

Observational Asteroseismology

From data to science

Cole Johnston

06/07/2023

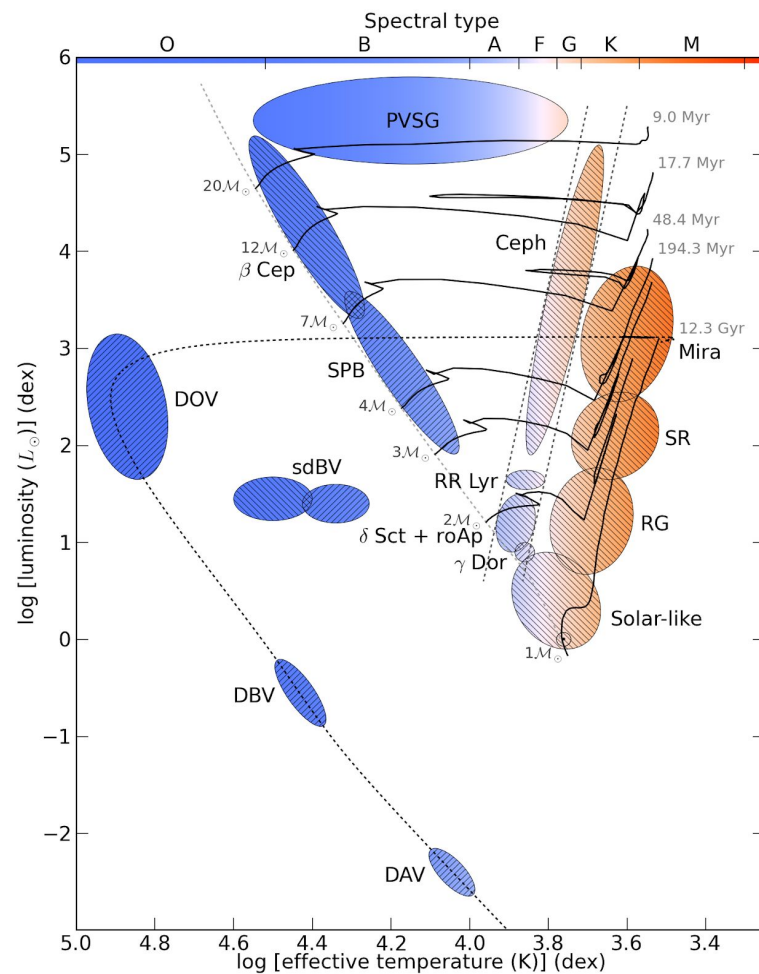
Asteroseismology



Image credit: atesevich/DepositPhotos

Asteroseismology

Stars pulsate at every corner of the HRD!



How do we go from data to science

Pulsation frequencies are the fundamental data of asteroseismology

$$\xi(r, \theta, \phi, t) = [(\xi_{r,n,\ell} \hat{e}_r + \xi_{h,n,\ell} \nabla_h) Y_\ell^m(\theta, \phi)] \exp(-i\omega t)$$

We need to identify (n, l, m)

How do we go from time-series observations to modelling?

Time-space \rightarrow Frequency space

How do we go from data to science

Pulsation frequencies are the fundamental data of asteroseismology

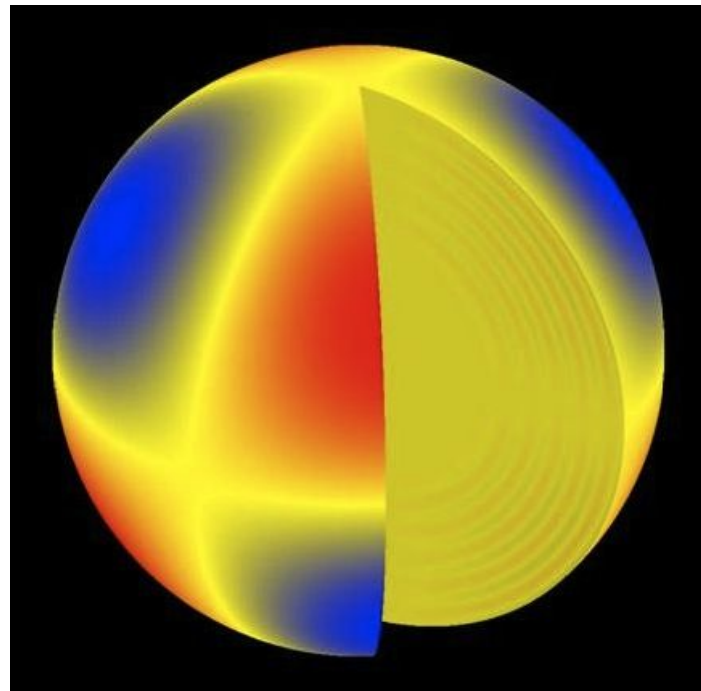
We need to identify (n, l, m)

What are (n, l, m) ?

$n \rightarrow$ number of radial nodes

$l \rightarrow$ number of surface nodal lines

$m \rightarrow$ number of longitudinal surface nodal lines



How do we go from data to science

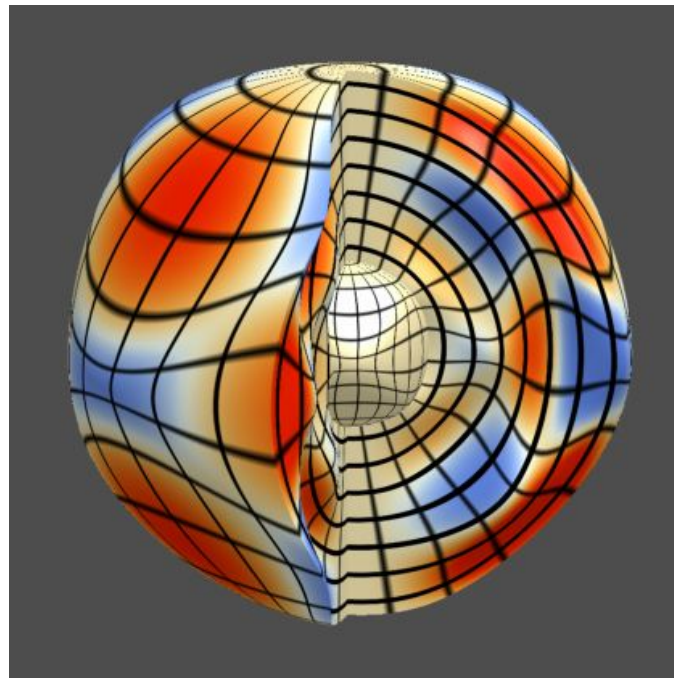
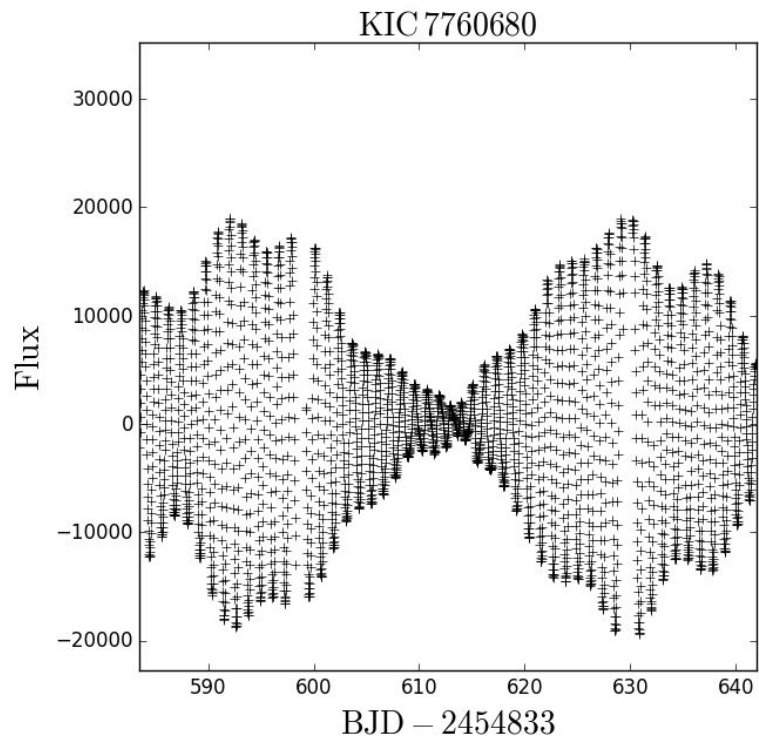
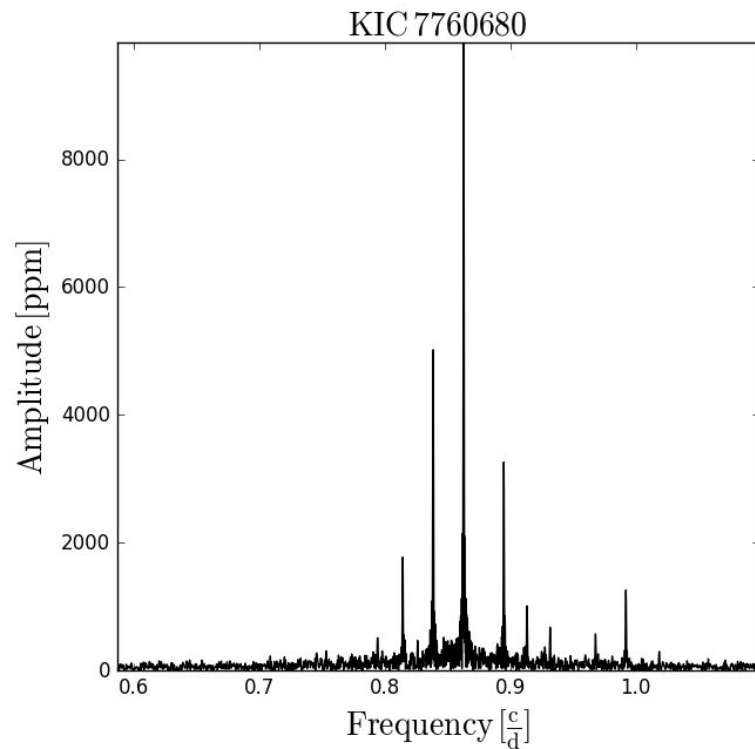
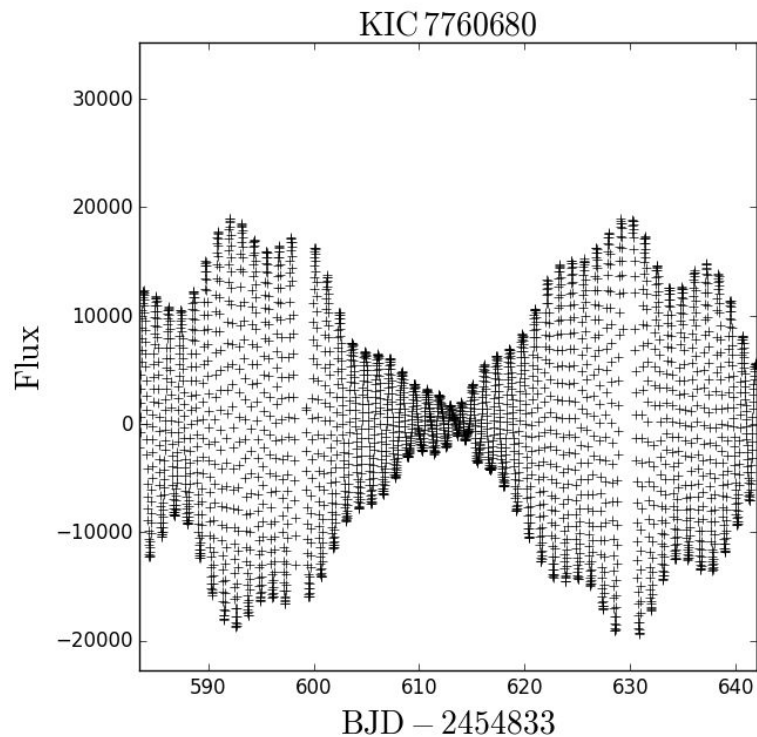


