

Example Concurrent Program

```
int x = 0
```

```
co
```

```
    x = x + 1
```

```
//
```

```
    x = x + 2
```

```
oc
```

```
print x
```

What are the possible outputs of this program?

Example Concurrent Program (cont.)

- One possible execution order is:
 - Thread 0: $R1 := x$ ($R1 == 0$)
 - Thread 1: $R2 := x$ ($R2 == 0$)
 - Thread 1: $R2 := R2 + 2$ ($R2 == 2$)
 - Thread 1: $x := R2$ ($x == 2$)
 - Thread 0: $R1 := R1 + 1$ ($R1 == 1$)
 - Thread 0: $x := R1$ ($x == 1$)
- Final value of x is 1 (!!)
- Question: what if Thread 1 also uses $R1$?

Example Concurrent Program

```
int x = 0
```

```
co
```

```
    x = x + 1
```

```
//
```

```
    x = x + 2
```

```
oc
```

```
print x
```

Possible outputs are 1, 2, and 3

The output **cannot** be 0 because of the oc

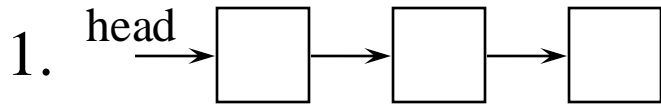
More Concurrent Programming: Linked Lists (head is shared)

```
Insert(head, elem) {  
    elem→next := head;  
    head := elem;  
}
```

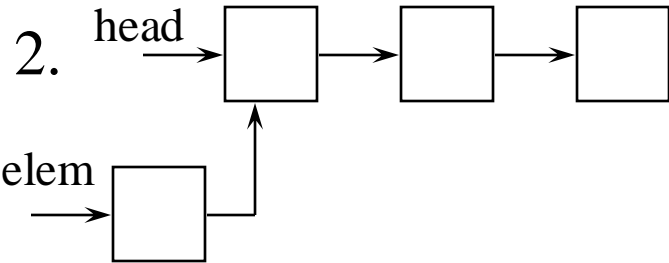
```
Void *Remove(head) {  
    Void *t;  
    t := head;  
    head := head→next;  
    return t;  
}
```

(Assume one thread calls Insert and
one calls Remove, concurrently)

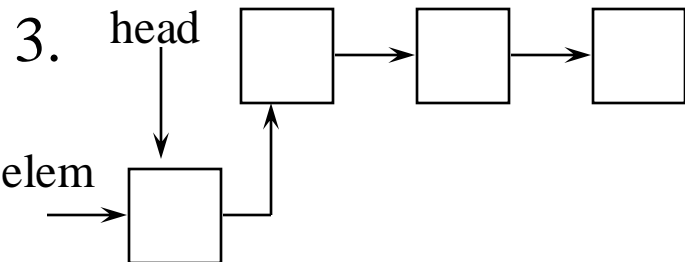
One Possible (Fine) Execution



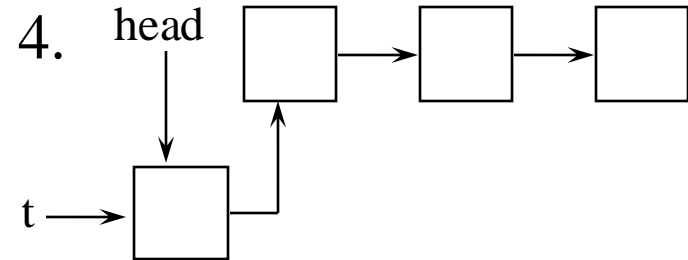
Insert: $\text{elem} \rightarrow \text{next} := \text{head};$



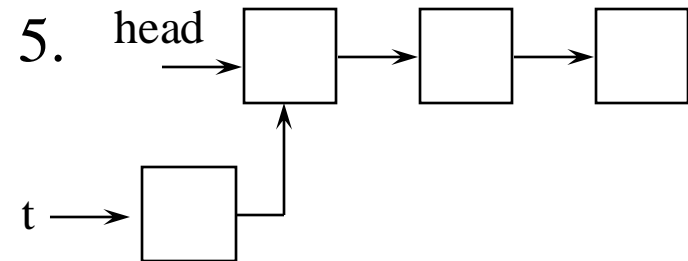
Insert: $\text{head} := \text{elem};$



Remove: $t := \text{head};$

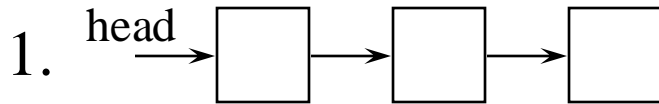


Remove: $\text{head} := \text{head} \rightarrow \text{next};$

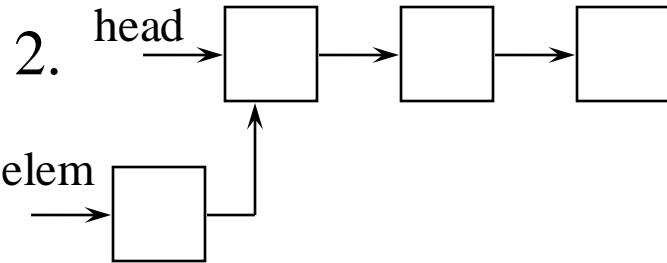


Remove: return t;

