CS420

Introduction to the Theory of Computation

Lecture 1: Introduction

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About the course



- Intructor: Tiago (蒂亚戈) Cogumbreiro
- Classes: M01-0207, McCormack 4:00pm to 5:15pm, Monday, Wednesday
- Office hours: 1:00pm to 2:00pm, Monday, Wednesday, Friday

Course webpage

cogumbreiro.github.io/teaching/cs420/s20/

Syllabus



cogumbreiro.github.io/teaching/cs420/s20/syllabus.pdf

- Course divided into 4 modules
- 2 homework assignment + 1 mini-test per module (30mins)
- Final grade: 26% mini-tests + 70% homework + 4% participation
- Homework grade: average of 8
 assignments (possibly weighted)
- **Participation grade:** in-class quizzes, attendance classroom
- Classroom attendance is required!

	Grade		Letter
95 ≤	P		A
90 ≤	Р	< 95	A-
85 ≤	Р	< 90	В
75 ≤	Р	< 85	В
70 ≤	Р	< 75	B-
65 ≤	Р	< 70	C+
55 ≤	Р	< 65	С
50 ≤	Р	< 55	C-
45 ≤	Р	< 50	D+
35 ≤	Р	< 45	D
30 ≤	Р	< 35	D-
30 ≤	Р		F





Checklist

- Install Coq 8.10: coq.inria.fr
- Sign in on Gradescope: www.gradescope.com/courses/81793
- Sign in on Piazza: piazza.com/class/k5ubsxch57r196
- Sign in on Estalee: www.estalee.com

Heads up

- Please, register using your UMB email address.
- Homework 1 is due February 10 at 11:59pm.

Course overview





Formal Languages

- Understanding the limits of what computers and programs
 - Regular languages
 - Context-Free languages
 - Turing-recognizable languages

A birdseye view of CS420

What are the limits of programs?

Limits of computation



- Different classes of machines
- The limits of each of these classes
- What properties each class enjoys





- Different classes of machines
- The limits of each of these classes
- What properties each class enjoys

Classes of machines

Class of machine	Applications	
Finite Automata	Parse regular expressions	
Pushdown Automata	Parse structured data (programs)	
Turing Machines	Any program	

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• State-machines

Structure concurrency/parallelism/User Interfaces; UML diagrams



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- Regular expressions (regex)
 String matching rules



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 Data specification; Parsing data



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 Data specification; Parsing data
- Turing machines
 Theory of computation



- State-machines
 - Structure concurrency/parallelism/User Interfaces; UML diagrams
- Regular expressions (regex)
 String matching rules
- Grammars
 - Data specification; Parsing data
- Turing machines
 - Theory of computation
- Programs are proofs
 - Using a programming language to write formal proofs

Some applications of formal languages

Use Case 1: DFA/NFA

Using a DFA/NFA to structure hardware usage

Use Case 1: DFA/NFA



Using a DFA/NFA to structure hardware usage

- Arduino is an open-source hardware to design **microcontrollers**
- Programming can be difficult, because it is highly concurrent
- Finite-state-machines structures the logical states of the hardware
- **Input:** a string of hardware events
- String acceptance is not interesting in this domain

Example

The FSM represents the logical view of a micro-controller with a light switch



Declare states

```
#include "Fsm.h"
// Connect functions to a state
State state_light_on(on_light_on_enter, NULL, &on_light_on_exit);
// Connect functions to a state
State state_light_off(on_light_off_enter, NULL, &on_light_off_exit);
// Initial state
Fsm fsm(&state_light_off);
```

Source: platformio.org/lib/show/664/arduino-fsm



Declare transitions

Source: platformio.org/lib/show/664/arduino-fsm



Code that runs on before/after states

```
// Transition callback functions
void on_light_on_enter() {
  Serial.println("Entering LIGHT_ON");
void on_light_on_exit() {
  Serial.println("Exiting LIGHT_ON");
void on_light_off_enter() {
  Serial.println("Entering LIGHT_OFF");
```