Image Credit: Rich Townsend

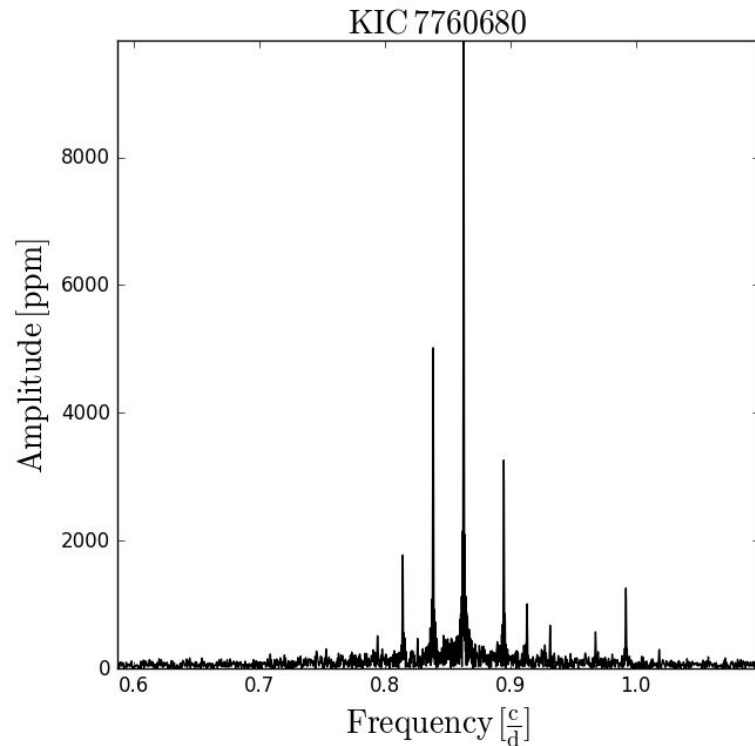
How do we go from data to science



How do we go from data to science

What does a periodogram do:

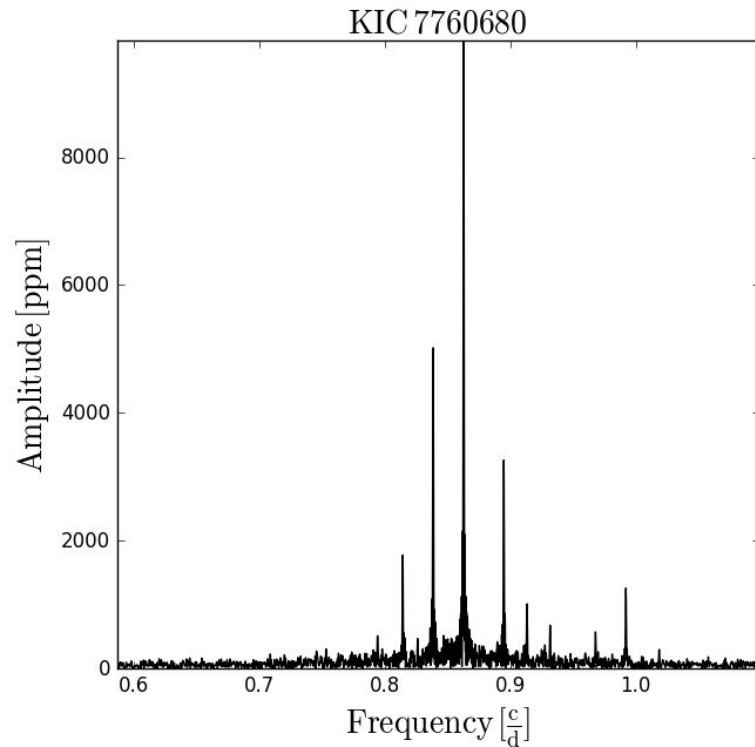
- Picks a range of frequencies
- Make a sine-wave for each frequency
- If the sine-wave matches the data, it has a high amplitude at that frequency



How do we go from data to science

Periodogram options:

- Period04
- Lightkurve
- pythia
- astropy
- numpy
- etc.



Data Considerations

Things to consider:

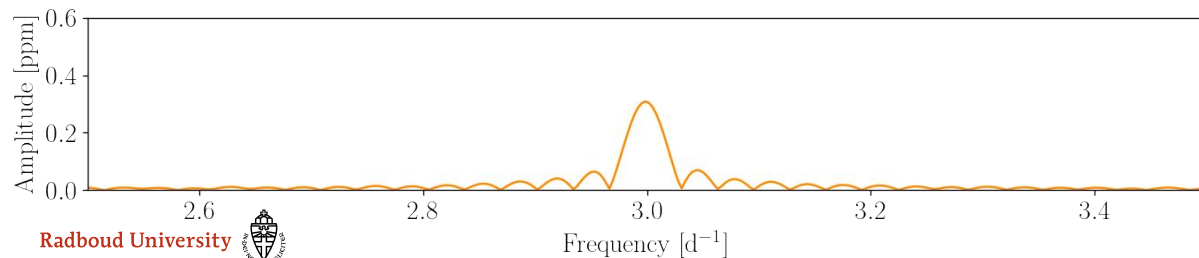
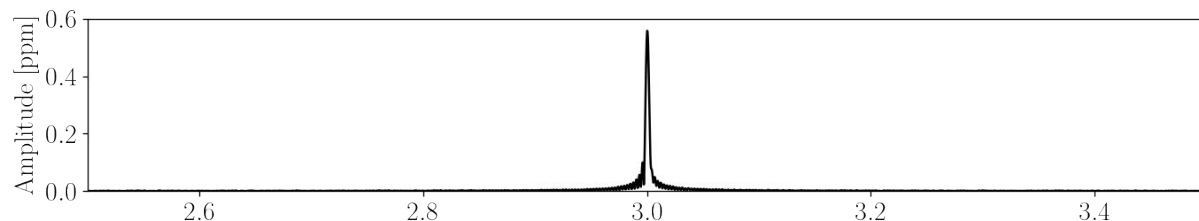
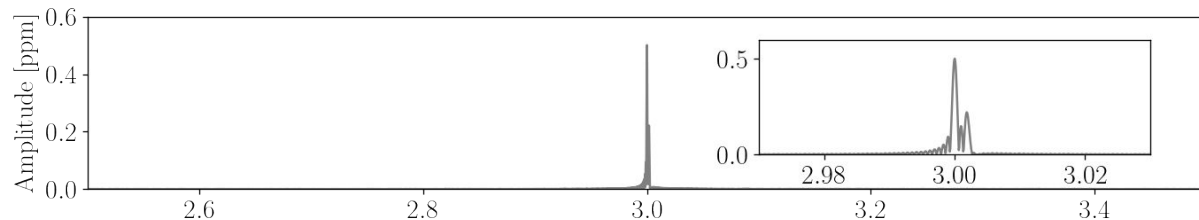
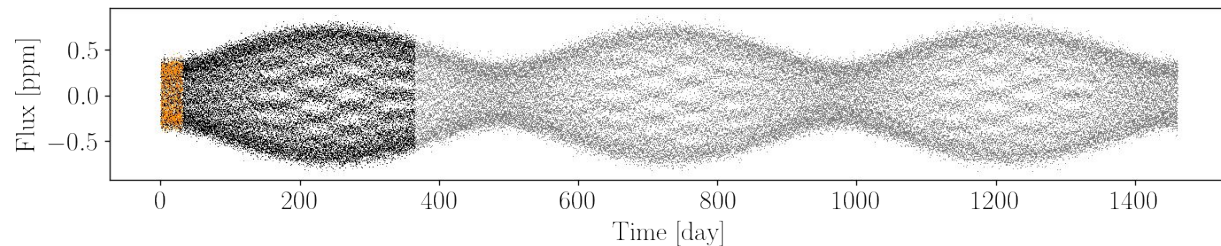
- Time-span
- Integration time
- Cadence
- Duty-cycle
- Number of data points
- Sources of noise

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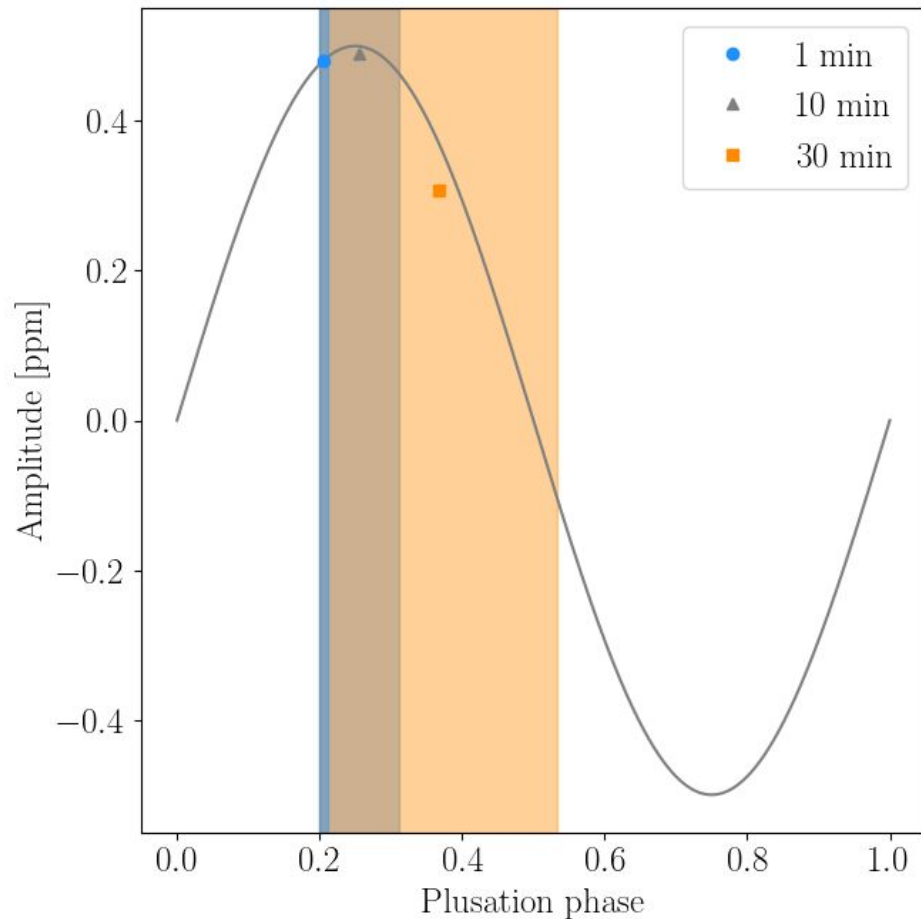
$$\Delta f = \frac{1}{\max(t) - \min(t)}$$



