

SUPPORT VECTOR MACHINES

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AGENDA

- Motivating example for today's class
- Intro to SVMs
- Visual example
- Common terms in SVMs
- Assumptions and adv/disadv
- Implement in sklearn

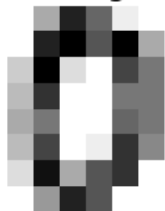
OBJECTIVES

- SVM big picture
- Understand the assumptions and strength/weaknesses of SVMs
- Implement SVMs in Python

MOTIVATING EXAMPLE: HANDWRITTEN DIGITS

PREDICTING HANDWRITING

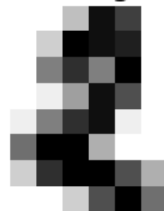
Training: 0



Training: 1



Training: 2



Training: 3



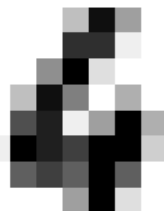
Prediction: 8



Prediction: 8



Prediction: 4



Prediction: 9



HOW WELL CAN YOU PREDICT HANDWRITTEN DIGITS? BANKS EXPECT AROUND 99%

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INTRO TO SUPPORT VECTOR MACHINES

WHY ARE SCIENTISTS SO BAD AT NAMES???

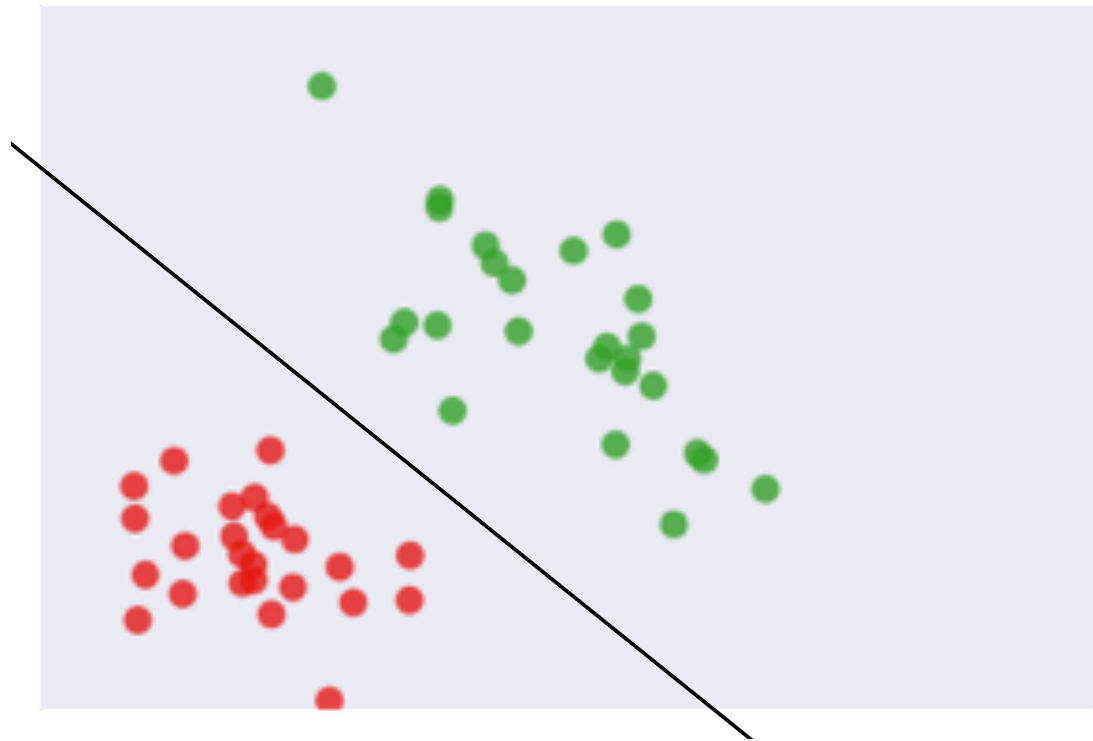
Not sure why anyone would call an algorithm a machine...

