## Exercise Solutions for Math 20

Graphs of Circular Functions

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November 22, 2024

- 1 From the following sine waves, determine the amplitude, period, phase shift, and vertical shift and then sketch one cycle of the graph. Label maximum and minimium points.
- 1.1  $f(x) = 2\cos(\frac{1}{2}(x+\pi)) 1$

$\Rightarrow a = 2$	Final answer. $f(x) = a\cos(b(x-c)) + d$
$\Rightarrow b = \frac{1}{2}$	
$\Rightarrow c = -\pi$	
$\Rightarrow d = -1$	
$\Rightarrow M = 1$	M =  a  - d
$\Rightarrow m = -3$	M = - a  - d
$\Rightarrow$ See Figure 1.	

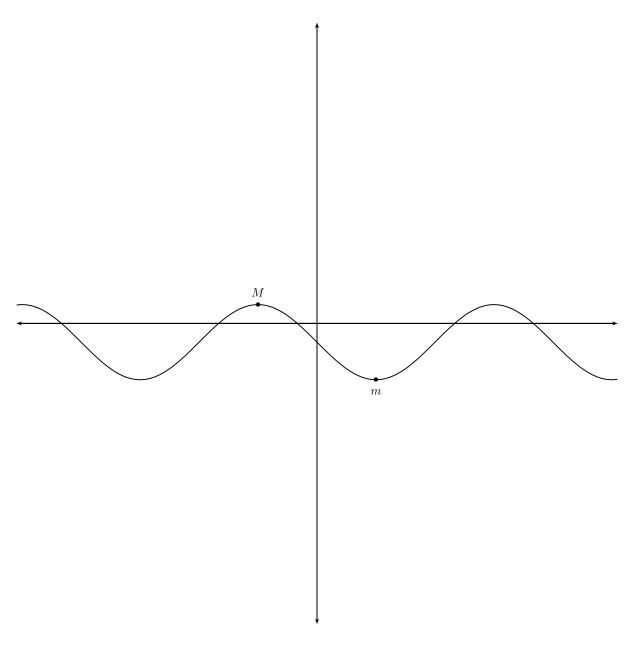


Figure 1. Graph of 
$$f(x) = 2\cos(\frac{1}{2}(x+\pi)) - 1$$

## 1.2 $f(x) = -\frac{3}{2}\sin(\pi - 2x) + 2$

$\Rightarrow f(x) = -\frac{3}{2}\sin(-2(x-\frac{\pi}{2})) + 2$	Rewrite in standard form.
$\Rightarrow a = -\frac{3}{2}$	Final answer.
$\Rightarrow b = -2$	
$\Rightarrow c = \frac{\pi}{2}$	
$\Rightarrow d = 2$	
$\Rightarrow M = \frac{7}{2}$	
$\Rightarrow m = \frac{1}{2}$	
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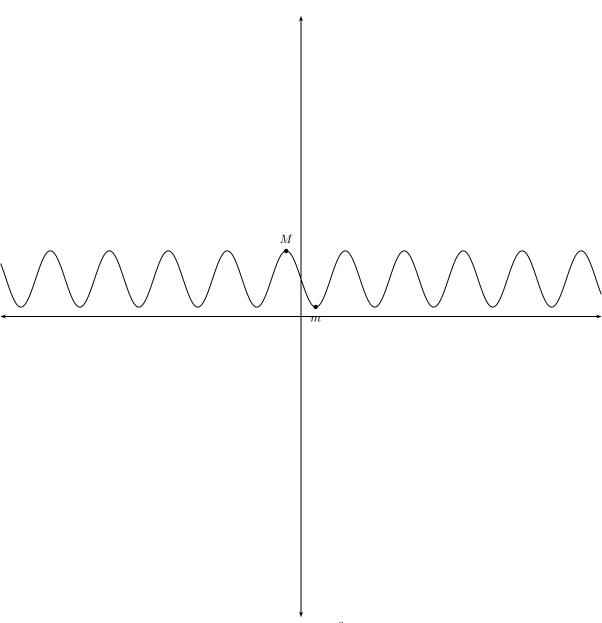