Data Considerations

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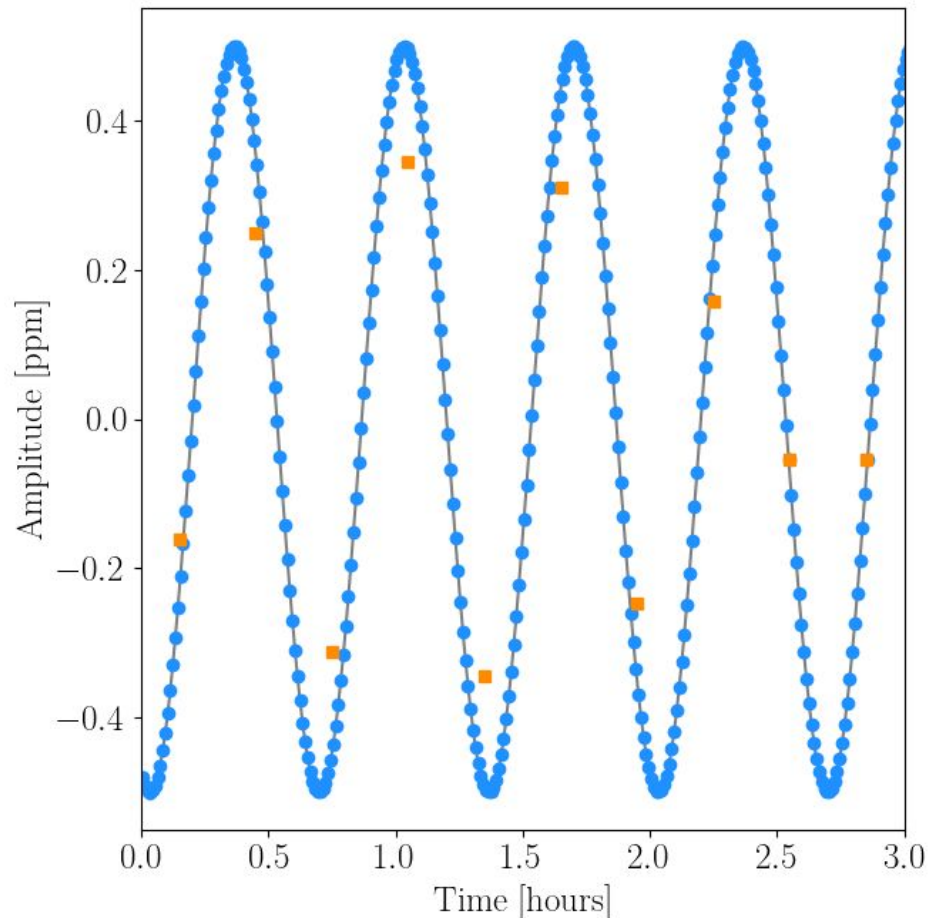
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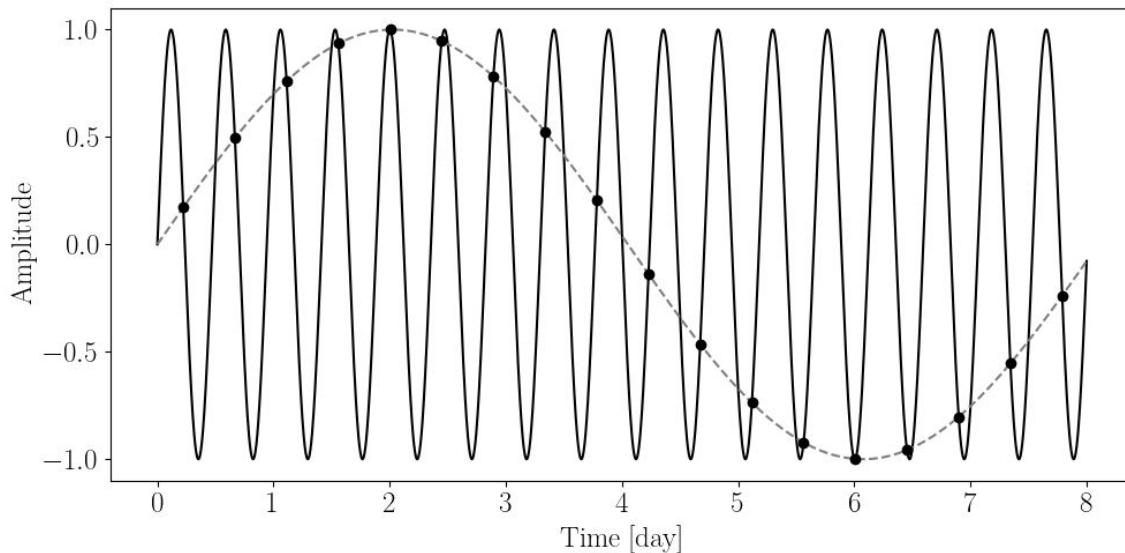
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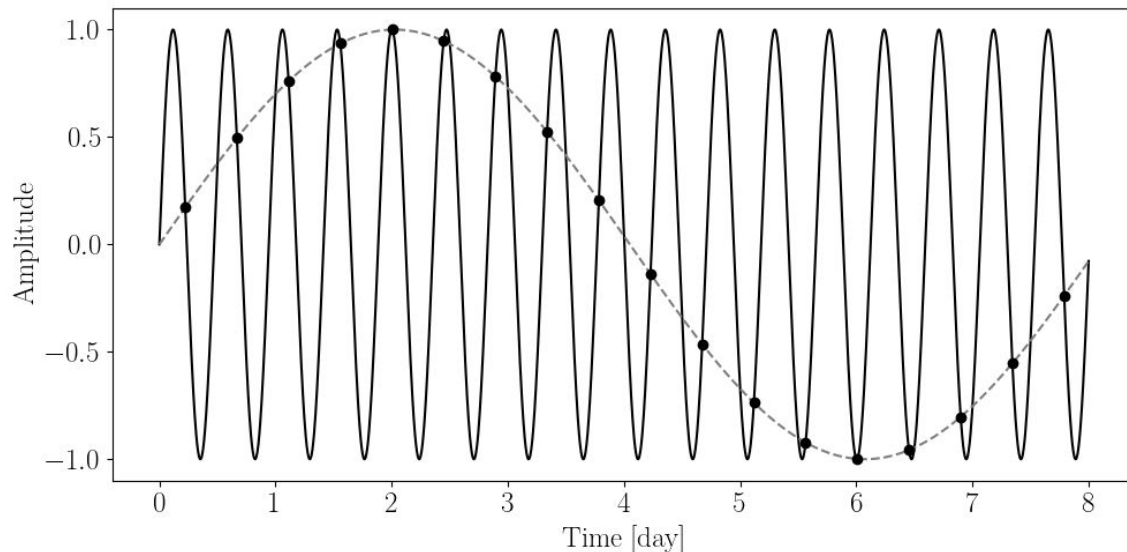


$$f_{\text{nyq}} = \frac{1}{2\Delta t}$$

Data Considerations

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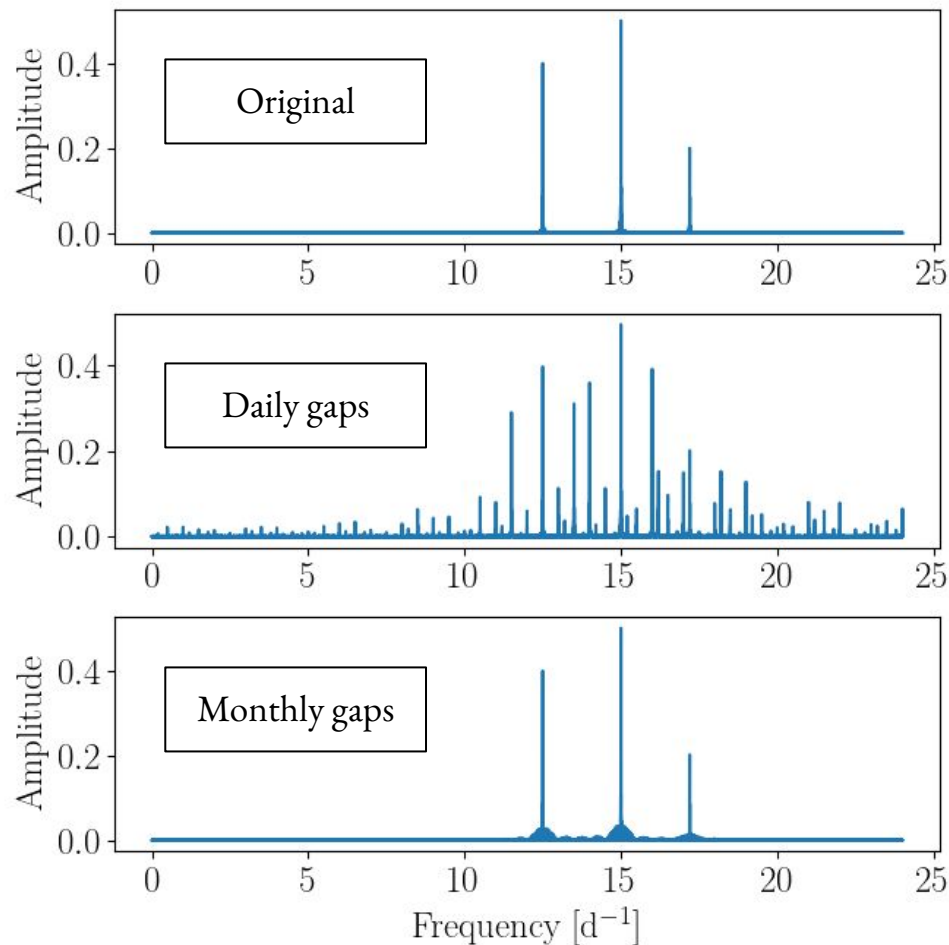
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** Does not strictly apply to un-evenly sampled data**

Data Considerations

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$$\sigma_\nu = \frac{\sqrt{6} \sigma_N}{\pi \sqrt{N} A T}, \quad \sigma_A = \sqrt{\frac{2}{N}} \sigma_N$$

$$\sigma_\delta = \frac{\sigma_N}{\pi \sqrt{2N} A}$$

Data Considerations

Things to consider:

- Time-span
- Integration time
- Cadence
- Duty-cycle
- Number of data points
- Sources of noise

Ground based

- Clouds
- Atmosphere
- Air-mass
- CCD sensitivity
- Non-linearity
- Thermal issues
- Trailing issues

Space based

- Scattered light
- Pointing loss
- Thermal issues
- CCD sensitivity
- Jitter
- Correlated noise

- Crowding
- Third light
- Background subtraction

How do we go from data to science

Pulsation frequencies are the fundamental data of asteroseismology

How do we go from observations to modelling?

