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```
clc  
clear all  
close all
```

---

## Initial Conditions

---

```
phi = 0;  
theta = pi/2;  
psi = 0;  
  
W_ic = [.2 .2 1]';
```

---

## Time Periods

---

```
tstep = 1000;  
control_time = 25;  
waitingperiod = (control_time*3)/tstep;  
  
tspan_con = linspace(0,control_time,tstep);  
  
tspan_detumble = linspace(control_time,control_time*2,tstep);  
  
tspan_phi=linspace(control_time*2,control_time*2.5,tstep);  
  
tspan_theta=linspace(control_time*2.5,control_time*3,tstep);  
  
tspan_psi=linspace(control_time*3,control_time*4,tstep);  
  
syms W1 W2 W3
```

---

## ODE45

---

```
%ODE 45: W1 and W2 Reduction  
[t, W1_W2_Detumble] = ode45(@(t,state) controller1(t,state), tspan_con, [W_ic(1) W_ic(2) W_ic(3) phi theta psi]);  
  
%ODE45: W3 Reduction, using final conditions of previous ODE for continuity  
[t2, W3_Detumble] = ode45(@(t,state) detumble(t,state), tspan_detumble, [W1_W2_Detumble(end,1) W1_W2_Detumble(end,2) W1_W2_Detumble(end,3) W1_W2_Detumble(end,4) W1_]  
  
%ODE 45: Angle Correction, using final conditions of previous ODE for continuity  
[t3, Angle_Correction_Phi] = ode45(@(t,state) angle_phi(t,state), tspan_phi, [W3_Detumble(end,1) W3_Detumble(end,2) W3_Detumble(end,3) W3_Detumble(end,4) W3_Detumb]  
  
%ODE 45: Angle Correction, using final conditions of previous ODE for continuity  
[t3, Angle_Correction_Theta] = ode45(@(t,state) angle_theta(t,state), tspan_theta, [Angle_Correction_Phi(end,1) Angle_Correction_Phi(end,2) Angle_Correction_Phi(en]  
  
%ODE 45: Angle Correction, using final conditions of previous ODE for continuity  
[t3, Angle_Correction_Psi] = ode45(@(t,state) angle_psi(t,state), tspan_psi, [Angle_Correction_Theta(end,1) Angle_Correction_Theta(end,2) Angle_Correction_Theta(en
```

---

## Plots

---

```
%Plot W1 Control Timeline  
subplot(3,1,1)  
plot(tspan_con,W1_W2_Detumble(1:tstep,1),tspan_detumble,W3_Detumble(1:tstep,1),tspan_phi,Angle_Correction_Phi(1:tstep,1),tspan_theta,Angle_Correction_Theta(1:tstep,  
xlabel('Time (s)')  
ylabel('omega_1 (rad/s)', 'FontSize',12)  
legend('omega_1+omega_2 Detumble','omega_3 Reduction','Phi Correction','Theta Correction','Psi Correction')  
title('Satellite omega_1 Control')  
  
%Plot W2 Control Timeline  
subplot(3,1,2)  
plot(tspan_con, W1_W2_Detumble(1:tstep,1),tspan_detumble, W3_Detumble(1:tstep,1),tspan_phi,Angle_Correction_Phi(1:tstep,2),tspan_theta,Angle_Correction_Theta(1:tste  
xlabel('Time (s)')  
ylabel('omega_2 (rad/s)', 'FontSize',12)  
legend('omega_1+omega_2 Detumble','omega_3 Reduction','Phi Correction','Theta Correction','Psi Correction')  
title('Satellite omega_2 Control')  
  
%Plot W3 Control Timeline  
subplot(3,1,3)  
plot(tspan_con,W1_W2_Detumble(1:tstep,3),tspan_detumble,W3_Detumble(1:tstep,3),tspan_phi,Angle_Correction_Phi(1:tstep,3),tspan_theta,Angle_Correction_Theta(1:tstep,
```

---

