute the number of combinations that make up that amount. You may assume that you have infinite number of each kind of coin.

```
Input: amount = 5, coins = [1, 2, 5]
Output: 4
Explanation: there are four ways to make up the amount:
5=5
5=2+2+1
5=2+1+1+1
5=1+1+1+1+1
```

```
Example 2:
```

```
Explanation: the amount of 3 cannot be made up just with coins of 2.
Example 3:
```

```
Input: amount = 10, coins = [10]
Output: 1
```

Note:

You can assume that

0 <= amount <= 5000 • 1 <= coin <= 5000

- the number of coins is less than 500

This is a classical dynamic programming problem.

· Define the base cases for which the answer is obvious.

- · Develop the strategy to compute more complex case from more simple one.
- Link the answer to base cases with this strategy.
- Let's pic up an example: amount = 11, available coins 2 cent, 5 cent and 10 cent. Note, that coins are

Another base case is no coins: zero combinations for amount > 0 and one combination for amount == 0.

Base Cases: No Coins or Amount = 0

0

0 1 2 3 4 5 7 8 9 10 11 amount = 6 combinations

0

Base cases

0

0

0

0

0

0

0

0

0

0

0

0

0

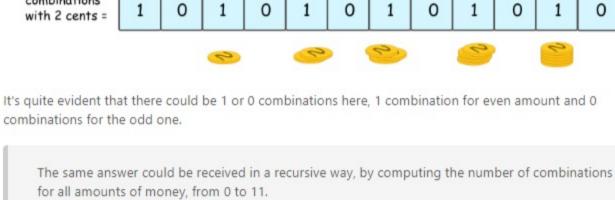
0

0

Cent Coins												
et's do one step fu	rther a	nd cons	ider th	e situat	ion wit	h one k	ind of a	availabl	e coins	2 cent		
amount =		1		_	_	_	,	7			10	
amount =	U	1	2	3	4	5	6	/	8	9	10	11

0

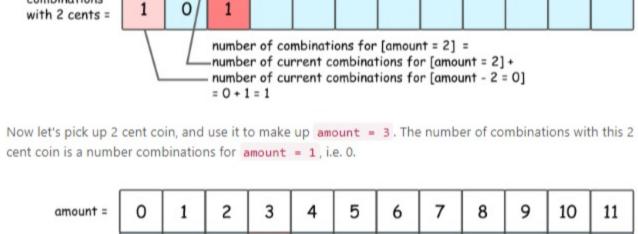
combinations 1 0 1 0 0 0 0 1 with 2 cents =



First, that's quite obvious that all amounts less than 2 are not impacted by the presence of 2 cent coins. Hence for amount = 0 and for amount = 1 one could reuse the results from the figure 2.

So let's pick up 2 cent coin, and use it to make up amount = 2. The number of combinations with this 2 cent coin is a number combinations for amount = 0, i.e. 1.

0 1 2 3 7 8 10 11 amount = 6 combinations 0 0 0 0 0 0 0 0 using no coins =



combinations 0 1 with 2 cents = number of combinations for [amount = 3] =

0



Now let's add 5 cent coins. The formula is the same, but do not forget to add dp[x], number of

7

0

0

8

0

1

9

0

0

10

0

1

3

Сору

1

11

0

0

0

1

0

1

amount = 0 2 3 4 5 1 combinations 1 0 0 0 0 0 using no coins =

0

0

1

1

0 2 1 with 2 and 5 cents = dp[x] for x < coin = 5 cents dp[x] = dp[x] + dp[x - coin]are not going to change coin = 5 cents

0

1

The story is the same for 10 cent coins. combinations 0 0 0 0 0 0 0 0 0 0 0 1 using no coins = combinations 1 0 1 0 1 0 1 0 1 0 1 0 with 2 cents = combinations 2 1 0 0 1 1 1 1 1 1 1 with 2 and 5 cents =

0

are not going to change dp[x] = dp[x] + dp[x - coin]coin = 10 cents

· Loop over all coins:

Return dp[amount].

