

Q1

a) Population mean = 72 bpm

Sample mean = 69 bpm

b) $H_0: R_u \text{ bpm} \geq N_p$ (Relaxation app users have greater/equal bpm rate than Normal People).
 $H_1: R_u \text{ bpm} < N_p$ (Relaxation app users have less bpm rate than Normal people.)

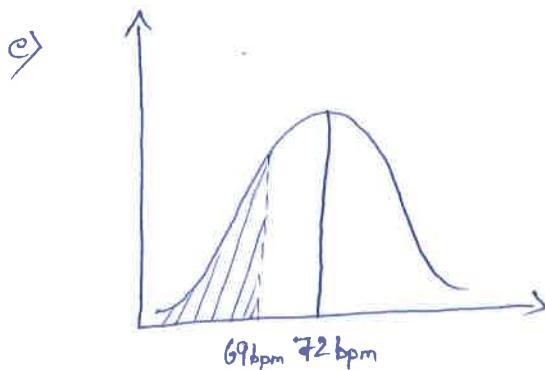
c) $d = 72 - 69 = 3$

Given, Standard deviation = 10 bpm

$$Se = \frac{\sigma}{\sqrt{n}} = \frac{10}{\sqrt{64}} = \frac{10}{8} = \underline{\underline{1.25}}$$

Standard error = The distance b/w the population & sample means.

d) $Z = \frac{d}{Se} = \frac{3}{1.25}$



Q2

Given, $P(M) = 20\%$

$P(M \cap S) = 90\%$

$P(M \cap \sim S) = 5\%$

a) The probability of prior in the above equation is,

$$P(A) = \frac{P(A|B) \cdot P(B)}{P(B|A)} \Rightarrow \frac{P(A|B) \cdot P(B|A) \cdot P(A) + P(B|A^c) \cdot P(A^c)}{P(B|A)}$$

The prior probability based on the example above is 20%.

b) The posterior probability in the above equation is,

$$P(A|B) = \frac{P(B|A)P(A)}{P(B|A)P(A) + P(B|A^c)P(A^c)} = \frac{\cancel{P(B|A)P(A)}}{P(B|A) + \cancel{P(B|A^c)P(A^c)}}$$

Posterior = Probability of spam Message marked as spam.

$$\hookrightarrow P(A|B) = \frac{90 \times 20}{90 \times 20 + 5 \times 80} = \frac{1800}{1800 + 400} = \frac{1800}{2200} = \frac{9}{11} = \underline{\underline{0.81}}$$

c) The probability of posterior will be lower than the prior.

Justification:- As the probability of getting messages is itself low.