# Colbyn's Exam #1 Corrections

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## Question #1

> **Question:** Consider the angle $\theta$ in with measure $-495°$.

The problem with this question is that I was trying to be smart by simplifying $-495°$ to $225°$, so thereafter all of my subsequent work was using an angle co-terminal to $-495°$. In this context, my mistake was equating co-terminal angles as being the same, but this only applies to the output of periodic functions where co-terminal angles **map to the same value**, but the arguments themselves represent different measures.

### Question #1 (A)
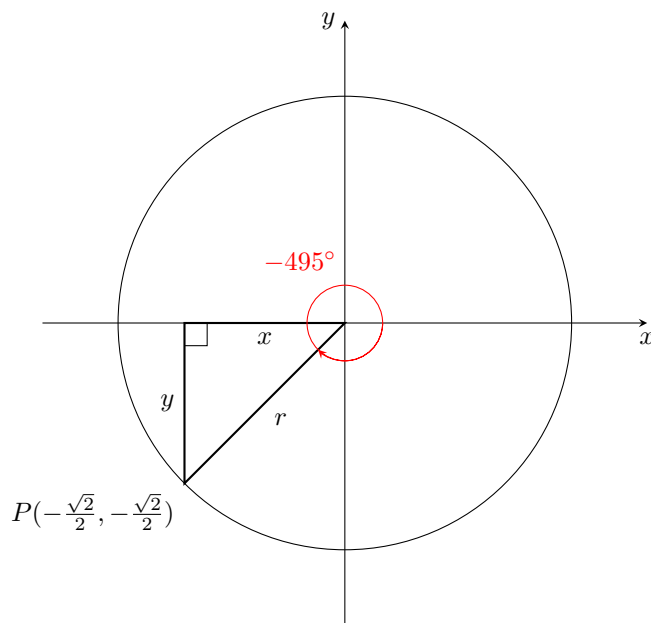
Using the following relation:

$$x° = \frac{x}{360}\tau \text{ rad} \tag{1}$$

I can express $-495°$ in terms of turns (or $\tau$) like so:

$$
\begin{aligned}
-495° &= \frac{-495}{360}\tau \text{ rad} \\
&= -\frac{11}{8}\tau \text{ rad} \\
&= -1\frac{3}{8}\tau
\end{aligned}
\tag{2}
$$

Since this angle is expressed in terms of turns, we have a intuitive idea about how the graph the given angle. I.e. because $-\frac{3}{8}$ can be considered a ratio of a circle, which is easy to picture, in the same manner that $\frac{3}{4}$ of a circle is easy to imagine, compared to e.g. $\frac{3}{2}$ half circles.

Therefore, I know that this angle makes one full revolution, and $-\frac{3}{8}$ of a revolution (going clockwise), which results in the following figure correctly drawn in the context of a $-495°$ angle:



## Question #1 (B)

Using the following relation:

$$x° = \frac{x}{360}(2\pi) \text{ rad} \tag{3}$$

I can **correctly** express $-495°$ degrees in terms of radians like so:

$$
\begin{aligned}
-495° &= \frac{-495}{360}(2\pi) \text{ rad} \\
&= -\frac{11}{8}(2\pi) \text{ rad} \tag{4} \\
&= -\frac{11}{4}\pi \text{ rad}
\end{aligned}
$$

**Answer:** $-\frac{11}{4}\pi$ rad

## Question #3

This should have been correct, what happens is my brain frequently gets things mixed up, i.e. there was a disconnect between my internal thoughts and what manifested on paper. I know that $\sec(x)$ is the reciprocal of $\cos(x)$, just as $\csc(x)$ is the reciprocal of $\sin(x)$, and that $\cot(x)$ is the reciprocal of $\tan(x)$, and furthermore in the context of the unit circle, that $\sin(\theta)$ represents the y value, and that $\cos(\theta)$ represents the x value.
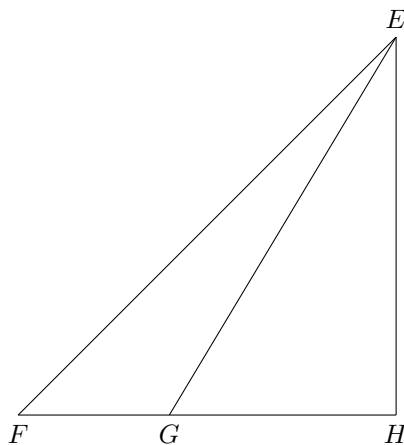
Therefore, given the some $P(-20, 21)$ for $\theta$:

$$r = \sqrt{x^2 + y^2} = 29$$
$$\sin(\theta) = \frac{y}{r} = \frac{21}{29} \tag{5}$$
$$\sec(\theta) = \frac{r}{x} = \frac{29}{-20} = -\frac{29}{20}$$

**Answer:** $\sin(\theta) = \frac{21}{29}$, $\sec(\theta) = -\frac{29}{20}$

## Question #4

This was one of those questions where I wonder if I'm just dumb, or if it's legitimately a hard problem... Either way something I would have failed at regardless.



Information given:

- FG = 600 m

- $\angle EFH = 1.91°$

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# Question #5

# Question #6

# Miscellaneous

Location: https://github.com/colbyn/exam-1-extra-corrections.