```

xlabel('Time (s)')
ylabel('\omega_3 (rad/s)', 'FontSize',12)
legend('\omega_1+\omega_2 Detumble','\omega_3 Reduction','\Phi Correction','\Theta Correction','\Psi Correction')
title('Satellite \omega_3 Control')

%Phi Control Timeline (0-2pi)
figure(2)
subplot(3,1,1)
plot(tspan_con,rem(W1_W2_Detumble(1:tstep,4)/(2*pi),1)*2*pi,tspan_detumble,rem(W3_Detumble(1:tstep,4)/(2*pi),1)*2*pi,tspan_phi,rem(Angle_Correction_Phi(1:tstep,4)/(2*pi),1)*2*pi,tspan_theta,Angle_Correction_Theta(1:tstep,4))
xlabel('Time (s)')
ylabel('Phi (rad)')
legend('\omega_1+\omega_2 Detumble','\omega_3 Reduction','\Phi Correction','\Theta Correction','\Psi Correction')
title('Satellite \Phi Control (0 through 2\pi)')

%Theta Control Timeline (0-2pi)
subplot(3,1,2)
plot(tspan_con, rem(W1_W2_Detumble(1:tstep,5)/(2*pi),1)*2*pi,tspan_detumble,rem(W3_Detumble(1:tstep,5)/(2*pi),1)*2*pi,tspan_phi,rem(Angle_Correction_Phi(1:tstep,5)/(2*pi),1)*2*pi,tspan_theta,Angle_Correction_Theta(1:tstep,5))
xlabel('Time (s)')
ylabel('Theta (rad)')
legend('\omega_1+\omega_2 Detumble','\omega_3 Reduction','\Phi Correction','\Theta Correction','\Psi Correction')
title('Satellite \Theta Control (0 through 2\pi)')

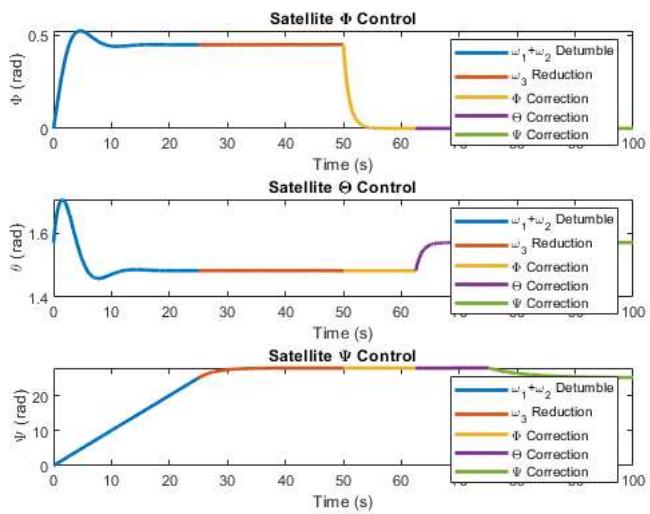
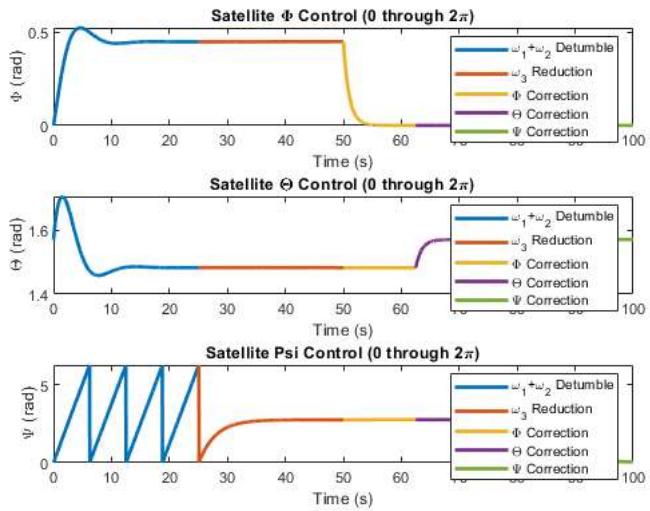
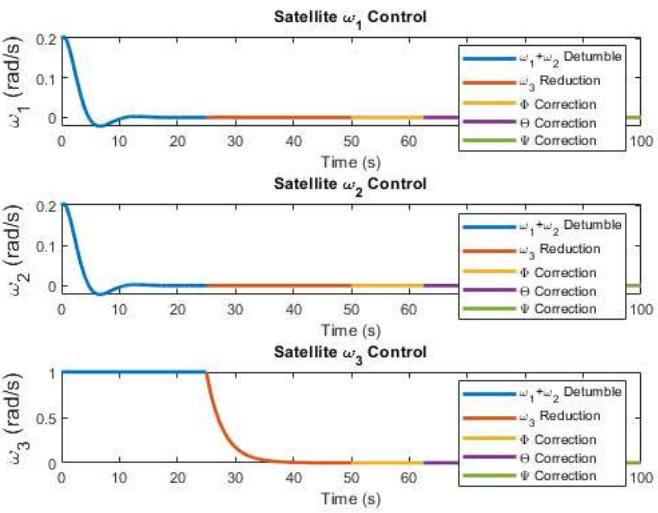
%Psi Control Timeline (0-2pi)
subplot(3,1,3)
plot(tspan_con,rem(W1_W2_Detumble(1:tstep,6)/(2*pi),1)*2*pi,tspan_detumble,rem(W3_Detumble(1:tstep,6)/(2*pi),1)*2*pi,tspan_phi,rem(Angle_Correction_Phi(1:tstep,6)/(2*pi),1)*2*pi,tspan_theta,Angle_Correction_Theta(1:tstep,6))
xlabel('Time (s)')
ylabel('Psi (rad)')
legend('\omega_1+\omega_2 Detumble','\omega_3 Reduction','\Phi Correction','\Theta Correction','\Psi Correction')
title('Satellite Psi Control (0 through 2\pi)')

