

Exercise Solutions for Math 20

Lines and Circles

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1.1 Find the value of k such that the lines with equations $3x + 2y - 4 = 0$ and $kx - 3y + 8$ are:

1.1.a Parallel.

$\Rightarrow 2y = -3x + 4$ $\Rightarrow y = -\frac{3}{2}x + 4$	Rewrite the first equation in slope-intercept form.
$\Rightarrow -3y = -kx - 8$ $\Rightarrow 3y = kx + 8$ $\Rightarrow y = \frac{k}{3}x + \frac{8}{3}$	Rewrite the second equation in slope-intercept form.
$\Rightarrow \frac{k}{3} = -\frac{3}{2}$	Parallel slopes are equal.
$\Rightarrow k = -\frac{9}{2}$	Final answer. ■

1.1.b Perpendicular.

$\Rightarrow \frac{k}{3} = -\frac{1}{-\frac{3}{2}}$ $\Rightarrow \frac{k}{3} = \frac{2}{3}$	Perpendicular slopes are the negative reciprocal of each other.
$\Rightarrow k = 2$	Final answer. ■

1.2 Line l is perpendicular to the line segment with endpoints $P(-4, 7)$ and $Q(2, -3)$. If l passes through the midpoint of the line segment \overline{PQ} , find an equation for l in slope-intercept form.

$\Rightarrow m = \frac{-3-7}{2+4}$ $\Rightarrow m = \frac{-10}{6}$ $\Rightarrow m = -\frac{5}{3}$	Find the slope of \overline{PQ} .
$\Rightarrow M = (\frac{-4+2}{2}, \frac{7-3}{2})$ $\Rightarrow M = (\frac{-2}{2}, \frac{4}{2})$ $\Rightarrow M = (-1, 2)$	Find the midpoint of \overline{PQ} .
$\Rightarrow y - 2 = -\frac{5}{3}(x + 1)$ $\Rightarrow y - 2 = -\frac{5}{3}x - \frac{5}{3}$ $\Rightarrow y = -\frac{5}{3}x - \frac{5}{3} + 2$ $\Rightarrow y = -\frac{5}{3}x - \frac{5}{3} + \frac{6}{3}$ $\Rightarrow y = -\frac{5}{3}x - \frac{1}{3}$	Use the point-slope formula. ■