

Student: Cole Lamers
Date: 06/23/19

Instructor: Kelly Galarneau
Course: CA&T Internet (70263)
Galarneau

Assignment: 4.3 Rules of Logarithms

1. $\log_a MN = \underline{\hspace{2cm}} + \underline{\hspace{2cm}}$.

Choose the correct answer below.

- A. $\log_a MN = \log_a M + \log_a N$
 B. $\log_a MN = M \log_a N + N \log_a M$
 C. $\log_a MN = M + \log_a N$
 D. $\log_a MN = \log_a M + N$

2. $\log_a M^r = \underline{\hspace{2cm}}$.

$$\log_a M^r = r \log_a M$$

3. $\log_a(u+v) = \log_a u + \log_a v$. State whether the statement is true or false.

Choose the correct answer below.

- True
 False

4. Use $\log_b 4 = 1.386$ and/or $\log_b 7 = 1.946$ to find $\log_b 28$.

$$\log_b 28 = \underline{\hspace{2cm}} 3.332$$

5. Given that $\log x = 3$, $\log y = 7$, and $\log 5 \approx 0.7$, evaluate the following expression without using a calculator.

$$\log(5x^2y)$$

$$\log(5x^2y) \approx \underline{\hspace{2cm}} 13.7 \quad (\text{Type an integer or a decimal.})$$

6. Watch the video and then solve the problem given below.

[Click here to watch the video.¹](#)

Write the expression $\log_7 \frac{x^3(3x+2)^2}{(x-5)^4}$ in expanded form.

$$\log_7 \frac{x^3(3x+2)^2}{(x-5)^4} = \underline{\hspace{2cm}} 3 \log_7 x + 2 \log_7 (3x+2) - 4 \log_7 (x-5)$$

1: http://mediaplayer.pearsoncmg.com/assets/ii54F1eDgFfJUZJdhM4DXkWIVyscF_C6?clip=2

7. Write the following expression in expanded form.

ln [x(x - 7)]

ln [x(x - 7)] = **ln** (x) + **ln** (x - 7)

8. Write the following expression in expanded form.

$$\log \frac{\sqrt{x^2 + 5}}{x + 3}$$

Choose the correct answer below.

- A. $\log \frac{\sqrt{x^2 + 5}}{x + 3} = 2 \log (x^2 + 5) + \log (x + 3)$
- B. $\log \frac{\sqrt{x^2 + 5}}{x + 3} = \frac{1}{2} \log (x^2 + 5) - \log (x + 3)$
- C. $\log \frac{\sqrt{x^2 + 5}}{x + 3} = 2 \log (x^2 + 5) - \log (x + 3)$
- D. $\log \frac{\sqrt{x^2 + 5}}{x + 3} = \frac{1}{2} \log (x^2 + 5) + \log (x + 3)$

9. Express in terms of logarithms without exponents.

log_c(x²y⁴z)

What is the equivalent expression?

2 **log**_c(x) + 4 **log**_c(y) + **log**_c(z)

10. Watch the video and then solve the problem given below.

[Click here to watch the video.²](#)

Write the expression $2 \ln(5x + 3) - 5 \ln(x - 3) - 4 \ln x$ in condensed form.

$$2 \ln(5x + 3) - 5 \ln(x - 3) - 4 \ln x = \ln \frac{(5x + 3)^2}{x^4(x - 3)^5}$$

2: http://mediaplayer.pearsoncmg.com/assets/ii54F1eDgFfJUZJdhM4DXkWIVscF_C6?clip=3

11. Write the sum as the logarithm of a single expression. Assume that variables represent positive numbers.

log₂9 + **log**₂z

log₂9 + **log**₂z = **log**₂(9z)

12. Write the given expression in condensed form.

$$\frac{1}{2} \log x - \log(9y) + \log(5z)$$

$$\frac{1}{2} \log x - \log(9y) + \log(5z) = \log \frac{5z\sqrt{x}}{9y}$$

(Type an exact answer. Use integers or fractions for any numbers in the expression.)

13. Write the following expression in condensed form.

$$\ln a + 4 \ln b + 6 \ln c$$

$$\ln a + 4 \ln b + 6 \ln c = \ln(ab^4c^6)$$

(Simplify your answer.)

14. Watch the video and then solve the problem given below.

[Click here to watch the video.](#)³

Use the base changing formula to compute $\log_3 12$.

$$\log_3 12 \approx 2.262$$

(Round to the nearest thousandth as needed.)

3: http://mediaplayer.pearsoncmg.com/assets/ii54F1eDgFfJUZJdhM4DXkWIVyscF_C6?clip=5

15. Use the change of base formula to find the value of the following logarithm. Do not round logarithms in the change of base formula.

$$\log_4 18$$

$$\log_4 18 = 2.085$$

(Simplify your answer. Do not round until the final answer. Then round to four decimal places as needed.)

16. Use the change-of-base formula and a calculator to evaluate the following logarithm.

$$\log_7 2 + \log_3 4$$

$$\log_7 2 + \log_3 4 = 1.6$$

(Simplify your answer. Type an integer or decimal rounded to one decimal place as needed.)

17. Find the value of the following expression without using a calculator.

$$\log_6 \sqrt[3]{216}$$

$$\log_6 \sqrt[3]{216} = \frac{3}{2}$$

(Simplify your answer. Type an integer or a fraction.)

18. Evaluate the expression without using a calculator.

$$\log_4(\log_2 16)$$

$$\log_4(\log_2 16) = 1$$

19. Find the value of the following expression without using a calculator.

$$\frac{2 \log_7 4 + \log_7 3}{7}$$

$$\frac{2 \log_7 4 + \log_7 3}{7} = \boxed{48} \quad (\text{Simplify your answer.})$$

20. Find the value of the expression without using a calculator.

$$\log 40 + 2 \log 5$$

Rewrite the expression as a single logarithm.

$$\log 40 + 2 \log 5 = \log \boxed{1000} \quad (\text{Simplify your answer.})$$

Evaluate the expression without using a calculator.

$$\log 40 + 2 \log 5 = \boxed{3} \quad (\text{Simplify your answer.})$$

21. Suppose that \$2000 is invested in an account that pays interest compounded continuously. Find the amount of time that it would take for the account to grow to \$5000 at 4.75%.

It would take approximately years.
(Round to the nearest tenth.)