

Obtain Mark:	Trigonometry	Time: 50 min
Date: 08/08/2024		Total Mark: 96

1. If $A+B+C=\pi$ prove that, $\cot B \cot C + \cot C \cot A + \cot A \cot B = 1$. **(08)**
2. If $x=10$ prove that, $\cos(2x)^0 \cos(4x)^0 \cos(6x)^0 \cos(8x)^0 = \frac{1}{16}$. **(08)**
3. Prove it, $(\cos\theta + i\sin\theta)^3 = \cos 3\theta + i\sin 3\theta$, when $I = \sqrt{-1}$. **(08)**
4. If $\sin\theta = \frac{a-b}{a+b}$ prove that, $\tan\left(\frac{\pi}{4} - \frac{\theta}{2}\right) = \pm \sqrt{\frac{b}{a}}$. **(08)**
5. Prove that, $\tan \frac{45^\circ + \theta}{2} + \tan \frac{45^\circ - \theta}{2} = \frac{\sqrt{2}\cos\theta - 1}{\sqrt{2}\cos\theta + 1}$. **(08)**
6. If $\sin\alpha = \frac{m^2 - n^2}{m^2 + n^2}$ prove that, $\frac{\tan(\alpha-\beta) + \tan\beta}{1 - \tan(\alpha-\beta)\tan\beta} = \frac{m^2 - n^2}{2mn}$. **(08)**
7. If $\tan\theta = \sqrt{\frac{1-e}{1+e}} \tan\frac{\theta}{2}$ show that, $\sec\theta = \frac{1 - e\cos x}{\cos x - e}$. **(08)**
8. If $x=5$ prove it, $\frac{1}{\sin(2x)^0} - \frac{\sqrt{3}}{\cos(2x)^0} = 4$ **(08)**
9. If $\alpha + \beta = \theta$ and $\cos\alpha = k\cos\beta$, then prove that, $\tan\frac{1}{2}(\alpha - \beta) = \frac{1-k}{1+k} \cot\frac{\theta}{2}$. **(08)**
10. If $\operatorname{cosec}A + \sec A = \operatorname{cosec}B + \sec B$, then show that, $\tan A \cdot \tan B = \cot\frac{1}{2}(A + B)$. **(08)**
11. Given, $\tan\frac{\theta}{2} = \tan^3\frac{\Phi}{2}$ and $\tan\Phi = 2\tan\alpha$ now prove it, $\theta + \Phi = 2\alpha$. **(08)**
12. Evaluate: $\cos^2\frac{\pi}{8} + \cos^2\frac{3\pi}{8} + \cos^2\frac{5\pi}{8} + \cos^2\frac{7\pi}{8}$. **(08)**