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*Suppose we have data with binary labels,
which we would like to classify*



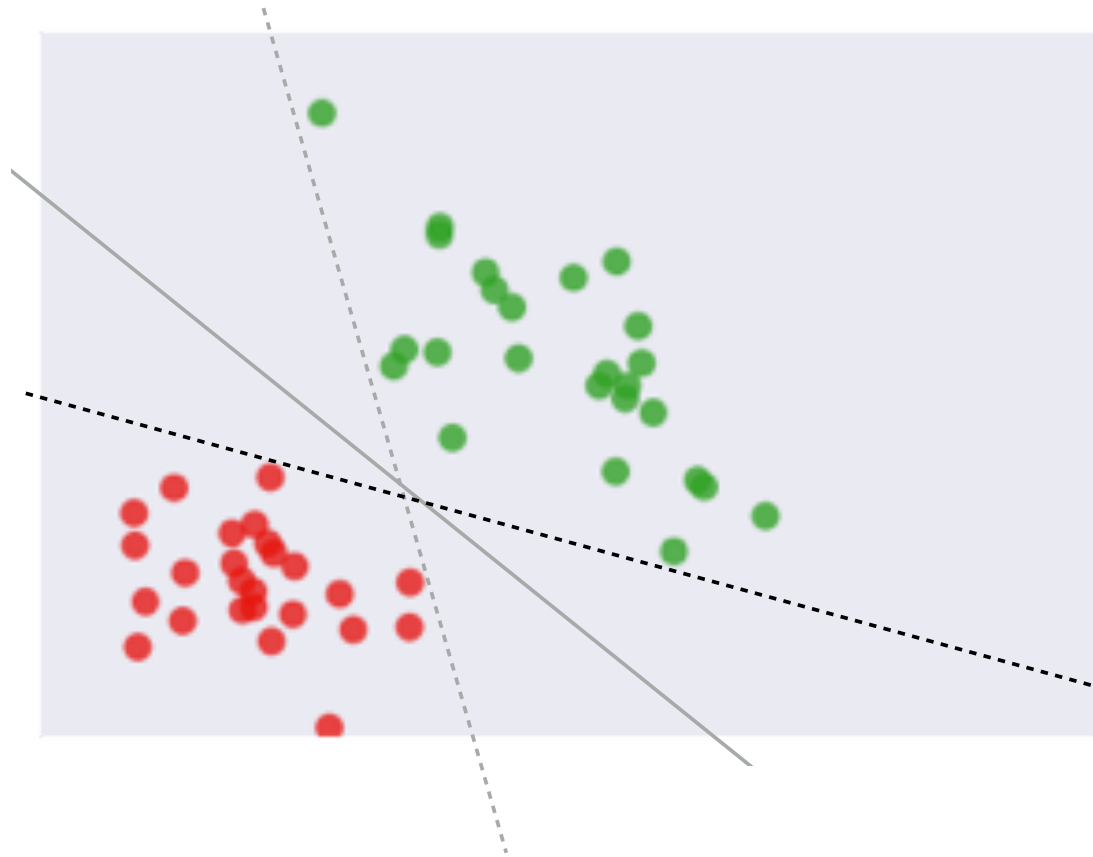
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*Suppose we have data with binary labels,
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*Recall that after fitting a classifier, we can draw
the **decision boundary** which separates the
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These boundaries depend on the specific optimization method. For example, logistic regression gives a different one than naive Bayes

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NOTE

These are all different ways of looking at the same problem.

Familiarity with more than one leads to deeper understanding!

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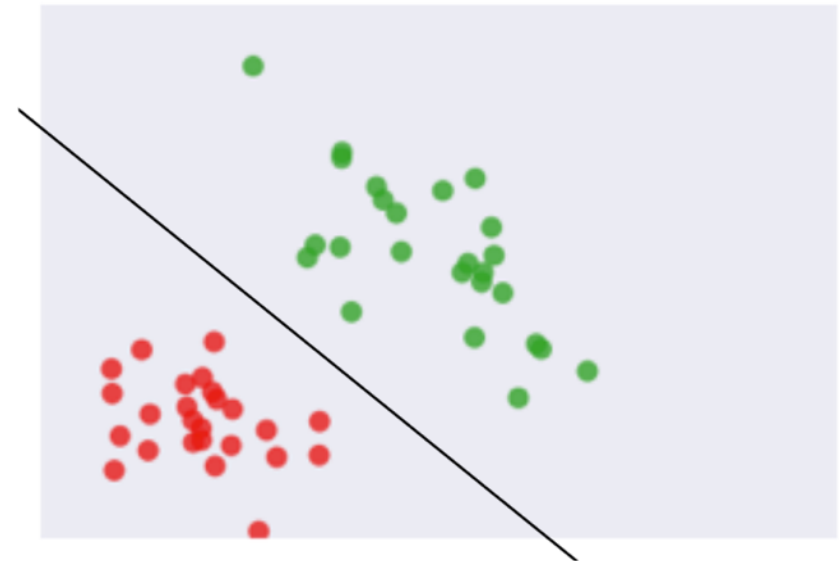
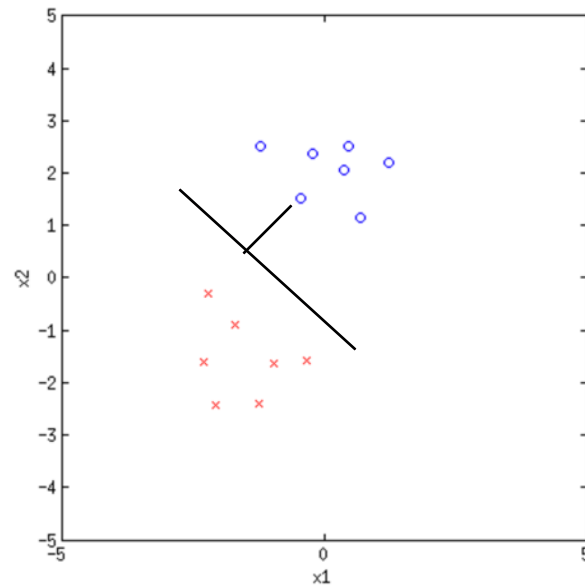
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Q: How is the decision boundary derived?

