

MTSCCLeav: a Multivariate Time Series Classification (MTSC)-based method for predicting human Dicer cleavage sites

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Abstract

Background: MicroRNAs (miRNAs) are small non-coding RNAs (ncRNAs) that regulate gene expression at the post-transcriptional level and hence play essential roles in diverse biological processes such as development and differentiation. The biogenesis of miRNAs requires Dicer, which is an enzyme, to cleave at specific sites on the precursor miRNAs (pre-miRNAs). These sites are called cleavage sites. Several machine learning approaches, such as ReCGBM and DiCleave, have been proposed to predict human dicer cleavage sites. Given an input sequence, these classifiers predict whether it contains a cleavage site. Despite the advances made, existing studies have several limitations. They have ignored the probabilities of the base pairs in the secondary structure predicted by RNA secondary structure prediction tools in the classification. Besides, they rely heavily on complicated feature engineering or opaque deep neural models. It results in a lack of generalizability and interoperability. Also, they have a long running time. There is a need for alternative modeling paradigms that are simple, fast, and provide comparable accuracy while offering better model transparency. **Results:** We propose a novel approach to predict human Dicer cleavage sites by reframing the task as a multivariate time series classification problem. To reframe, we have proposed different transformation schemes to convert the RNA sequence and the information about its secondary structure into time series. Hence, the data can be represented in the form of a multivariate time series. We also proposed a novel transformation scheme that involves the probabilities of the base pairs in the predicted secondary structure, which have been long ignored in

the literature. Computational experiments show that our proposed scheme can achieve comparable results using a simpler, intuitive model and less computation time. Besides, we test our models with perturbation-based experiments. We found that the regions or subsequences close to the cleavage sites and hence to the center of pre-miRNAs are essential to the predictions of the human dicer cleavage sites. Of note, the transformation of RNA data to time series allows the use of many state-of-the-art algorithms in the time series community and can relate some novel problem definitions in time series, such as motifs, discords, and chains, to the computational study of RNA data that paves novel ways using the well-established tools in the time series community.

Conclusion: Our proposed scheme allows us to study this problem in a new way. By transforming the RNA sequence and its secondary structure information into time series and using simple state-of-the-art time series classifiers, we obtain comparable or even superior performance in a simpler, faster way. We introduce a novel RNA transformation method that leverages the base pair probabilities. We also analyze the importance of the subsequences of the multivariate time series to the classification task, which hints that the regions that are close to the center are essential for this problem. Code is available at: <https://github.com/cyuab/time-series-classification-cleavage>.

Keywords: miRNA, Dicer Cleavage Site, Genomic signal processing (GSP), (Multivariate) time Series Classification (MTSC, TSC)

1 Background

One of the most important theories in molecular biology is the central dogma. It depicts the flow of genetic information [1, 2]. Proteins are the functional units. And the information stored in DNA is used to make them up. This process involves transcription and translation. Genes (segments of DNA encoding proteins) in DNA are used as templates for messenger RNAs (mRNAs) synthesis. This synthesis process is called transcription. An mRNA acts as a set of instructions to assemble a chain of amino acids, which form a linear polypeptide. This construction process is called translation. This chain is not yet functional. To become biologically active, this chain is folded into a specific three-dimensional structure, a proper configuration to perform desired functions. This process is called protein folding. And this folded polypeptide is called a functional protein, or a protein in short.

This whole process is remarkably similar to the process of running a computer program on a computer. The source code does not function by itself. The source code turns into assembly code (less human-readable code) first, and finally into an executable that does the work. In this analogy, DNA acts as the whole source code, in which genes refer to the functions in the code (segments of the code) [3]. mRNA is the assembly code. And the final product proteins are the running executables.

These mRNAs are called “coding RNAs” because they code for proteins. There are other genes in which the final product is the RNA molecule itself. They are called non-coding RNAs (ncRNAs). They function by themselves, such as by regulating gene

expression. Gene expression refers to the process by which the genetic information is transcribed into RNA, which may be translated into protein or ncRNAs. Two types of small ncRNAs are particularly important. They are microRNAs (miRNAs) and small interfering RNAs (siRNAs). Their discovery was recognized with the 2006 Nobel Prize in Physiology or Medicine¹, awarded for work completed only eight years prior [1]. They play essential roles in gene expression regulation.

