CS420

Introduction to the Theory of Computation

Lecture 1: Introduction

Tiago Cogumbreiro

About the course

- Location: (W04-0138) Room 0138, 4th floor, Wheatley
- Schedule: Tuesday, Thursday / 11:00am to 12:15pm

Instructor:

- Name: Tiago (蒂亚戈) Cogumbreiro (he/him)
- Email: Tiago.Cogumbreiro@umb.edu
- Office: (M03-0201-16) Room 0201-16, 3rd floor, McCormack
- Office hours: TBD



Course webpage

- URL: cogumbreiro.github.io/teaching/cs420/s25/
- Holds the class schedule and the syllabus



Other resources

- gitlab.com: Homework assignment PDFs
- gradescope.com: Homework/mini-test submission site
- discord.com: Office hours, communication, Q&A

Make sure you have access to each of these sites!



Course requirements

Checklist

- Install Rocq Prover: rocq-prover.org
 - ∘ CoqIDE in Windows: coqû2024.10.0 (via Scoop)
 - VSCoq in macOS: coq 8.20.1 (via homebrew)
 - CoqIDE in Linux: latest coq (via opam)
- Can you access Gradescope?
- Can you access #cs420 and #cs420-news in Discord? If not ask in #cs420-lounge
- Can you access Gitlab?

Heads up

Please, register using your UMB email address.



Course overview

Introduction to Theory of Computation

Formal Languages

- Understanding the limits of what computers and programs
 - Regular languages
 - Context-Free languages
 - Turing-recognizable languages



A birds-eye view of CS420

What are the limits of programs?

Limits of computation

- Different classes of machines
- The limits of each of these classes
- What properties each class enjoys



Limits of computation

- Different classes of machines
- The limits of each of these classes
- What properties each class enjoys

Classes of machines

Class of machine	Applications
Finite Automata	Parse regular expressions
Pushdown Automata	Parse structured data (programs)
Turing Machines	Any program



• State-machines
Structure concurrency/parallelism/User Interfaces; UML diagrams



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- Regular expressions (regex)
 String matching rules



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 Data specification; Parsing data



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 Data specification; Parsing data
- Turing machines
 Theory of computation



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 Structure concurrency/parallelism/User Interfaces; UML diagrams
- Regular expressions (regex)
 String matching rules
- Grammars
 Data specification; Parsing data
- Turing machines
 Theory of computation
- Programs are proofs
 Using a programming language to write formal proofs



Some applications of formal languages

Use Case 1: DFA/NFA

Using a DFA/NFA to structure hardware usage

Use Case 1: DFA/NFA

Using a DFA/NFA to structure hardware usage

- Arduino is an open-source hardware to design micro-controllers
- Programming can be difficult, because it is highly concurrent
- Finite-state-machines structures the logical states of the hardware
- **Input:** a string of hardware events
- String acceptance is not interesting in this domain

Example

The FSM represents the logical view of a micro-controller with a light switch



Declare states

```
#include "Fsm.h"
// Connect functions to a state
State state_light_on(on_light_on_enter, NULL, &on_light_on_exit);
// Connect functions to a state
State state_light_off(on_light_off_enter, NULL, &on_light_off_exit);
// Initial state
Fsm fsm(&state_light_off);
```

Source: platformio.org/lib/show/664/arduino-fsm



Declare transitions

Source: platformio.org/lib/show/664/arduino-fsm



Code that runs on before/after states

```
// Transition callback functions
void on_light_on_enter() {
  Serial.println("Entering LIGHT_ON");
void on_light_on_exit() {
  Serial.println("Exiting LIGHT_ON");
void on_light_off_enter() {
  Serial.println("Entering LIGHT_OFF");
```

Source: platformio.org/lib/show/664/arduino-fsm



Regular Expressions: Input validation

Regular Expressions: Input validation

HTML includes regular expressions to perform client-side form validation.

```
<input id="uname" name="uname" type="text"
    pattern="_([a-z]|[A-Z]|[0-9])+" minlength="4" maxlength="10">
```

- _[a-zA-Z0-9]+
- [a-zA-Z0-9] means any character beween a and z, or between A and Z, or between 0 and 9
- R+ means repeat R one or more times
- In this case, the username must start with an underscore _, and have one or more letters/numbers
- minlength and maxlength further restrict the string's length

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Regular Expressions: Text manipulation

Regular Expressions: Text manipulation

Programming languages include regular expressions for fast and powerful text manipulation.

Example (JS)

```
let txt1 = "Hello World!";
let txt2 = txt1.replace(/[a-zA-Z]+/, "Bye"); // Replaces the first word by "Bye"
console.log(txt2);
// Bye World!
```



Parsing JSON

Grammar for JSON

ANTLR is a parser generator.

