

# Exercise Solutions for Math 20

## Lines and Circles

Nile Jocson <novoseiversia@gmail.com>

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# 1

**1.1 Find the value of  $k$  such that the lines with equations  $3x + 2y - 4 = 0$  and  $kx - 3y + 8$  are:**

**1.1.a Parallel.**

$\Rightarrow 2y = -3x + 4$ $\Rightarrow y = -\frac{3}{2}x + 4$	Rewrite the first equation in slope-intercept form.
$\Rightarrow -3y = -kx - 8$ $\Rightarrow 3y = kx + 8$ $\Rightarrow y = \frac{k}{3}x + \frac{8}{3}$	Rewrite the second equation in slope-intercept form.
$\Rightarrow \frac{k}{3} = -\frac{3}{2}$	Parallel slopes are equal.
$\Rightarrow k = -\frac{9}{2}$	Final answer. ■

**1.1.b Perpendicular.**

$\Rightarrow \frac{k}{3} = -\frac{1}{-\frac{3}{2}}$ $\Rightarrow \frac{k}{3} = \frac{2}{3}$	Perpendicular slopes are the negative reciprocal of each other.
$\Rightarrow k = 2$	Final answer. ■

**1.2 Line  $l$  is perpendicular to the line segment with endpoints  $P(-4, 7)$  and  $Q(2, -3)$ . If  $l$  passes through the midpoint of the line segment  $\overline{PQ}$ , find an equation for  $l$  in slope-intercept form.**

$\Rightarrow m = \frac{-3-7}{2+4}$ $\Rightarrow m = \frac{-10}{6}$ $\Rightarrow m = -\frac{5}{3}$	Find the slope of $\overline{PQ}$ .
$\Rightarrow M = (\frac{-4+2}{2}, \frac{7-3}{2})$ $\Rightarrow M = (\frac{-2}{2}, \frac{4}{2})$ $\Rightarrow M = (-1, 2)$	Find the midpoint of $\overline{PQ}$ .
$\Rightarrow y - 2 = -\frac{5}{3}(x + 1)$ $\Rightarrow y - 2 = -\frac{5}{3}x - \frac{5}{3}$ $\Rightarrow y = -\frac{5}{3}x - \frac{5}{3} + 2$ $\Rightarrow y = -\frac{5}{3}x - \frac{5}{3} + \frac{6}{3}$	Use the point-slope formula.
$\Rightarrow y = -\frac{5}{3}x - \frac{1}{3}$	Final answer. ■

**1.3 Find a general equation of the line that is parallel to the line with equation  $3x - y + 1 = 0$  and whose x-intercept is also the x-intercept of the line with equation  $2x - 3y + 6 = 0$**

$\Rightarrow -y = -3x - 1$ $\Rightarrow y = 3x + 1$ $\Rightarrow m = 3$	Find the slope of the first equation.
$\Rightarrow 2x - 3(0) + 6 = 0$ $\Rightarrow 2x + 6 = 0$ $\Rightarrow 2x = -6$ $\Rightarrow x = -3$	Find the x-intercept of the second equation.
$\Rightarrow y - 0 = 3(x + 3)$	Use the point-slope formula.
$\Rightarrow y = 3x + 9$	Final answer. <span style="float: right;">■</span>