

Q1).

a) Population mean = 72

Sample mean = 64

b) H_0 : New relaxation app doesn't reduce the average heart rate of its regular users.

$$\mu_{\text{app}} = \mu_{\text{avg rate}}$$

H_1 : New relaxation app reduces the average heart rate of its regular users.

$$\mu_{\text{r-app}} \neq \mu_{\text{avg rate}}$$

c).

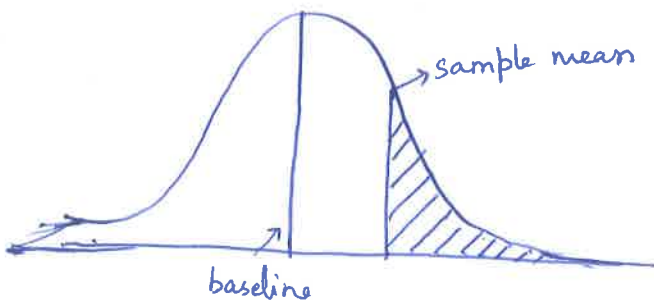
$$s.e = \frac{\sigma}{\sqrt{n}} = \frac{10}{\sqrt{64}} = \frac{10}{8} = \frac{5}{4} = 1.2$$

Standard deviation of the sample mean is known as standard error.

d)

$$z = \frac{x - \mu}{se} = \frac{72 - 69}{1.2} = \frac{3}{1.2} = \frac{3}{1} = \underline{\underline{3}}$$

e)



Q2). Data :

$$P(A) = 0.20$$

$$P(B|A) = 0.9$$

$$P(B|\sim A) = 0.05$$

$$P(\sim A) = 0.80$$

a). Prior probability is the probability representing before the event which has already happened without knowing the evidence. The value of prior probability is 20% $\rightarrow 0.20$.

b). Posterior probability - the probability represents, event happening after we know the evidence. The value for posterior probability is 0.9.

$$c). P(A|B) = \frac{P(B|A) P(A)}{P(B)}$$

$$P(B) = P(B|A) \cdot P(A) + P(B|\sim A) \cdot P(\sim A)$$

$$= 0.9 \times 0.20 + 0.05 \times 0.80$$

$$= 0.18 + 0.40$$

$$= \boxed{0.58}$$

$$P(A|B) = \frac{P(B|A) \cdot P(A)}{P(B)}$$

$$= \frac{0.9 \times 0.20}{0.58} = \frac{0.18}{0.58} = \boxed{0.31 \approx 31\%}$$

The values used are

$$P(A) = 0.20$$

$$P(B|A) = 0.9$$

$$P(B|\sim A) = 0.05$$

$$P(\sim A) = 0.80$$

d). The posterior probability is higher than the prior probability. As prior is 20% and posterior is 31%.