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Assignment: 4.3 Rules of Logarithms

1. $\log_a MN = \underline{\hspace{1cm}} + \underline{\hspace{1cm}}$.

Choose the correct answer below.

- ☒ **A.** $\log_a MN = \log_a M + \log_a N$
☐ **B.** $\log_a MN = M \log_a N + N \log_a M$
☐ **C.** $\log_a MN = M + \log_a N$
☐ **D.** $\log_a MN = \log_a M + N$

2. $\log_a M^r = \underline{\hspace{1cm}}$.

$\log_a M^r = r \log_a M$

3. $\log_a(u + v) = \log_a u + \log_a v$. State whether the statement is true or false.

Choose the correct answer below.

- ☐ True
☒ False

4. Use $\log_b 4 = 1.386$ and/or $\log_b 7 = 1.946$ to find $\log_b 28$.

$\log_b 28 = \underline{\hspace{1cm}} 3.332$

5. Given that $\log x = 3$, $\log y = 7$, and $\log 5 \approx 0.7$, evaluate the following expression without using a calculator.

$\log(5x^2y)$

$\log(5x^2y) \approx \underline{\hspace{1cm}} 13.7$ (Type an integer or a decimal.)

6. Watch the video and then solve the problem given below.

[Click here to watch the video.](#)¹

Write the expression $\log_7 \frac{x^3(3x+2)^2}{(x-5)^4}$ in expanded form.

$\log_7 \frac{x^3(3x+2)^2}{(x-5)^4} = \underline{\hspace{1cm}} 3 \log_7 x + 2 \log_7(3x+2) - 4 \log_7(x-5)$

1: http://mediaplayer.pearsoncmg.com/assets/ii54F1eDgFfJUzJdhM4DXkWiVyscF_C6?clip=2

7. Write the following expression in expanded form.

$$\ln [x(x - 7)]$$

$$\ln [x(x - 7)] = \ln (x) + \ln (x - 7)$$

8. Write the following expression in expanded form.

$$\log \frac{\sqrt{x^2 + 5}}{x + 3}$$

Choose the correct answer below.

☐ A. $\log \frac{\sqrt{x^2 + 5}}{x + 3} = 2 \log (x^2 + 5) + \log (x + 3)$

☒ B. $\log \frac{\sqrt{x^2 + 5}}{x + 3} = \frac{1}{2} \log (x^2 + 5) - \log (x + 3)$

☐ C. $\log \frac{\sqrt{x^2 + 5}}{x + 3} = 2 \log (x^2 + 5) - \log (x + 3)$

☐ D. $\log \frac{\sqrt{x^2 + 5}}{x + 3} = \frac{1}{2} \log (x^2 + 5) + \log (x + 3)$

9. Express in terms of logarithms without exponents.

$$\log_c (x^2 y^4 z)$$

What is the equivalent expression?

$$2 \log_c (x) + 4 \log_c (y) + \log_c (z)$$

10. Watch the video and then solve the problem given below.

[Click here to watch the video.](#)²

Write the expression $2 \ln (5x + 3) - 5 \ln (x - 3) - 4 \ln x$ in condensed form.

$$2 \ln (5x + 3) - 5 \ln (x - 3) - 4 \ln x = \ln \frac{(5x + 3)^2}{x^4 (x - 3)^5}$$

2: http://mediaplayer.pearsoncmg.com/assets/ii54F1eDgFfJUzJdhM4DXkWIVyscF_C6?clip=3

11. Write the sum as the logarithm of a single expression. Assume that variables represent positive numbers.

$$\log_2 9 + \log_2 z$$

$$\log_2 9 + \log_2 z = \log_2 (9z)$$

12. Write the given expression in condensed form.

$$\frac{1}{2} \log x - \log (9y) + \log (5z)$$

$$\frac{1}{2} \log x - \log (9y) + \log (5z) = \log \frac{5z\sqrt{x}}{9y}$$

(Type an exact answer. Use integers or fractions for any numbers in the expression.)

13. Write the following expression in condensed form.

$$\ln a + 4 \ln b + 6 \ln c$$

$$\ln a + 4 \ln b + 6 \ln c = \ln (ab^4c^6) \quad (\text{Simplify your answer.})$$

14. Watch the video and then solve the problem given below.

[Click here to watch the video.](#)³

Use the base changing formula to compute $\log_3 12$.

$$\log_3 12 \approx 2.262 \quad (\text{Round to the nearest thousandth as needed.})$$

3: http://mediaplayer.pearsoncmg.com/assets/ii54F1eDgFfJUZJdhM4DXkWIVyscF_C6?clip=5

15. Use the change of base formula to find the value of the following logarithm. Do not round logarithms in the change of base formula.

$$\log_4 18$$

$$\log_4 18 = 2.085$$

(Simplify your answer. Do not round until the final answer. Then round to four decimal places as needed.)

16. Use the change-of-base formula and a calculator to evaluate the following logarithm.

$$\log_7 2 + \log_3 4$$

$$\log_7 2 + \log_3 4 = 1.6$$

(Simplify your answer. Type an integer or decimal rounded to one decimal place as needed.)

17. Find the value of the following expression without using a calculator.

$$\log_6 \sqrt{216}$$

$$\log_6 \sqrt{216} = \frac{3}{2} \quad (\text{Simplify your answer. Type an integer or a fraction.})$$

18. Evaluate the expression without using a calculator.

$$\log_4 (\log_2 16)$$

$$\log_4 (\log_2 16) = 1$$

19. Find the value of the following expression without using a calculator.

$$7^{2\log_7 4 + \log_7 3}$$

$$7^{2\log_7 4 + \log_7 3} = \text{48} \quad (\text{Simplify your answer.})$$

20. Find the value of the expression without using a calculator.

$$\log 40 + 2 \log 5$$

Rewrite the expression as a single logarithm.

$$\log 40 + 2 \log 5 = \log \text{1000} \quad (\text{Simplify your answer.})$$

Evaluate the expression without using a calculator.

$$\log 40 + 2 \log 5 = \text{3} \quad (\text{Simplify your answer.})$$

21. Suppose that \$2000 is invested in an account that pays interest compounded continuously. Find the amount of time that it would take for the account to grow to \$5000 at 4.75%.

It would take approximately 19.3 years.
(Round to the nearest tenth.)