%Phi Control Timeline Total Magnitude
figure(3)
subplot(3,1,1)
plot(tspan_con,W1_W2_Detumble(1:tstep,4),tspan_detumble,W3_Detumble(1:tstep,4),tspan_phi,Angle_Correction_Phi(1:tstep,4),tspan_theta,Angle_Correction_Theta(1:tstep,4))
xlabel('Time (s)')
ylabel('Phi (rad)')
legend('\omega_1+\omega_2 Detumble','\omega_3 Reduction','\Phi Correction','\Theta Correction','\Psi Correction')
title('Satellite \Phi Control')

%Theta Control Timeline Total Magnitude
subplot(3,1,2)
plot(tspan_con,W1_W2_Detumble(1:tstep,5),tspan_detumble,W3_Detumble(1:tstep,5),tspan_phi,Angle_Correction_Phi(1:tstep,5),tspan_theta,Angle_Correction_Theta(1:tstep,5))
xlabel('Time (s)')
ylabel('theta (rad)')
legend('\omega_1+\omega_2 Detumble','\omega_3 Reduction','\Phi Correction','\Theta Correction','\Psi Correction')
title('Satellite \Theta Control')

%Psi Control Timeline Total Magnitude
subplot(3,1,3)
plot(tspan_con,W1_W2_Detumble(1:tstep,6),tspan_detumble,W3_Detumble(1:tstep,6),tspan_phi,Angle_Correction_Phi(1:tstep,6),tspan_theta,Angle_Correction_Theta(1:tstep,6))
xlabel('Time (s)')
ylabel('Psi (rad)')
legend('\omega_1+\omega_2 Detumble','\omega_3 Reduction','\Phi Correction','\Theta Correction','\Psi Correction')
title('Satellite \Psi Control')

```



### 3D Plot

