CS450

Structure of Higher Level Languages

Lecture 07: foldr, looping first-to-last

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Exercises on lists

Searching

Element in list?

```
(require rackunit)
(check-true (member? "d" (list "a" "b" "c" "d")))
(check-false (member? "f" (list "a" "b" "c" "d")))
```



Element in list?



Prefix in list?

```
(require rackunit)
(check-true (string-prefix? "Racket" "R")) ; available in standard library
(check-true (match-prefix? "R" (list "foo" "Racket")))
(check-false (match-prefix? "R" (list "foo" "bar")))
```



Prefix in list?

Spec

```
(require rackunit)
(check-true (string-prefix? "Racket" "R")) ; available in standard library
(check-true (match-prefix? "R" (list "foo" "Racket")))
(check-false (match-prefix? "R" (list "foo" "bar")))
```

```
(define (match-prefix? p 1)
  (match 1
      [(list) #f]
      [(list h _ ...) #:when (string-prefix? h p) #t]
      [(list _ 1 ...) (match-prefix? p 1)]))
```



Can we generalize the search algorithm?

```
; Example 1
(define (member? x 1)
   (match 1
       [(list) #f]
       [(list h _ ...) #:when (equal? h x) #t]
       [(list _ 1 ...) (member? x 1)]))
```

```
; Example 2
(define (match-prefix? p 1)
  (match 1
      [(list) #f]
      [(list h _ ...) #:when (string-prefix? h p) #t]
      [(list _ 1 ...) (match-prefix? p 1)]))
```



Can we generalize the search algorithm?

```
; Example 1
(define (member? x 1)
    (match 1
       [(list) #f]
       [(list h _ ...) #:when (equal? h x) #t]
       [(list _ 1 ...) (member? x 1)]))
```

```
; Example 2
(define (match-prefix? p 1)
  (match 1
      [(list) #f]
      [(list h _ ...) #:when (string-prefix? h p) #t]
      [(list _ 1 ...) (match-prefix? p 1)]))
```

```
(define (exists? found? 1)
  (match 1
      [(list) #f]
      [(list h _ ...) #:when (found? h) #t]
      [(list _ 1 ...) (exists? found? 1)]))
```

```
; Example 1
(define (member? x 1)
  (exists?
      (lambda (y) (equal? x y)) 1))
; Example 2
(define (match-prefix? x 1)
  (exists?
      (lambda (y) (string-prefix? y x))) 1)
```

Removing elements from list

Remove zeros from a list

```
(require rackunit)
(check-equal? (list 1 3 4) (remove-0s (list 0 1 3 0 4)))
(check-equal? (list 1 2 3) (remove-0s (list 1 2 3)))
```



Remove zeros from a list

Spec

```
(require rackunit)
(check-equal? (list 1 3 4) (remove-0s (list 0 1 3 0 4)))
(check-equal? (list 1 2 3) (remove-0s (list 1 2 3)))
Solution
```

```
(define (remove-0s 1)
  (match 1
     [(list) (list)]
     [(list h 1 ...) #:when (not (equal? h 0))
       (cons h (remove-0s 1))]
     \lceil (\text{list} \ \_ \ 1 \ \dots) \ (\text{remove-0s} \ 1) \rceil) \rangle
```

Solution in Python

```
def remove_0s(1):
  result = []
  for h in 1:
    if h != 0:
      result.append(h)
  return result
```



Can we generalize this functional pattern?

Original

```
(define (remove-0s 1)
  (match 1
      [(list) (list)]
      [(list h 1 ...) #:when (not (equal? h 0))
          (cons h (remove-0s 1))]
      [(list _ 1 ...) (remove-0s 1)]))
```

Generalized

```
(define (filter keep? 1)
  (match 1
      [(list) (list)]
      [(list h 1 ...) #:when (keep? h)
          (cons h (filter keep? 1))]
      [(list _ 1 ...) (filter keep? 1)]))

;; Usage example
(define (remove-0s 1)
  (filter
      (lambda (x) (not (equal? x 0))) 1))
```



Concatenate two lists

Concatenate two lists

Implement function (append 11 12) that appends two lists together. Spec

```
(check-equal?
  (append (list 1 2) (list 3 4))
  (list 1 2 3 4))
```



