

Analysis of Algorithms - Assignment 6

Colby Rush

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1 Section 6.4

1.1 No. 2

1. For $i = 1, 2, \dots, n/2$, check $A(i) \geq \max(A(2i), A(2i + 1))$. If not true, it's not a heap. Since the algorithm makes $2(n/2)$ compares, it's efficiency is in $O(n)$.

1.2 No. 7

1. No

2 Section 6.5

2.1 No. 4

1. See attached paper

2.2 No. 7

1. See attached paper

2.3 No. 8

1. See attached paper

3 RSA Encryption

See paper

4 Section 8.1

4.1 No. 2

1. See figure 8.1 in the book

4.2 No. 12

1. We set the probability of A winning a series to $P(a,b)$, where a is how many more games A needs and b how many more games B needs. If A wins (probability p), they need $a-1$ more wins while B still needs b wins. If A loses (probability $q = 1 - p$), A still needs a wins and B needs $b - 1$ wins. This leads to recurrence
$$P(a,b) = pP(a - 1, b) + qP(a, b - 1) \text{ for } a, b > 0$$
with initial condition
$$P(0,b) = 1 \text{ for } b > 0 \text{ and } P(a,0) = 0 \text{ for } a > 0.$$
2. See attached paper