

Q1.

(a) population mean = 64

sample mean = 69

(b) null = new app does not reduce resting heart rates

Alternative : new app reduces resting heart rates

$$H_0: A_{\text{new}} \geq A_{\text{old}}$$

$$H_1: A_{\text{new}} < A_{\text{old}}$$

(c)

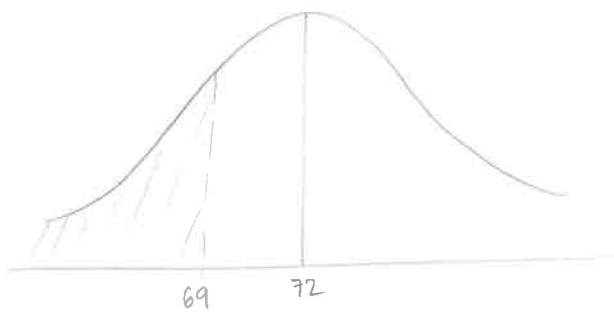
$$S_e = \frac{\sigma}{\sqrt{n}} = \frac{10}{\sqrt{64}} = \frac{10}{8} = \frac{5}{4}$$

it shows how far the sample mean is from the baseline

$$(d) z = \frac{69 - 72}{10/8} = \frac{3}{10/8} = \frac{24}{5}$$

$$z = \frac{S_m - \mu}{S_e}$$

(e)



Q2

$$P(S) = 20\% = 0.2$$

$$P(M|S) = 0.9$$

$$P(M|\sim S) = 0.05$$

$$P(S|M) = \frac{P(S) \times P(M|S)}{P(M)}$$

(a) prior probability $\rightarrow P(S)$

$$P(S) = 0.2$$

(b) posterior probability $\Rightarrow P(S|M)$

it is the probability that we are searching for which in this case is probability of spam given the message is spam.

(c)

$$P(S|M) = 0.2 \times 0.9$$

$$\frac{P(M|S) \cdot P(S) + P(M|\sim S) \cdot P(\sim S)}{P(M|S) \cdot P(S) + P(M|\sim S) \cdot P(\sim S)}$$

$$= \frac{0.2 \times 0.9}{(0.9 \times 0.2) + (0.05 \times 0.8)}$$

$$P(M) = P(M|S) \cdot P(S) + P(M|\sim S) \cdot P(\sim S)$$

$$= 0.9 \times 0.2 + 0.05 \times 0.8 \quad \leftarrow \text{Ans}$$

$P(M)$ = total probability

(d) lower, since it is a conditional probability, we have a new world.
Since world is smaller, posterior probability will also be lower