

Q1

a) population mean = 72 bpm & sample mean = 69 bpm.

b) Null hypothesis: Relaxation app doesn't reduce the avg resting heart rate ($H_0: \mu_{\text{with app}} \geq \mu_{\text{without app}}$)Alternative hypothesis: Relaxation app reduces avg resting heart rate ($H_1: \mu_{\text{with app}} < \mu_{\text{without app}}$)

c) $SE = \frac{\sigma}{\sqrt{n}}$

$$= \frac{10}{\sqrt{16}} = \frac{10}{4}$$

$$SE = 2.5$$

$$\frac{10}{4} = 2.5$$

It is the standard deviation of the sample mean.

d) $Z = \frac{x - \mu}{SE}$ $x = 64, \mu = 72, SE = 2.5$

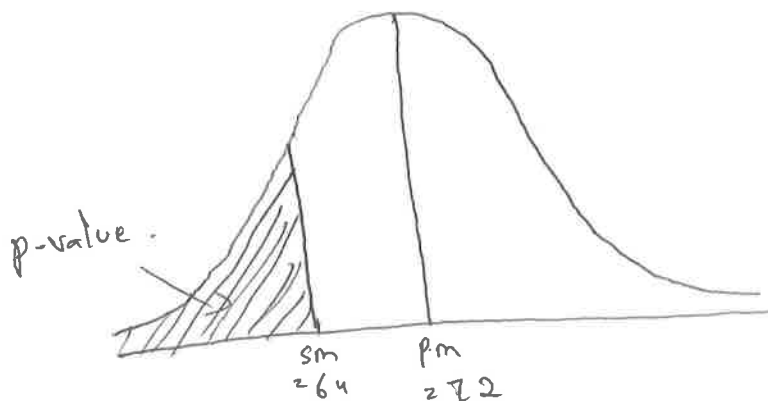
$$\frac{0.1}{2.5}$$

$$Z = \frac{64 - 72}{2.5} = \frac{-8}{2.5}$$

$$\frac{8}{2.5} = 3.2$$

$$Z = -3.2$$

e)



Q2.

a) It is the initial believed probability, in the eq "P(A)". It is the $P(S) = 0.2$ from ex.

b) The posterior probability is the updated probability after multiplying the prior with the evidence factor. In the eq it is "P(A/B)". In the ex. it is the probability of spam given it is marked as "Spam".
 $P(S/SM) =$

c) $P(B) = P(B/A) P(A) + P(B/\sim A) P(\sim A)$

In example :-

$$\begin{aligned} P(SM) &= P(SM/S) P(S) + P(SM/\sim S) P(\sim S) \\ &= 0.9 \times 0.2 + 0.05 \times 0.8 \\ &= 0.18 \end{aligned}$$

d) The posterior probability will be higher because the evidence factor will be greater than 1.

$$P(S) = 0.2$$

$$P(SM/\sim S) = 0.9$$

$$P(\sim S/SM) = 0.05$$

$$P(SM/S) =$$

$$P(SM/\sim S) = 0.9$$

$$P(S/\sim S) = 0.05$$

$$P(S/SM) =$$