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*The generalization error is equated with the geometric concept of **margin**, which is the region along the decision boundary that is free of data points.*

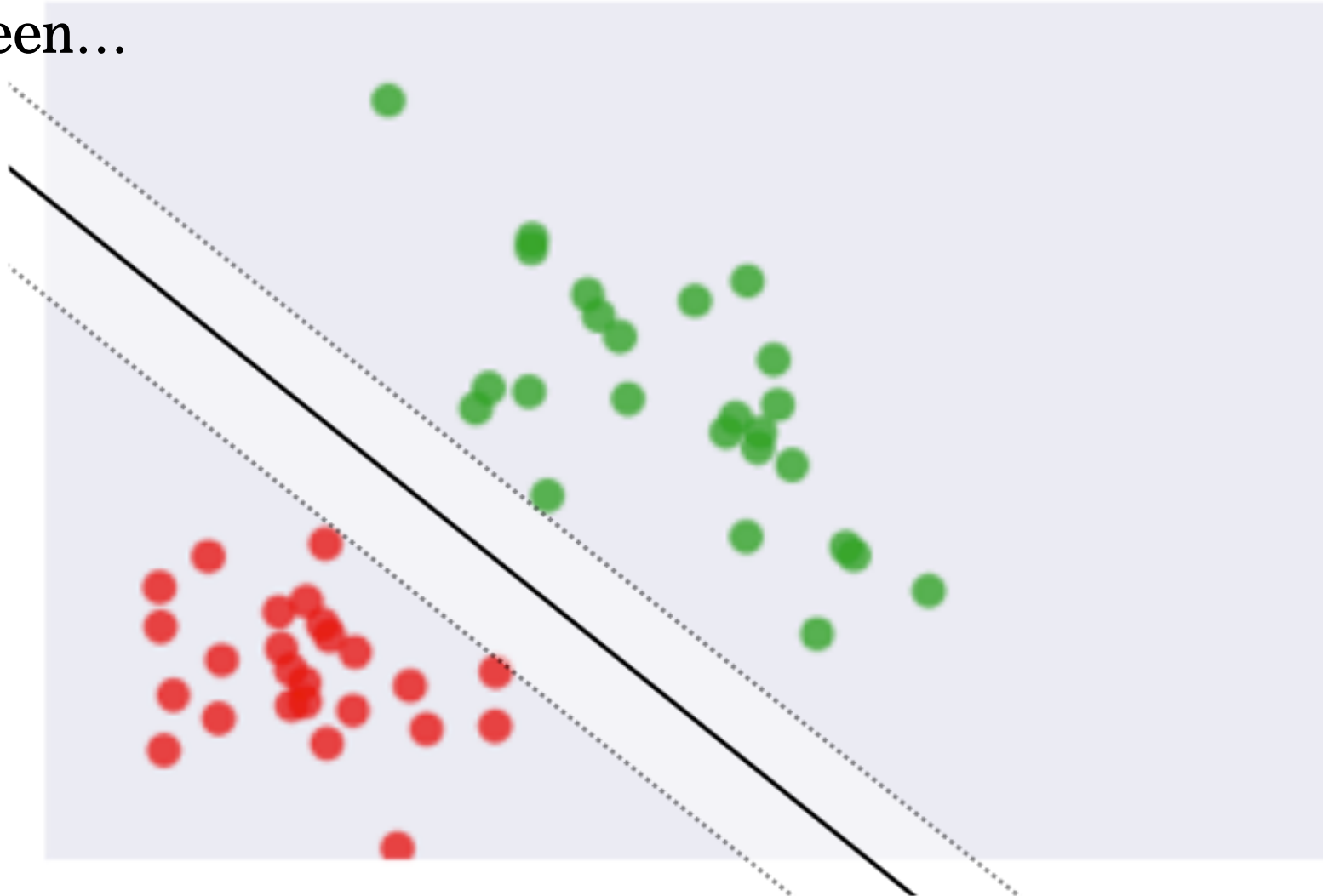