Source: platformio.org/lib/show/664/arduino-fsm

Regular Expressions: Input validation



Regular Expressions: Input validation

HTML includes regular expressions to perform client-side form validation.

```
<input id="uname" name="uname" type="text"
    pattern="_([a-z]|[A-Z]|[0-9])+" minlength="4" maxlength="10">
```

- _[a-zA-Z0-9]+
- [a-zA-Z0-9] means any character beween a and z, or between A and Z, or between 0 and 9
- R+ means repeat R one or more times
- In this case, the username must start with an underscore _, and have one or more letters/numbers
- minlength and maxlength further restrict the string's length

Regular Expressions: Text manipulation



Regular Expressions: Text manipulation

Programming languages include regular expressions for fast and powerful text manipulation.

Example (JS)

```
let txt1 = "Hello World!";
let txt2 = txt1.replace(/[a-zA-Z]+/, "Bye"); // Replaces the first word by "Bye"
console.log(txt2);
// Bye World!
```

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Parsing JSON

Grammar for JSON



ANTLR is a **parser generator**.

- Input: a grammar; Output: a parser, and data-structures that represent the parse tree (known as a Concrete Syntax Tree)
- The HTML DOM is an example of an *Abstract* Syntax Tree

```
json: value; // initial rule

obj: '{' pair (',' pair)* '}' | '{' '}'; // a sequence of comma-separated pairs

pair: STRING ':' value; // Example: "foo": 1

array: '[' value (',' value)* ']' | '[' ']'; // a sequence of comma-separated values

value: STRING | NUMBER | obj | array | 'true' | 'false' | 'null';
// ...
```

Source: raw.githubusercontent.com/antlr/grammars-v4/master/json/JSON.g4

A grammar for JSON integers



```
NUMBER: '-'? INT ('.' [0-9] +)? EXP?; fragment INT: '0' | [1-9] [0-9]*; // fragment means do not generate code for this rule fragment EXP: [Ee] [+\-]? INT; // fragment means do not generate code for this rule
```

Source: raw.githubusercontent.com/antlr/grammars-v4/master/json/JSON.g4

A grammar for JSON



```
> ls *.java
JSONBaseListener.java JSONParser.java JSONVisitor.java
JSONBaseVisitor.java JSONLexer.java JSONListener.java
> cat JSONBaseListener.java
// Generated from ../JSON.g4 by ANTLR 4.7.2
import org.antlr.v4.runtime.tree.ParseTreeListener;
* This interface defines a complete listener for a parse tree produced by
* {Olink JSONParser}.
public interface JSONListener extends ParseTreeListener {
         * Enter a parse tree produced by {@link JSONParser#json}.
         * Oparam ctx the parse tree
        void enterJson(JSONParser.JsonContext ctx);
         * Exit a parse tree produced by {@link JSONParser#json}.
         * Oparam ctx the parse tree
        void exitJson(JSONParser.JsonContext ctx);
```

CS420



- Study **algorithms** and **abstractions**
- Theoretical study of the **boundaries of computing**

Course schedule



- 1. Learn Coq programming
- 2. Regular languages
 - Design state machines
 - Prove properties on regular languages
- 3. Context-free languages
 - Design pushdown automata
 - Prove properties on regular languages
- 4. Turing-machines
 - Prove properties on computable and non-computable languages

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On studying effectively for this content



Suggestions

- Read the chapter before the class:

 This way we can direct the class to specific details of a chapter, rather than a more topical end-to-end description of the chapter.
- Attempt to write the exercises before the class:
 We can guide a class to cover certain details of a difficult exercise.
- **Use the office hours and our online forum:** Coq is a unusual programming language, so you will get stuck simply because you are not familiar with the IDE or a quirk of the language

Module 1

Basics.v: Part 1

A primer on the programming language Coq

We will learn the core principles behind Coq

Enumerated type



A data type where the user specifies the various distinct values that inhabit the type.