- Photometry
- Spectroscopy

How do we go from data to science

Pulsation frequencies are the fundamental data of asteroseismology

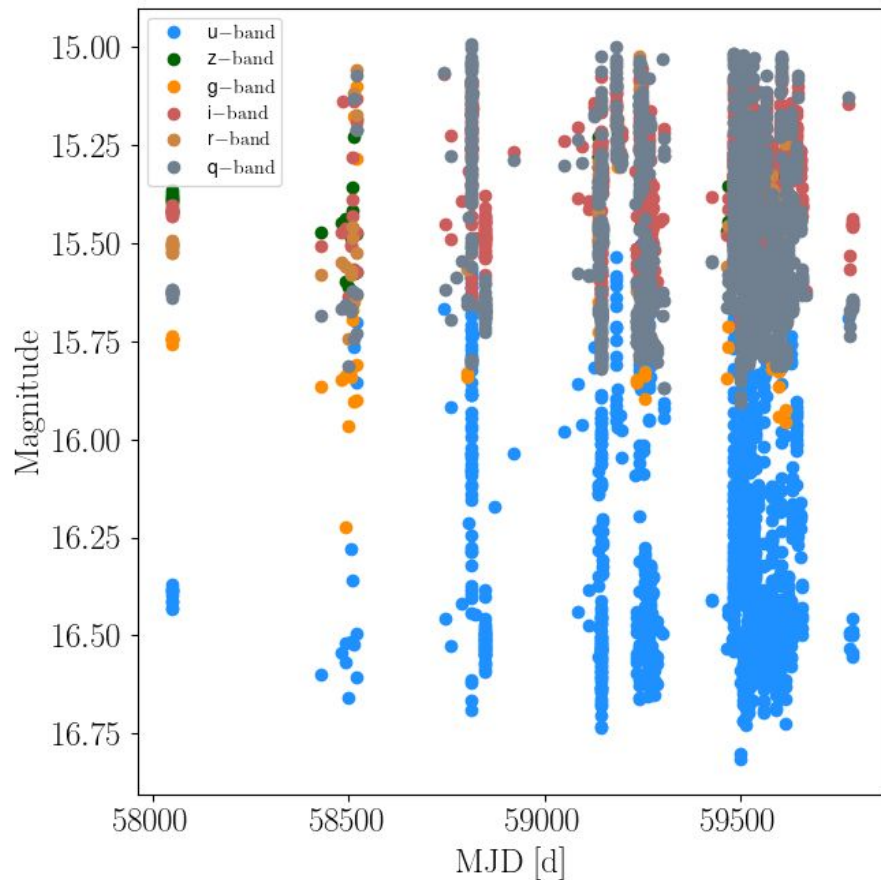
How do we go from observations to modelling?

- **Photometry**
- Spectroscopy

How do we go from data to science

What do we need to consider?

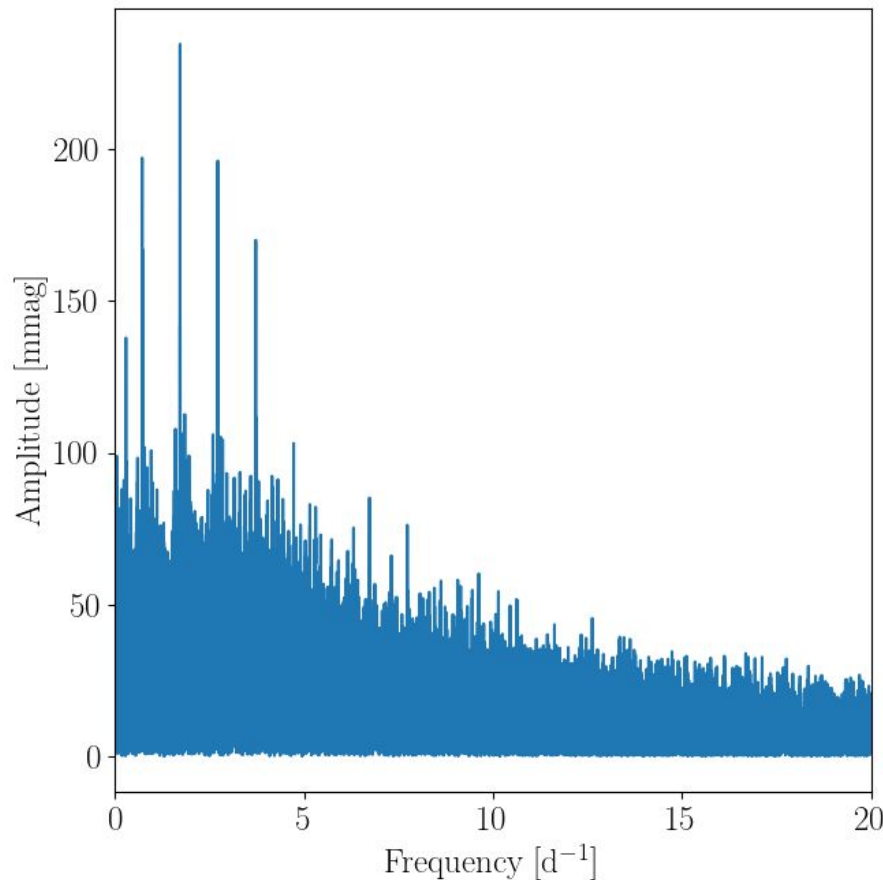
- 6 filters (technically)
- 60 sec exposures
- u has 1419 data points
- i has 1405 data points
- q has 1677 data points
- g,r,z have 99 data points each
- Time-base = 1737.11 days
- $df = 0.0006$ c/d
- Very, very irregular sampling



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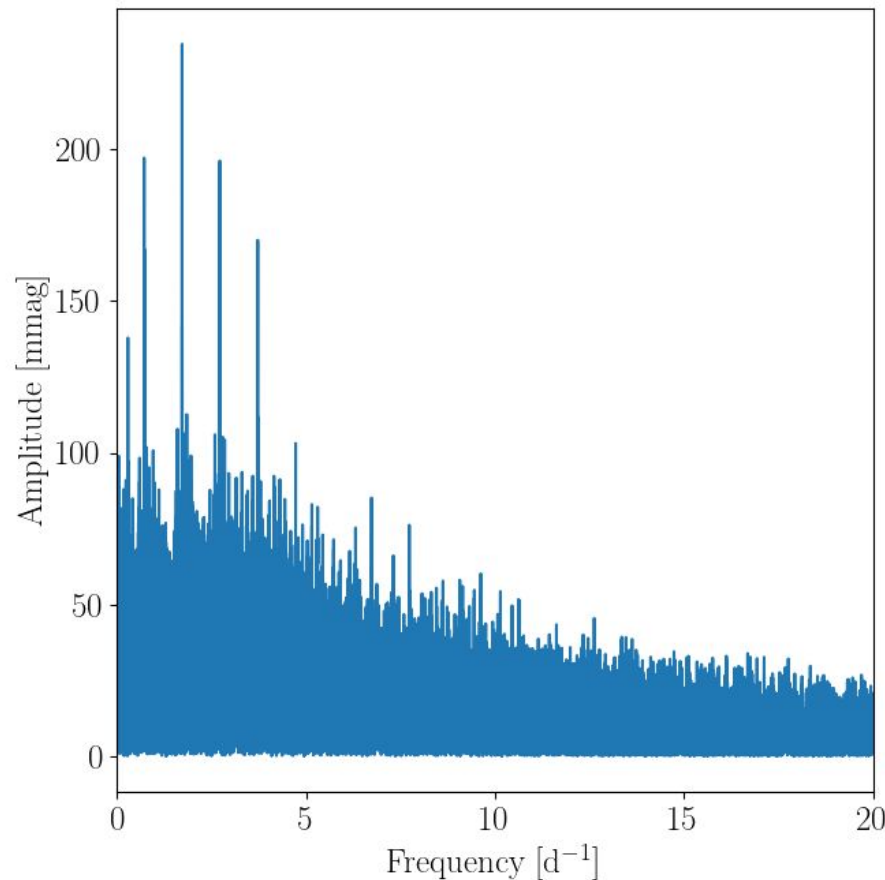


How do we go from data to science

Are there 8 independent frequencies?

$$F_N(\nu) = (F * W_N)(\nu) \longrightarrow$$

$$\left| W_N \left(\nu + \frac{n}{\Delta t} \right) \right| = |W_N(\nu)|$$

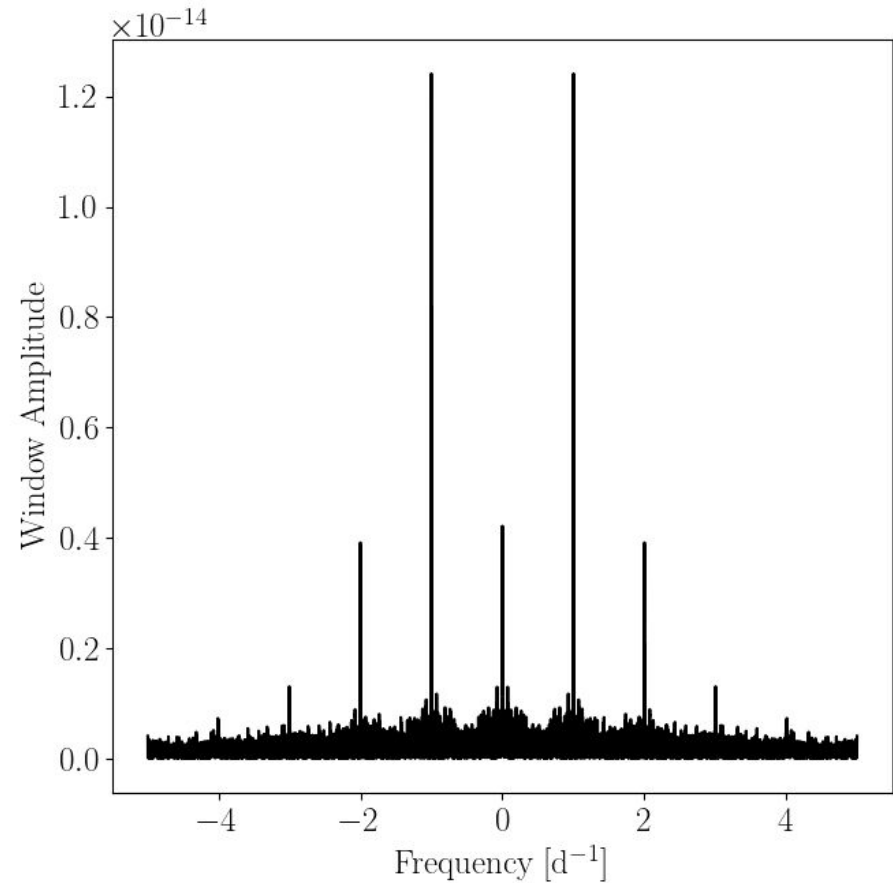


How do we go from data to science

Check the window function!!

