

Q1.

- (a) population mean = 64
sample mean = 69

- (b) null = new app does not reduce resting heart rates

Alternative = new app reduces resting heart rates

$$H_0 = \mu_{\text{new}} \geq \mu_{\text{old}}$$

$$H_1 = \mu_{\text{new}} < \mu_{\text{old}}$$

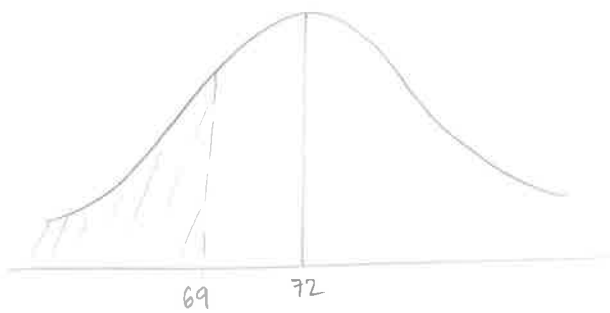
(c)
$$SE = \frac{\sigma}{\sqrt{n}} = \frac{10}{\sqrt{64}} = \frac{10}{8} = \frac{5}{4}$$

it shows how far the sample mean is from the baseline

(d)
$$Z = \frac{69 - 72}{10/8} = \frac{3 \times 8}{10} = \frac{24}{5}$$

$$Z = \frac{S_m - \mu}{SE}$$

(e)



Q2

$$P(S) = 20\% = 0.2$$

$$P(M/S) = 0.9$$

$$P(M/\sim S) = 0.05$$

$$P(S/M) = \frac{P(S) \times P(M/S)}{P(M)}$$

(a) prior probability $\rightarrow P(S)$

$$P(S) = 0.2$$

(b) posterior probability $\Rightarrow P(S/M)$

it is the probability that we are searching for which in this case is probability of spam given the message is spam.

(c)

$$P(S/M) = 0.2 \times 0.9$$

$$P(M/S) \cdot P(S) + P(M/\sim S) \cdot P(\sim S)$$

$$= \frac{0.2 \times 0.9}{(0.9 \times 0.2) + (0.05 \times 0.8)}$$

$$(0.9 \times 0.2) + (0.05 \times 0.8)$$

$$P(M) = P(M/S) \cdot P(S) + P(M/\sim S) \cdot P(\sim S)$$

$$= 0.9 \times 0.2 + 0.05 \times 0.8 \leftarrow \text{Ans}$$

$P(M)$ = total probability

(d) lower, since it is a conditional probability, we have a new world. Since world is smaller, posterior probability will also be lower