Task 1

```
import matplotlib.pyplot as plt
        from IPython.display import display, Markdown
        import numpy as np
        import pandas as pd
        from sklearn.metrics.pairwise import pairwise distances
        from sklearn.metrics import accuracy score
        import warnings
        warnings.filterwarnings('ignore')
In [2]: class KMeansClustering:
            def init (self, k, stopping criterion="no change") -> None:
                self.stopping criterion = stopping criterion
                self.centroids = None
                self. sse score = None
                self. last sse score = float('inf')
                self. iterations = 0
            def euclidean distance (self, data point, centroids):
                return np.sqrt(np.sum((centroids - data point)**2, axis=1))
            def    sum of squared errors calc(self, centroids, data, y):
                sum of errors = 0.0
                for idx, d in enumerate(data):
                    sum of errors += np.sum((centroids[y[idx]] - d) ** 2)
                return sum of errors
            def get sum of squared error(self):
                return self. sse score
            def get iterations to converge(self):
                return self. iterations
            def fit(self, X, max iterations=200):
                self.centroids = np.random.uniform(
                    low=np.amin(X, axis=0),
                    high=np.amax(X, axis=0),
                    size=(self.k, X.shape[1]))
                y = []
                for in range(max iterations):
                    y = []
                    for data point in X:
                        distances = self.euclidean distance(
                            data point=data point,
                            centroids=self.centroids)
                        # print(distances.shape)
                        cluster num = np.argmin(distances)
                        y.append(cluster num)
                    y = np.asarray(y)
                    cluster indices = []
                    for idx in range(self.k):
                        cluster indices.append(np.argwhere(y == idx))
                    cluster centers = []
```

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for i, indices in enumerate(cluster indices):
                        if len(indices) == 0:
                            cluster centers.append(self.centroids[i])
                        else:
                            cluster centers.append(np.mean(X[indices], axis=0)[0])
                    if self.stopping criterion == "no change" and np.max(self.centroids - np.arr
                        break
                    elif self.stopping criterion == "increase sse":
                        current sse = self. sum of squared errors calc(X, np.array(cluster cent
                        if current sse > self. last sse score:
                            break
                        self. last sse score = current sse
                    else:
                        self.centroids = np.array(cluster centers)
                    self. iterations += 1
                # Calculate the final SSE after performing K-means
                self. sse score = self. sum of squared errors calc(X, self.centroids, y)
                return y
        data = np.array(pd.read csv('datasets/kmeans data/data.csv', header=None))
In [3]:
        labels = np.ravel(pd.read csv('datasets/kmeans data/label.csv', header=None))
        print('Data: ', data.shape)
        print('Labels: ', labels.shape)
        Data: (10000, 784)
        Labels: (10000,)
In [4]: | unique_labels = np.unique(labels)
        no of clusters = unique labels.size
        MAX ITERATIONS = 100
In [5]: euclidean kmeans m = KMeansClustering(k=no of clusters)
        euclidean kmeans m labels = euclidean kmeans m.fit(X=data, max iterations=MAX ITERATIONS
In [6]: np.unique(euclidean kmeans m labels)
        array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9], dtype=int64)
Out[6]:
In [7]:
        cosine distances = pairwise distances(data, metric='cosine')
        cosine kmeans m = KMeansClustering(k=no of clusters)
        cosine kmeans m labels = cosine kmeans m.fit(cosine distances, max iterations=MAX ITERAT
In [8]: jaccard distances = pairwise distances(data, metric='hamming')
        jaccard kmeans m = KMeansClustering(k=no of clusters)
        jaccard kmeans m labels = jaccard kmeans m.fit(X=jaccard distances, max iterations=MAX I
        Q1. Run K-means clustering with Euclidean, Cosine and Jarcard similarity. Specify K= the
        number of categorical values of y (the number of classifications). Compare the SSEs of
```

Euclidean-K-means, Cosine-K-means, Jarcard-K-means. Which method is better?

```
In [9]: sse euclidean m = euclidean kmeans m.get sum of squared error()
         sse euclidean m
         41236194.16275564
Out[9]:
In [10]: | sse_cosine_m = cosine_kmeans_m.get sum of squared error()
         sse cosine m
         6375.237914066556
Out[10]:
```

```
In [11]: see_jaccard_m = jaccard_kmeans_m.get_sum_of_squared_error()
    see_jaccard_m

Out[11]: 