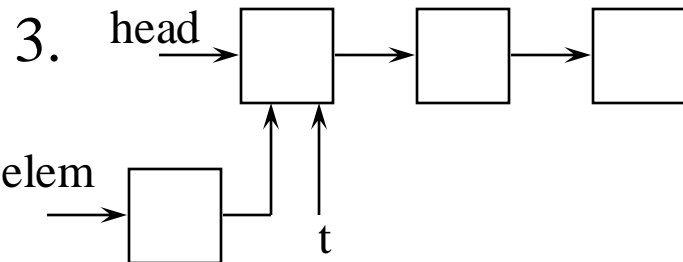
One Possible (Bad!) Execution



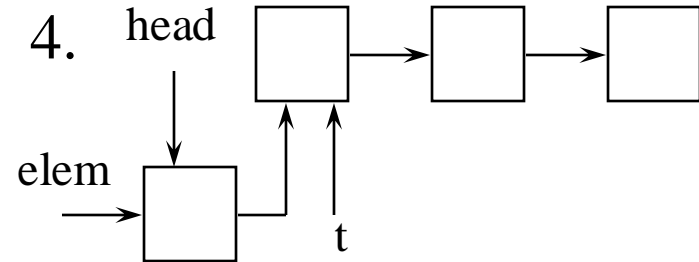
Insert: $\text{elem} \rightarrow \text{next} := \text{head};$



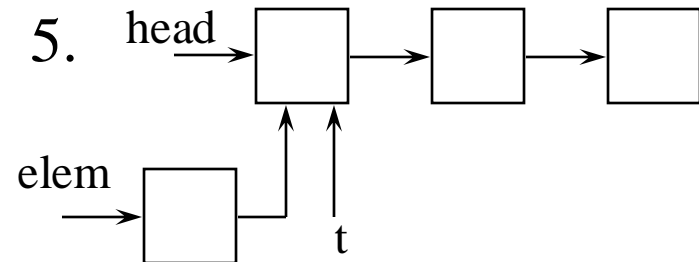
Remove: $t := \text{head};$



Insert: $\text{head} := \text{elem};$



Remove: $\text{head} := \text{head} \rightarrow \text{next};$



Remove: return $t;$

Definitions

- Several important terms
 - State
 - The values of all program variables, both implicit and explicit, at a given point in time
 - Atomic action
 - an action that indivisibly examines or changes program state
 - an operation that, once started, runs to completion
 - **more precisely, logically runs to completion**
 - we assume **individual** loads/stores are physically atomic
 - meaning: if thread A stores 1 into variable x and thread B stores 2 into variable x at about the same time, result is either 1 or 2

Definitions, continued

- Additional terms
 - History
 - Linearization (interleaving) of the atomic actions of all threads
 - **Different histories may lead to the same output**
 - **Atomic actions of a particular thread must appear in the linearization in program order**
 - Safety: program never enters a bad state
 - Example: partial correctness
 - Liveness: program eventually enters a good state
 - Example: termination

Definitions, continued

- Additional terms
 - Interference
 - Thread 1 interferes with Thread 2 if:
 - Thread 1 executes an assignment statement that modifies a shared variable that invalidates an assertion in Thread 2

Example of Interference

Assertions are in {...}

int x = 0

co

{x == 0}

Assertion: represents state before assignment in thread 1

x = x + 1

Assignment in thread 1

{x == 1}

Assertion: represents state after assignment in thread 1

//

{x == 0}

Assertion: represents state before assignment in thread 2

Invalidated!

x = x + 2

Assignment in thread 2

{x == 2}

Assertion: represents state after assignment in thread 2

oc

Race Condition

- When output depends on ordering of thread execution
- More formally:
 - (1) two or more threads access a shared variable with no synchronization (*or incorrect/insufficient synchronization*), **and**
 - (2) at least one of the threads writes to the variable

Both the addition code and the list code shown previously have race conditions

General Form of Atomic Operation

(Removes Race Conditions)

- $\langle \text{await } (B) \ S \rangle$ *Called a conditional atomic action*
 - Atomically do (all of) the following:
 - Evaluate B
 - Wait until B is true
 - Execute S (an arbitrary statement list)
 - If the “await (B)” is omitted, S is immediately executed, but still atomically
 - $\langle \dots \rangle$ hides intermediate states and reduces number of histories

Example With Await

```
int x = 0  
co  
    x = x + 1  
//  
    <(await x == 1) x = x + 2>  
oc  
print x
```

This program will always output 3.
(It also serializes execution.)

Example with Atomic Operations

```
int x = y = 0, z
```

```
co
```

```
    <x = 1>; <z = x+y>
```

```
//
```

```
    <y = 2>; <z = x-y>
```

```
oc
```

What are the possible final values of x, y, and z?

How many histories are there?