```
% Define angles over lifetime of satellite phi_life =
vertical(W1_W2_Detumble(1:tstep,4),W3_Detumble(1:tstep,4),Angle_Correction_Phi(1:tstep,4),Angle_Correction_Theta(1:tstep,4),Angle_Correction_Psi(1:tstep,4)); theta_life =
vertical(W1_W2_Detumble(1:tstep,5),W3_Detumble(1:tstep,5),Angle_Correction_Phi(1:tstep,5),Angle_Correction_Theta(1:tstep,5),Angle_Correction_Psi(1:tstep,5)); psi_life =
vertical(W1_W2_Detumble(1:tstep,6),W3_Detumble(1:tstep,6),Angle_Correction_Phi(1:tstep,6),Angle_Correction_Theta(1:tstep,6),Angle_Correction_Psi(1:tstep,6));
```

```
% Create the cylinder vertices r = 1; [x_cylinder,y_cylinder,z_cylinder] = cylinder(r,100); z_cylinder = z_cylinder*2;
```

```

figure; h = surf(x_cylinder, y_cylinder,z_cylinder, 'FaceColor', 'none', 'EdgeColor', 'b');

for i = 1:length(phi_life) % Compute the rotation matrix for the current time step R = euler2rotmat(phi_life(i), theta_life(i), psi_life(i));

    if i < tstep
        title('Controller Correction')
    end

    if i > tstep && i < (2*tstep)
        title('Spin Reduction')
    end

    if i > (2*tstep)
        title('Single Axis Rotations')
    end

    % Apply rotation around phi
    rotate(h, [1 0 0], rad2deg(phi_life(i)));

    % Apply rotation around theta
    rotate(h, [0 1 0], rad2deg(theta_life(i)));

    % Apply rotation around psi
    rotate(h, [0 0 1], rad2deg(psi_life(i)));

    pause(waitingperiod);
    M(i) = getframe(gcf);

end grid on; axis([-2 2 -2 2 -2 2]); xlabel('X-axis'); ylabel('Y-axis'); zlabel('Z-axis'); title('Satellite Orientation in 3D - Rotating Cylinder'); hold off

% Save video videoWriter = VideoWriter('SatelliteRotationAnimation.mp4', 'MPEG-4'); open(videoWriter); writeVideo(videoWriter, M); close(videoWriter);

```

## Determine Characteristics of Undamped System Initial Conditions

```

% State Space Model Undampened System
Am=[0,.25,.05;-.25,0,-.05;0,0,0];
Bm=[1/100,0,0;0,1/100,0;0,0,1/50];
Cm=[1,1,1];
Dm=[];

%Convert Matrices to Transfer Function
sys=ss(Am,Bm,Cm,Dm);
sys=tf(sys);

%Determine Natural Frequency of Undampened System
damp(sys(1));

```

Pole	Damping	Frequency (rad/seconds)	Time Constant (seconds)
0.00e+00 + 2.50e-01i	0.00e+00	2.50e-01	Inf
0.00e+00 - 2.50e-01i	0.00e+00	2.50e-01	Inf

## Controller 1

```

%W1 and W2 Reduction Controller
function state_array1 = controller1(t,state)

%Define Variables in terms of initial conditions
W1 = state(1);
W2 = state(2);
W3 = state(3);
phi = state(4);
theta = state(5);
psi = state(6);

%define Moments of Inertia
I11 = 100;
I22 = 100;
I33 = 50;

%Define Desired Pole Locations for Controller
zeta_wn = 4/25;
wn=.25;
zeta = zeta_wn/wn;
pd_neg = -zeta_wn - wn*sqrt(1-zeta^2);
p = [pd_neg, pd_neg,0];

%State Space Model Using Euler's Moment
A =[0,(I22-I33)*W3/(2*I11),(I22-I33)*W2/(2*I11);(I33-I11)*W3/(2*I22),0,(I33-I11)*W1/(2*I22);(I11-I22)*W2/(2*I33),(I11-I22)*W1/(2*I33),0];
B = [1/100,0,0,0,1/100,0;0,0,1/50];
x = [W1 W2 W3]';

