## Interacting Peers Picture

Integer: 7

0

Integer: 1

4

Integer: 24

1

Integer: 3

3

Integer: 16

2

- Each process has an integer
  - Goal: disseminate max and min integers
- Approaches
  - Centralized: use coordinator
  - Symmetric: every process sends value to every other
  - Ring: form a circle; send values around
  - Tree: create a binary (in general, n-ary) tree

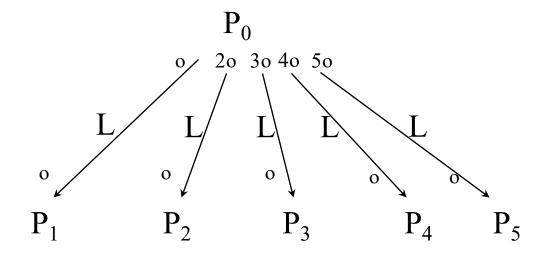
- Each process has an integer
  - Goal: disseminate max and min integers to each process
- Approaches
  - Centralized: use coordinator
    - 2 \* (P-1) messages but a bottleneck
  - Symmetric: every process sends value to every other
    - P \* (P-1) messages
  - Ring: form a circle; send values around
    - 2 \* (P-1) messages; no bottleneck, but sequential
  - Tree: create a binary (in general, n-ary) tree
    - 2 \* (P-1) messages; less bottleneck, but log(P) steps

- How to know which implementation to choose?
- Can use analytical models
  - LogP model most widely used model
  - L (latency), o (overhead), g (gap), P (number of cores)
    - Allows mostly architecture-independent analysis of parallel algorithms
    - Latency: time for a single byte to travel between endpoints
    - Overhead: time to copy a message from user address space to network
    - Gap: mandatory time between consecutive messages (represents the inverse of network bandwidth, bytes/second)

## LogP Model applied to broadcast

Sent at time:

Message travels

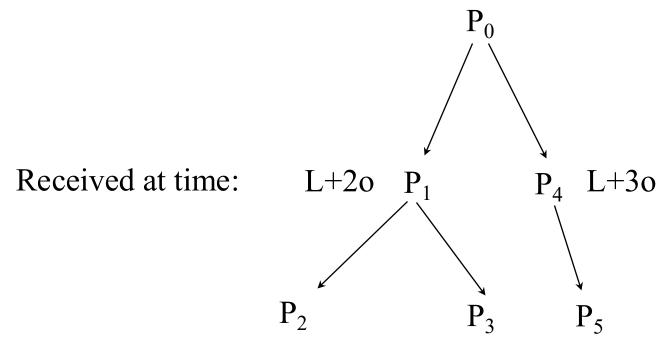


Received at time: L+20 L+30 L+40 L+50 L+60

Broadcast completion time is L+60, assuming o > gMore accurate to say completion time is roughly L + 6 \* max(o,g)

## LogP Model applied to broadcast

(Assumes o > g)



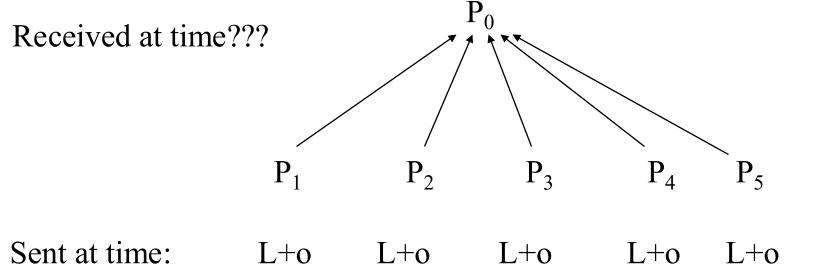
Received at time: 2L+4o 2L+5o 2L+5o

Broadcast completion time is 2L+50 (compared to L+60 on previous slide). Which is better depends on the values of L and o.

# What about a reduction (fan-in and fan-out)

- Let's use LogP to compare a two-level tree to symmetric
  - Two-level tree clearly takes L+60 for the fan-out (see previous slide; it's just a broadcast).
    - What about the fan-in? Is it just L+20, since P1 through P5 all send to P0?

# LogP Model applied to fan-in



Fan-in completion time (when  $P_0$  receives all messages) is not L+20

- -- would imply infinite bandwidth (imagine if a million processes sent to  $P_0$ )
- -- in reality, receives all messages at roughly L+6\*max(o, g), just like fan-out

# What about a reduction (fan-in and fan-out)

- Let's use LogP to compare a two-level tree to symmetric
  - Two-level tree clearly takes L+60 for the fan-out (see previous slide; it's just a broadcast).
    - What about the fan-in? Is it just L+20, since P1 through P5 all send to P0?
      - No, because overheads cannot be parallelized
      - In addition, the gap parameter represents finite bandwidth
  - Symmetric?
    - Seems like maybe L+60
      - But in reality, that is the minimum---much more complicated than this; involves sends and receives at each node

- Generalizations
  - Example: all-to-all
    - Implementations are not at all clear here
    - Must worry about contention
    - May want intelligent scheduling

For details, if interested, the LogP paper is at: <a href="https://dl.acm.org/doi/10.1145/155332.155333">https://dl.acm.org/doi/10.1145/155332.155333</a>