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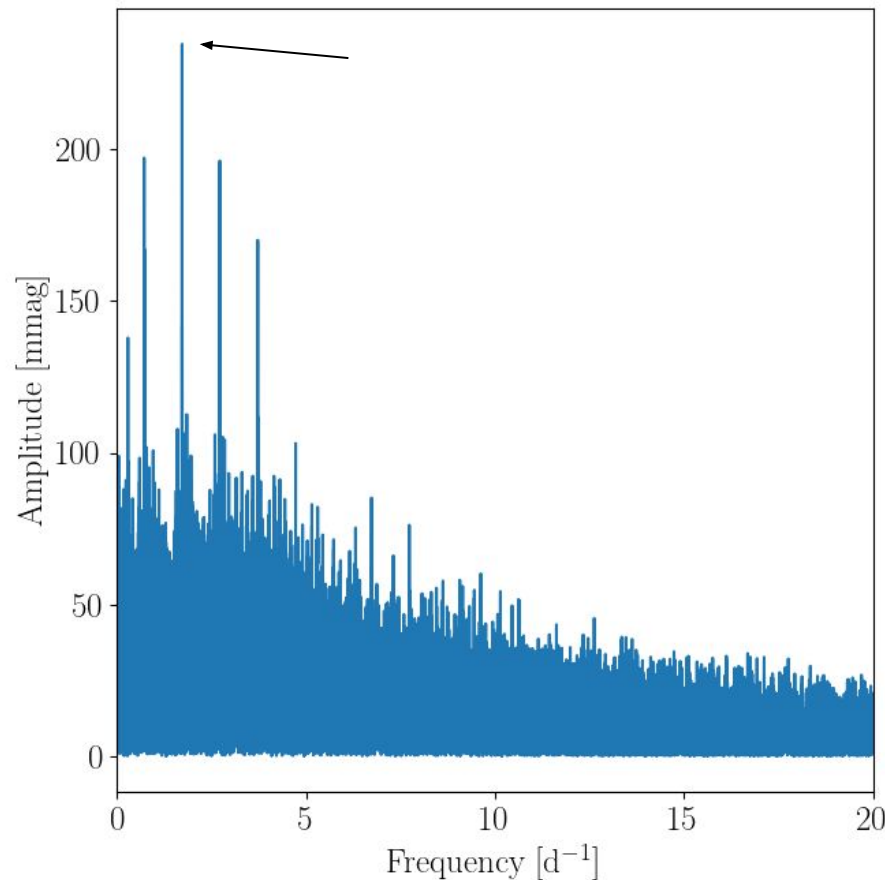
How do we go from data to science

Pick the highest amplitude signal

Phase fold:
 $((t-t_0)/P_{\text{orb}}) \bmod 1$

Frequency: 1.717794 c/d

Period: 0.582142 d



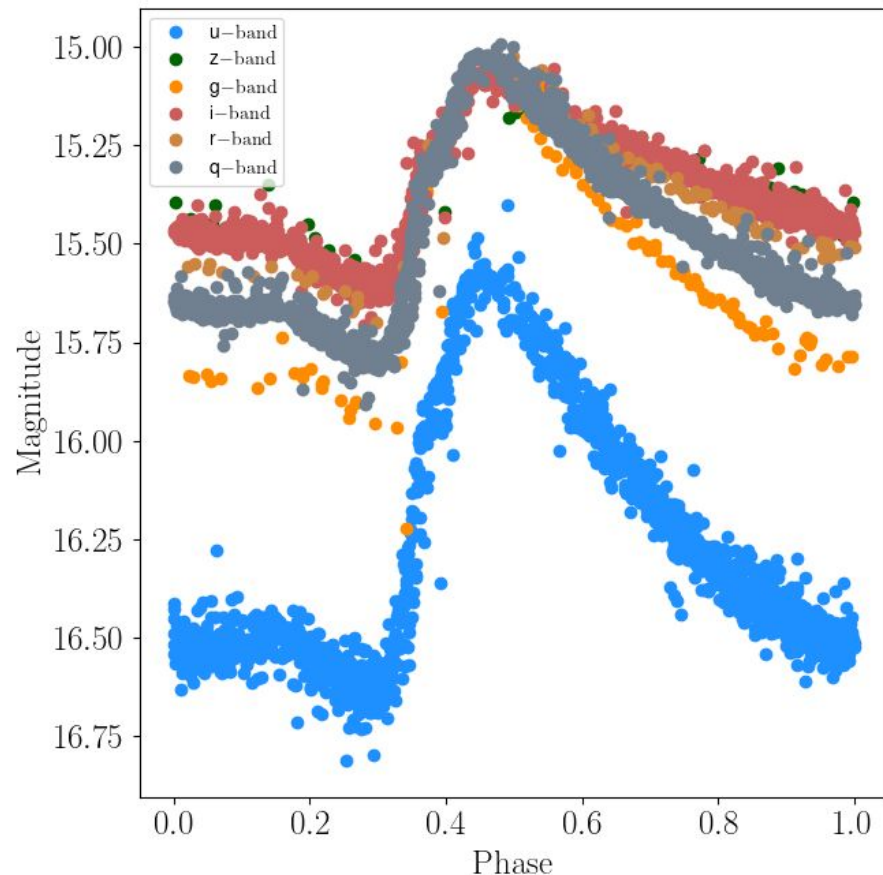
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How do we go from data to science