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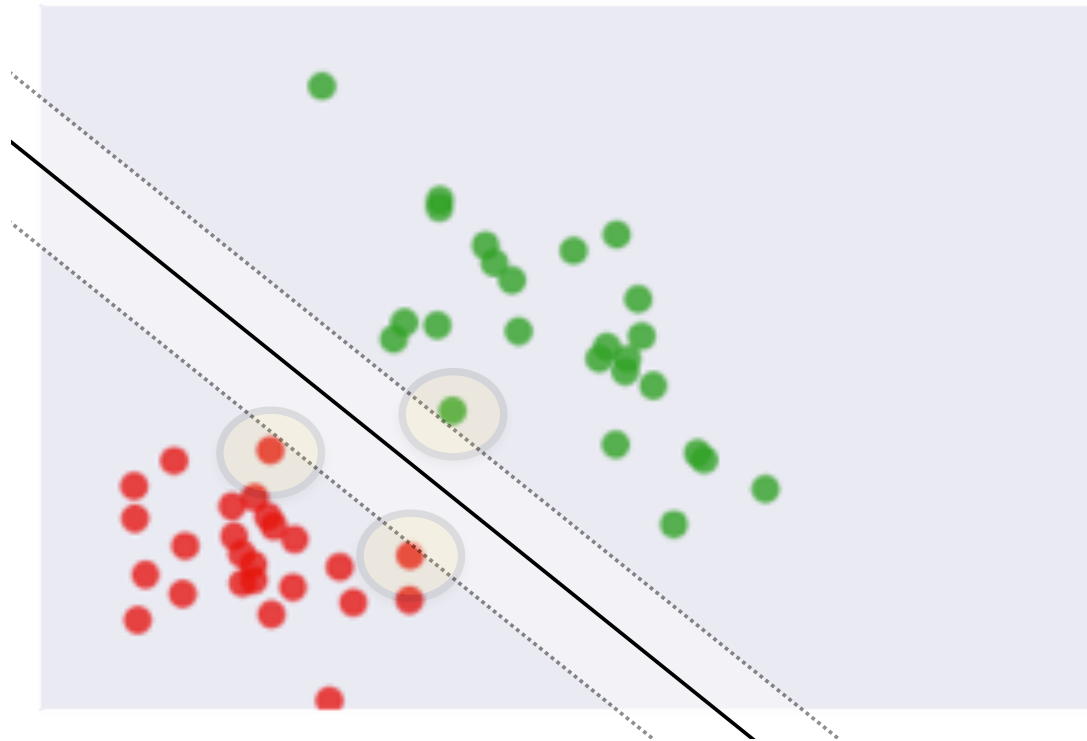
*The goal of an SVM is to create the linear decision boundary with the largest margin. This is commonly called the **maximum margin hyperplane**.*

MAXIMUM MARGINE HYPERPLANE

The space between...