In this study, we focus on miRNAs. They are small RNAs with a length of about 22 nt. They regulate gene expression post-transcriptionally [4]. A miRNA can regulate the expression of several proteins. They are essential in diverse biological processes, such as development, differentiation, and disease [5, 6]. Hence, it is of great value to understand the formation or the biogenesis of miRNAs. It involves the processing of primary miRNAs (pri-miRNAs). RNAs are 3D molecules, but it is hard to measure the 3D structure (tertiary structure). However, we can understand their behavior by analyzing their 1D sequence. It is easy to obtain through sequencing. A predicted secondary structure of a pri-miRNA's sequence is shown in Figure 1.

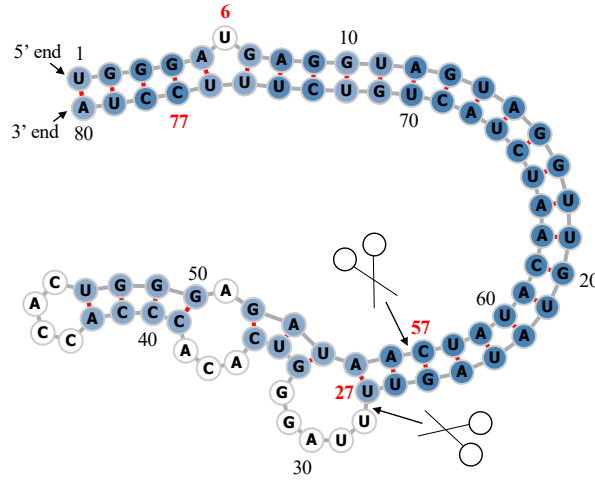


Fig. 1 Predicted secondary structure of the pri-miRNA “hsa-let-7a-1”². We denote the sequence as S . Experimental evidence suggests that the two deviated mature miRNAs are $UGA \cdots GUU$ and $CUA \cdots UUC$. They are $S[6 : 27]$ and $S[57 : 77]$. Since $S[6 : 27]$ ($S[57 : 77]$) is near the 5' (3') end, we call it “5p (3p) mature miRNA”. The starting and ending indices of these two subsequences are indicated in **bold and red**. It suggests that the two cleavage sites are the two bonds immediately after the 27th nucleotide and before the 57th nucleotide. The two scissors indicate the two cleavage sites. The color intensity of the nodes reflects their base pair probability in this predicted secondary structure configuration. The deeper the color, the higher the probability. The unpaired nodes are uncolored. The raw figure is generated by RNAfold web server³.

¹The Nobel Prize in Physiology or Medicine 2006 - NobelPrize.org: <https://www.nobelprize.org/prizes/medicine/2006/summary/> (Accessed on: 2025-06-13).
²Its miRBase entry: <https://mirbase.org/hairpin/MI0000060>. (Accessed on: 2025-06-12).
³RNAfold web server: <http://rna.tbi.univie.ac.at/cgi-bin/RNAWebSuite/RNAfold.cgi>. (Accessed on: 2025-06-12). The figure is viewed in forna. This view option can be chosen on the previous website.

Recall that a pri-miRNA contains a hairpin loop, also called a stem loop. It is located on the bottom left part of Figure 1. A microprocessor complex comprising Drosha and DGCR8 cleaves the pri-miRNA to form a precursor miRNA (pre-miRNA) inside the nucleus. The stem-loop is still preserved, but the two arms become shorter. The two arms refer to the two ends of the sequence. The sequence or strand has the end-to-end chemical orientation. One end is called 5' end, and the other is called 3' end. After that, the pri-miRNA is transported by Exportin 5 from the nucleus to the cytoplasm (i.e., outside the nucleus). It is further cleaved by an enzyme called Dicer [7]. The Dicer cleaves the stem-loop from the two arms at the two cleavage sites, shown as the two scissors in figure 1. We call the bond between two nucleotides along the strand that is cleaved by Dicer the Dicer cleavage site. The stem-loop is removed. It results in a short double-stranded miRNA molecule. Furthermore, these molecules may be subjected to additional trimming. Some nucleotides are removed from the two ends.

