

# Mini-rotations - Trophic overyielding and infection dynamics

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2024-04-04

Working through ideas for the mini-rotations project

## Table of contents

<b>1</b>	<b>Background</b>	<b>1</b>
<b>2</b>	<b>Methods</b>	<b>1</b>
<b>3</b>	<b>References</b>	<b>2</b>

## 1 Background

Previous work has shown that the coexistence of a pair or mixture of species can reach higher abundance than the species with the highest carrying capacity (Loreau 2004; Poisot *et al.* 2013). This idea of “transgressive overyielding” is the basis for much work on biodiversity-ecosystem functioning relationships (BEF) (i.e., Schmid *et al.* 2008). Some research has suggested approaches to linking this concept to disease dynamics (Johnson *et al.* 2015), however, few studies have explicitly developed theory to this effect. Notably

## 2 Methods

We start from the assumption of two species competing, in a Lotka-Volterra model. We use the form of Abrams (2022, pg. 39), which includes terms for both inter- and intra-specific competition. We then have

$$\frac{dN_1}{dt} = N_1(r_1 - \alpha_{11}N_1 - \alpha_{12}N_2) \quad (1)$$

$$\frac{dN_2}{dt} = N_2(r_2 - \alpha_{21}N_1 - \alpha_{22}N_2) \quad (2)$$

The relation to the original generalized Lotka-Volterra model (as pointed out by Abrams 2022) is that  $\alpha_{ii} = \frac{1}{K_i}$  and  $\alpha_{ij} = \frac{\alpha_{ij}}{K_i}$ .

Model Parameters	
Term	Description
$N_i$	Abundance of species $i$
$r_i$	Growth rate of species $i$
$\alpha_{ii}$	Intraspecific competition within species $i$
$\alpha_{ij}$	Interspecific competition between species $i$ and $j$

Table 1: Parameter values for our model systems

Since we are also ultimately interested in the dynamics when one of these competing species is infected with some type of pathogen, we can additionally consider species 1 as being infected with a generalized pathogen.

### 3 References

Source: [Article Notebook](#)

- Abrams, P.A. (2022). *Competition theory in ecology*. Oxford University Press.
- Johnson, P.T.J., Ostfeld, R.S. & Keesing, F. (2015). [Frontiers in research on biodiversity and disease](#). *Ecology Letters*, 18, 1119–1133.
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