

**Score:** 1 of 1 pt

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6.1.3

Complete the following statements.

a.  $\sin^2 x + \underline{\hspace{2cm}} = 1$     b.  $1 + \underline{\hspace{2cm}} = \sec^2 x$     c.  $\csc^2 x - \cot^2 x = \underline{\hspace{2cm}}$

- A.  $\sin^2 x + \cot^2 x = 1$
- B.  $\sin^2 x + \cos^2 x = 1$
- C.  $\sin^2 x + \tan^2 x = 1$
- D.  $\sin^2 x + \csc^2 x = 1$

b. Select the correct response from the choices below.

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6.1.3

Complete the following statements.

a.  $\sin^2 x + \underline{\hspace{2cm}} = 1$     b.  $1 + \underline{\hspace{2cm}} = \sec^2 x$     c.  $\csc^2 x - \cot^2 x = \underline{\hspace{2cm}}$

- A.  $\sin^{-2} x + \tan^{-2} x = 1$
- B.  $\sin^2 x + \csc^2 x = 1$

b. Select the correct response from the choices below.

- A.  $1 + \cos^2 x = \sec^2 x$
- B.  $1 + \csc^2 x = \sec^2 x$
- C.  $1 + \tan^2 x = \sec^2 x$
- D.  $1 + \cot^2 x = \sec^2 x$

c. Select the correct response from the choices below.

- A.  $\csc^2 x - \cot^2 x = -1$
- B.  $\csc^2 x - \cot^2 x = 2$
- C.  $\csc^2 x - \cot^2 x = 0$
- D.  $\csc^2 x - \cot^2 x = 1$

Question is complete.

**Score:** 1 of 1 pt

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6.1.25

Simplify so that no quotients appear in the final expression.

$$\frac{\tan \theta - \sin \theta}{\sin \theta \tan \theta}$$

Choose the correct answer below.

- A.  $\csc \theta \cot \theta$
- B.  $\cot \theta$
- C.  $-\cot \theta \csc \theta$
- D.  $\csc \theta - \cot \theta$
- E.  $\cot \theta - \csc \theta$
- F.  $\sin \theta - \tan \theta$

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**Test Score:** 90.63

6.1.27

Simplify the expression  $\cos(-x) \cdot \tan(-x)$ .

Choose the correct simplified form of  $\cos(-x) \cdot \tan(-x)$ .

- A.  $\tan x$
- B.  $\sin x$
- C.  $-\sin x$
- D.  $\cos x$

**Score:** 1 of 1 pt

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Test S

6.1.30

Write the expression in terms of sine and cosine, and then simplify so that no quotients appear in the final expression.

$$-\sin^2 \theta (-1 - \cot^2 \theta)$$

Choose the correct answer below.

A.  $\sec^2 \theta$

B.  $-\frac{\cos^2 \theta}{\sin^2 \theta}$

C.  $\tan^2 \theta$

D.  $\frac{\cos^2 \theta}{\sin^2 \theta}$

E. 1

F. -1

**Score:** 1 of 1 pt

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6.1.33

Simplify the expression.

$$(\tan x + \sec x)(\tan x - \sec x)$$

$$(\tan x + \sec x)(\tan x - \sec x) = -1$$

(Use integers or decimals for any numbers in the expression.)

**Score:** 1 of 1 pt

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6.1.33

Simplify the expression.

$$(\tan x + \sec x)(\tan x - \sec x)$$

$$(\tan x + \sec x)(\tan x - \sec x) = -1$$

(Use integers or decimals for any numbers in the expression.)

**Score:** 0 of 1 pt

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Test

6.1.35

Factor and simplify.

$$\cos^4 x - \sin^4 x$$

Choose the most simplified form of  $\cos^4 x - \sin^4 x$  below.

- A.  $1 - 2 \sin^2 x$
- B.  $(\cos^2 x - \sin^2 x)(\cos^2 x + \sin^2 x)$
- C.  $\sin^2 x$
- D.  $4 \cos x - 4 \sin x$



The factoring thus far is correct, but one of these factors can be simplified by the use of a Pythagorean identity.

OK

You can swap  $\cos^2 x + \sin^2 x$  to = 1, then you can swap  $\cos^2 x$  with  $1 - \sin^2 x$ . Then you'll have  $1 - \sin^2 x - \sin^2 x$  which equals the answer above.

**Score:** 1 of 1 pt

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6.1.36

Multiply and simplify.

$$\sin x \cos x (\tan x + \csc x)$$

$$\sin x \cos x (\tan x + \csc x) = \sin^2 x + \cos x$$

**Score:** 1 of 1 pt

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6.2.1

Complete the following statement.

$$\sin(A+B) = \underline{\hspace{2cm}}$$

Choose the correct answer below.

