

CS 321, Assignment 6

Cody Malick
malickc@oregonstate.edu

November 13, 2016

1

a

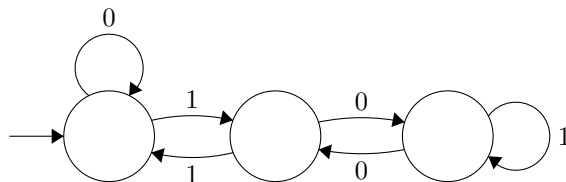
Base case: Given some machine $M = \{Q, \Sigma, \delta, s, F\}$ and a CFG $G = \{A_p \rightarrow cA_q | \delta(p, c)\} \cup \{A_p \rightarrow \epsilon | p \in F\}$ with a start state $A_s = S$ where the start state has not read any characters.

$$A_s = A_p \rightarrow cA_q, \text{ where } |w| = 1$$

Inductive Step: We need to show that

b

Original:



CFG:

$$S \rightarrow 0S | 1T | \epsilon$$

$$T \rightarrow 1S | 0U$$

$$U \rightarrow 0T | 1U$$

2

Starting state:

$$S \rightarrow aSddd | T$$

$$T \rightarrow bTdd | R$$

$$R \rightarrow cR | \epsilon$$

Step 1, add new start symbol S^* , add rule $S^* \rightarrow S$

$$S^* \rightarrow S$$

$$S \rightarrow aSddd | T$$

$$T \rightarrow bTdd | R$$

$$R \rightarrow cR | \epsilon$$

Step 2, Shorten RHS rules for each rule $A \rightarrow \alpha_1, \alpha_2, \dots, \alpha_k$ where $k \geq 3$

$$S^* \rightarrow S$$

$$\begin{aligned}
S &\rightarrow MN \mid T \\
M &\rightarrow aS \\
N &\rightarrow dO \\
O &\rightarrow dd \\
T &\rightarrow PO \mid R \\
P &\rightarrow bT \\
R &\rightarrow cR \mid \epsilon
\end{aligned}$$

Step 3, Clean up mixed RHS

$$\begin{aligned}
S^* &\rightarrow S \\
S &\rightarrow MN \mid T \\
M &\rightarrow AS \\
N &\rightarrow DO \\
O &\rightarrow DD \\
T &\rightarrow PO \mid R \\
P &\rightarrow BT \\
R &\rightarrow CR \mid \epsilon \\
A &\rightarrow a \\
B &\rightarrow b \\
C &\rightarrow c
\end{aligned}$$

Step 4, determine which nonterminal are "nullable" ($A \Rightarrow^* \epsilon$)

The only rule that goes to ϵ is R, so:

$$\begin{aligned}
S^* &\rightarrow S \\
S &\rightarrow MN \mid T \\
M &\rightarrow AS \\
N &\rightarrow DO \\
O &\rightarrow DD \\
T &\rightarrow PO \mid C \\
P &\rightarrow BT \\
A &\rightarrow a \\
B &\rightarrow b \\
C &\rightarrow c
\end{aligned}$$

Step 5, for each rule $A \rightarrow B$, copy all $B \rightarrow \alpha$ rules to $A \rightarrow \alpha$. Repeat until no more changes, then delete $A \rightarrow B$

$$\begin{aligned}
S^* &\rightarrow MN \mid TS \\
M &\rightarrow AS \\
N &\rightarrow DO \\
O &\rightarrow DD \\
T &\rightarrow PO \mid c \\
P &\rightarrow BT \\
A &\rightarrow a \\
B &\rightarrow b \\
C &\rightarrow c
\end{aligned}$$

3

a

b