One strand of the resulting molecule is loaded into an RNA-induced silencing complex (RISC). This loaded strand guides the RISC to the target mRNA to silence it, and it results in gene silencing. This mechanism was discovered in the aforementioned Nobel Prize. This loaded strand is called the guide strand or mature miRNA. The other strand, which is called the passenger strand, is usually degraded. Note that both miRNA single strands, resulting from the unwinding of the double-stranded miRNA molecule, can become the guide strand. For example, "hsa-let-7a-1" has two guide strands or mature miRNA products.

Dicer plays an important role in the biogenesis of miRNAs. Hence, accurate cleavage of pre-miRNAs by Dicer is crucial for gene silencing. It is reasonable to argue that the structure of the pre-miRNAs informs Dicer about the cleavage process (i.e., where the cleavage sites are). A recent study shows that a particular secondary RNA structure, namely 22-bulge, enhances the accuracy of miRNA biogenesis experimentally [8].

It would be of great benefit to understand how Dicer selects cleavage sites from the neighborhood information near the cleavage sites. The neighborhood information refers to both the sequence and the secondary structure information. Studies [9–11] revealed that the secondary structures of the sequence are essential for cleavage site determination. Hence, to predict or classify whether a subsequence, extracted from pri-miRNAs, contains a cleavage site, we need to make use of both the sequence and secondary structure information.

1.1 Related work

Cleavage site prediction is not only defined on human dicer. Other examples include the calpain [12] and caspases [13], which are proteases that cleave proteins. Most of the studies about cleavage site prediction focus on protein cleavage sites. A wide range of computational methods has been applied to this topic, including support vector machine [13], deep neural networks [14]. In this study, we focus on human dicer cleavage sites. We review the studies on human dicer cleavage sites here. PHDcleav employed support vector machines (SVM), leveraging sequence and structure-based features [15] for the prediction. LBSIZEcleav improved upon it by considering the loop and bulge lengths [16]. [17] proposed an ensemble learning approach, using a gradient boosting

machine for better accuracy. [18] developed a deep learning model, namely DiCleave. This model used an autoencoder to learn the secondary structure embeddings of pre-miRNAs from all the species (not only human) presented in the miRBase database and leveraged this information in the prediction of human dicer cleavage sites. These methods begin with curated pre-miRNA sequences from the miRBase database. Their secondary structures are predicted using tools such as Quickfold or RNAfold. These secondary structures are stored in the dot bracket notation. They are also sequences. Patterns are extracted from these 2-tuple sequences. These patterns are called cleavage patterns. If the patterns contain a cleavage site, they are called positive patterns. If not, they are called negative patterns. They create the positive patterns by setting the cleavage sites at the middle of the patterns. Details of creating cleavage patterns would be discussed in Section 2. One exception is the follow-up work of [18], which creates the cleavage pattern by allowing cleavage sites to appear at any position within the pattern, instead of the middle [19]. Then, these works use different encoding schemes to represent these patterns and use different machine learning models to perform classification on them.

Despite the advances made, which mainly focus on the prediction accuracy, these models suffer several limitations. They rely heavily on complicated feature engineering and opaque deep learning models [18, 19]. It results in a lack of generalizability and interoperability. Also, they have a long running time. There is a need to design a simpler model so that it can be easily extended to other prediction tasks on RNA data. The RNA data in miRBase are sequence data. And the predicted secondary structure can also be presented as sequences. These sequences are strings because the entries are discrete. One of the ways to analyze string data is to transform it into time series data where the entries are continuous. By doing that, it builds a strong bridge between RNA analysis and time-series data mining. In response to that, we introduce the transformation method of RNA data to time series. In addition, we leverage the base pair probabilities in the predicted secondary structure in the transformation. To the best of our knowledge, this information has not yet been leveraged in the transformation. For the resulting time series data, we employ state-of-the-art convolution based classifiers, whose superiority has been experimentally tested on data from diverse domains [20]. Besides, we also perform perturbation-based experiments of classification on the resulting time series to investigate the importance of the subsequences to the prediction.

In summary, our contributions are shown as follows.

1. To the best of our knowledge, we are the first to frame the prediction of the cleavage sites, not only Dicer cleavage sites, as a multivariate time series classification problem. Time series modeling bridges bioinformatics and time series, which allows us to use state-of-the-art time series classification algorithms. Besides, the visualization power of time series allows us to understand the data more intuitively.
2. We propose making use of the base-pair probabilities in the predicted secondary structure in the prediction. To our surprise, this information has been ignored in the existing works. We leverage these base-pair probabilities in our novel transformation scheme for RNA sequence and its complementary sequence.

