

Q1.

a) population mean is 72 bpm
sample mean is 69 bpm

b) Null hypothesis (H_0): New relaxation app does not reduce the average heart resting rate

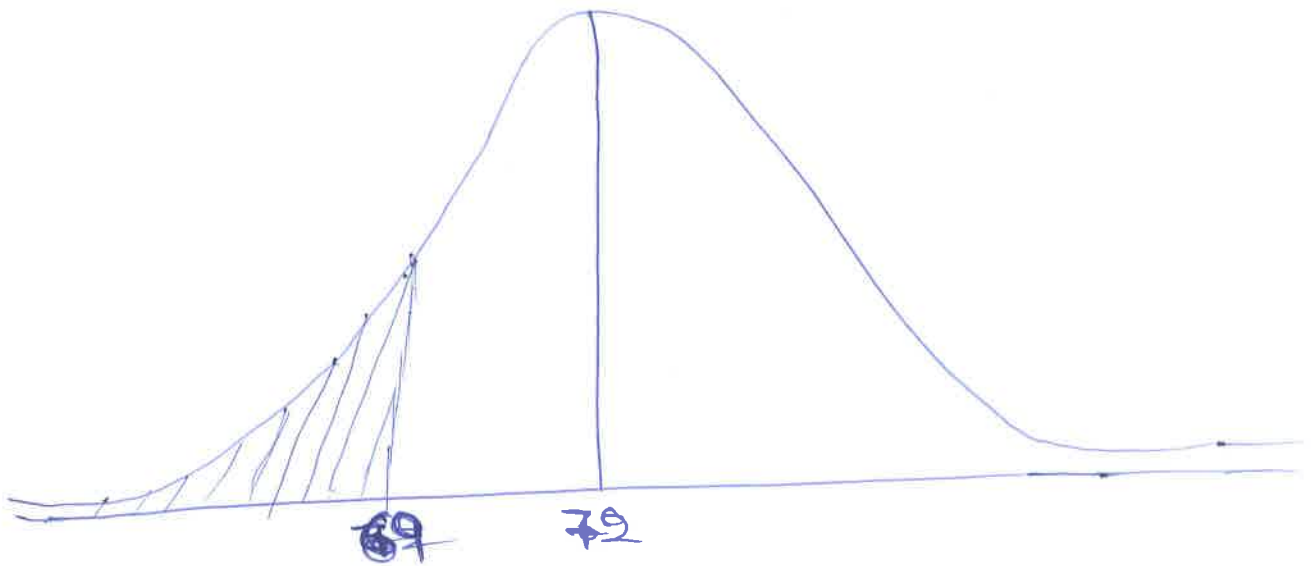
Alternative hypothesis (H_1): New relaxation app will reduce the average resting heart rate.

c) standard error $= \frac{\sigma}{\sqrt{n}} \Rightarrow \frac{72}{\sqrt{64}} \Rightarrow \frac{72}{8} \Rightarrow 9$

Standard error means population mean divided by ~~the~~ root of sample size.

d) z-score $= \frac{x - \mu}{se} \Rightarrow \frac{69 - 72}{9} \Rightarrow \frac{-3}{9} \Rightarrow -\frac{1}{3} \Rightarrow -0.3$

e)



Q2.

$$P(A) = 20\% = 0.2 \quad P(A^c) = 100 - 20 = 80\% = 0.8$$

$$P(B|A) = 90\% = 0.9$$

$$P(B|A^c) = 5\% = 0.05$$

a) The prior probability in the above equation is $P(A)$.
The prior probability based on the example is $P(A) = 0.2$

b) In the equation $P(A|B)$ is the posterior probability.
In the above example the posterior probability is
spam message is marked as spam by the filter.

c) $P(B|A)P(A) + P(B|A^c)P(A^c)$ is the expression from the equation that gives total probability.

$$P(A|B) = 0.2 \frac{0.9}{(0.9)(0.2) + (0.05)(0.8)}$$

d) The posterior probability will become higher once we update the prior. So, in the above equation it will be higher.