- **Input:** a *grammar*; **Output:** a parser, and data-structures that represent the parse tree (known as a Concrete Syntax Tree)
- The HTML DOM is an example of an *Abstract* Syntax Tree

```
json: value; // initial rule

obj: '{' pair (',' pair)* '}' | '{' '}'; // a sequence of comma-separated pairs

pair: STRING ':' value; // Example: "foo": 1

array: '[' value (',' value)* ']' | '[' ']'; // a sequence of comma-separated values

value: STRING | NUMBER | obj | array | 'true' | 'false' | 'null';

// ...

Source: pay githubuse resortent sem/antln/growmens u4/meeten/isen/150N g4
```

Source: raw.githubusercontent.com/antlr/grammars-v4/master/json/JSON.g4

A grammar for JSON integers

```
NUMBER: '-'? INT ('.' [0-9] +)? EXP?;

fragment INT: '0' | [1-9] [0-9]*; // fragment means do not generate code for this rule

fragment EXP: [Ee] [+\-]? INT; // fragment means do not generate code for this rule
```

Source: raw.githubusercontent.com/antlr/grammars-v4/master/json/JSON.g4



A grammar for JSON

```
> ls *.java
JSONBaseListener.java JSONParser.java JSONVisitor.java
JSONBaseVisitor.java JSONLexer.java JSONListener.java
> cat JSONBaseListener.java
// Generated from ../JSON.g4 by ANTLR 4.7.2
import org.antlr.v4.runtime.tree.ParseTreeListener;
 * This interface defines a complete listener for a parse tree produced by
* {Olink JSONParser}.
public interface JSONListener extends ParseTreeListener {
         * Enter a parse tree produced by {@link JSONParser#json}.
         * Oparam ctx the parse tree
        void enterJson(JSONParser.JsonContext ctx);
         * Exit a parse tree produced by {@link JSONParser#json}.
         * Oparam ctx the parse tree
        void exitJson(JSONParser.JsonContext ctx);
```



CS420

- Study **algorithms** and **abstractions**
- Theoretical study of the **boundaries of computing**



Course schedule

- 1. Learn the Rocq programming language
- 2. Regular languages
 - Design state machines
 - Prove properties on regular languages
- 3. Context-free languages
 - Design pushdown automata
 - Prove properties on regular languages
- 4. Turing-machines
 - Prove properties on computable and non-computable languages



On studying effectively for this content

Suggestions

- Read the chapter before the class:
 - This way we can direct the class to specific details of a chapter, rather than a more topical end-to-end description of the chapter.
- Attempt to write the exercises before the class: We can guide a class to cover certain details of a difficult exercise.
- Use the office hours and our online forum: Rocq is a unusual programming language, so you will get stuck simply because you are not familiar with the IDE or a quirk of the language



Module 1

Basics.v: Part 1

A primer on the programming language Rocq

We will learn the core principles behind Rocq

Enumerated type

A data type where the user specifies the various distinct values that inhabit the type.

Examples?



Enumerated type

A data type where the user specifies the various distinct values that inhabit the type.

Examples?

- boolean
- 4 suits of cards
- byte
- int32
- int64



Declare an enumerated type

- Inductive defines an (enumerated) type by cases.
- The type is named day and declared as a: Type (Line 1).
- Enumerated types are delimited by the assignment operator (:=) and a dot (.).
- Type day consists of 7 cases, each of which is is tagged with the type (day).



Printing to the standard output

Compute prints the result of an expression (terminated with dot):

```
Compute monday.
```

prints

= tuesday

: day



Interacting with the outside world

- Programming in Rocq is different most popular programming paradigms
- Programming is an **interactive** development process
- The IDE is very helpful: workflow similar to using a debugger
- It's a REPL on steroids!
- Compute evaluates an expression, similar to printf



Inspecting an enumerated type

```
match d with
| monday ⇒ tuesday
| tuesday ⇒ wednesday
| wednesday ⇒ thursday
| thursday ⇒ friday
| friday ⇒ monday
| saturday ⇒ monday
| sunday ⇒ monday
end
```



Inspecting an enumerated type

```
match d with
| monday ⇒ tuesday
| tuesday ⇒ wednesday
| wednesday ⇒ thursday
| thursday ⇒ friday
| friday ⇒ monday
| saturday ⇒ monday
| sunday ⇒ monday
| sunday ⇒ monday
```

- match performs pattern matching on variable d.
- Each pattern-match is called a branch; the branches are delimited by keywords with and end.
- Each branch is prefixed by a mid-bar (|) (⇒), a pattern (eg, monday), an arrow (⇒), and a return value

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Pattern matching example

```
Compute match monday with

| monday ⇒ tuesday
| tuesday ⇒ wednesday
| wednesday ⇒ thursday
| thursday ⇒ friday
| friday ⇒ monday
| saturday ⇒ monday
| sunday ⇒ monday
end.
```



Create a function

```
Definition next_weekday (d:day) : day :=
  match d with
  | monday ⇒ tuesday
  | tuesday ⇒ wednesday
  | wednesday ⇒ thursday
  | thursday ⇒ friday
  | friday ⇒ monday
  | saturday ⇒ monday
  | sunday ⇒ monday
  end.
```



Create a function

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  | friday ⇒ monday
  | saturday ⇒ monday
  | sunday ⇒ monday
  end.
```

- Definition is used to declare a function.
- In this case next_weekday has one parameter d of type day and returns (:) a value of type day.
- Between the assignment operator (:=) and the dot (.), we have the body of the function.

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Example 2

```
Compute (next_weekday friday).
```

yields (Message pane)

= monday

: day

next_weekday friday is the same as monday (after evaluation)



Your first proof

```
Example test_next_weekday:
    next_weekday (next_weekday saturday) = tuesday.
Proof.
    simpl. (* simplify left-hand side *)
    reflexivity. (* use reflexivity since we have tuesday = tuesday *)
Qed.
```



Your first proof

- Example prefixes the name of the proposition we want to prove.
- The return type (:) is a (logical) **proposition** stating that two values are equal (after evaluation).
- The body of function test_next_weekday uses the ltac proof language.
- The dot (.) after the type puts us in proof mode. (Read as "defined below".)
- This is essentially a unit test.