Implementation Java Python 1 class Solution:

for x in range(coin, amount + 1):

 $dp = [\theta] * (amount + 1)$

for coin in coins:

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babhishek21 # 88 @ June 10, 2020 1:31 PM

If you're wondering why, here's a hint:

answer almost doubles! Learnt it the hard way.

dp[0] = 1

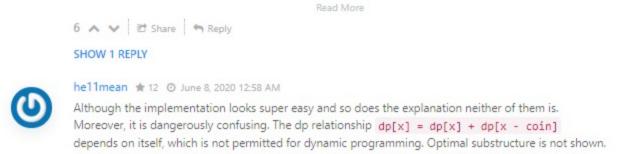
 $dp[x] \leftarrow dp[x - coin]$ return dp[amount]

Time complexity: O(N × amount), where N is a length of coins array.

Space complexity: O(amount) to keep dp array.

Complexity Analysis

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The fun part about this solution is that if you switch the order of the for loops in the code, your

5 A V Et Share Share SHOW 2 REPLIES jkrishna 🛊 5 🛈 February 1, 2020 9:16 PM nice answer 5 A V & Share + Reply

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using ith coin to make change for j amount + The combination when we use ith coin to make change for j amount.

SHOW 5 REPLIES Zaizi # 2 @ March 16, 2020 1:19 PM

Your input: 0, [] Output: 0

public class CoinChangeRecursiveApproach {

The corner case for this problem feels strange to me:

david2999999 ★ 49 ② June 14, 2020 7:19 PM Brute Force Recursive. TLE error

public int change(int amount, int[] coins) { return change(amount. coins. 0): 1 A V & Share Share

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Example 1: Input: amount = 3, coins = [2]

 the answer is guaranteed to fit into signed 32-bit integer Solution

Approach 1: Dynamic Programming Template

Here is a template one could use:

Example

Number of combinations that make up 11

If the total amount of money is zero, there is only one combination: to take zero coins.

0

2 Le combinations

using no coins =

using no coins =

0 1

to the previously known combinations.

combinations

combinations

using no coins =

with 2 cents =

0

0

2 Cent Coins + 5 Cent Coins + 10 Cent Coins

combinations with 2 cent coins.

combinations

with 2 cents =

combinations

combinations

with 2, 5, and 10 cents =

Now the strategy is here:

0 to amount.

Algorithm

1

0

0

0

1

0 0

Starting from amount = 2, one could use 2 cent coins in the combinations. Since the amounts are considered gradually from 2 to 11, at each given moment one could be sure to add not more than one coin 5 4

0 0

0

0

0

0

0

0

0

0

0

-number of current combinations for [amount = 3] + number of current combinations for [amount - 2 = 1]

1 dp[x] = dp[x] + dp[x - coin]

0 coin = 2 cents

1

dp[x] for x < coin = 10 cents

 Add coins one-by-one, starting from base case "no coins". For each added coin, compute recursively the number of combinations for each amount of money from Initiate number of combinations array with the base case "no coins": dp[0] = 1, and all the rest = 0.

o For each coin, loop over all amounts from 0 to amount : For each amount x, compute the number of combinations: dp[x] += dp[x - coin]. def change(self, amount: int, coins: List[int]) -> int:

Rate this article: * * * * * great article...it would be great if you guys can first explain top down approach..then bottom up 16 ∧ ∨ 🗈 Share 🦘 Reply

So this is indeed a solution, but it is not a dynamic programming one (strictly speaking at least). The 6 A V E Share Share SHOW 2 REPLIES egch 🛊 12 🗿 June 8, 2020 2:18 AM This video describe the problem in a great way https://www.youtube.com/watch?v=jaNZ83Q3QGc Coin Change Proble.. kevin2702 * 141 June 8, 2020 6:26 AM I would say the dp formula dp[x] += dp[x - coin] can be explained as The combination of i number of coins to make change for j amount = The combination when we not

SHOW 1 REPLY namidairo777 🛊 5 🗿 May 5, 2020 8:50 AM DFS + backtracking can also solve it. But for large amount of inputs, it will fail due to Time Limit 4 A V E Share A Reply

3 A V E Share A Reply

Wrong Answer 2 A V & Share A Reply SHOW 2 REPLIES

SHOW 1 REPLY What is the rationale behind making dp[0] = 1? 1 A V & Share A Reply

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