CS450

Structure of Higher Level Languages

Lecture 08: Functions as values

Tiago Cogumbreiro

Today we will learn about...



- Modules in Racket
- Functions as values
- Creating functions dynamically
- Using functions as data-structures

Modules

Modules



- Modules encapsulate a unit of functionality
- A module groups a set of constants and functions
- A module encapsulates (hides) auxiliary top-level functions
- Each file represents a module

Modules in Racket



Each file represents a module. A bindings becomes visible through the **provide** construct. Function (require "filename") loads a module

- (provide (all-defined-out)) makes all bindings visible
- (provide a c) makes binding a and c visible
- (require "foo.rkt") makes all bindings of the module in file foo.rkt visible in the current module. Both files have to be in the same directory.

```
File: foo.rkt
```

```
#lang racket
; Make variables a and c visible
(provide a c)
(define a 10)
(define b (+ a 30)
(define (c x) b)
```

File: main.rkt

```
(require "foo.rkt")
(c a)
; b is not visible
```

Functions as values

What is functional programming



- Functional programming has different meanings to different people
 - Avoid mutation
 - Using functions as values
 - A programming style that encourages recursion and recursive data structures
 - A programming model that uses *lazy* evaluation (discussed later)

First-class functions



- **Functions are values:** can be passed as arguments, stored in data structures, bound to variables, ...
- Functions for extension points: A powerful way to factor out a common functionality



Monotonic increasing function (for one input)

Function monotonic? takes a function f as a parameter and a value x, and then checks if f increases monotonically for a given x.

Example

```
#lang racket
(define (double n) (* 2 n))
(define (monotonic? f x)
  (≥ (f x) x))
;; Tests
(require rackunit)
(check-true (monotonic? double 3))
(check-false (monotonic? (lambda (x) (- x 1)) 3))
```

How do we evaluate?

```
(monotonic? double 3)
```



Monotonic increasing function (for one input)

Function monotonic? takes a function f as a parameter and a value x, and then checks if f increases monotonically for a given x.

Example

```
#lang racket
(define (double n) (* 2 n))
(define (monotonic? f x)
  (≥ (f x) x))
;; Tests
(require rackunit)
(check-true (monotonic? double 3))
(check-false (monotonic? (lambda (x) (- x 1)) 3))
```

How do we evaluate?

```
(monotonic? double 3)

= (≥ (double 3) 3)
= (≥ ((lambda (n) (* 2 n) 3) 3)
= (≥ (* 2 3) 3)
= (≥ 6 3)
= #t
```



Recursively apply a function n-times

Function apply-n takes a function f as parameter, a number of times n, and some argument x, and then recursively calls (f(f(...(fx)))) an n-number of times.

Example apply-n



Let us unfold the following...

```
(apply-n double 3 1) ; (\leq 3 \theta) = \#f
```

Example apply-n



Let us unfold the following...

```
(apply-n double 3 1) ; (\le 3 \ 0) = \#f

= (apply-n double (- 3 1) (double 1))
= (apply-n double 2 2) ; (\le 2 \ 0) = \#f
= (apply-n double (- 2 1) (double 2))
= (apply-n double 1 4) ; (\le 1 \ 0) = \#f
= (apply-n double (- 1 1) (double 4))
= (apply-n double 0 8) ; (\le 0 \ 0) = \#f
```

Functions as data-structures

Functions as data-structures



The following is a function that returns a constant value (returns 3 always):

Note the difference...

The following is a variable binding (not a function!):

```
(define three:1 3)
```

Variable three: 1 evaluates to the number 3.





We can generalize the procedure by creating a function that returns a new function declaration that returns a given parameter n.

Implementing a pair with functions alone



If we can capture one parameter, then we can also capture two parameter. **Let us implement a pair-data structure with only functions!**