Figure 2. Graph of  $f(x) = -\frac{3}{2}\sin(\pi - 2x) + 2$ 

## 1.3 $f(x) = 4\sin(4x - 3\pi)$

$\Rightarrow f(x) = 4\sin(4(x - \frac{3\pi}{4}))$	Rewrite in standard form.
$\Rightarrow a = 4$	Final answer.
$\Rightarrow b = 4$	
$\Rightarrow c = \frac{3\pi}{4}$	
$\Rightarrow d = 0$	
$\Rightarrow M = 4$	
$\Rightarrow m = -4$	

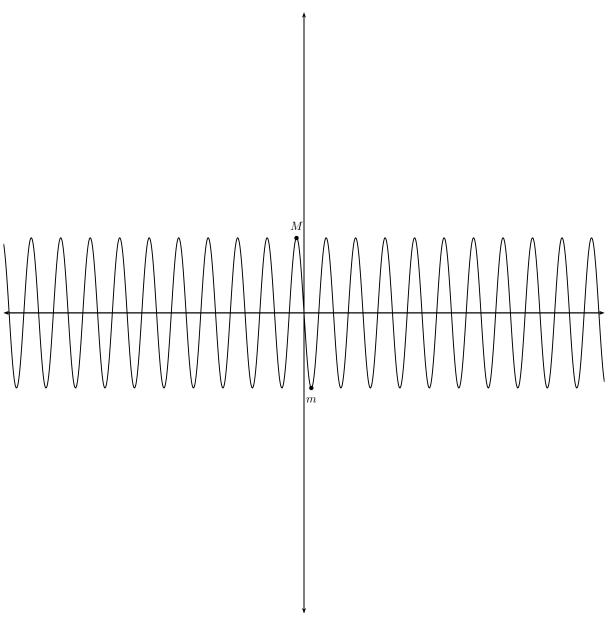


Figure 3. Graph of  $f(x) = 4\sin(4x - 3\pi)$ 

## 1.4 $f(x) = -2\cos(\frac{x}{2} - \frac{\pi}{4}) + 1$

$\Rightarrow f(x) = -2\cos(\frac{1}{2}(x - \frac{\pi}{2})) + 1$	Rewrite in standard form.
$\Rightarrow a = -2$	Final answer.
$\Rightarrow b = \frac{1}{2}$	
$\Rightarrow c = \frac{\pi}{2}$	
$\Rightarrow d = 1$	
$\Rightarrow M = 3$	
$\Rightarrow m = -1$	

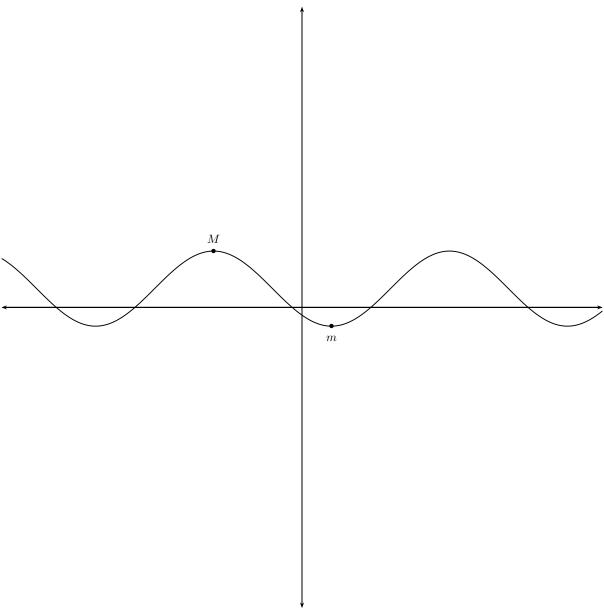


Figure 3. Graph of  $f(x) = -2\cos(\frac{x}{2} - \frac{\pi}{4}) + 1$