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**Date:** 07/27/19

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**Course:** CA&T Internet (70263)  
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**Assignment:** 7.5 The Dot Product

1. Complete the sentence below.

The dot product of  $\mathbf{v} = \langle a_1, a_2 \rangle$  and  $\mathbf{w} = \langle b_1, b_2 \rangle$  is defined as  $\mathbf{v} \cdot \mathbf{w} = \underline{\hspace{2cm}}$ .

The dot product of  $\mathbf{v} = \langle a_1, a_2 \rangle$  and  $\mathbf{w} = \langle b_1, b_2 \rangle$  is defined as  $\mathbf{v} \cdot \mathbf{w} = a_1 b_1 + a_2 b_2$ .

2. Complete the sentence below.

If  $\mathbf{v}$  and  $\mathbf{w}$  are orthogonal, then  $\mathbf{v} \cdot \mathbf{w} = \underline{\hspace{2cm}}$ .

If  $\mathbf{v}$  and  $\mathbf{w}$  are orthogonal, then  $\mathbf{v} \cdot \mathbf{w} = \underline{\hspace{2cm}} 0 \underline{\hspace{2cm}}$ .

3. Complete the sentence below.

If  $\mathbf{v} \cdot \mathbf{w} = 0$ , then the two vectors  $\mathbf{v}$  and  $\mathbf{w}$  are  $\underline{\hspace{2cm}}$ .

If  $\mathbf{v} \cdot \mathbf{w} = 0$ , then the two vectors  $\mathbf{v}$  and  $\mathbf{w}$  are orthogonal.

4. Decide whether the following statement is true or false.

If  $\mathbf{v} \cdot \mathbf{w} < 0$  then the angle between  $\mathbf{v}$  and  $\mathbf{w}$  is an obtuse angle.

Choose the correct answer below.

- True  
 False

5. For  $\mathbf{u} = \langle 5, -5 \rangle$  and  $\mathbf{v} = \langle -2, 2 \rangle$  find  $\mathbf{u} \cdot \mathbf{v}$ .

$\mathbf{u} \cdot \mathbf{v} = \underline{\hspace{2cm}} -20 \underline{\hspace{2cm}}$

6. For the following vectors, find  $\mathbf{u} \cdot \mathbf{v}$ .

$$\mathbf{u} = \langle 6, -12 \rangle \text{ and } \mathbf{v} = \langle 2, 1 \rangle$$

$\mathbf{u} \cdot \mathbf{v} = \underline{\hspace{2cm}} 0 \underline{\hspace{2cm}}$

7. Find the dot product of  $\mathbf{u}$  and  $\mathbf{v}$ .

$$\mathbf{u} = 2\mathbf{i} - \mathbf{j} \text{ and } \mathbf{v} = -5\mathbf{i} + 4\mathbf{j}$$

$\mathbf{u} \cdot \mathbf{v} = \underline{\hspace{2cm}} -14 \underline{\hspace{2cm}}$  (Simplify your answer.)

8. Find the dot product  $\mathbf{u} \cdot \mathbf{v}$ .

$$\mathbf{u} = 2\mathbf{i} - 2\mathbf{j} \quad \mathbf{v} = 3\mathbf{j}$$

$\mathbf{u} \cdot \mathbf{v} = \underline{\hspace{2cm}} -6 \underline{\hspace{2cm}}$  (Simplify your answer.)

9. Find  $\mathbf{u} \cdot \mathbf{v}$ , where  $\theta$  is the angle between the vectors  $\mathbf{u}$  and  $\mathbf{v}$ .

$$\|\mathbf{u}\| = 4, \|\mathbf{v}\| = 2, \theta = \frac{\pi}{3}$$

$\mathbf{u} \cdot \mathbf{v} \approx \underline{\hspace{2cm}} 4 \underline{\hspace{2cm}}$  (Round to one decimal place as needed.)

10. Find  $\mathbf{u} \cdot \mathbf{v}$ , where  $\theta$  is the angle between the vectors  $\mathbf{u}$  and  $\mathbf{v}$ .

$$\|\mathbf{u}\| = 9, \|\mathbf{v}\| = 4, \theta = 75^\circ$$

$\mathbf{u} \cdot \mathbf{v} \approx \underline{\hspace{2cm}} 9.3 \underline{\hspace{2cm}}$  (Round to the nearest tenth as needed.)