In [12]: text1 = f"**SSE** of Euclidean K-means = {sse_euclidean_m} <br/>text2 = f"**SSE** of Cosine K-means = {sse_cosine_m} <br/>text3 = f"**SSE** of Jarcard K-means = {see_jaccard_m} <br/>display(Markdown(f"{text1}{text2}{text3}"))
```

Looking at the values above I can see Euclidean K-means having the highest SSE, followed by Cosine K-means with the Jarcard K-means havign the lowest SSE.

Q2. Compare the accuracies of Euclidean-K-means Cosine-K-means, Jarcard-K-means. First, label each cluster using the majority vote label of the data points in that cluster. Later, compute the predictive accuracy of Euclidean-K-means, Cosine-K-means, Jarcard-K-means. Which metric is better? (10 points)

```
In [13]: def label clusters(labels, true labels):
             unique labels = np.unique(true labels)
             cluster labels = np.zeros(len(labels), dtype=np.int)
             for cluster in range(no of clusters):
                cluster indices = np.where(labels == cluster)[0]
                 cluster true labels = true labels[cluster indices]
                 majority label = np.argmax([np.sum(cluster true labels == label) for label in un
                 cluster labels[cluster indices] = majority label
             return cluster labels
         # Label clusters using majority vote
         cluster labels euclidean = label clusters(euclidean kmeans m labels, labels)
         cluster labels cosine = label clusters(cosine kmeans m labels, labels)
         cluster labels jaccard = label clusters(jaccard kmeans m labels, labels)
         # Compute predictive accuracy
         accuracy euclidean = accuracy score(labels, cluster labels euclidean)
         accuracy cosine = accuracy score(labels, cluster labels cosine)
         accuracy_jaccard = accuracy_score(labels, cluster labels jaccard)
```

```
In [14]: acc_text1 = f"**Accuracy** of Euclidean-K-means = {accuracy_euclidean * 100}%<br>"
    acc_text2 = f"**Accuracy** of Cosine-K-means = {accuracy_cosine * 100}%<br>"
    acc_text3 = f"**Accuracy** of Jaccard-K-means = {accuracy_jaccard * 100}%<br>"
    display(Markdown(f"{acc_text1}{acc_text2}{acc_text3}"))
```

Accuracy of Euclidean-K-means = 60.06%

SSE of Euclidean K-means = 41236194.16275564 **SSE** of Cosine K-means = 6375.237914066556 **SSE** of Jarcard K-means = 1687.7102222070575

Accuracy of Cosine-K-means = 40.62%

Accuracy of Jaccard-K-means = 25.66999999999998%

Based on the accuracy computation of majority vote, Euclidean accuracy seems to perform better.

Q3: Set up the same stop criteria: "when there is no change in centroid position OR when the SSE value increases in the next iteration OR when the maximum preset value (e.g., 500, you can set the preset value by yourself) of iteration is complete", for Euclidean-K-means, Cosine-K means, Jarcard-K-means. Which method requires more iterations and times to converge? (10 points)

```
In [26]: euclidean_iterations = euclidean_kmeans_m.get_iterations_to_converge()
    cosine_iterations = cosine_kmeans_m.get_iterations_to_converge()
    jarcard_iterations = jaccard_kmeans_m.get_iterations_to_converge()

text_0 = f"Note : Max iterations have been set to 100 and the change in centroid positio
    text_1 = f"Iterations to converge for Euclidean-K-means = **{euclidean_iterations}** <br/>text_2 = f"Iterations to converge for Cosine-K-means = **{cosine_iterations}** <br/>text_3 = f"Iterations to converge for Jaccard-K-means = **{jarcard_iterations}** <br/>display(Markdown(f"{text_0}{text_1}{text_2}{text_3}"))
```

Note: Max iterations have been set to 100 and the change in centroid position is less than 1e-3.

Iterations to converge for Euclidean-K-means = 41

Iterations to converge for Cosine-K-means = 21

Iterations to converge for Jaccard-K-means = 8

From the results we Euclidean K-means take more iterations than Cosine and Jarcard K-means to converge.

Q4: Compare the SSEs of Euclidean-K-means Cosine-K-means, Jarcard-K-means with respect to the following three terminating conditions: (10 points)

- when there is no change in centroid position
- when the SSE value increases in the next iteration
- when the maximum preset value (e.g., 100) of iteration is complete

(a) Check for SSE for Euclidean K-means, Cosine K-means and Jacard K-means when there is no change in centroid position

```
In [16]: euclidean_kmeans_1 = KMeansClustering(k=no_of_clusters, stopping_criterion="no_change")
    euclidean_kmeans_1_predicted_labels = euclidean_kmeans_1.fit(data, max_iterations=MAX_IT
    sse_euclidean_kmeans_1 = euclidean_kmeans_1.get_sum_of_squared_error()
    print('SSE of Euclidean K-means when there is no change in centroid position =', sse_euc
```

SSE of Euclidean K-means when there is no change in centroid position = 43746676.1436866 75