3. We conduct extensive experiments on different transformation methods and convolution-based classification methods.
4. We test our models with perturbation-based experiments. It shows that the regions that are close to the cleavage sites, the 3' arm and 5' arm that are close to the cleavage sites, as shown in figure 1, are important for the human dicer cleavage sites prediction. It agrees with the existing study [17].

2 Methods

Our main goal is to classify whether an input pattern contains a cleavage site of Dicer. We aim to transform the problem of predicting human dicer cleavage sites into a multivariate time series classification problem. This allows us to use algorithms from the time series community. It gives us more ways to analyze and visualize the data.

In this session, we first discuss how to prepare the dataset. We briefly review the definitions of time series and then propose transformation algorithms which allow us to transform the data into time series representations. After that, time series classifiers are discussed. Finally, we discuss the evaluation metrics used in this study.

2.1 Data preparation

We used miRBase database [21]⁴. The database consists of miRNA data from different organisms, such as humans, mice, and *C. elegans* [22]. Each data entry refers to a miRNA sequence, along with other properties such as name, accession which is the identifier used in miRBase, organism which indicates from which it comes, and information on its derivative miRNA products. We are interested in pri-miRNA in humans. The derivative miRNA products are the mature miRNAs. The database also annotates the location of the mature miRNA in the original pri-miRNA and states whether or not its existence has experimental evidence.

Accession	Name	Organism	Sequence	Mature miRNA 1	Mature miRNA 2
MI0000001	cel-let-7	Caenorhabditis elegans	UACAC...UUCGA	cel-let-7-5p 17:38 experimental	cel-let-7-3p 60:81 experimental
MI0000060	hsa-let-7a-1	Homo sapiens	UGGGA...UCCUA	hsa-let-7a-5p 6:27 experimental	hsa-let-7a-3p 57:77 experimental
MI0000114	hsa-mir-107	Homo sapiens	CUCUC...ACAGA	hsa-miR-107 50:72 experimental	NA
MI0000238	hsa-mir-196a-1	Homo sapiens	GUGAA...UUCAC	hsa-miR-196a-5p 7:28 experimental	hsa-miR-196a-1-3p 45:65 not experimental

Table 1 Selected representative records from miRBase. For the last two columns, there are three lines in each cell. The first line shows the name of this mature miRNA product. The second line shows its location in the original sequence. We use the $x : y$ notation to denote that this product is located from the x position to the y position in the original sequence. Both ends are inclusive.

⁴The website is www.mirbase.org, and the newest version of the database is Release 22.1 (Accessed on 2025-06-22).

The database contains 38589 miRNA records. Table 1 shows four representative records from miRBase database. We use it to elucidate our selection criteria. The records are rows in the table. We selected the records from humans (*Homo sapiens*). It resulted in 1917 records. In order to have the actual locations of the two cleavage sites in the pri-miRNA sequence that have experimental evidences, we selected the records with the two mature miRNAs resulting from cleavage at the 5p arm and the 3p arm that have experimental supports. According to the above selection criteria, only “MI0000060” would be selected.

Sequence	Secondary Structure (In Dot-bracket notation)
1 UGGGAUGAGGUAGUAGGUUGUAUAGUU 27 28 UUAGGGUCACACCCACCACUGGGAGAU 54 55 AACUAUACAACUACUGUCUUUCCUA 80	1 ((((((.((((((((((((((((((((27 28 UUAGGGUCACACCCACCACUGGGAGAU 54 55)))))))((((((((((((((((80
Base-pair probabilities sequence (the first 10 bases)	
1 (0.549, 0.946, 0.987, 0.987, 0.904) 5 6 (0.000 , 0.841, 0.974, 0.981, 0.890) 10	

Table 2 The whole sequence of “hsa-let-7a-1” with the locations of its two mature miRNAs and its predicted secondary structure by RNAfold. We have numbered each line with the starting and ending positions. The corresponding positions of the two mature miRNAs and the probability of the unpaired “U” are **bolded and in red**.

After the selection process, we selected 827 experimental validated pre-miRNA sequences together with its two mature miRNA products, and this formed our dataset. We use “hsa-let-7a-1” as our running example. The whole sequence of it and its necessary information for our downstream analysis is listed in Table 2.

