CS450

Structure of Higher Level Languages

Lecture 20: Implementing Language λ_{F} ; Church encoding

Tiago Cogumbreiro

Today we will...



- ullet Go through the implementation of language λ_E
- Write some examples that manipulate hash-tables
- Go through some examples of λ_E programs

Implementing the new AST

Implementing the new AST



Values

$$v ::= n \mid (E, \lambda x.e)$$

Racket implementation

```
(define (e:value? v) (or (e:number? v) (e:closure? v)))
(struct e:number (value) #:transparent)
(struct e:closure (env decl) #:transparent)
```

Implementing the new AST



Expressions

$$e ::= v \mid x \mid (e_1 \ e_2) \mid \lambda x.e$$

Racket implementation

```
(define (e:expression? e) (or (e:value? e) (e:variable? e) (e:apply? e) (e:lambda? e)))
(struct e:lambda (params body) #:transparent)
(struct e:variable (name) #:transparent)
(struct e:apply (func args) #:transparent)
```

How can we represent environments in Racket?

Hash-tables



TL;DR: A data-structure that stores pairs of key-value entries. There is a lookup operation that given a key retrieves the value associated with that key. Keys are unique in a hash-table, so inserting an entry with the same key, replaces the old value by the new value.

- Hash-tables represent a (partial) <u>injective function</u>.
- Hash-tables were covered in <u>CS310</u>.
- Hash-tables are also known as maps, and dictionaries. We use the term hash-table, because that is how they are known in Racket.

Hash-tables in Racket



Constructors

- 1. Function (hash k1 v1 ... kn vn) a hash-table with the given key-value entries. Passing zero arguments, (hash), creates an empty hash-table.
- 2. Function (hash-set h k v) copies hash-table h and adds/replaces the entry k v in the new hash-table.

Accessors

- Function (hash? h) returns #t if h is a hash-table, otherwise it returns #f
- Function (hash-count h) returns the number of entries stored in hash-table h
- Function (hash-has-key? h k) returns #t if the key is in the hash-table, otherwise it returns #f
- Function (hash-ref h k) returns the value associated with key k, otherwise aborts





```
(define h (hash))
    (check-equal? 0 (hash-count h))
    (check-true (hash? h))
    (define h1 (hash-set h "foo" 20))
    (check-equal? (hash "foo" 20) h1)

(define h2 (hash-set h1 "foo" 30))
    (check-equal? (hash "foo" 30) h2)
    (check-equal? (hash "foo" 30) h2)
    (check-equal? (hash "foo" 30) h2)
    (check-equal? (hash "foo" 30) h3)
    (check-equal? (hash "foo" 30) h4)
    ; in h2 "foo" is the key, and 30 the value
    (check-equal? 30 (hash-ref h2 "foo"))
    ; ensures that hash-ref retrieves the value of "foo"
    (check-equal? (hash "foo" 20) h1)
    ; h1 remains the same
```



• How can we encode an empty environment \emptyset :

10/14



- How can we encode an empty environment \emptyset : (hash)
- How can we encode a lookup E(x):



- How can we encode an empty environment \emptyset : (hash)
- How can we encode a lookup E(x): (hash-ref E x)
- How can we encode environment extension $E[x\mapsto v]$:



- How can we encode an empty environment \emptyset : (hash)
- How can we encode a lookup E(x): (hash-ref E x)
- How can we encode environment extension $E[x \mapsto v]$: (hash-set E x v)

Test-cases

Test-cases



Function (check-e:eval? env exp val) is given in the template to help you test effectively your code.

- The use of check-e:eval is optional. You are encouraged to play around with e:eval directly.
 - 1. The first parameter is an S-expression that represents an **environment**. The S-expression must be a list of pairs representing each variable binding. The keys must be symbols, the values must be serialized λ_E values

```
[]; The empty environment
[(x . 1)]; An environment where x is bound to 1
[(x . 1)(y . 2)]; An environment where x is bound to 1 and y is bound to 2
```

- 2. The second parameter is an S-expression that represents the a valid λ_E expression
- 3. The third parameter is an S-expression that represents a valid λ_E value





Each line represents a **quoted** expression as a parameter of function e:parse-ast. For instance, (e:parse-ast '(x y)) should return (e:apply (e:variable 'x) (list (e:variable 'y))).

Test cases



```
; x is bound to 1, so x evaluates to 1
(check-e:eval? '[(x . 1)] 'x 1)
: 20 evaluates to 20
(check-e:eval? '[(x . 2)] 20 20)
; a function declaration evaluates to a closure
(check-e:eval? \lceil \rceil '(lambda (x) x) '(closure \lceil \rceil (lambda (x) x)))
; a function declaration evaluates to a closure; notice the environment change
(check-e:eval? '[(y . 3)] '(lambda (x) x) '(closure [(y . 3)] (lambda (x) x)))
; because we use an S-expression we can use brackets, curly braces, or parenthesis
(check-e:eval? '{(y . 3)} '(lambda (x) x) '(closure [(y . 3)] (lambda (x) x)))
; evaluate function application
(check-e:eval? '{} '((lambda (x) x) 3) 3)
; evaluate function application that returns a closure
(check-e:eval? '{} '((lambda (x) (lambda (y) x)) 3) '(closure {[x . 3]} (lambda (y) x)))
```