%Determine Gain Value Necesarry for Control

```

```

K = place(A,B,p);
%Define U Matrix with Determined Gains
u = [-K(1,1)*W1 ; -K(2,2)*W2;0*W3];

%Define Angle Relationships
phi_dot=(cos(psi)*W2+sin(psi)*W1)/sin(theta);
theta_dot=(cos(psi)*W1-sin(psi)*W2);
psi_dot=W3-((cos(psi)*W2+sin(psi)*W1)*cos(theta))/sin(theta);

%Define Output of State Space Function
xdot = A*x + B*u;
%Defining Output for ODE 45 in terms of W1 W2 W3 Phi Theta Psi
state_array1 = [xdot; phi_dot;theta_dot;psi_dot];

```

## **Controller 2**

---

```

%Define Function for W3 Control
function state_array2 = detumble(t,state) % Drives Transverse Angular Velocities to 0

%Define Variables Based on Initial Conditions
W1 = state(1);
W2 = state(2);
W3 = state(3);
phi = state(4);
theta = state(5);
psi = state(6);

%Define Moments of Inertia
I11 = 100;
I22 = 100;
I33 = 50;

%Define Desired Pole Locations for Controller
zeta_wn = 4/25;
wn=.25;
zeta = zeta_wn/wn;
pd = -zeta_wn - wn*sqrt(1-zeta^2);
p = [0,0,pd];

%State Space Model Using Euler's Moment Equation
A=[0,(I22-I33)*W3/(2*I11),(I22-I33)*W2/(2*I11);(I33-I11)*W3/(2*I22),0,(I33-I11)*W1/(2*I22);(I11-I22)*W2/(2*I33),(I11-I22)*W1/(2*I33),0];
B = [1/100,0,0,0,1/100,0,0,0,1/50];
x = [W1 W2 W3]';

%Determine Gain Value Necesarry for Control
K = place(A,B,p);
%Define U Matrix with Determined Gains
u = [-0*W1 ; -0*W2;-K(3,3)*W3];

%Define Angle relationships
phi_dot=(cos(psi)*W2+sin(psi)*W1)/sin(theta);
theta_dot=(cos(psi)*W1-sin(psi)*W2);
psi_dot=W3-((cos(psi)*W2+sin(psi)*W1)*cos(theta))/sin(theta);

%Define Ouptut of State Space Function
xdot = A*x + B*u;
%Defining Output for ODE 45 in terms of W1 W2 W3 Phi Theta Psi
state_array2 = [xdot;phi_dot;theta_dot;psi_dot];
end

```

### Controller 3

```
%Define Function for Phi Correction
function state_array_phi=angle_phi(t,state)

%Define Variables Based on Initial Conditions
W1 = state(1);
W2 = state(2);
W3 = state(3);
phi = state(4);
theta = state(5);
psi = state(6);

%Define Moments of Inertia
I11=100;
I22=100;
I33=50;

%Define Desired Angles
desired_phi = 0;

%Define Angle Differences and Gain Value
K = .8;
phi_error = desired_phi-phi;

%Define State Space model using Euler's Equation
A=[0,(I22-I33)*W3/(2*I11),(I22-I33)*W2/(2*I11);(I33-I11)*W3/(2*I22),0,(I33-I11)*W1/(2*I22);(I11-I22)*W2/(2*I33),(I11-I22)*W1/(2*I33),0];
```

```

B = [1/100,0,0;0,1/100,0;0,0,1/50];
u=[-K*W3;-K*W2;-K*W1];
x = [W1 W2 W3]';

%Define Output of State Space Function
xdot=A*x+B*u;

%Define Angle Relationships
phi_dot=(cos(psi)*W2+sin(psi)*W1)/sin(theta);
theta_dot=(cos(psi)*W1-sin(psi)*W2);
psi_dot=W3-((cos(psi)+sin(psi)*W1)*cos(theta))/sin(theta))*W2;

