

03

January 23, 2024

```
[1]: %pylab inline
import numpy as np
from sklearn import linear_model
cls = linear_model.SGDClassifier(max_iter=1000)

# Some sklearn versions spam warnings
import warnings
warnings.simplefilter(action='ignore', category=FutureWarning)
```

%pylab is deprecated, use %matplotlib inline and import the required libraries.
Populating the interactive namespace from numpy and matplotlib

```
[2]: def separate_points(N=2000, d=2):
    X = np.random.normal(0,1,size=(N, d))
    y = np.random.rand(N) >= 0.8

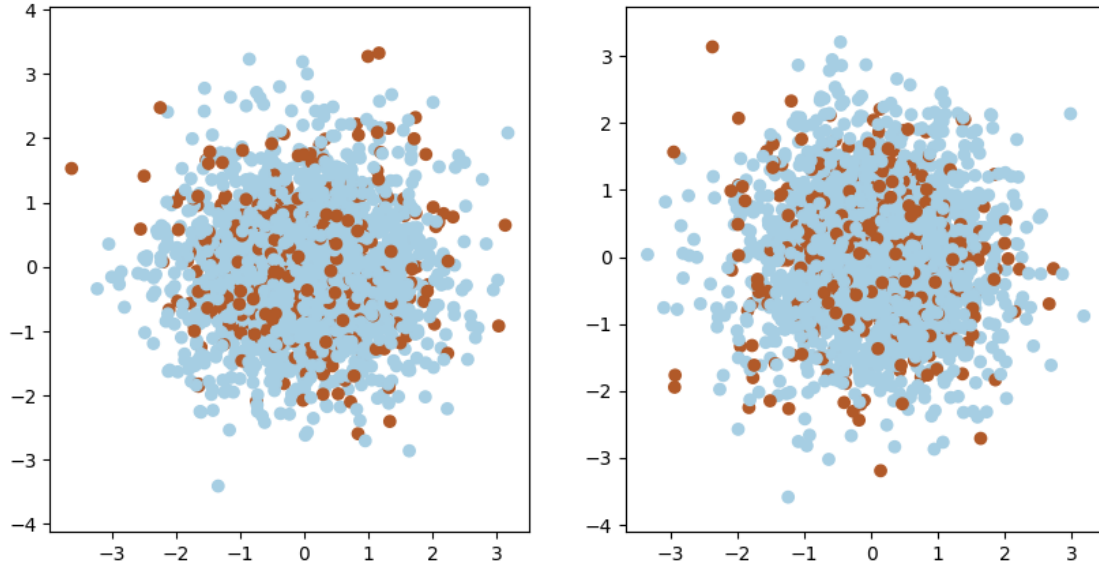
    # Fit the first classifier
    cls.fit(X, y)
    # Let's project all points along the decision boundary of the first
    ↪ classifier
    p1 = cls.coef_ / np.linalg.norm(cls.coef_)
    d1 = X.dot(p1.T)
    score = cls.score(X, y)

    cls.fit(X - d1*p1, y)
    p2 = cls.coef_ / np.linalg.norm(cls.coef_)
    d2 = X.dot(p2.T)

    figure(figsize=(10,5))
    subplot(1,2,1)
    scatter(*X[:, :2].T, c=y.flat, cmap='Paired')
    axis('equal')
    subplot(1,2,2)
    scatter(d1.flat, d2.flat, c=y.flat, cmap='Paired')
    axis('equal')

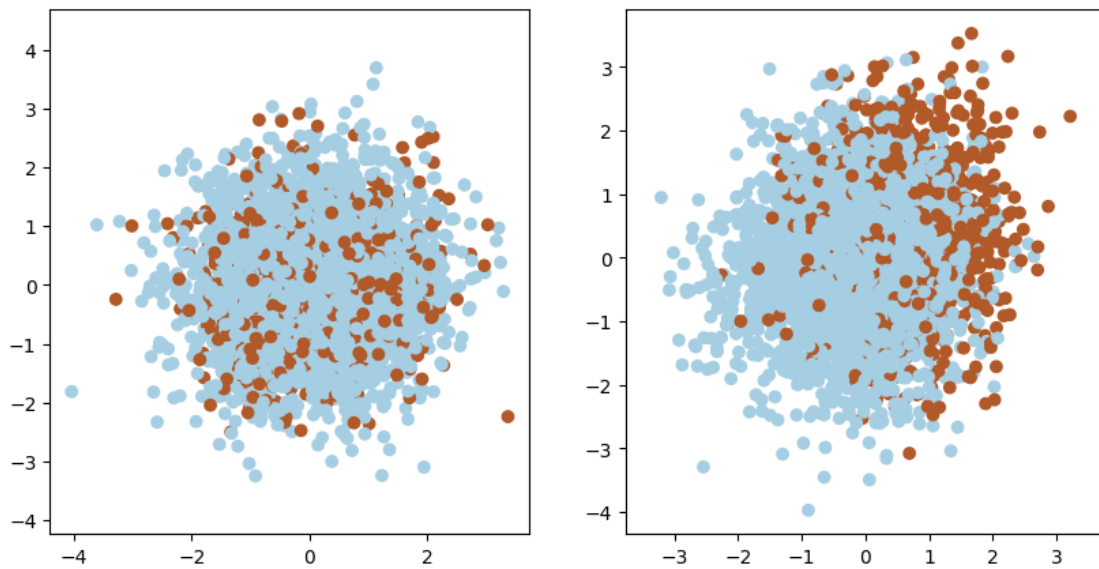
    print( score )
separate_points(2000, 2)
```