11. Find the angle between the vectors  $\mathbf{v}$  and  $\mathbf{w}$ .

$$\|\mathbf{v}\| = 2, \|\mathbf{w}\| = \sqrt{7}, \text{ and } \mathbf{v} \cdot \mathbf{w} = \sqrt{3} \sqrt{7}$$

The angle between the vectors  $\mathbf{v}$  and  $\mathbf{w}$  is  °.

(Type an integer or a decimal. Do not include the degree symbol in your answer.)

12. Given  $\mathbf{v} = 9\mathbf{i} + 4\mathbf{j}$  and  $\mathbf{w} = 5\mathbf{i} - \mathbf{j}$ , find the angle between  $\mathbf{v}$  and  $\mathbf{w}$ .

What is the angle between  $\mathbf{v}$  and  $\mathbf{w}$ ?

$$35.3$$

°

(Type your answer in degrees. Do not round until the final answer. Then round to the nearest tenth as needed.)

13. Find the angle between the vectors  $\mathbf{v}$  and  $\mathbf{w}$ .

$$\mathbf{v} = 2\mathbf{i} + 7\mathbf{j}, \mathbf{w} = -7\mathbf{i} + 2\mathbf{j}$$

The angle between the vectors  $\mathbf{v}$  and  $\mathbf{w}$  is  °.

(Type an integer or a decimal. Do not include the degree symbol in your answer.)

14. Let  $\mathbf{v}$  and  $\mathbf{w}$  be two vectors in the plane of magnitudes 7 and 8, respectively. The angle between  $\mathbf{v}$  and  $\mathbf{w}$  is  $61^\circ$ . Find  $\|\mathbf{v} + \mathbf{w}\|$ .

$$\|\mathbf{v} + \mathbf{w}\| \approx$$

$$12.9$$

(Round to one decimal place as needed.)

15. Let  $\mathbf{v}$  and  $\mathbf{w}$  be two vectors in the plane of magnitudes 3 and 6, respectively. The angle between  $\mathbf{v}$  and  $\mathbf{w}$  is  $60^\circ$ . Find  $\|2\mathbf{v} + \mathbf{w}\|$ .

$$\|2\mathbf{v} + \mathbf{w}\| =$$

$$6\sqrt{3}$$

(Type an exact answer, using radicals as needed.)

16. Let  $\mathbf{v}$  and  $\mathbf{w}$  be two vectors in the plane of magnitudes 8 and 7, respectively. The angle between  $\mathbf{v}$  and  $\mathbf{w}$  is  $58^\circ$ . Find the angle between  $\mathbf{v} + \mathbf{w}$  and  $\mathbf{w}$ .

The measure of the angle is about  °.

(Do not round until the final answer. Then round to one decimal place as needed.)

17. This question has been removed from this assignment by your instructor; you have received full credit.

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19. A vector  $\mathbf{F}$  represents a force that has a magnitude of 16 pounds, and  $\frac{\pi}{3}$  is the angle for its direction. Find the work done by the force in moving an object from the origin to the point  $(8,3)$ . Distance is measured in feet.

The work done is  foot-pounds.

(Type an integer or a decimal rounded to the nearest tenth as needed.)

20. This question has been removed from this assignment by your instructor; you have received full credit.

21. Watch the video and then solve the problem below.

[Click here to watch the video.](#)<sup>1</sup>

Let  $\mathbf{v}$  and  $\mathbf{w}$  be two vectors of magnitude 8 and 13, respectively. Let the angle between  $\mathbf{v}$  and  $\mathbf{w}$  be  $62^\circ$ . Find  $\mathbf{v} \cdot \mathbf{w}$ .

$$\mathbf{v} \cdot \mathbf{w} \approx$$

$$48.8$$

(Type an integer or decimal rounded to one decimal place as needed.)

1: <http://mediaplayer.pearsoncmg.com/assets/cQ7VEyH3hkw9x1AlHz6L82LJG2Mh3b4t?clip=2>

22. This question has been removed from this assignment by your instructor; you have received full credit.