- A.  $\sin(A+B) = \sin A \cos B - \cos A \sin B$
- B.  $\sin(A+B) = \cos A \cos B - \sin A \sin B$
- C.  $\sin(A+B) = \cos A \cos B + \sin A \sin B$
- D.  $\sin(A+B) = \sin A \cos B + \cos A \sin B$

**Score:** 1 of 1 pt

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 6.2.2

Complete the following statement.

$\cos A \cos B - \sin A \sin B = \underline{\hspace{2cm}}$

Choose the correct answer below.

- A.  $\cos A \cos B - \sin A \sin B = \cos(A + B)$
- B.  $\cos A \cos B - \sin A \sin B = \cos(A - B)$
- C.  $\cos A \cos B - \sin A \sin B = \sin(A - B)$
- D.  $\cos A \cos B - \sin A \sin B = \sin(A + B)$

**Score:** 1 of 1 pt

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 6.2.3

Complete the following statement.

$\tan(A + B) = \underline{\hspace{2cm}}$

Choose the correct answer below.

- A.  $\tan(A + B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$
- B.  $\tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$
- C.  $\tan(A + B) = \frac{\tan A - \tan B}{1 - \tan A \tan B}$
- D.  $\tan(A + B) = \frac{\tan A + \tan B}{1 + \tan A \tan B}$

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 6.2.5

True or False.

$$\sin\left[\frac{\pi}{2} + x\right] = \cos x$$

Choose the correct answer below.

- A. True, because the value of the sine function of  $x$  is equal to the cosine of the supplement of  $x$ .
- B. False, because the value of the sine function of  $x$  is equal to the cosecant of the supplement of  $x$ .
- C. False, because the value of the sine function of  $x$  is equal to the tangent of the complement of  $x$ .
- D. True, because the value of the sine function of  $x$  is equal to the cosine of the complement of  $x$ .

**Score:** 1 of 1 pt

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 6.2.7

Use one or more of the six sum and difference identities to find the exact value of the expression.

$$\sin(180^\circ - 45^\circ)$$

$$\sin(180^\circ - 45^\circ) = \frac{\sqrt{2}}{2}$$

(Type an exact answer, using radicals as needed. Simplify your answer.)

**Score:** 0 of 1 pt

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 6.2.11

Use one or more of the six sum and difference identities to find the exact value of the expression.

$\sin(105^\circ)$

$\sin(105^\circ) = \frac{\sqrt{6} + \sqrt{2}}{4}$

(Type an exact answer using fraction, radicals and a rationalized denominator. Simplify your answer.)

You answered:  $\frac{7\pi}{12}$

**Score:** 1 of 1 pt

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 6.2.28

Verify the following identity.

$\cos(\pi - \theta) = -\cos \theta$

Which of the following four statements establishes the identity?

- A.  $\cos(\pi - \theta) = \sin \pi \cos \theta + \cos \pi \sin \theta = -\cos \theta$
- B.  $\cos(\pi - \theta) = \sin \pi \cos \theta - \cos \pi \sin \theta = -\cos \theta$
- C.  $\cos(\pi - \theta) = \cos \pi \cos \theta + \sin \pi \sin \theta = -\cos \theta$
- D.  $\cos(\pi - \theta) = \cos \pi \cos \theta - \sin \pi \sin \theta = -\cos \theta$

**Score:** 1 of 1 pt



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6.2.29

Establish the identity  $\sin\left(\frac{3\pi}{2} + \theta\right) = -\cos \theta$ .

Which of the following four statements establishes the identity?

- A.  $\sin\left(\frac{3\pi}{2} + \theta\right) = \sin\frac{3\pi}{2}\sin\theta + \cos\frac{3\pi}{2}\cos\theta = (0)\sin\theta + (-1)\cos\theta = -\cos\theta$
- B.  $\sin\left(\frac{3\pi}{2} + \theta\right) = \sin\frac{3\pi}{2}\sin\theta - \cos\frac{3\pi}{2}\cos\theta = (-1)\cos\theta - (0)\sin\theta = -\cos\theta$
- C.  $\sin\left(\frac{3\pi}{2} + \theta\right) = \sin\frac{3\pi}{2}\cos\theta + \cos\frac{3\pi}{2}\sin\theta = (-1)\cos\theta + (0)\sin\theta = -\cos\theta$
- D.  $\sin\left(\frac{3\pi}{2} + \theta\right) = \sin\frac{3\pi}{2}\cos\theta - \cos\frac{3\pi}{2}\sin\theta = (-1)\cos\theta - (0)\sin\theta = -\cos\theta$

**Score:** 1 of 1 pt



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6.2.47

Find the exact value of the expression

$$\sin\frac{5\pi}{12}\cos\frac{\pi}{3} + \cos\frac{5\pi}{12}\sin\frac{\pi}{3}$$

$$\sin\frac{5\pi}{12}\cos\frac{\pi}{3} + \cos\frac{5\pi}{12}\sin\frac{\pi}{3} = \frac{\sqrt{2}}{2}$$

(Simplify your answer, including any radicals. Use integers or fractions for any numbers in the expression.)

