# Colbyn's Exam #1 Corrections

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## Question #1

**Question:** Consider the angle  $\theta$  in with measure  $-495^{\circ}$ .

The problem with this question is that I was trying to be smart by simplifying  $-495^{\circ}$  to  $225^{\circ}$ , so thereafter all of my subsequent work was using an angle coterminal to  $-495^{\circ}$ . In this context, my mistake was equating co-terminal angles as being the same, but this only applies to the output of periodic functions where co-terminal angles **map to the same value**, but the arguments themselves represent different measures.

### Question #1 (A)

Using the following relation:

$$x^{\circ} = \frac{x}{360}\tau \text{ rad} \tag{1}$$

I can express  $-495^{\circ}$  in terms of turns (or  $\tau$ ) like so:

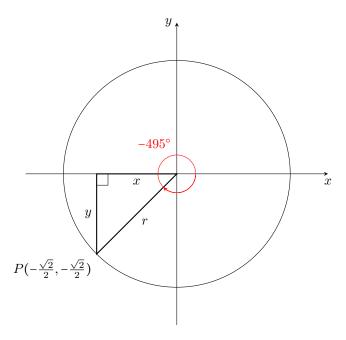
$$-495^{\circ} = \frac{-495}{360} \tau \text{ rad}$$

$$= -\frac{11}{8} \tau \text{ rad}$$

$$= -1\frac{3}{8} \tau$$
(2)

Since this angle is expressed in terms of turns, we have a intuitive idea about how the graph the given angle. I.e. because  $-\frac{3}{8}$  can be considered a ratio of a circle, which is easy to picture, in the same manner that  $\frac{3}{4}$  of a circle is easy to imagine, compared to e.g.  $\frac{3}{2}$  half circles.

Therefore, I know that this angle makes one full revolution, and  $-\frac{3}{8}$  of a revolution (going clockwise), which results in the following figure correctly drawn in the context of a  $-495^{\circ}$  angle:



### Question #1 (B)

Using the following relation:

$$x^{\circ} = \frac{x}{360} (2\pi) \text{ rad} \tag{3}$$

I can **correctly** express  $-495^{\circ}$  degrees in terms of radians like so:

$$-495^{\circ} = \frac{-495}{360} (2\pi) \text{ rad}$$

$$= -\frac{11}{8} (2\pi) \text{ rad}$$

$$= -\frac{11}{4} \pi \text{ rad}$$
(4)

**Answer:**  $-\frac{11}{4}\pi$  rad

#### Question #1 (C)

### Question #3

This should have been correct, what happens is my brain frequently gets things mixed up, i.e. there was a disconnect between my internal thoughts and what manifested on paper. I know that  $\sec(x)$  is the reciprocal of  $\cos(x)$ , just as  $\csc(x)$  is the reciprocal of  $\sin(x)$ , and that  $\cot(x)$  is the reciprocal of  $\tan(x)$ , and furthermore in the context of the unit circle, that  $\sin(\theta)$  represents the y value, and that  $\cos(\theta)$  represents the x value.

Therefore, given the some P(-20,21) for  $\theta$ :

$$r = \sqrt{x^2 + y^2} = 29$$

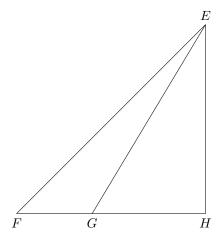
$$\sin(\theta) = \frac{y}{r} = \frac{21}{29}$$

$$\sec(\theta) = \frac{r}{x} = \frac{29}{-20} = -\frac{29}{20}$$
(5)

**Answer:**  $\sin(\theta) = \frac{21}{29}$ ,  $\sec(\theta) = -\frac{29}{20}$ 

## Question #4

This was one of those questions where I wonder if I'm just dumb, or if it's legitimately a hard problem... Either way something I would have failed at regardless.



Information given:

- $\overline{FG}$  = 600m
- $\angle EFH = 1.91^{\circ}$
- $\angle EGH = 2.67^{\circ}$

Solution:

$$\tan(2.67^{\circ}) = \frac{\overline{EH}}{x}$$

$$x = \frac{\overline{EH}}{\tan(2.67^{\circ})}$$

$$\tan(1.91^{\circ}) = \frac{\overline{EH}}{600 + x}$$

$$(600 + x)(\tan(1.91^{\circ})) = (600 + x)\frac{\overline{EH}}{600 + x}$$

$$(600 + x)(\tan(1.91^{\circ})) = \overline{EH}$$

$$(600 \cdot \tan(1.91^{\circ}) + x \cdot \tan(1.91^{\circ}) = \overline{EH}$$

$$600 \cdot \tan(1.91^{\circ}) = \overline{EH} - \overline{EH}\frac{\tan(1.91^{\circ})}{\tan(2.67^{\circ})}$$

$$600 \cdot \tan(1.91^{\circ}) = \overline{EH}(1 - \frac{\tan(1.91^{\circ})}{\tan(2.67^{\circ})})$$

$$\frac{600 \cdot \tan(1.91^{\circ})}{1 - \frac{\tan(1.91^{\circ})}{\tan(2.67^{\circ})}} = \overline{EH} \approx 70$$

During the exam I was stuck on the gap between G and H, in hindsight it all makes sense, i.e. just solve for  $\overline{GH}$  using an unknown value for  $\overline{EH}$ , since we can factor this quantity out in the ensuing expression for  $\tan(1.91^{\circ})$ . Although this realization occurred after spending an hour or so on the problem, I suppose failing this question was inevitable.

**Answer:**  $\overline{EH} \approx 70 \text{ m}$ 

Question #5

Question #6

Miscellaneous

Location: https://github.com/colbyn/exam-1-extra-corrections.