

Hets/Ontohub Tutorial

Mihai Codescu Till Mossakowski Christian Maeder
Oliver Kutz Fabian Neuhaus

Otto-von-Guericke Universität Magdeburg

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Overview

- 1 Presentation of HETS
- 2 HETS demo
- 3 Ontohub demo

The *Heterogenous Tool Set* (Hets)

- **a tool integration platform for heterogeneous specification**
- connects state-of-the art provers
- parsers and static analysis tools for logical formalisms
- Hets understands
 - logic-specific module languages
 - **DOL**: logic-independent, heterogeneous module language
- logic-independent proof management

The *Heterogenous Tool Set* (Hets)

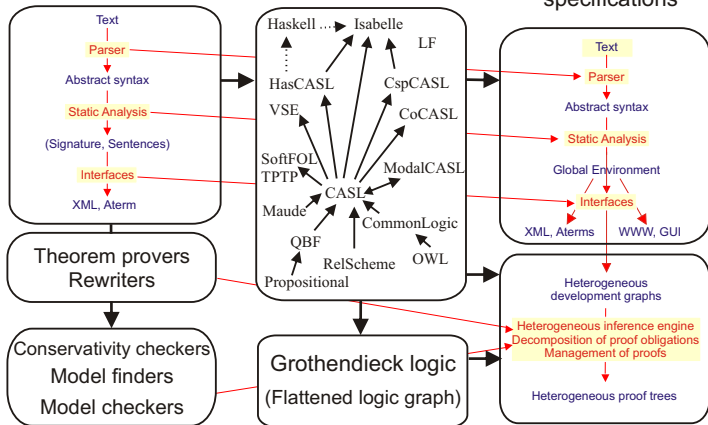
- uniform but heterogeneous **semantics** via the Grothendieck institution
- easy way to **plug-in** new formalisms and translations
- systematic connection of **new formalisms** to **tools** using translations
- currently 25 logics, 50 translations, 20 tools

Architecture of the heterogeneous tool set Hets

Tools for specific logics

Logic graph

Tools for heterogeneous specifications



Logics supported by Hets

- **General-purpose logics**

Classical propositional logic Propositional, QBF

First-order logic SoftFOL / TPTP

Datatypes CASL: multi-sorted first-order logic with
subsorts, partial functions and datatypes

Higher-order logic THF0, HasCASL (polymorphism, type
classes)

- **logical frameworks**

Higher-order logic Isabelle, HOL-light

Dependent types DFOL, LF

- **Ontologies**

OWL Web Ontology Language (OWL)

Common Logic ISO-Standard for specification of ontologies

Relational Database Schemas RelScheme

Logics supported by Hets (ctd.)

- **Reactive and parallel systems**

Process algebra CspCASL

Coalgebra CoCASL (Coalgebraic specification of reactive systems)

First-order modal and temporal logic ModalCASL

Rewriting Maude

- **Programming languages**

First-order dynamic logic VSE (Pascal-like programs)

Functional programming languages Haskell, FPL, Adl

- **Tool-specific logics**

Computer algebra systems EnCL (for *reduce*)

CAD-Systems DMU, FreeCAD (ABoxes for the CAD-Systems CATIA and FreeCAD)

- planned: **UML, Java, JML**

Sound Integration of Heterogeneity

- logics are formalized as **institutions** (Goguen, Burstall 1984)
- logic translations are formalized as **institution (co)morphisms** (Goguen, Rosu 2002)
- logic translations embed or encode logical structure in a way that **truth is preserved**
- Grothendieck logic = **flat combination** of the logics in a logic graph (Diaconescu 2002)
- Hets provides an object-oriented interface for **plugging in institutions and (co)morphisms**