**Score:** 1 of 1 pt

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 6.3.1

Complete the following statement.

The double-angle identity for  $\sin 2x$  is  $\sin 2x = \underline{\hspace{2cm}}$ .

$\sin 2x = 2 \sin x \cos x$

**Score:** 1 of 1 pt

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**Test Score:** 90.63%, 29 of 32 pts

 6.3.2 

Complete the following statement.

In the double-angle identity  $\cos 2x = \cos^2 x - \sin^2 x$ , replace  $\cos^2 x$  with  $1 - \sin^2 x$  to obtain a double-angle identity  $\cos 2x = \underline{\hspace{2cm}}$  in terms of  $\sin^2 x$ . Solve this identity for  $\sin^2 x$  to obtain the power-reducing identity  $\sin^2 x = \underline{\hspace{2cm}}$ .

$\cos 2x = 1 - 2 \sin^2 x$

$\sin^2 x = \frac{1 - \cos 2x}{2}$

**Score:** 1 of 1 pt

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**Test Score:** 90.63%, 29 of 32

 6.3.3

Complete the following statement.

The identity for  $\cos 2x$  in terms of  $\cos^2 x$  is  $\cos 2x = \underline{\hspace{2cm}}$ . Solve this identity for  $\cos^2 x$  to obtain the power-reducing identity  $\cos^2 x = \underline{\hspace{2cm}}$ .

$\cos 2x = 2 \cos^2 x - 1$

$\cos^2 x = \frac{1 + \cos 2x}{2}$

**Score:** 1 of 1 pt



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6.3.5

State whether the following statement is true or false.

$$\frac{1}{2} \tan 2x = \tan x$$

Choose the correct answer below.

- A. False, because the double-angle formula for tangent is not applied correctly.
- B. False, because  $\frac{1}{2} \tan 2x = \tan^2 x$ .
- C. False, because  $\frac{1}{2} \tan 2x = \tan x$ .
- D. True, because the double-angle formula for tangent is applied correctly.

**Score:** 1 of 1 pt



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6.4.1

Complete the following.

We can rewrite the product of two sines as a difference of two cosines by using the identity  $\sin x \sin y = \underline{\hspace{2cm}}$ .

$$\sin x \sin y = \frac{1}{2} [\cos(x - y) - \cos(x + y)]$$

**Score:** 1 of 1 pt

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6.4.5

Identify whether the following equation is true or false.

$$\sin x + \sin y = \sin(x + y)$$

Choose the correct answer below.

- A. True, because  $\sin x + \sin y = 2 \sin\left(\frac{x+y}{2}\right) \cos\left(\frac{x-y}{2}\right)$  which is equal to  $\sin(x+y)$ .
- B. False, because  $\sin x + \sin y = \sin(x+y) \cos(x-y)$  and  $\sin(x+y) = \sin x \cos y + \cos x \sin y$ .
- C. False, because  $\sin x + \sin y = 2 \sin\left(\frac{x+y}{2}\right) \cos\left(\frac{x-y}{2}\right)$  and  $\sin(x+y) = \sin x \cos y + \cos x \sin y$ .
- D. True, because  $\sin x + \sin y = \sin x \cos y + \cos x \sin y$  which is equal to  $\sin(x+y)$ .

**Score:** 1 of 1 pt

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6.4.15

Use the product-to-sum identities to rewrite the expression.

$$\sin\left(\frac{\pi}{3}\right) \cos\left(\frac{\pi}{7}\right)$$

Which of the following is equivalent to  $\sin\left(\frac{\pi}{3}\right) \cos\left(\frac{\pi}{7}\right)$ ?

- A.  $\frac{1}{2} \left( \sin \frac{10\pi}{21} - \sin \frac{4\pi}{21} \right)$
- B.  $\frac{1}{2} \left( \cos \frac{10\pi}{21} + \cos \frac{4\pi}{21} \right)$
- C.  $\sin \frac{10\pi}{21} + \sin \frac{4\pi}{21}$
- D.  $\frac{1}{2} \left( \sin \frac{10\pi}{21} + \sin \frac{4\pi}{21} \right)$

**Score:** 1 of 1 pt

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T

6.4.19

Express the given product as a sum containing only sines or cosines.

$\sin(80)\cos(20)$

$\sin(80)\cos(20) = \frac{1}{2}[\sin(100) + \sin(60)]$

(Simplify your answer, including any radicals. Use integers or fractions for any numbers in the expression.)