%Define Angle Change Between Steps
phi_dot = psi_dot+phi_error;

%Defining Output for ODE 45 in terms of W1 W2 W3 Phi Theta Psi
state_array_phi = [xdot;phi_dot;theta_dot;psi_dot];

end

%Define Function for Theta Correction
function state_array_theta=angle_theta(t,state)

%Define Variables Based on Initial Conditions
W1 = state(1);
W2 = state(2);
W3 = state(3);
phi = state(4);
theta = state(5);
psi = state(6);

%Define Moments of Inertia
I11=100;
I22=100;
I33=50;

%Define Desired Angles
desired_theta = pi/2;

%Define Angle Differences and Gain Value
K = .8;
theta_error = desired_theta-theta;

%Define State Space model using Euler's Equation
A =[0,(I22-I33)*W3/(2*I11),(I22-I33)*W2/(2*I11);(I33-I11)*W3/(2*I22),0,(I33-I11)*W1/(2*I22);(I11-I22)*W2/(2*I33),(I11-I22)*W1/(2*I33),0];
B = [1/100,0,0;0,1/100,0;0,0,1/50];
u=[-K*W1;-K*W2;-K*W3];
x = [W1 W2 W3]';

%Define Output of State Space Function
xdot=A*x+B*u;

%Define Angular Acceleration Values
phi_dot=(cos(psi)*W2+sin(psi)*W1)/sin(theta);
theta_dot=(cos(psi)*W1-sin(psi)*W2);
psi_dot=W3-((cos(psi)*W2+sin(psi)*W1)*cos(theta))/sin(theta);

%Define Angle Change Between Steps
theta_dot = phi_dot+theta_error;

%Defining Output for ODE 45 in terms of W1 W2 W3 Phi Theta Psi
state_array_theta = [xdot;phi_dot;theta_dot;psi_dot];

end

%Define Function for Psi Correction
function state_array_psi=angle_psi(t,state)

%Define Variables Based on Initial Conditions
W1 = state(1);
W2 = state(2);
W3 = state(3);
phi = state(4);
theta = state(5);
psi = state(6);

%Define Moments of Inertia
I11=100;
I22=100;
I33=50;

%Define Desired Angles
desired_psi=psi-(pi/(2*pi),1);

%Define Angle Differences and Gain Value
K = 10;
psi_error =desired_psi-ps;

%Define State Space model using Euler's Equation
A =[0,(I22-I33)*W3/(2*I11),(I22-I33)*W2/(2*I11);(I33-I11)*W3/(2*I22),0,(I33-I11)*W1/(2*I22);(I11-I22)*W2/(2*I33),(I11-I22)*W1/(2*I33),0];
x = [W1 W2 W3]';

```

```

B = [1/100,0,0;0,1/100,0;0,0,1/50];
u=[-K*W1;-K*W2;-K*W3];

%Define Output of State Space Function
xdot=A*x+B*u;

%Define Angular Acceleration Values
phi_dot=(cos(psi)*W2+sin(psi)*W1)/sin(theta);
theta_dot=(cos(psi)*W1-sin(psi)*W2);
psi_dot=W3-((cos(psi)*W2+sin(psi)*W1)*cos(theta))/sin(theta);

%Define Angle Change Between Steps
psi_dot = psi_dot+psi_error;

%Defining Output for ODE 45 in terms of W1 W2 W3 Phi Theta Psi
state_array_psi = [xdot;phi_dot;theta_dot;psi_dot];

end

% function R = euler2rotmat(phi, theta, psi)
%     R_phi = [1 0 0; 0 cos(phi) -sin(phi); 0 sin(phi) cos(phi)];
%     R_theta = [cos(theta) 0 sin(theta); 0 1 0; -sin(theta) 0 cos(theta)];
%     R_psi = [cos(psi) -sin(psi) 0; sin(psi) cos(psi) 0; 0 0 1];
%     R = R_phi * R_theta * R_psi;
% end

```

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