

Q1)

a) Population mean is 72 sample mean is 3 69, 3

b) null hypothesis H_0 : new relaxation app doesn't reduce the average resting heart rate of regular user
 $H_0: R_A \neq R_H$
alternative hypothesis H_1 : new relaxation app reduce the average resting heart rate of regular user
 $H_1: R_A < R_H$

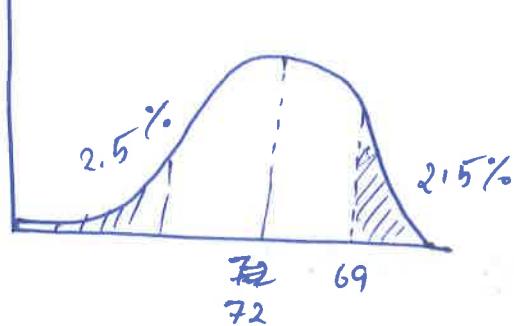
c) S.e. = $\frac{\sigma}{\sqrt{n}} = \frac{10}{\sqrt{64}} = \frac{10}{8} = \frac{5}{4} = 1.25$

Standard error is the number of standard deviation (slam) from the baseline to the mean.

d)

$$Z\text{-score} = \frac{x - \mu}{S.E.} = \frac{69 - 72}{1.25} = \frac{-3}{1.25} = -2.4$$

e)



we reject null hypothesis

Q2)

$$\begin{aligned}
 P(A) &= 0.2 & P(S) &= 0.2 & P(F) &= 0.8 \\
 P(A|S) &= 0.9 & P(A \cup B) &= P(B|A) \\
 P(\text{post.}) & & P(S|P) &= 0.9 & \\
 P(\neg A|S) &= 0.05 & P(\neg S|F) &= 0.05 &
 \end{aligned}$$

a) Prior is $P(A)$, $P(A) = 20\%$, $P(S) = 20\%$

b) posterior probability is $P(A|B)$

Posterior probability is the result of the probability which we need to find

$$\text{c)} \quad P(F|S) = \frac{0.9 \cdot 0.2}{1.8 + 0.05 \cdot 0.8} = \frac{0.9 \cdot 0.2}{1.8 + 0.4} = \frac{1.8}{2.2} = \frac{18}{22} = \frac{9}{11}$$

$$P(B|A) = 0.9 \quad P(B|\bar{A}) = 0.05$$

$$P(A) = 0.2 \quad P(\bar{A}) = 0.8$$

d) Yes the posterior probability will be higher than the prior as the prior is small now it has increased so it will be higher.