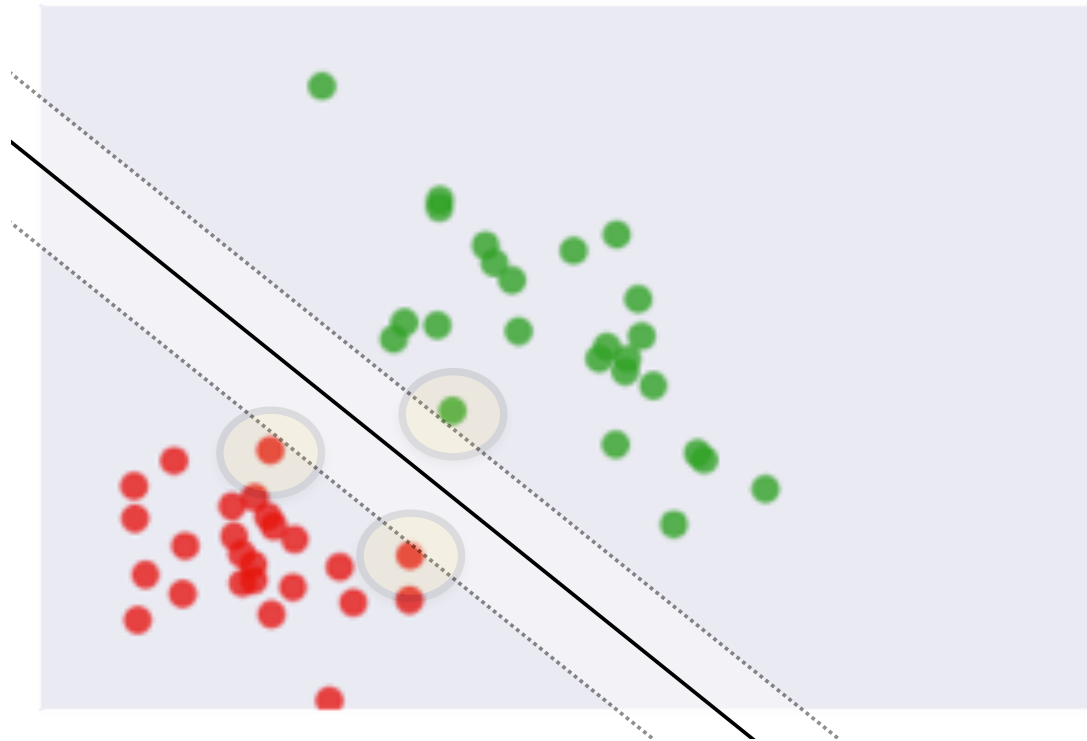
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Notice that the margin depends only on a subset of the training data – the points nearest to the decision boundary.

*These points are called the **support vectors**.*

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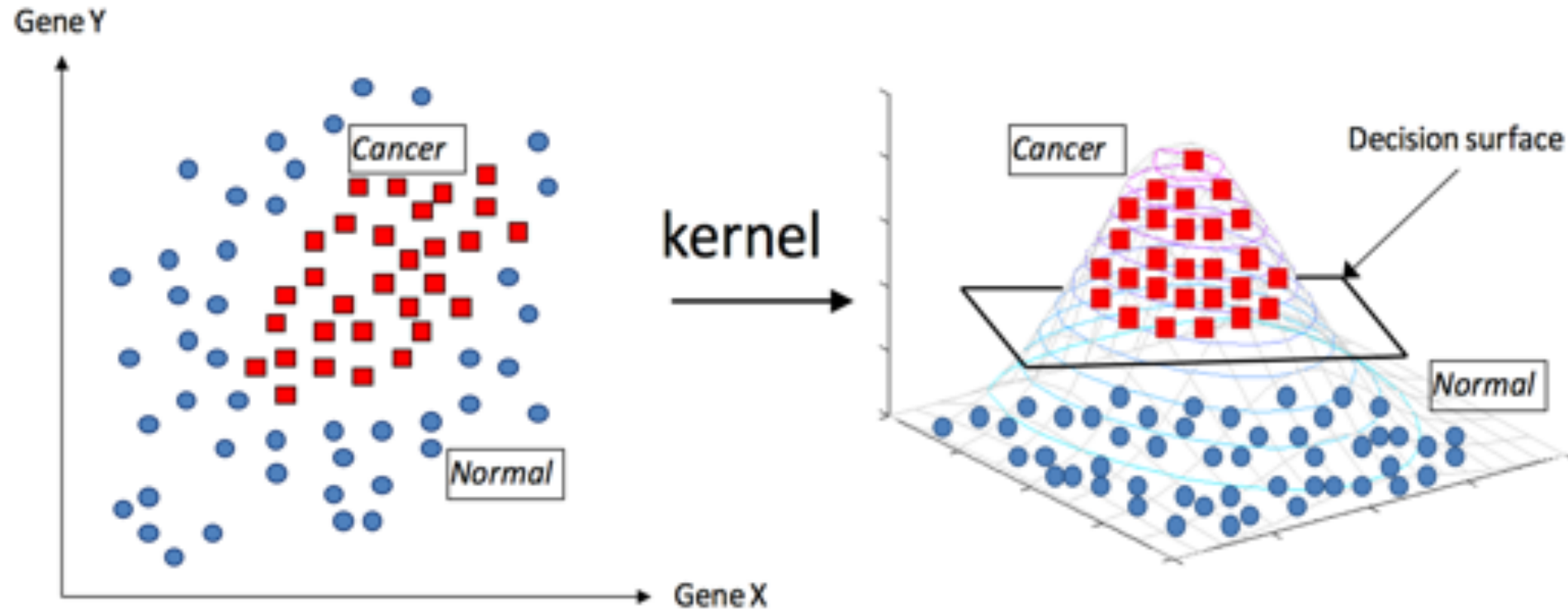
The other points don't affect the construction of the hyperplane at all!

