

I claim that we need to show that there is a process P and we need two distinct processes $A1$ which is not equal to $A2$ such that $P \rightarrow A1$ and $P \rightarrow A2$, and the relation is non-deterministic

Construction:

We define symbols:

0 (inaction)

$\bar{x}b \langle \text{yarrow} \rangle . P$ as the output tuple yarrow on channel x , which then continues as P

$x(z\text{arrow}).P$ as the input tuple on channel x , which binds to $z\text{arrow}$, then continues as P)

$P \mid A$ as the parallel composition

$\nu x.P$ (name restriction)

$!P$ (replication)

\sim is silent action

$P \sim \rightarrow P'$ is a transition

Proof:

We let $P = \bar{a}b \langle \text{b} \rangle . 0 \mid a(x).0 \mid a(x).0$

This means that one output on a sends a name b . We have two input processes both waiting to receive some name on channel a .

Let $R1 =$ the first $a(x).0$ and $R2 =$ the second $a(x).0$

We have $\bar{P} = \bar{a}b \langle \text{b} \rangle . 0 \mid R1 \mid R2$

Note that we need to use the communication rule of pi-calculus.

Now, Reduction 1:

As sender communicates with $R1$

$P \sim \rightarrow 0 \mid 0 \mid R2 \equiv Q1$

Reduction 2:

Sender communicates with $R2$

$P \sim \rightarrow 0 \mid R1 \mid 0 \equiv Q2$

$Q1 \neq Q2$, this proves that the same process has atleast two distinct transitions.

This holds for the definition of nondeterminism, so the polyadic pi calculus is non-deterministic.