2.1.1 Argument the dataset with Secondary Structure information

We want to use the domain knowledge about pre-miRNA sequences to improve our classifier’s accuracy. We leverage the secondary structure of these sequences to achieve this. Recall that a specific three-dimensional (3D) structure is required for DNA, RNA, and protein to perform functions [23]. However, finding these 3D structures using experimental methods such as X-ray crystallography or nuclear magnetic resonance (NMR) is costly and time-consuming. Hence, the prediction methods on such 3D structures are necessary and helpful for the downstream analysis. However, prediction of such 3D structures is difficult. One of the reasons is that there are some “nonconventional” base-pair interactions (e.g., A-G) that allow an RNA structure to fold into a 3D structure. It makes the search space for prediction much larger than, in the 2D case, the secondary structure. The local structure of the 3D structures, the secondary structures, only focus on the conventional (G-C and A-U) base-pair interactions [2]. It makes the prediction of the secondary structure easier and more applicable than predicting the 3D structure.

Secondary structure can still shed light on some of these functions in the structure-function relationships. We employ RNAfold from the ViennaRNA Package⁵. RNAfold

⁵The latest stable release is Version 2.7.0, accessed on 2025-06-22) to predict the secondary structure for a given pri-miRNA [24].

returns the secondary structure in the dot-bracket notation and a matrix for the base-pair probabilities. Equipped with the matrix, we can construct the base-pair probability sequence of the original sequence. For the unpaired nucleotide, its base pair probability is 0. The first ten entries of the probability sequence of our running example are shown in Table 2.

The secondary structure of “hsa-let-7a-1” in dot-bracket notation has been shown in Table 2. The visualization of it has been shown in Figure 1.

Definition 1 (Dot-bracket notation) Dot-bracket notation is a way of representing the secondary structure of the given string s . One of the following symbols is assigned to each base in s .

- Open parentheses (indicates that the base is paired with a complementary base further along in s .
- Close parentheses) indicates that the base is paired with a complementary base earlier in s .
- Dot . indicates that the base is unpaired.

2.1.2 Extract cleavage patterns

The locations of the two mature miRNAs on the main sequence indicate the probable locations of the two cleavage sites. The 5p cleavage site must be beyond and near the ending location of the 5p mature miRNA. For example, the ending position of the 5p mature miRNA for “hsa-let-7a-1” (i.e., “hsa-let-7a-5p”) is 27, as shown in Figure 1. So, the 5p cleavage site would be one of the bonds beyond the 27th nucleotide, as indicated by a scissor in the Figure. We deemed the immediate bond next to the ending position of the 5p mature miRNA the 5p cleavage site, with the knowledge that the actual cleavage site may not be this immediate bond but the nearby bonds after it. The same applies to the 3p cleavage site. It is at the immediate bond before the starting position of the 3p mature miRNA, which is 57.

We extract a 14-string (i.e., string with length = 14) with the cleavage site located at the center. The first 7 nt (nucleotide) before the center are **bolded and in red**. In our running example, it would be “**UAUAGUUUU**AGGU” for the 5p cleavage site and “**GAGAUAA**CUAUACA” for the 3p cleavage site. We call these 14-strings cleavage patterns as they contain the cleavage sites.

We can also generate non-cleavage patterns by selecting a 14-string with the center 6 nt away from the corresponding cleavage sites towards the corresponding mature miRNA [16, 17]. For example, the bond that is 6nt away from the 5p cleavage site towards 5p mature miRNA is the bond between 21st and 22nd nucleotides. It is based on the assumption that the dicer is less likely to cut the middle of the mature miRNA than the opposite side. So, in our example, the 5p non-cleavage pattern would be “**AGGUUGU**AUAGUUU”. The center of the 3p non-cleavage pattern is the bond between 62nd and 63rd nucleotides. The 3p non-cleavage pattern would be “**ACUAUACA**AUCUAC”.

In conclusion, for a given pri-miRNA, we can generate two cleavage patterns (positive samples) and two non-cleavage patterns (negative samples). For convenient,

we also call these four patterns simply the “four strings” of a given pri-miRNA. The four strings of “hsa-let-7a-1” are listed in Table 3. We could construct the

	5p-cleav	non-5p-cleav	3p-cleav	3p-non-cleav
Input strand	UAUAGUUUUAGGGU	AGGUUGUAUAGUUU	GAGAUAACUAUACA	ACUAUACAAUCUAC
Complementary strand	AUAUCAA_____UA	C_CUGUUGAUUAGU	UCUAAACAUAUCAA_	UGAUUUGUUGGAUG

Table 3 The first row shows the four strings of “hsa-let-7a-1”. Their complementary strands are shown in the second row.

complementary strand of each of the strand in the “four strings” by finding the corresponding paired base for each of the bases in the input strand by considering the secondary structure information. Bases refer to the nucleotides. We will use these two terms interchangeably. We use ‘_’ to denote the unpaired base in the complementary strand. For example, in Figure 1, the sub-string “UUAGG” in the 5p-cleavage pattern “UAUAGUUUUAGGGU” are unpaired while other bases do pair with some bases in the complementary strand, the resulting complementary strand is “AUAUCAA_____UA”. Note that the five underscores indicate that “UUAGG” is unpaired. There is a loop/ budge there.

The strand and its complementary strand together can then encode the loop/ budge information. We call the four original input strands and the constructed four complementary strands together as the “eight strings” of the input pre-miRNA, also shown in Table 3. We are now ready to transform the “eight strings” into time series. Of note, we also have the base pair probability sequences that are of the same length as these strings.

2.2 Time Series

Definition 2 (Time Series) A time series $T = t_1, t_2, \dots, t_n$ is a sequence of real-valued numbers with length $= n$.

A short contiguous region of T is called a subsequence.

Definition 3 (Subsequence) A subsequence $T(i : j)$ of a time series T is a shorter time series that starts from position i and ends at position j . Formally, $T(i : j) = t_i, t_{i+1}, \dots, t_j$, where $1 \leq i \leq j \leq n$.

The above two notations are also used to represent string and its subsequence.

2.2.1 Transform strings into time series

Both strings and time series are temporal sequences. The order in a sequence usually represents time ordering. The only difference between strings and time series is the behavioral attributes [25]. For strings, also known as words, a y-value is a symbol from a predefined set called the alphabet. Thus, we also refer to the symbols as letters.

For example, the alphabet is $\{A, C, G, T\}$ in the DNA string, while $\{A, C, G, U\}$ in the RNA string. For time series, a y-value is a scalar number. The number can be an integer or a real number. The important point is that they are naturally ordered. The “greater than” and “smaller than” are well-defined. There is no ordering in the alphabet unless some external domain knowledge is introduced.

In the bioinformatics community, the study of applying signal processing techniques to genomic data, which includes DNA and RNA strings, is called “Genomic Signal Processing” (GSP) [26]. In the field of GSP, the time series representations of DNA strings are called DNA numeric representations (DNR). Many DNRs have been proposed in the field of GSP, with applications including identifying protein-coding regions in DNA sequences [27], biological sequence querying [28], and finding similarities between DNA sequences [29]. We noted that DNA strings and RNA strings are the same from the computational point of view. They are simply strings with different alphabets. Recall that the alphabet of DNA is $\{A, C, G, T\}$ and that of RNA is $\{A, C, G, U\}$. Many transformation methods designed for DNA are applicable to RNA by simply substituting T for U . In this study, our default alphabet is $\{A, C, G, U\}$. One of the simple, if not the simplest, transformations is to map the letters in the alphabet into integer numbers without considering any domain knowledge about the nucleotides. This method belongs to a group of methods called the “Single value mapping” approach [26, 30–33]. One single value is assigned to each of the letters.

A more reasonable approach in this category is to employ the domain knowledge during assignments. For example, [34] employs the atomic number of each nucleotide as the transformed values where $\{78, 70, 58, 66\}$ is assigned to $\{G, A, C, T\}$ respectively. [35] uses “electron-ion” interaction potential representation (EIIP) as such values. These values are $\{0 : 0806, 0 : 1260, 0 : 1340, 0 : 1335\}$. Our goal is to transform the input strand and its complementary strand into two time series and aim to capture the information of these sequences and the secondary structure. So, we need to employ the complementarity property during the transformation [36]. Recall that in the base-pairing rules, “A” pairs with “U”⁶ to form two hydrogen bonds while “G” pairs with “C” to form three hydrogen bonds. Hence, “A” (“C”) can be regarded as the “inverse” of “U” (“G”) ⁷. We can preserve these base-pairing rules in the time series representation by assigning A (G) and U (C) opposite values. The time series of the complementary strand would then be a flipped version along the y-axis of the original strand. We group the four nucleotides by their chemical structures. ‘A’ and ‘G’ have a two-ring structure. They are purines. ‘U’ and ‘C’ have a one-ring structure. They are pyrimidines. We put ‘A’ and ‘G’ (‘U’ and ‘C’) in the same group. These two groups would be on the two sides of the number line with zero in the middle.

Now the only remaining question before assigning $\{-2, -1, +1, +2\}$ to $\{A, C, G, U\}$ is which nucleotide in the same group we should assign a larger absolute value. We adopted the “A = 2 and G = 1” assignment. The reasoning is as follows. The main goal of this manuscript is to find the two cleavage sites on the pre-miRNA. The cleavage sites are the bonds along the strands, the phosphodiester linkages, or bonds. After this pre-miRNA is cleaved, the resulting double-stranded miRNA molecule is unwound to

⁶In DNA, “A” pairs with “T”

⁷Recall that we call “-1” as the inverse of “1” and vice versa under addition in Algebra.

form the guide strand and the passenger strand. The stability of the double strand would affect the unwinding process. There are three hydrogen bonds in C-G pairs and two in A-U pairs. Hence, C-G pairs are more stable than A-U pairs. This means that in regions with more C-G pairs, the double strands hold more tightly, and the unwinding process is less likely to occur than in regions with more A-U pairs. So, we want to emphasize the existence of such less stable A-U pairs in the double strands in our time series representations. We assign A and U with larger absolute values than those of G and C. With this reasoning, we propose the our first transformation method, in row 1 in Table 4. We can also transform each RNA sequence into a multivariate time series using grouped binary encoding, where nucleotides are grouped into (A, U) and (G, C). Each time series channel indicates the presence of a nucleotide from the respective group at each time step. The kind of methods release our assumption that A (U) has a larger absolute value than G (C). Noted that each channel may differ in length depending on group-specific occurrences, we propose two variation. The first one allows the output to be variable-length sequences per channel. The second one always return two resulting sequences with fixed length. These methods are rows 2 and 3 in Table 4.

Instead of looking at the values in the time series one by one, we can accumulate the values assigned to each nucleotide. The “Single value mapping” and its two variations allows us to focus on the absolute values of the alphabet and ignore what has happened in the past. The “cumulative version” allows us to focus on analyzing the “trend” such as increasing and decreasing, by accumulating what has happened in the past. We show the “Cumulative mapping” in row 4 in the Table 4. We can also use two channels to represents the time dynamics of a nucleotide group in “Cumulative mapping”. For the output, we can allow variable-length channels or fixed-length channels. These two variations has been shown in rows 5 and 6 in the table.

Of note, some our proposed transformations are lossy. Lossy transformation refers to a transformation that does not allow us to restore the original string from the new time series representation. Methods 2, 4 and 5 are lossy. It does not guarantee that lossless transformation performs better than lossy transformation for the downstream analysis because lossy transformation may provide better generalization.

2.2.2 Incorporating base-pair probabilities

We propose a novel time series transformation for RNA sequences incorporating the predicted secondary structures and the base-pair probabilities. Recall that RNA secondary structure prediction algorithm is a kind of RNA folding algorithm. The RNA folding algorithms attempt to solve a harder problem: predicting the 3D structure of a given RNA sequence. Meanwhile, the RNA secondary structure prediction algorithm returns the predicted secondary structure of a given RNA sequence, a planar graph such as the minimum free energy structure. It also returns a probability matrix for the base-pair probabilities, which denote the probabilities of pairing one nucleotide with the other nucleotide. In our case, the bases in an RNA sequence will be either paired up with another base in the same sequence or remain unpaired. For example in Figure 1, the 1st base ‘U’ is paired up with the 80th base ‘A’. The 6th base ‘U’ is unpaired. The width and height of the probability matrix are the length of the RNA

sequence because it is a pairwise matrix. From this matrix, we can construct the base-pair probability time series s^P of the whole sequence s . The unpaired base will have very small probabilities in any base-pair. In our formulation, we deemed these small probabilities as 0 to emphasize that these bases are deemed to be unpaired in the resulting predicted secondary structure.