Examples?

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A data type where the user specifies the various distinct values that inhabit the type.

Examples?

- boolean
- 4 suits of cards
- byte
- int32
- int64

Declare an enumerated type



```
Inductive day : Type :=
    monday : day
    tuesday : day
    wednesday : day
    thursday : day
    friday : day
    saturday : day
    sunday : day
```

- Inductive defines an (enumerated) type by cases.
- The type is named day and declared as a: Type (Line 1).
- Enumerated types are delimited by the assignment operator (:=) and a dot (.).
- Type day consists of 7 cases, each of which is is tagged with the type (day).

Printing to the standard output



Compute prints the result of an expression (terminated with dot):

Compute monday.
prints

= tuesday

: day

Interacting with the outside world



- Programming in Coq is different most popular programming paradigms
- Programming is an **interactive** development process
- The IDE is very helpful: workflow similar to using a debugger
- It's a REPL on steroids!
- Compute evaluates an expression, similar to printf





```
match d with
| monday ⇒ tuesday
| tuesday ⇒ wednesday
| wednesday ⇒ thursday
| thursday ⇒ friday
| friday ⇒ monday
| saturday ⇒ monday
| sunday ⇒ monday
end
```

Inspecting an enumerated type



```
match d with
| monday ⇒ tuesday
| tuesday ⇒ wednesday
| wednesday ⇒ thursday
| thursday ⇒ friday
| friday ⇒ monday
| saturday ⇒ monday
| sunday ⇒ monday
end
```

- match performs pattern matching on variable d.
- Each pattern-match is called a **branch**; the branches are delimited by keywords with and end.
- Each branch is prefixed by a mid-bar (|) (⇒), a pattern (eg, monday), an arrow (⇒), and a
 return value





```
Compute match monday with
  | monday ⇒ tuesday
  | tuesday ⇒ wednesday
  | wednesday ⇒ thursday
  | thursday ⇒ friday
  | friday ⇒ monday
  | saturday ⇒ monday
  | sunday ⇒ monday
  end.
```





```
Definition next_weekday (d:day) : day :=
  match d with
  | monday ⇒ tuesday
  | tuesday ⇒ wednesday
  | wednesday ⇒ thursday
  | thursday ⇒ friday
  | friday ⇒ monday
  | saturday ⇒ monday
  | sunday ⇒ monday
  end.
```

Create a function



```
Definition next_weekday (d:day) : day :=
  match d with
  | monday ⇒ tuesday
  | tuesday ⇒ wednesday
  | wednesday ⇒ thursday
  | thursday ⇒ friday
  | friday ⇒ monday
  | saturday ⇒ monday
  | sunday ⇒ monday
  | sunday ⇒ monday
  end.
```

- Definition is used to declare a function.
- In this case next_weekday has one parameter d of type day and returns (:) a value of type day.
- Between the assignment operator (:=) and the dot (.), we have the body of the function.

Example 2



```
Compute (next_weekday friday).
yields (Message pane)
= monday
: day
```

next_weekday friday is the same as monday (after evaluation)

Your first proof



```
Example test_next_weekday:
   next_weekday (next_weekday saturday) = tuesday.
Proof.
   simpl. (* simplify left-hand side *)
   reflexivity. (* use reflexivity since we have tuesday = tuesday *)
Qed.
```

Your first proof



```
Example test_next_weekday:
   next_weekday (next_weekday saturday) = tuesday.

Proof.
   simpl. (* simplify left-hand side *)
   reflexivity. (* use reflexivity since we have tuesday = tuesday *)

Qed.
```

- Example prefixes the name of the proposition we want to prove.
- The return type (:) is a (logical) **proposition** stating that two values are equal (after evaluation).
- The body of function test_next_weekday uses the 1tac proof language.
- The dot (.) after the type puts us in proof mode. (Read as "defined below".)
- This is essentially a unit test.