Look at the following FST, implemented using Pynini:

```
import pynini as pn fst = (pn.a("a") \mid pn.a("e")) + pn.t("a", pn.a("0").closure(0,5)) \mid pn.t(pn.a("a").star, "0") + pn.a("xxx") You may use a computer to answer the following questions:
```

- 1. Give a regular expression that is equivalent to the input language of this finite state transducer. (1 point)
- 2. Give inputs that are mapped by this FST to 0 outputs, 1 output, 2 outputs, and more than 2 outputs. (4 points)
- 3. Make program that uses Pynini to map numbers (represented as strings) to French words (up to 999999999). Use provided numbers2words.py as starter.

It's a good idea to implement this with two FSTs. The first FST will factorize a number into into sequences annotated with powers of ten:

```
0 -> 0
1 -> 1
10 -> 1^
23 -> 2^3
203 -> 2^3
```

A second FST will convert the factorized form into words:

```
0 -> zero
1 -> un
1^ -> dix
2^ 3 -> vingt et un
```

Finally, you should also handle decimals. Decimals should be verbalized digit-by-digit: 0.046 whould be converted into "zero virgule zero quatre six".

You are not expected to know French to complete this task. Use materials on the web, e.g. https://tuto.pages-informatique.com/writing-out-numbers-in-french-letters.php

Yes, this does give some advantage to the French students. However, the situation is quite realistic: when you work in NLP, you often have to deal with a language that you don't know.

You should submit the program, which is a modification of the provided template. It should run as is, without any additional dependencies. Scoring: an undisclosed test set (similar to the provided unit test) will be used for scoring. Depending on the number of successful and failed tests, you will get 0 to 10 points. The scale is linear: score = 10.0 * num_successful_tests / num_tests