0.802



```
[3]: separate_points(4000, 1000)
```

0.81525



```
[4]: def plot_sep(d=2, N=[10,25,50,100,250,500,1000,2000]):  
      S = []  
      mnS, mxS = [], []
```

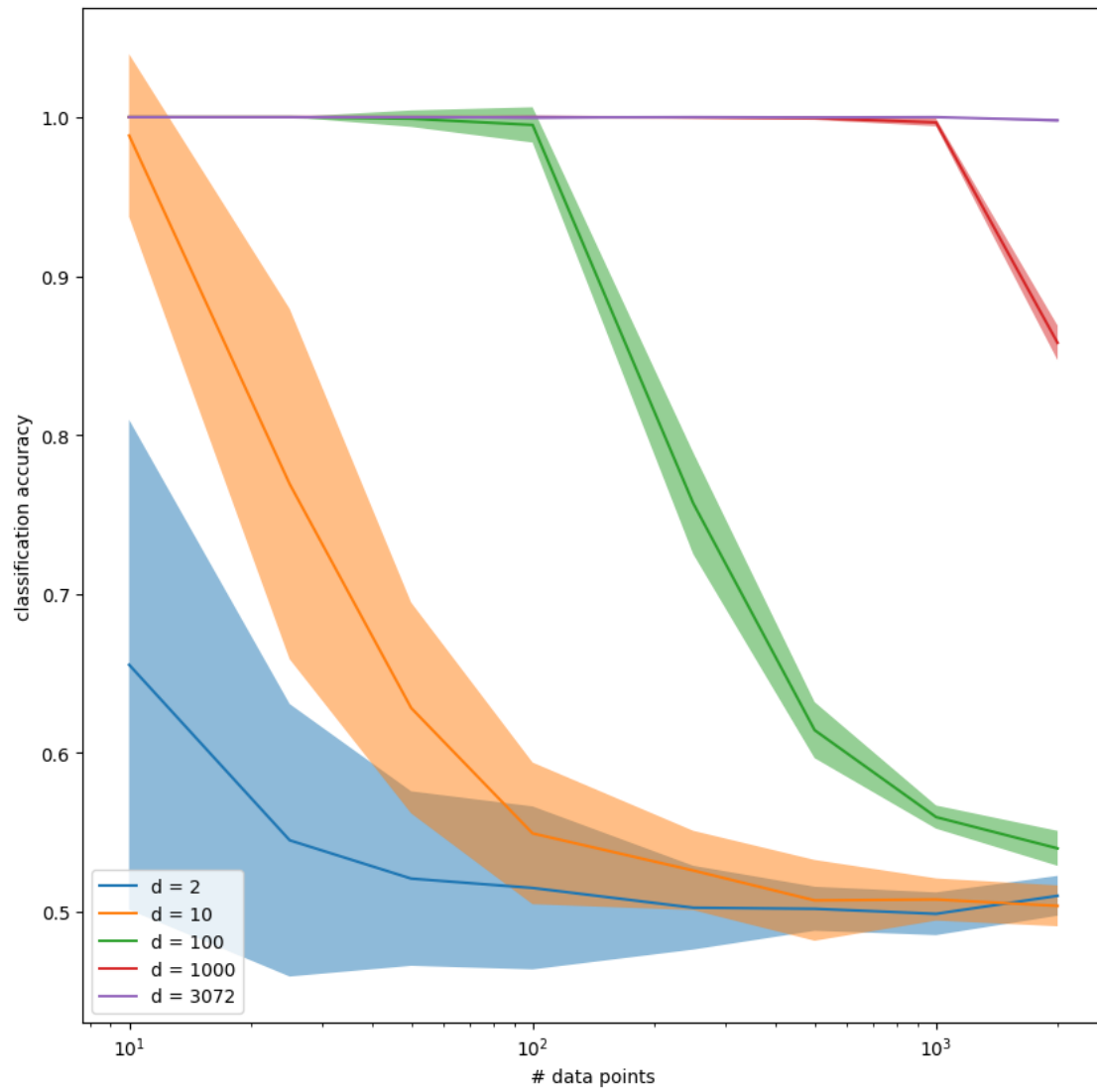
```

for n in N:
    s = []
    for it in range(5000 // n + 1):
        X = np.random.normal(0,1,size=(n, d))
        y = np.random.rand(n)
        y = y > np.median(y)

        # Fit the first classifier
        s.append( cls.fit(X, y).score(X,y) )
    S.append(np.mean(s))
#     mnS.append(np.min(s))
#     mxS.append(np.max(s))
    mnS.append(np.mean(s) - np.std(s))
    mxS.append(np.mean(s) + np.std(s))
fill_between(N, mnS, mxS, alpha=0.5)
plot(N,S, label='d = %d'%d)
xlabel('# data points')
ylabel('classification accuracy')
xscale('log')
legend()

figure(figsize=(10,10))
plot_sep(2)
plot_sep(10)
plot_sep(100)
plot_sep(1000)
plot_sep(32*32*3)

```



[5]: 224*224*3

[5]: 150528

[]: