## **CSE 102**

## **Homework Assignment 3**

1. Define T(n) by the recurrence

$$T(n) = \begin{cases} 2 & \text{if } n = 1\\ 3T(\lfloor n/2 \rfloor) + n^2 & \text{if } n \ge 2 \end{cases}$$

Use the substitution method to show that  $T(n) = O(n^2)$ .

2. Define T(n) by the recurrence

$$T(n) = \begin{cases} 1 & \text{if } n = 1 \\ T(n-1) + n & \text{if } n \ge 2 \end{cases}$$

Use the iteration method to find the exact solution to this recurrence, then determine an asymptotic solution.

3. Define T(n) by the recurrence

$$T(n) = \begin{cases} 9 & \text{if } 1 \le n < 15 \\ T(|n/2|) + 6 & \text{if } n \ge 15 \end{cases}$$

Use the iteration method to find the exact solution to this recurrence, then determine an asymptotic solution.

4. Define T(n) by the recurrence

$$T(n) = \begin{cases} 4 & \text{if } 1 \le n < 3 \\ T(\lfloor n/3 \rfloor) + n & \text{if } n \ge 3 \end{cases}$$

Use iteration to find a tight asymptotic bound for T(n).

- 5. Use the Master Theorem to find tight asymptotic bounds for the recurrences in problems 3 and 4 above.
- 6. Use the Master Theorem to find tight asymptotic bounds on the following recurrences.

a. 
$$T(n) = 3T(2n/3) + n^3$$

b. 
$$T(n) = 2T(n/3) + \sqrt{n}$$

c. 
$$T(n) = 5T(n/4) + n^{\lg \sqrt{5}}$$

$$d. T(n) = 3T(2n/5) + n\log n$$

e. 
$$S(n) = aS(n/4) + n^2$$
 (your answer will depend on the parameter a.)