Institutions

Signatures

$$\Sigma \xrightarrow{\sigma} \Sigma'$$

Sentences

 $\text{Sen } \Sigma$ $\xrightarrow{\text{Sen } \sigma}$ $\text{Sen } \Sigma'$

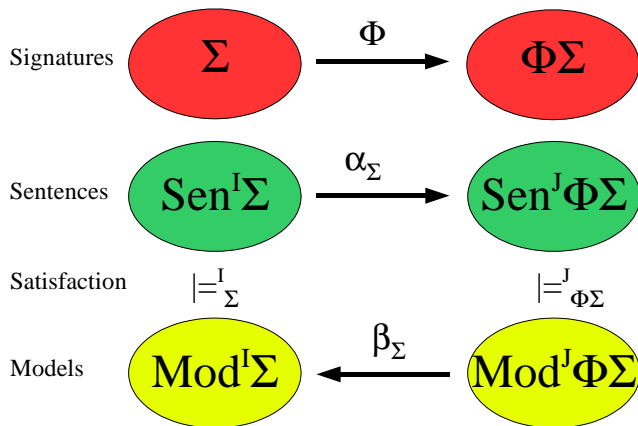
Satisfaction

 $|=_{\Sigma}$ $|=_{\Sigma'}$

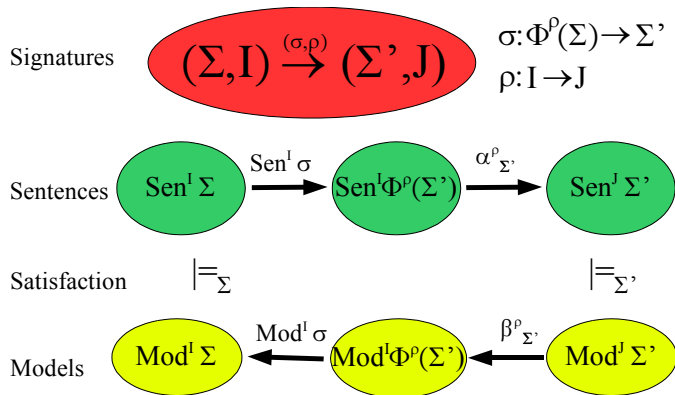
Models

 $\text{Mod } \Sigma$ $\xleftarrow{\text{Mod } \sigma}$ $\text{Mod } \Sigma'$

Institution comorphisms



The Grothendieck institution



Syntax of Structured Specifications

SP ::= BASIC-SPEC basic specification
 | SP then SP extension
 | SP and SP union
 | SP with SYMBOL-MAP renaming
 | SP hide SYMBOLS hiding
 | SPEC-NAME [PARAM*] reference to named spec
 | combine DIAGRAM colimit

LIBRARY-ITEM ::=
 spec SPEC-NAME [PARAM*] = SP end name a spec
 | view VIEW-NAME : SP to SP = SYMBOL-MAP end
 refinement between specifications
 | diagram DNAME = SPEC-NAME*, VIEW-NAME*, DNAME*
 excluding SPEC-NAME*, VIEW-NAME*, DNAME*
 diagrams

Syntax of Structured Specifications

```
SP ::=  BASIC-SPEC  
      |  SP then SP  
      |  SP and SP  
      |  SP with SYMBOL-MAP  
      |  SP hide SYMBOLS  
      |  SPEC-NAME [PARAM*]
```

```
LIBRARY-ITEM ::=  
  spec SPEC-NAME [PARAM*] = SP end  
  | view VIEW-NAME : SP to SP = SYMBOL-MAP end
```

Syntax of Heterogeneous Specifications

SP ::= BASIC-SPEC | logic LOGIC-NAME : {SP}
| SP then SP
| SP and SP
| SP with SYMBOL-MAP | SP with logic COMORPHISM
| SP hide SYMBOLS | SP hide logic MORPHISM
| SPEC-NAME [PARAM*]

LIBRARY-ITEM ::=
spec SPEC-NAME [PARAM*] = SP end
| view VIEW-NAME : SP to SP = SYMBOL-MAP end
| view VIEW-NAME : SP to SP = SYMBOL-MAP, COMORPHISM
| logic LOGIC-NAME

Heterogeneous Development Graphs

Heterogeneous structured specifications are mapped into heterogeneous development graphs:

- **nodes** correspond to individual specification modules
- **definition links** correspond to imports of modules
- **theorem links** express proof obligations

Development graphs are a tool for **management** and **reuse of proofs**.

Development graphs $\mathcal{S} = \langle \mathcal{N}, \mathcal{L} \rangle$

Nodes in \mathcal{N} : (Σ^N, Γ^N) with

- Σ^N **signature**,
- $\Gamma^N \subseteq \mathbf{Sen}(\Sigma^N)$ set of **local axioms**.

Links in \mathcal{L} :

- **global** $M \xrightarrow{\sigma} N$, where $\sigma : \Sigma^M \rightarrow \Sigma^N$,
- **local** $M \xrightarrow{\sigma} N$ where $\sigma : \Sigma^M \rightarrow \Sigma^N$, or
- **hiding** $M \xrightarrow[\text{hide}]{\sigma} N$ where $\sigma : \Sigma^N \rightarrow \Sigma^M$
going against the direction of the link.

Semantics of development graphs

$Mod_S(N)$ consists of those Σ^N -models n for which

- ① n satisfies the local axioms Γ^N ,
- ② for each $K \xrightarrow{\sigma} N \in S$, $n|_{\sigma}$ is a K -model,
- ③ for each $K \multimap^{\sigma} N \in S$,
 $n|_{\sigma}$ satisfies the local axioms Γ^K ,
- ④ for each $K \xrightarrow[\text{hide}]{\sigma} N \in S$,
 n has a σ -expansion k (i.e. $k|_{\sigma} = n$) that is a K -model.

Theorem links

Theorem links come, like definition links, in different versions:

- **global** theorem links $M \xrightarrow{\sigma} N$, where $\sigma: \Sigma^M \longrightarrow \Sigma^N$,
- **local** theorem links $M \xrightarrow[\sigma]{} N$, where $\sigma: \Sigma^M \longrightarrow \Sigma^N$

Semantics of theorem links

- $\mathcal{S} \models M \xrightarrow{\sigma} N$ iff for all $n \in \text{Mod}_S(N)$, $n|_{\sigma} \in \text{Mod}_S(M)$.
- $\mathcal{S} \models M \xrightarrow{\sigma} N$ iff for all $n \in \text{Mod}_S(N)$, $n|_{\sigma} \models \Gamma^M$.

Proof Calculus

Theorem

The proof calculus for heterogeneous development graphs is sound and complete under mild technical assumptions.

- decompose global theorem links semi-automatically into local ones
- choose specific provers for local proof goals