```
In [17]: cosine_kmeans_1 = KMeansClustering(k=no_of_clusters, stopping_criterion="no_change")
    cosine_kmeans_1_predicted_labels = cosine_kmeans_1.fit(cosine_distances, max_iterations=
    sse_cosine_kmeans_1 = cosine_kmeans_1.get_sum_of_squared_error()
    print('SSE of Cosine K-means when there is no change in centroid position =', sse_cosine
```

SSE of Cosine K-means when there is no change in centroid position = 3839.7509713725044

```
In [18]: jaccard_kmeans_1 = KMeansClustering(k=no_of_clusters, stopping_criterion="no_change")
    jaccard_kmeans_1_predicted_labels = jaccard_kmeans_1.fit(jaccard_distances, max_iteratio
    sse_jaccard_kmeans_1 = jaccard_kmeans_1.get_sum_of_squared_error()
    print('SSE of Jaccard K-means when there is no change in centroid position =', sse_jaccard_kmeans_1.get_sum_of_squared_error()
```

SSE of Jaccard K-means when there is no change in centroid position = 1747.803405833347

(b) Check for SSE for Euclidean K-means, Cosine K-means and Jacard K-means when the SSE value increases in the next iteration

SSE of Euclidean K-means when the SSE value increases in the next iteration = 128287732. 50852942

```
cosine_kmeans_2 = KMeansClustering(k=no_of_clusters, stopping criterion="increase sse")
In [20]:
         cosine kmeans 2 predicted labels = cosine kmeans 2.fit(cosine distances, max iterations=
         sse cosine kmeans 2 = cosine kmeans 2.get sum of squared error()
         print('SSE of Cosine K-means when the SSE value increases in the next iteration =',
               sse cosine kmeans 2)
         SSE of Cosine K-means when the SSE value increases in the next iteration = 11307.9960870
         08814
In [21]: jaccard kmeans 2 = KMeansClustering(k=no of clusters, stopping criterion="increase sse")
         jaccard kmeans 2 predicted labels = jaccard kmeans 2.fit(jaccard distances, max iteration
         sse jaccard kmeans 2 = jaccard kmeans 2.get sum of squared error()
         print('SSE of Jaccard K-means when the SSE value increases in the next iteration =',
               sse jaccard kmeans 2)
         SSE of Jaccard K-means when the SSE value increases in the next iteration = 2186.8230925
         709504
         (c) Check for SSE for Euclidean K-means, Cosine K-means and Jacard K-means when the maximum preset
         value (e.g., 100) of iteration is complete
         euclidean kmeans 3 = KMeansClustering(k=no of clusters, stopping criterion="max iteration"
In [22]:
         euclidean kmeans 3 predicted labels = euclidean kmeans 3.fit(data, max iterations=MAX IT
         sse euclidean max iteration = euclidean kmeans 3.get sum of squared error()
         print(f'SSE of Euclidean K-means when the maximum preset value {MAX ITERATIONS} is compl
               sse euclidean max iteration)
         SSE of Euclidean K-means when the maximum preset value 100 is complete = 42649590.181010
         805
In [23]: cosine kmeans 3 = KMeansClustering(k=no of clusters, stopping criterion="max iterations"
         cosine kmeans 3 predicted labels = cosine kmeans 3.fit(cosine distances, max iterations=
         sse cosine max iteration = cosine kmeans 3.get sum of squared error()
         print(f'SSE of Cosine K-means when the maximum preset value {MAX ITERATIONS} is complete
               sse cosine max iteration)
         SSE of Cosine K-means when the maximum preset value 100 is complete = 3268.7608047518597
In [24]: jaccard_kmeans_3 = KMeansClustering(k=no_of_clusters, stopping criterion="max iterations")
         jaccard kmeans 3 predicted labels = jaccard kmeans 3.fit(jaccard distances, max iteration
         sse jarcard max iteration = jaccard kmeans 3.get sum of squared error()
         print(f'SSE of Jaccard K-means when the maximum preset value {MAX ITERATIONS} is complet
               sse jarcard max iteration)
```

SSE of Jaccard K-means when the maximum preset value 100 is complete = 1593.077637176386

```
In [25]: table = f"""
    | Algorithm | No Change in Centroid Position | SSE Value Increases in Next Iteration | M
    [-----|
    { sse euclidean kmeans 2}
    display(Markdown(table))
```

Algorithm	No Change in Centroid Position	SSE Value Increases in Next Iteration	Maximum Preset Value of Iterations
Euclidean	43746676.143686675	128287732.50852942	42649590.181010805
Jaccard	1747.803405833347	2186.8230925709504	1593.0776371763864
Cosine	3839.7509713725044	11307.996087008814	3268.7608047518597