January 23, 2024

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[]: %pylab inline
     import torch
[]: x = torch.rand([1000,2])
     scatter(*x.numpy().T)
     axis('equal')
[]: x_{in}_{circle} = (x**2).sum(1) < 1
     scatter(*x.numpy().T, c=x_in_circle.numpy())
     axis('equal')
[]: weights = torch.as_tensor([1,1], dtype=torch.float)
     bias = torch.as_tensor(-1, dtype=torch.float)
     def classify(x, weights, bias):
         return (x * weights[None,:]).sum(dim=1) + bias > 0
     def accuracy(pred_label):
         return (pred_label==x_in_circle).float().mean()
     def show(y):
         scatter(*x.numpy().T, c=y.detach().numpy())
         axis('equal')
     pred_y = classify(x, weights, bias)
     show(pred_y)
     print('accuracy', accuracy(pred_y))
[]: def predict(x, weights, bias):
         logit = (x * weights[None,:]).sum(dim=1) + bias
         return 1/(1+(-logit).exp())
     def loss(prediction):
         return -(x_in_circle.float() * (prediction+1e-10).log() +
                  (1-x_in_circle.float()) * (1-prediction+1e-10).log() ).mean()
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p_y = predict(x, weights, bias)
print( 'loss =', loss(p_y), 'accuracy =', accuracy(pred_y) )

[]: weights = torch.as_tensor([-1,-1], dtype=torch.float)
bias = torch.as_tensor(1.0, dtype=torch.float)

pred_y = classify(x, weights, bias)
p_y = predict(x, weights, bias)

show(pred_y)
print( 'loss =', loss(p_y), 'accuracy =', accuracy(pred_y) )

[]: weights = torch.as_tensor([-1,-1], dtype=torch.float)
bias = torch.as_tensor(1.2, dtype=torch.float)

pred_y = classify(x, weights, bias)
p_y = predict(x, weights, bias)
show(pred_y)
print( 'loss =', loss(p_y), 'accuracy =', accuracy(pred_y) )

[]:
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