

# CS 321, Assignment 5

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## 1

### a

Step 1:

Adversary picks  $p$

Step 2:

I select  $w = (aa)^p(bbb)^p$ , where  $|w| \geq p$ , and  $w \in A$  and  $w \in$  real numbers

Step 3:

Split into  $w = xyz$  where  $|xy| \leq p$ , and  $|y| > 0$

Step 4:

I pick  $i = 0$ , I win if  $xy^iz \notin A$

Then  $xy^0z = xz = (aa)^{p-|y|}(bbb)^0 \notin A$  since  $|y| > 0$

The numbers of  $num(aa, w) \neq num(bbb, w)$

I win, A is not regular.

### b

Step 1:

Adversary picks  $p$

Step 2:

I select  $|w| = p^2$ , where  $|w| \geq p$ , and  $w \in A$  and  $w \in$  real numbers

Step 3:

Split into  $w = xyz$  where  $|xy| \leq p$ , and  $|y| > 0$

Step 4:

I pick  $i = p - 1$ , I win if  $xy^iz \notin A$

Then  $xy^{p-1}z, |w| = (p + y^i) + (p - 1)p < (p + 1)^2 \notin A$  since  $|y| > 0$

The length of  $w$  is not square

I win, A is not regular.

## 2

### a

$S \rightarrow 1S0 \mid 0S1 \mid \epsilon$

### b

$S \rightarrow aST \mid STa \mid aTS \mid TSa \mid aT \mid Ta \mid \epsilon$

$T \rightarrow bS \mid Sb \mid b$