Let's look from space

KIC 9751996

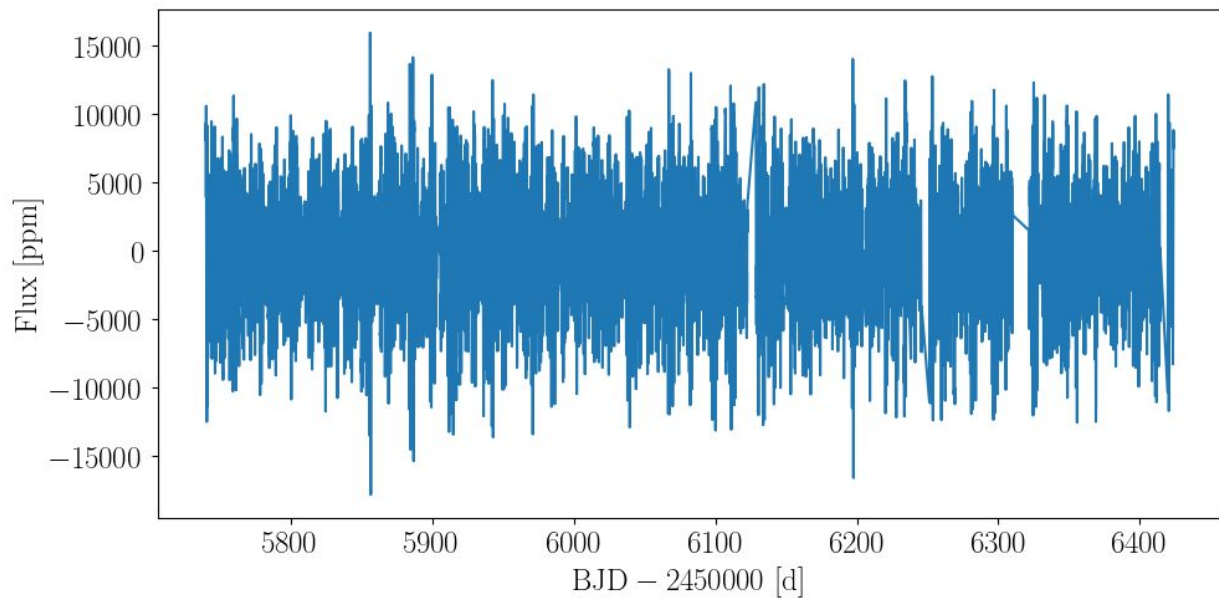
γ Doradus pulsator

$$\Delta T = 684.16 \text{ d}$$

$$\delta f = 0.0015$$

$$\delta t = 29.4 \text{ min}$$

$$f_{\text{nyq}} = 24 \text{ d}^{-1}$$



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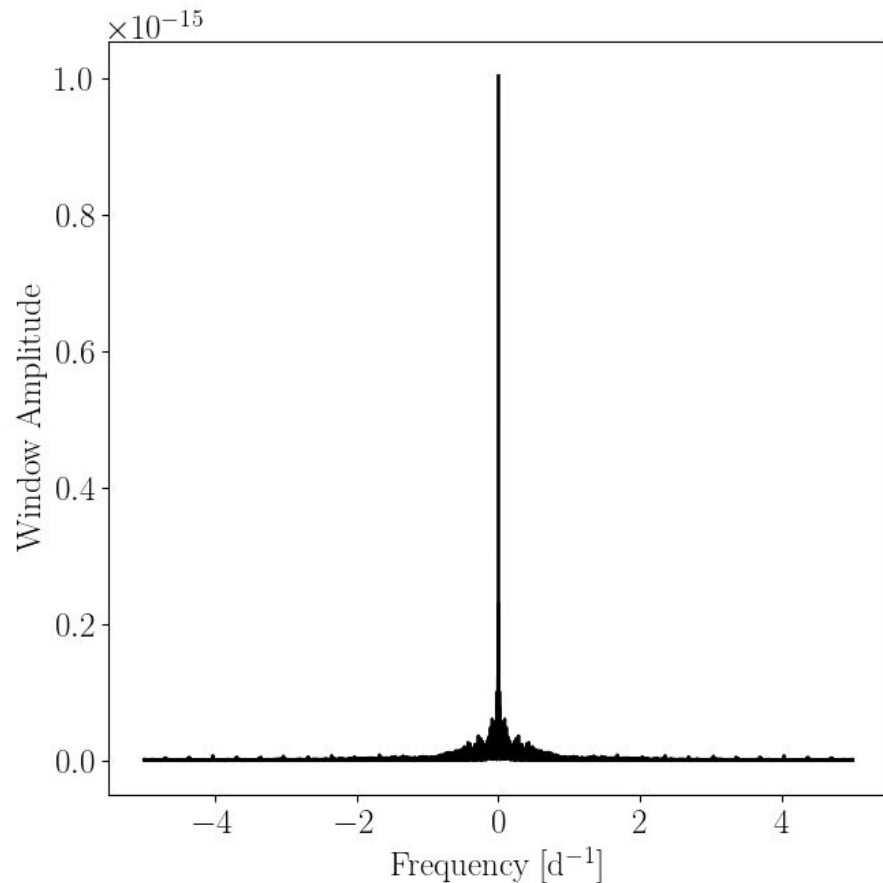
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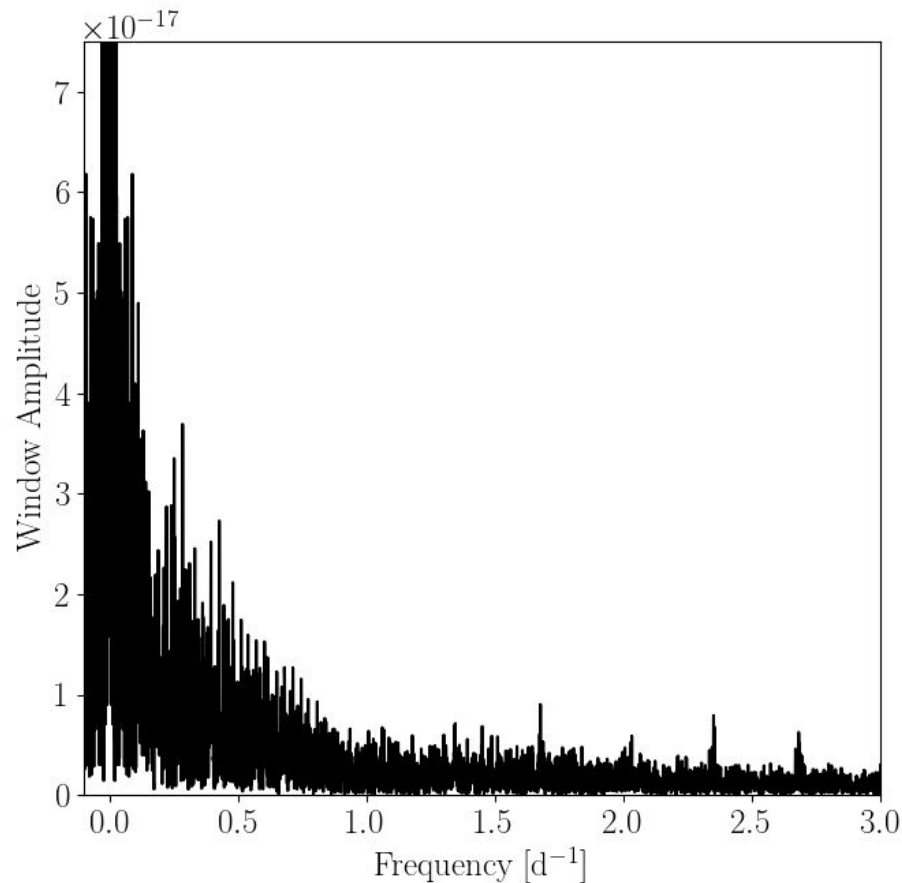
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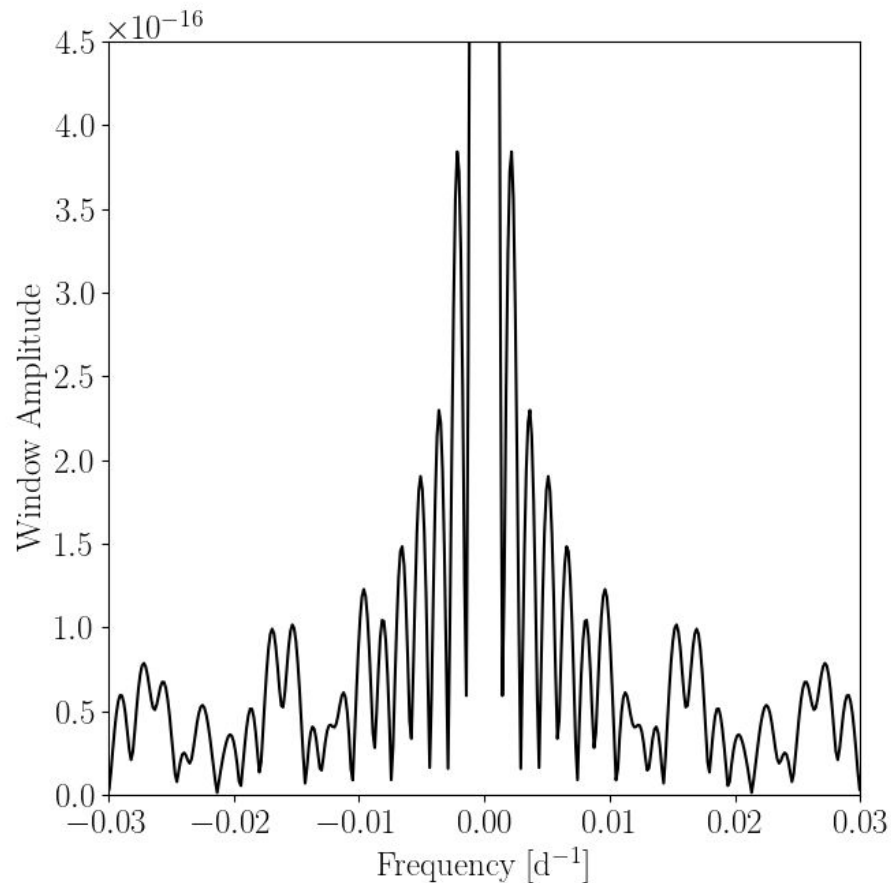
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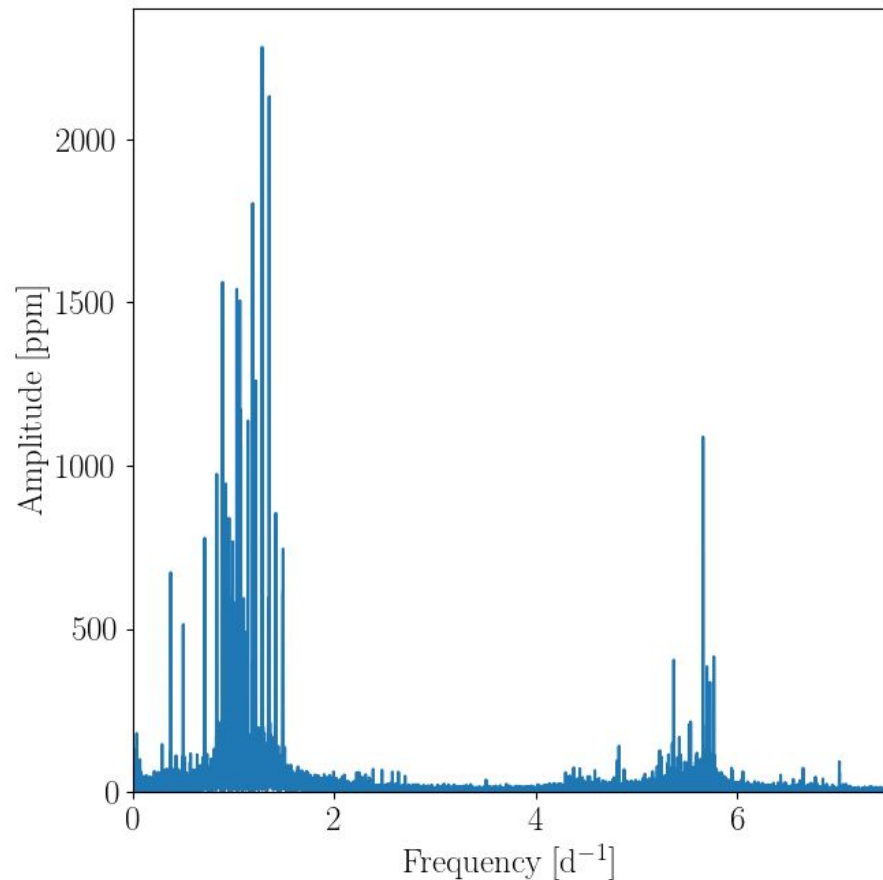
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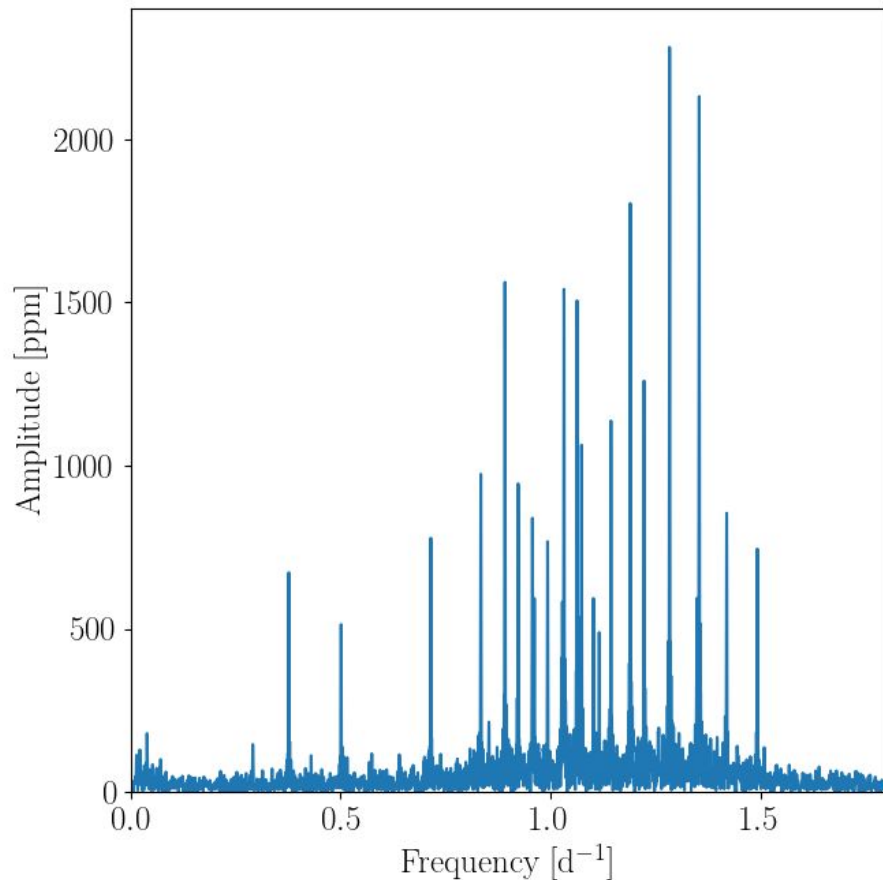
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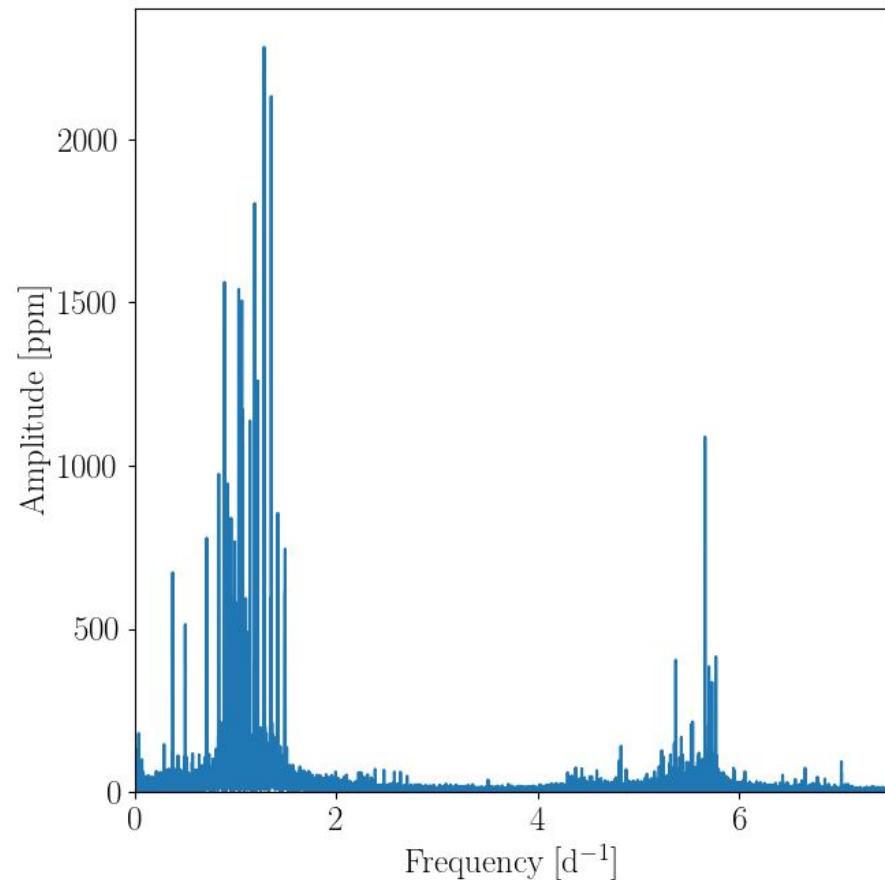
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Iterative pre-whitening