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Q: If SVM is a linear classifier, how can you use it for nonlinear classification?

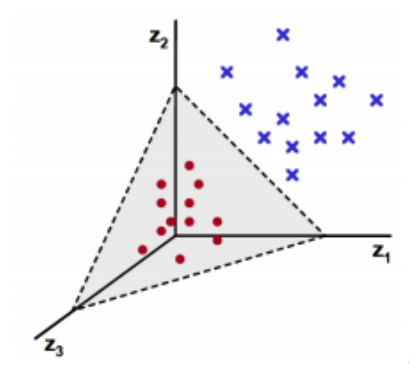
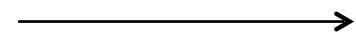
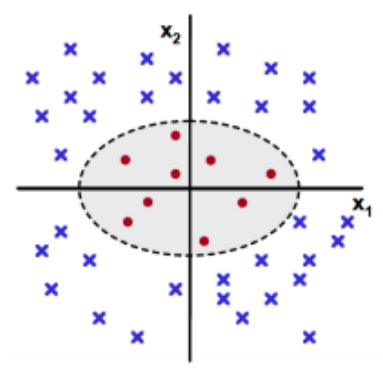
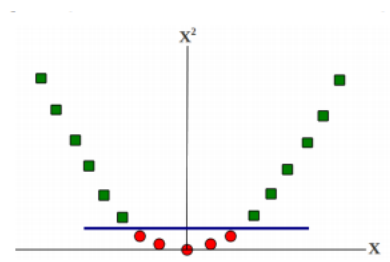
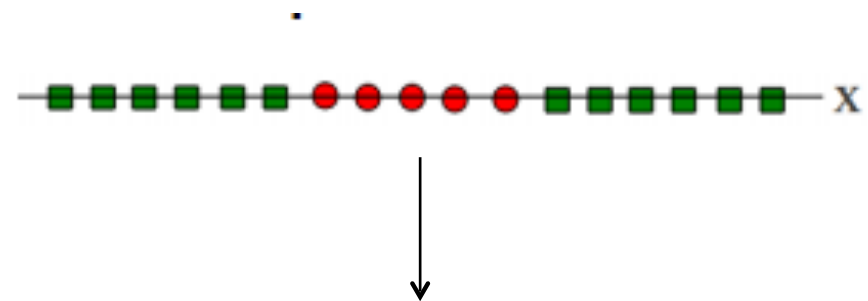
*A: Using a clever maneuver called the **kernel trick**.*