Concatenate two lists

Implement function (append 11 12) that appends two lists together. Spec

```
(check-equal?
  (append (list 1 2) (list 3 4))
  (list 1 2 3 4))
```



Generalizing order-preserving loops

An order-preserving recursion pattern

- 1. Case (list) (handle-base)
- 2. Case (list h 1 ...) (handle-step)
- 3. Recursive call handles "smaller"

Example 1

```
(define (map f 1)
  (match 1
      [(list) (list)]
      [(list h 1 ...)
            (define result (map f 1))
            (cons (f h) result)]))
      ; = (handle-step h result)
```

Example 2



An order-preserving recursion pattern

Searching

```
(define (exists? found? 1)
  (match 1
      [(list) #f]
      [(list h _ ...) #:when (found? h) #t]
      [(list _ 1 ...) (exists? found? 1)]))
```

Following the recursion pattern

```
(define (exists? found? 1)
  (match 1
    [(list) #f]
    [(list h 1 ...)
        (define result (exists? found? 1))
        (or (found? h) result)]))
```



An order-preserving recursion pattern

Removing

```
(define (filter keep? 1)
  (match 1
       [(list) (list)]
       [(list h 1 ...) #:when (keep? h)
            (cons h (filter keep? 1))]
       [(list _ 1 ...) (filter keep? 1)]))
```

Following the recursion pattern



Implementing this recursion pattern

Implementing this recursion pattern

Recursive pattern for lists

```
(define (rec 1)
  (match 1
    [(list) base-case]
    [(list h 1 ...)
        (define result (rec 1))
        (handle-step h result)]))
```

Fold right reduction

```
(define (foldr handle-step base-case 1)
  (match 1
    [(list) base-case]
    [(list h 1 ...)
        (define result (foldr step base-case 1))
        (handle-step h result)]))
```

```
# In Python
def foldr(step, base_case, 1):
    result = base_case
    for h in reversed(1):
        result = step(h, result)
    return result

UMass
Boston
```

Implementing map with foldr

```
(define (map f 1)
  (match l
    [(list) (list)]
    [(list h 1 ...)
        (define result (map f 1))
        (cons (f h) result)]))
```



Implementing map with foldr

```
(define (map f 1)
    (match 1
        [(list) (list)]
        [(list h 1 ...)
            (define result (map f 1))
            (cons (f h) result)]))
```

```
(define (map f 1)
  (foldr
    ; step: how do you build the next result
      (lambda (h result) (cons (f h) result))
    ; what to return when the list is empty
      (list)
    ; iterate/match over l
      1))
```

```
# Python pseudo-code
result = []
for h in reversed(1):
    # result = cons(f(h), result)
    result.append(f(h))
```



Implementing append with foldr



Implementing append with foldr

```
(define (append 11 12)
  (foldr
    ; step: add the element to the list being built
      (lambda (h result) (cons h result))
    ; base-case: start with list 12
      12
      ; iterate/match over 11
      11))
```



Implementing filter with foldr

```
(define (filter keep? 1)
  (match l
    [(list) (list)]
    [(list h l ...)
        (define result (filter keep? 1))
        (if (keep? h) (cons h result) result)]))
```



Implementing filter with foldr

```
(define (filter keep? 1)
    (match l)
    [(list) (list)]
    [(list h l ...)
        (define result (filter keep? 1))
        (if (keep? h) (cons h result) result)]))
```

```
(define (filter keep? 1)
  (foldr
    ; handle-step
    (lambda (h result) (if (keep? h) (cons h result) result))
    ; base-case
    (list)
    ; iterate/match over l
    1))
```



Implementing exists? with foldr

```
(define (exists? found? 1)
  (match l
    [(list) #f]
    [(list h l ...)
        (define result (exists? found? 1))
        (or (found? h) result)]))
```



Implementing exists? with foldr

```
(define (exists? found? 1)
  (match 1
    [(list) #f]
    [(list h 1 ...)
        (define result (exists? found? 1))
        (or (found? h) result)]))
```

```
(define (exists? found? 1)
  (foldr
    ; handle-step
     (lambda (h result) (or (found? h) result))
    ; base-case
    #f
    ; iterate over l
     1))
```

