

Q.1. $\mu = 72 \text{ bpm}$
 $\sigma = 10 \text{ bpm}$

It is given that,

$$\bar{x} = 69 \text{ bpm}$$

~~Population mean = 72 bpm~~

a) Population mean = 72 bpm
 Sample mean = 69 bpm

b) Null hypothesis $\rightarrow H_0: \bar{r} \geq 72 \text{ bpm}$

Alternative hypothesis $\rightarrow H_1: \bar{r} < 72 \text{ bpm}$

Here, $\bar{r} \Rightarrow$ resting heart rate.

c) S.E. =
$$\frac{\text{population mean} - \text{sample mean}}{\text{sample size}}$$

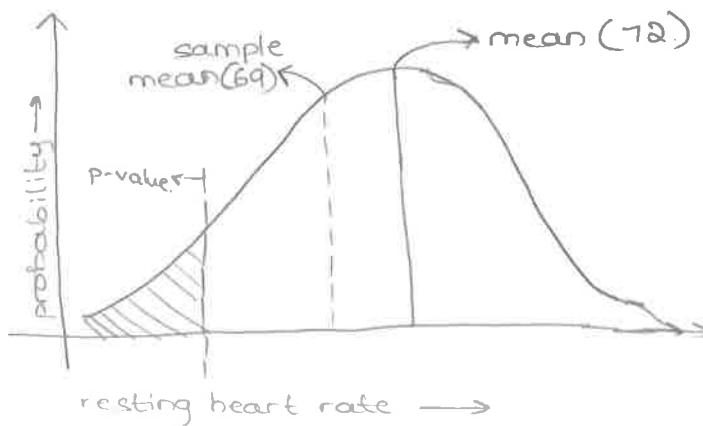
$$= \frac{72 - 69}{64} = \underline{\underline{21.3}}$$

$$\begin{array}{r} 21.3 \\ 3 \overline{) 64} \\ \underline{-3} \\ 34 \\ \underline{-30} \\ 4 \end{array}$$

Standard error is distance between or how far sample means are from each other.

d) Z-score =
$$\frac{72 - 69}{21.3} = \underline{\underline{7.1 \text{ se.}}}$$

e.)



$$Q.2. \quad P(A|B) = \frac{P(B|A) \cdot P(A)}{P(B|A) \cdot P(A) + P(B|-A) \cdot P(-A)}$$

a)

The prior probability here is $P(A)$.

The value of prior probability is 0.20.

b) Posterior probability in the equation is $P(A|B)$.

Posterior probability is the update belief after multiplying the prior (original belief) with the evidence factor. Here, multiply 0.20 with evidence factor where,

$$\text{if } m=S \rightarrow P=0.9$$

$$m \neq S \rightarrow P=0.05$$

$$\left| \begin{array}{l} P(\hat{A}|B) \xrightarrow{\text{spam}} = 0.9 \\ P(A|-B) \xrightarrow{\text{not spam}} = 0.05 \end{array} \right.$$

$$\begin{aligned} c) \text{ Total probability} \Rightarrow P(B) &= P(B \cap A) + P(B \cap -A) \\ &= P(B|A) \cdot P(A) + P(B|-A) \cdot P(-A) \end{aligned}$$

$$P(B|A) = \frac{P(B \cap A)}{P(A)} \quad \left| \begin{array}{l} P(\hat{A}|B) = 0.9 \\ P(B|A) = 0.05 \end{array} \right.$$

d.) The posterior will be higher because the probability of spam given marked as spam is 90%.