THE KERNEL TRICK

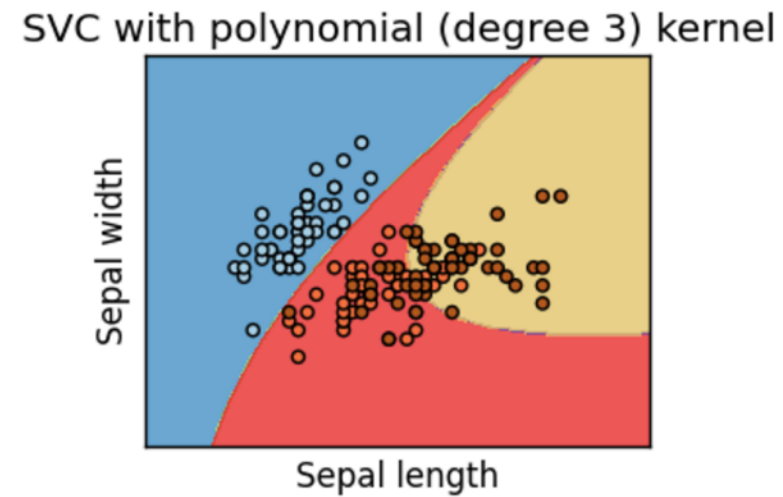
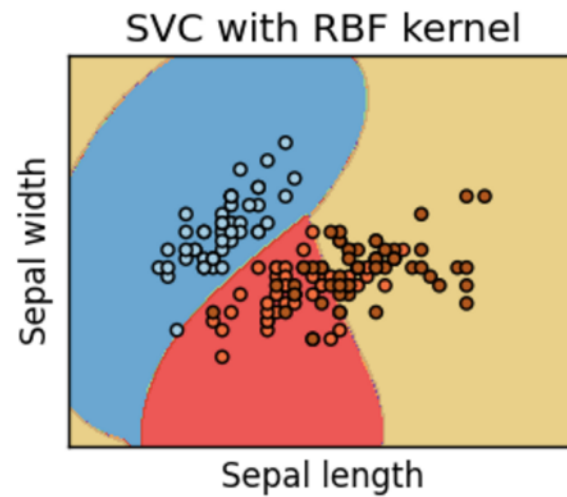
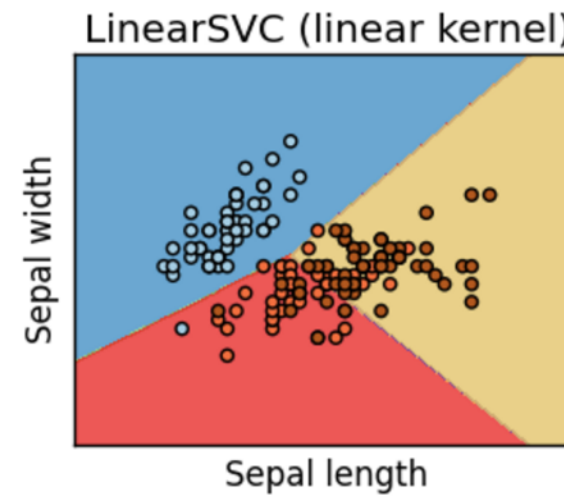
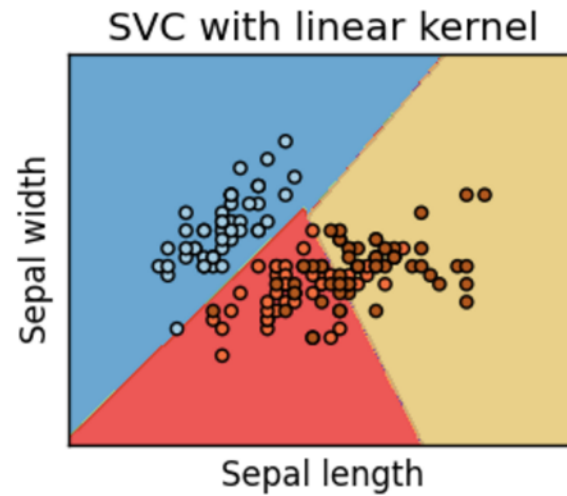


If a linear decision boundary cannot be found in the original space, we can map into a higher dimensional space and find the separating surface.

MORE DEMONSTRATIONS OF KERNEL TRICK



POPULAR TYPES OF KERNELS AVAILABLE IN SKLEARN



NONLINEAR CLASSIFICATION

some popular kernels:

linear kernel

$$k(\mathbf{x}, \mathbf{x}') = \langle \mathbf{x}, \mathbf{x}' \rangle$$

polynomial kernel

$$k(\mathbf{x}, \mathbf{x}') = (\mathbf{x}^\top \mathbf{x}' + 1)^d$$

Gaussian kernel

$$k(\mathbf{x}, \mathbf{x}') = \exp(-\gamma \|\mathbf{x} - \mathbf{x}'\|^2)$$

The hyperparameters d, γ affect the flexibility of the decision bdy.

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Q: What is a support vector machine?

A: A binary linear classifier whose decision boundary is explicitly constructed to minimize generalization error.

Quick review – who can define one of the underlined terms for us...?

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Q: What is a support vector machine?

A: A binary linear classifier whose decision boundary is explicitly constructed to minimize generalization error.

recall:

binary classifier – *solves two-class problem*

linear classifier – *creates linear decision boundary (in 2d)*

VISUAL EXAMPLE ON BOARD

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THE TERMS NO ONE EXPLAINS

KERNEL TRICK

THINK OF KERNEL TRICK AS ADDING TRANSFORMED FEATURES

<https://youtu.be/3liCbRZPrZA>

WTF IS A HYPERPLANE?