**Score:** 1 of 1 pt

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6.4.25

Find the exact value of the expression  $\sin 135^\circ \cdot \cos 75^\circ$ .

Choose the correct answer below.

A.  $\frac{\sqrt{3}}{2}$

B.  $\frac{\sqrt{3}-1}{4}$

C.  $-\frac{1}{2}$

D.  $\frac{\sqrt{2}}{2}$

Score: 1 of 1 pt

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Test Score: 90.63%, 29 of 32 pt

6.5.13



Find all solutions of the following equation.

$$\cot x = \sqrt{3}$$

All solutions of the equation  $\cot x = \sqrt{3}$  are given by  $x = \frac{\pi}{6} + n\pi$ .

(Type an expression using  $n$  as the variable. Type any angle measures in radians. Use angle measures greater than or equal to 0 and less than  $2\pi$ .)

Score: 0 of 1 pt

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Test Score: 90.63%, 29 of 32

6.5.15

Solve the equation. Give a general formula for all the solutions.

$$\cos x = -\frac{1}{2}$$

Give a general formula for all the solutions by using angle(s) in the interval  $[0, 2\pi]$ , and adding multiples of some integer  $n$ .

Select the correct choice below and, if necessary, fill in the answer box to complete your choice.

A.

$$x = \frac{2\pi}{3} + 2n\pi, \frac{4\pi}{3} + 2n\pi$$

(Simplify your answer. Type an exact answer using  $\pi$  as needed. Type your answer in radians. Use integers or fractions for any numbers in the expression.)

B. The

$$\text{You answered: } \frac{2\pi}{3}, \frac{4\pi}{3}$$

$$\text{Correct answer: } \frac{2\pi}{3} + 2n\pi, \frac{4\pi}{3} + 2n\pi$$

I had the answer right on this, the only reason it's wrong was they didn't specify well enough to tell me that they wanted those  $2n(\pi)$  things afterward. So I understand what's going on.

**Score:** 1 of 1 pt

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 6.5.17

Find all solutions of the equation. Express the solutions in degrees.

$$\tan x = -\sqrt{3}$$

Select the correct choice given below.

- A.  $x = 30^\circ + 360^\circ k$ , where  $k$  is any integer
- B.  $x = 30^\circ + 180^\circ k$ , where  $k$  is any integer
- C.  $x = 120^\circ + 360^\circ k$ , where  $k$  is any integer
- D.  $x = 120^\circ + 180^\circ k$ , where  $k$  is any integer

**Score:** 1 of 1 pt

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 6.5.19

Find all solutions of the equation. Express the solutions in degrees.

$$\sin x = -\frac{1}{2}$$

Select the correct choice given below.

- A.  $x = 30^\circ + 360^\circ k$  or  $x = 150^\circ + 360^\circ k$ , where  $k$  is any integer
- B.  $x = 210^\circ + 360^\circ k$  or  $x = 330^\circ + 360^\circ k$ , where  $k$  is any integer
- C.  $x = 30^\circ + 180^\circ k$  or  $x = 150^\circ + 180^\circ k$ , where  $k$  is any integer
- D.  $x = 210^\circ + 180^\circ k$  or  $x = 330^\circ + 180^\circ k$ , where  $k$  is any integer

**Score:** 1 of 1 pt



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6.5.21

Find all solutions of the equation. Express the solutions in degrees.

$$\sin x = 1$$

Select the correct choice given below.

- A.  $x = 0^\circ + 180^\circ n$ , where  $n$  is any integer
- B.  $x = 0^\circ + 360^\circ n$ , where  $n$  is any integer
- C.  $x = 90^\circ + 180^\circ n$ , where  $n$  is any integer
- D.  $x = 90^\circ + 360^\circ n$ , where  $n$  is any integer

**Score:** 1 of 1 pt



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6.5.23

Find all solutions of the equation. Express the solutions in degrees.

$$\frac{1}{2} \sec x + 1 = 0$$

Select the correct choice given below.

- A.  $x = 120^\circ + 180^\circ n$  or  $x = 240^\circ + 360^\circ n$ , where  $n$  is any integer
- B.  $x = 120^\circ + 360^\circ n$  or  $x = 240^\circ + 360^\circ n$ , where  $n$  is any integer
- C.  $x = 45^\circ + 360^\circ n$  or  $x = 315^\circ + 180^\circ n$ , where  $n$  is any integer
- D.  $x = 45^\circ + 180^\circ n$  or  $x = 315^\circ + 180^\circ n$ , where  $n$  is any integer

This is solved by first subtracting 1, then dividng secx. Then divide out the -1 on the right side to the  $\frac{1}{2}$  to make it  $-1/2$  and then you can refer to the unit circle.