You want to extract all **significant** pulsation frequencies.

How do you go about doing this?

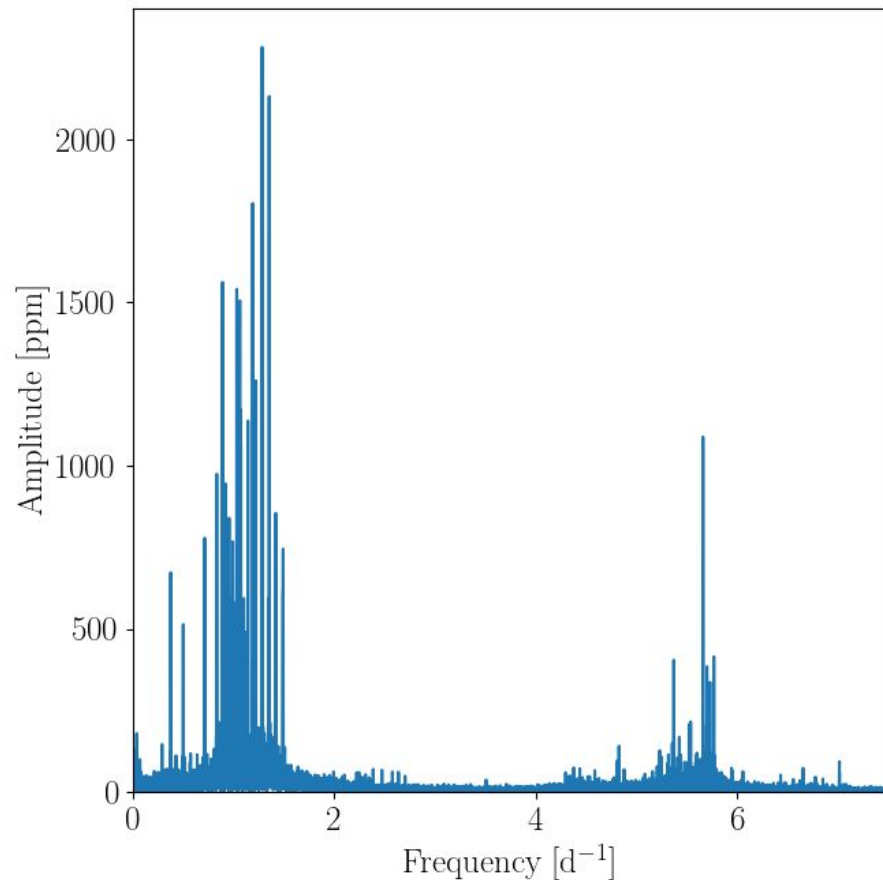


Iterative pre-whitening

Consider a time series as:

$$F(t_i) = C + \sum_j^N A_j \sin(2\pi f_j t_i + \phi_j)$$

- Pick a frequency
- Fit a sinusoid with amplitude A , frequency f , and phase ϕ
- Subtract sinusoid
- Repeat until stopping criterion

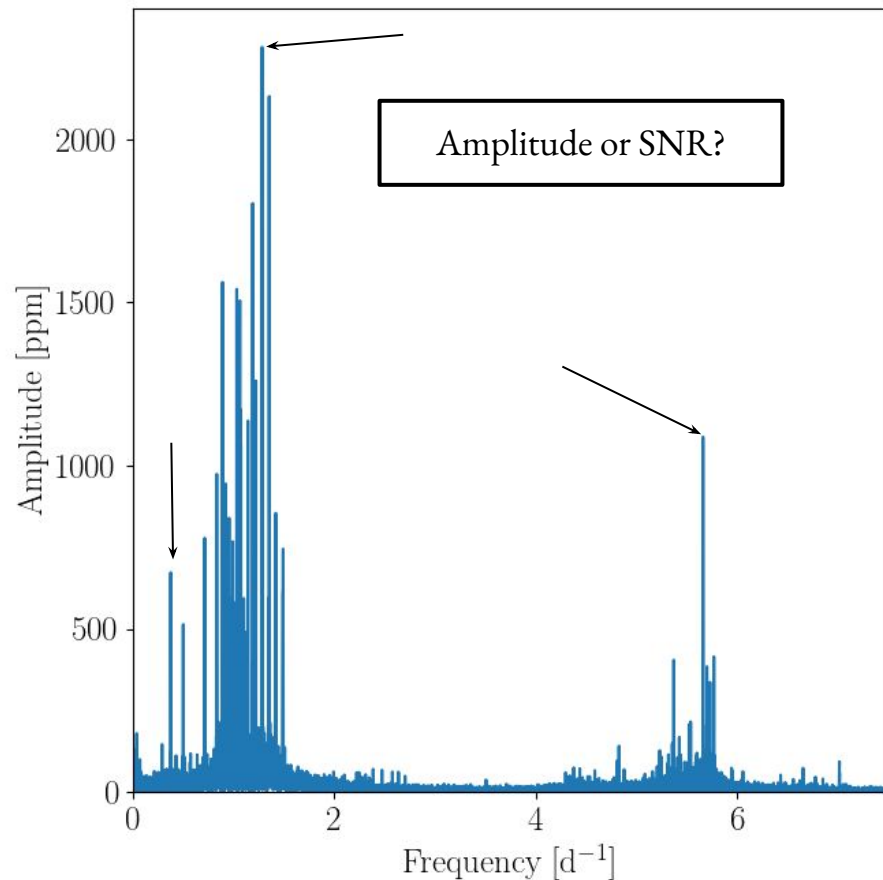


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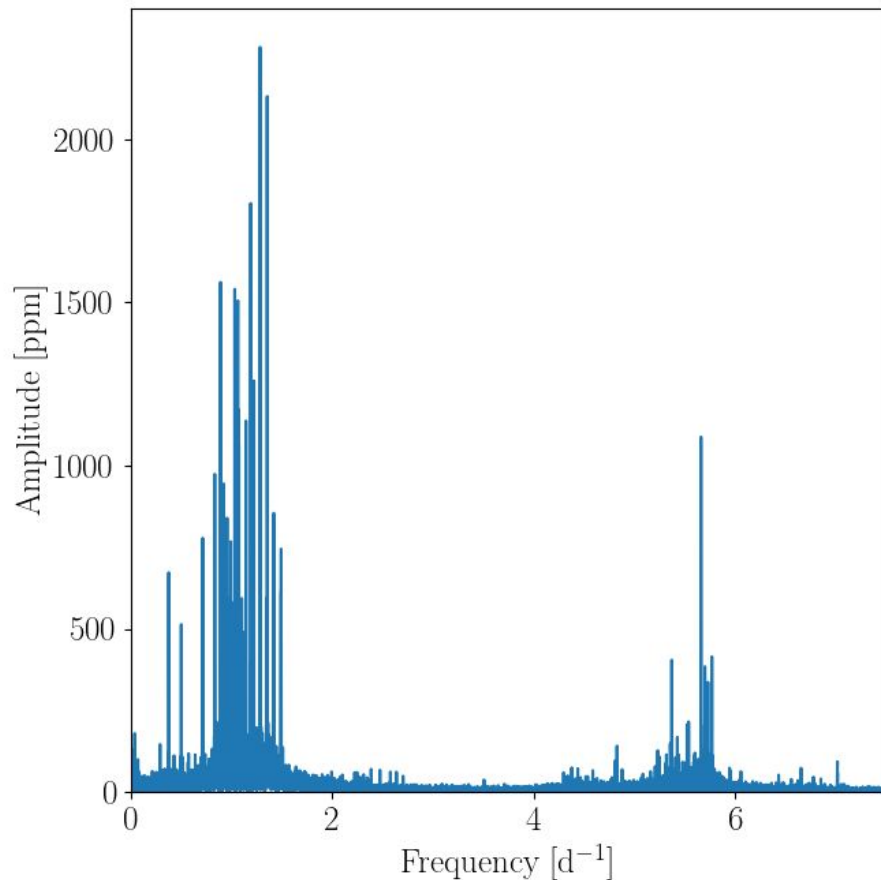
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Four red arrows point to the terms in the equation: one to C , one to A_j , one to f_j , and one to ϕ_j .