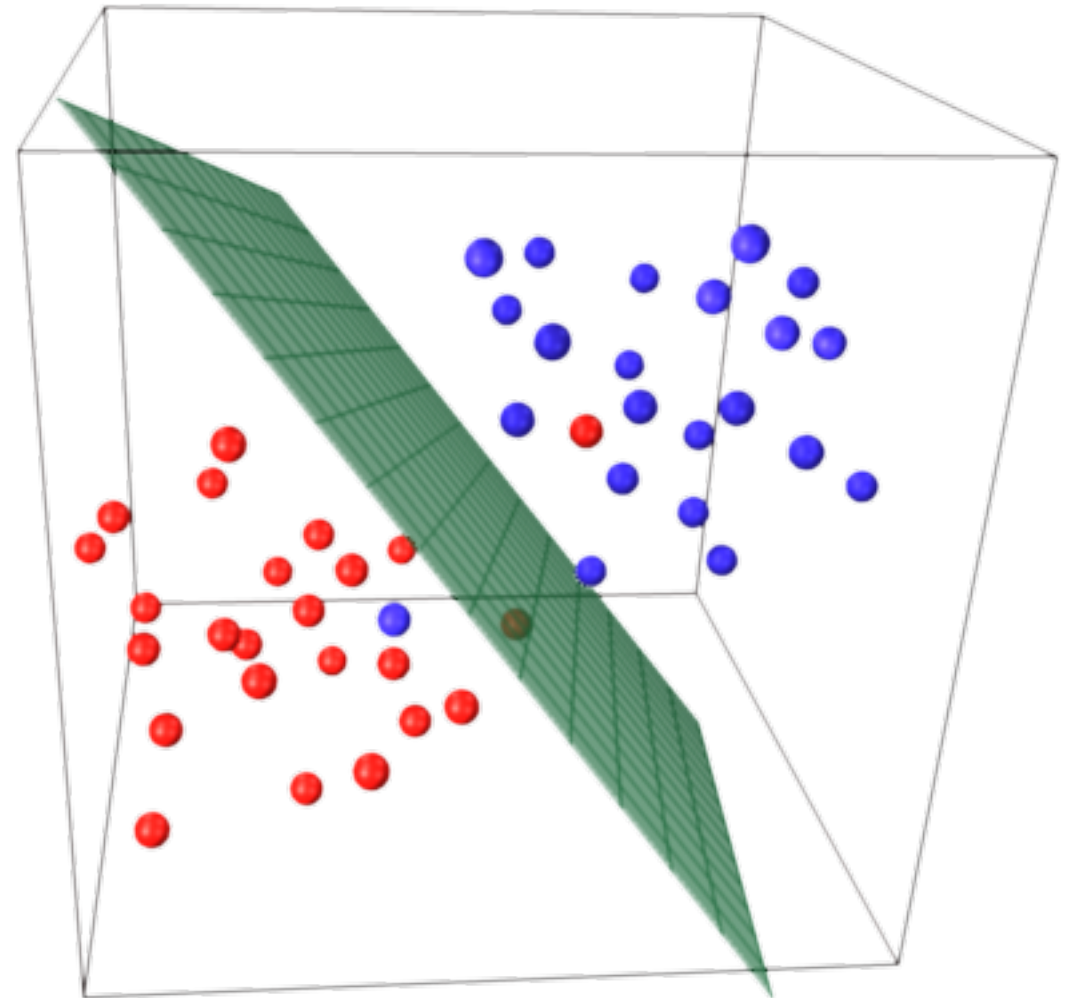
A HYPERPLANE IS A SMALLER WAY TO “CHOP” SOMETHING UP

Hyperplane of a line is a point

Think: a line is composed of points

Hyperplane of a plane is a line

Hyperplane of a cube is a plane



WHAT WE NEED TO DO SVM

ASSUMPTIONS NECESSARY FOR SUPPORT VECTOR MACHINES

- Features are scaled (since we're computing distance)
- Dataset isn't huge ($> 100k$ rows) and/or noisy
- We don't have significantly more features than observations
- Originally designed for binary data, so might not perform as well for multinomial

EVALUATING THE STRENGTHS AND WEAKNESSES OF SVMs

ADVANTAGES

- Extremely accurate when assumptions are met
- Solve non-linear decision boundaries
- No distribution assumptions or worries about feature correlation

DISADVANTAGES

- Extremely slow for anything medium-large sized
- Literal “black box” methodology
- Don’t bother trying to explain to your non-technical boss

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LET'S CODE!