Example with Atomic Operations

int x = y = 0, z

co

<x = 1>; <z = x+y>

//

<y = 2>; <z = x-y>

oc

Vars x and y must be 1 and 2; z can be -1 or 3

Number of histories is 6

General formula: $(n*m)! / (m!^n)$, where n is number of threads
and m is number of atomic actions per thread

Same Example, Removing Explicit Atomicity

```
int x = y = 0, z
```

```
co
```

```
    x = 1; z = x+y
```

```
//
```

```
    y = 2; z = x-y
```

```
oc
```

What are the possible final values of x, y, and z?

Same Example, Removing Explicit Atomicity

$x = k$ translates to a single Store

$z = x + y$ translates to Load, Load, Add, Store

$z = x - y$ translates to Load, Load, Subtract, Store

```
int x = y = 0, z
```

```
co
```

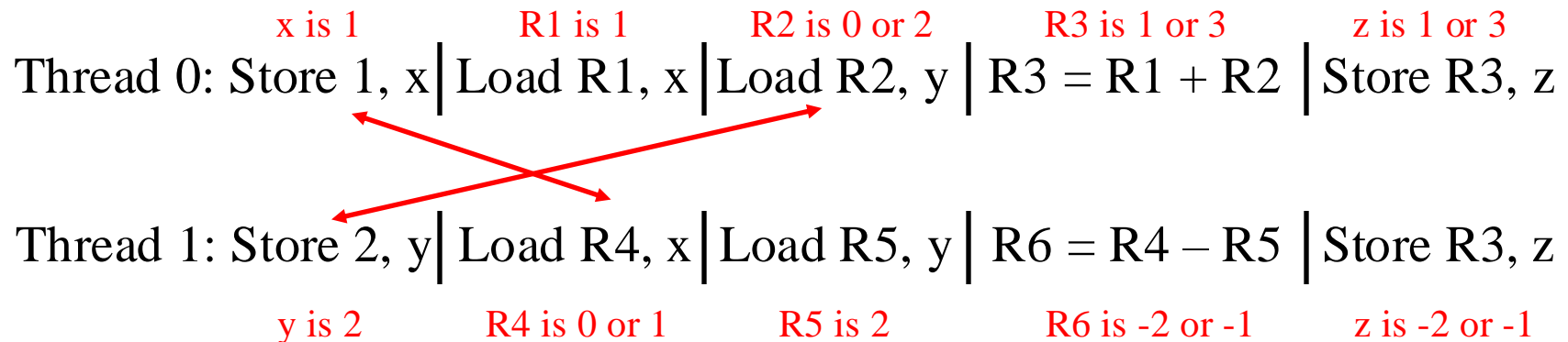
```
  x = 1; z = x+y
```

```
//
```

```
  y = 2; z = x-y
```

```
oc
```

One key point: Thread 0 can have loaded x and y and Thread 1 can be at any of its instructions. This is not the case in the first scenario, where $z = x+y$ and $z = x-y$ were atomic.



Same Example, Removing Explicit Atomicity

```
int x = y = 0, z  
co  
    x = 1; z = x+y  
//  
    y = 2; z = x-y  
oc
```

As before, x and y must be 1 and 2, but while z can still be -1 or 3 (as before), it can now also be -2 or 1

Note that enumerating all histories here is impractical

Via previous formula: $(10!) / (5!^2) == 252$ histories

(2 threads, 5 atomic actions each)

Scheduling policies for atomic actions

- Unconditional fairness
 - Every unconditional atomic action eventually executes
 - Round robin scheduling satisfies this
- Weak fairness: UC + conditional atomic actions execute if true and seen by the thread
- Strong fairness: UC + conditional atomic actions execute if true infinitely often

Scheduling policies: WF vs. SF

```
continue := true; try := false
```

```
co
```

```
  while (continue) { try := true ; try := false }
```

```
//
```

```
  <await (try) continue := false>
```

```
oc
```

- With weak fairness, program may never terminate; with strong fairness, it will terminate
 - Practical schedulers, however, are not strongly fair

Finding the max of an array in parallel

Sequential version

```
int max = MINVAL
int a[n]
for i = 0 to n-1 {
    if (a[i] > max)
        max = a[i]
}
```

Finding the max of an array in parallel

Incorrect parallel version

```
int max = MINVAL
int a[n]
co i = 0 to n-1 {
    if (a[i] > max)
        max = a[i]
}
```

Finding the max of an array in parallel

Correct but slow parallel version

```
int max = MINVAL
int a[n]
co i = 0 to n-1 {
    <if (a[i] > max)
        max = a[i]>
}
```

Finding the max of an array in parallel

Another incorrect parallel version

```
int max = MINVAL
int a[n]
co i = 0 to n-1 {
    if (a[i] > max)
        <max = a[i]>
}
```


Finding the max of an array in parallel

Correct, efficient (but complicated) parallel version

```
int max = MINVAL
```

```
int a[n]
```

```
co i = 0 to n-1 {
```

```
  if (a[i] > max) {
```

```
    < if (a[i] > max)
```

```
      max = a[i]
```

```
  }
```

```
}
```

Why do this?