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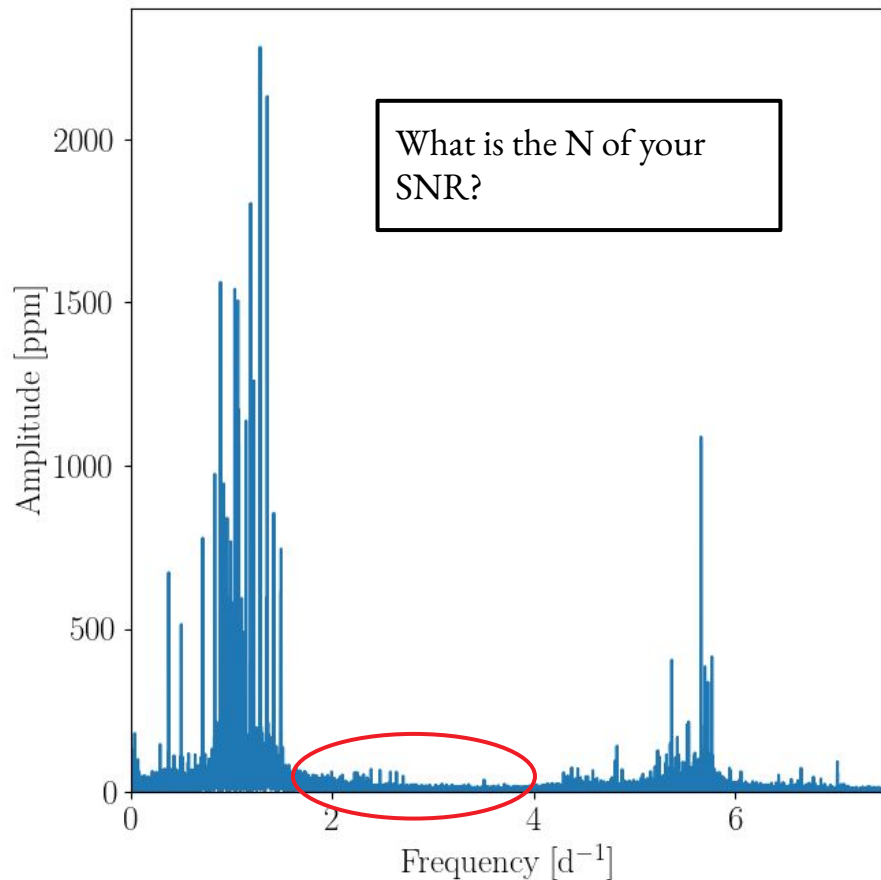


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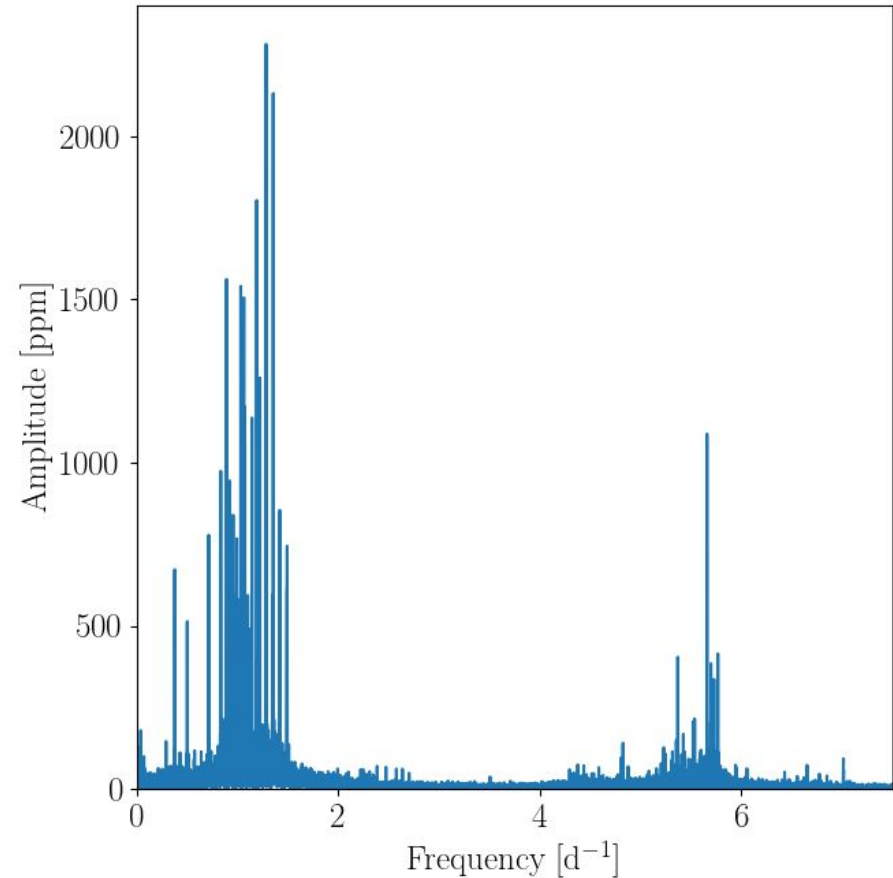
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Iterative pre-whitening

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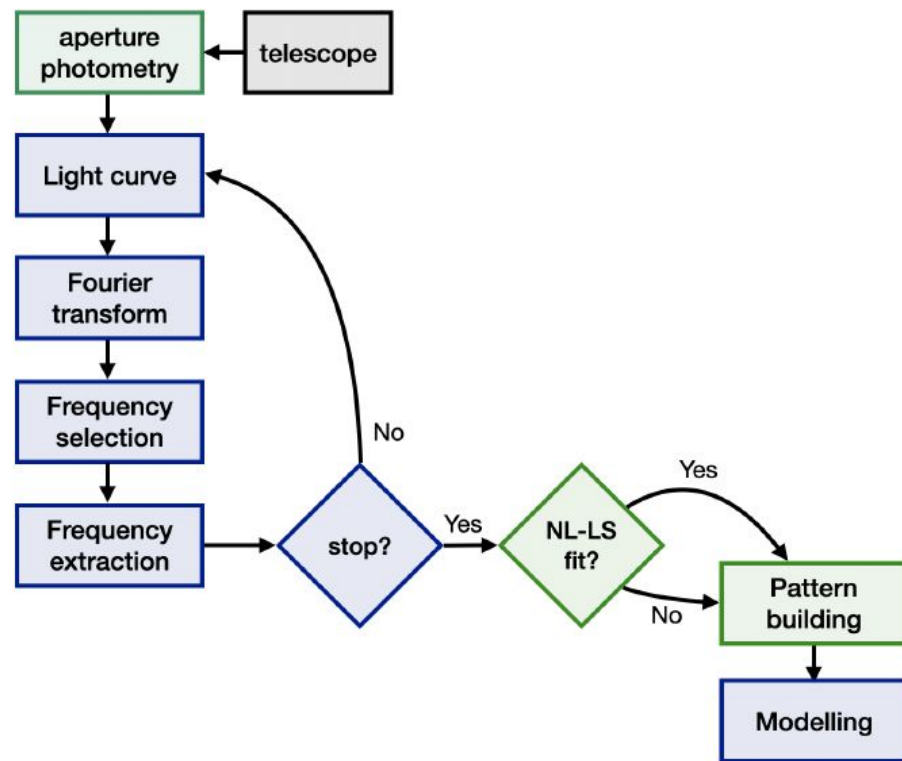
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- Check frequency resolution
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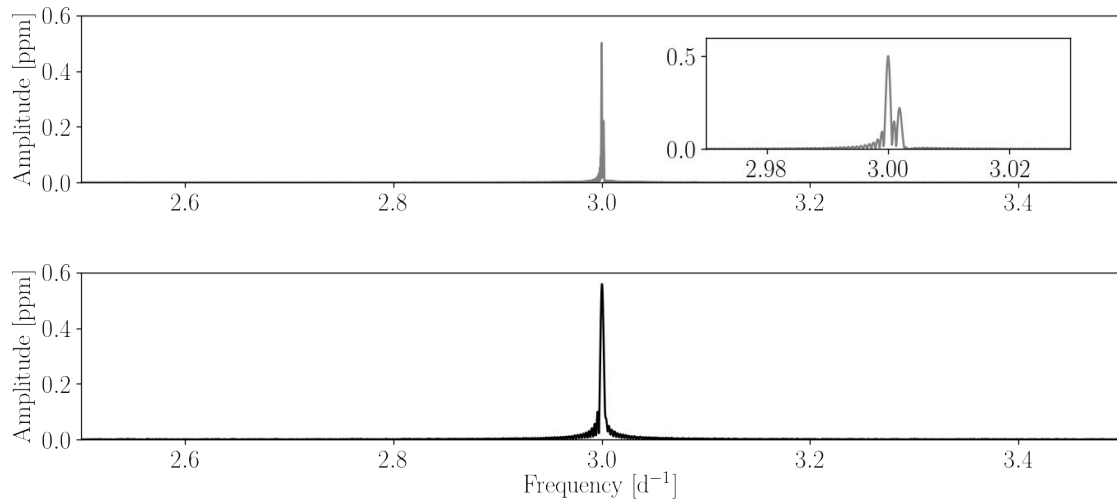
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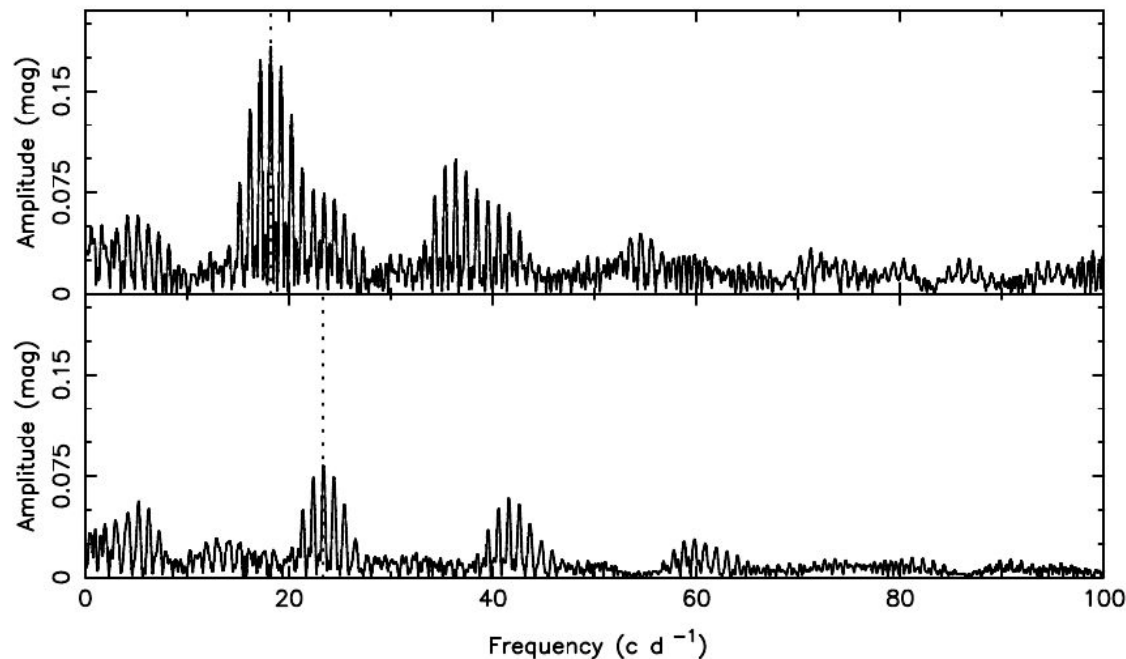


$$\sigma(\nu) = \frac{3}{2} \frac{1}{\Delta T}$$

Iterative pre-whitening

Window functions are a mess

But they do go away if you
remove the right frequency



On to the tutorials!