Table 5 incorporates the base-pair probability time series into the transformation methods listed in Table 4. We use the first ten bases of the sequence of “hsa-let-7a” as a running example. It is denoted as s and its corresponding probability time series is denoted as s^P .

2.2.3 Accumulating from the beginning of the pre-miRNA sequence

In cumulative encoding, it would return different result if we choose different starts for the accumulation. We can start the accumulation from the beginning of the full sequence or just from the beginning of the selected subsequence. The first one preserves the global context by recording the previous counts of the nucleotide up to the selected subsequence. It can be useful when early elements (those before the selected subsequence) influence later interpretation. In other words, the previous nucleotides may affect the chemical property of the selected subsequence. The second one only focus on the local history by ignoring the global history. The time series encoded in this way are more consistent. It is useful if the the previous nucleotides does not affect the chemical property of the selected subsequence.

Considering the time series representation of $s(6 : 10) = UUGAU$ of the running example s in Table 5, the “Cumulative” transformation without base-pair probability of it starting at the beginning of s (i.e., s_1) would be $t(7 : 11) = -3, -5, -7, -6, -4, -6$. If we start the “Cumulative” at the beginning of $s(6 : 10)$ (i.e., $s(6)$), the resulting time series would be $0, -2, -4, -3, -1, -3$. Note that these two time series have the same trend, but they start at different values. The first one starts at -3 while the latter one starts at 0 . We name the first approach as “Global Cumulative” and the later one as “Local Cumulative”.

Figure 2 shows how to use the discussed notion in transformations.

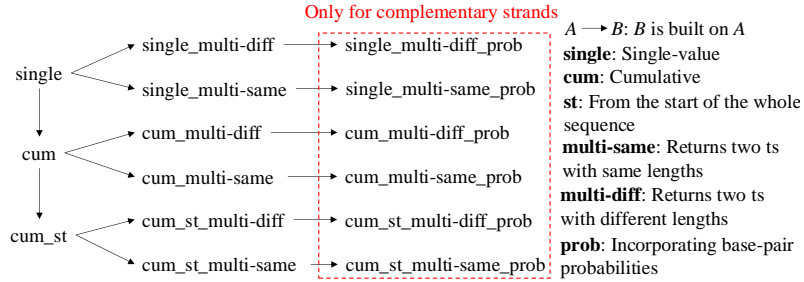


Fig. 2 Relationship of the proposed transformation methods. ts stands for time series.

2.3 Time series classification

In this study, we propose a novel approach to predict human dicer cleavage sites by reframing this task as a multivariate time series classification problem. We have introduced how to transform the information of the sequence, the secondary structure, and its probability sequence into a time series. In this session, we will introduce the time series classifier used in this manuscript.

There are many classifiers defined on time series data, including distance-based, feature-based, interval-based, shapelet-based, dictionary-based, convolution-based, and deep learning-based. Also, two or more of the above approaches can be combined, namely hybrid approaches [20]. For a complete review of time series classification, we would like to direct the readers to [20, 37, 38] for details. As our downstream classifier, we adopt convolution-based classifiers for their simplicity and accuracy. The convolution-based approaches leverage a simple design pattern, which is the over-production of features, followed by a selection strategy. In the first step, a large number of features about the instances are produced. The features encode the characteristics of the instances and the computational complexity of it is low. Then, a simple classifier such as a linear ridge classifier determines which features are most useful.

2.3.1 Convolution based classification

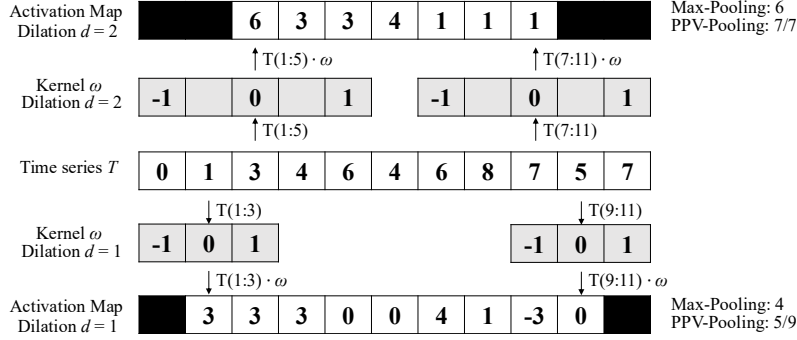


Fig. 3 Convolution

2.4 Evaluation

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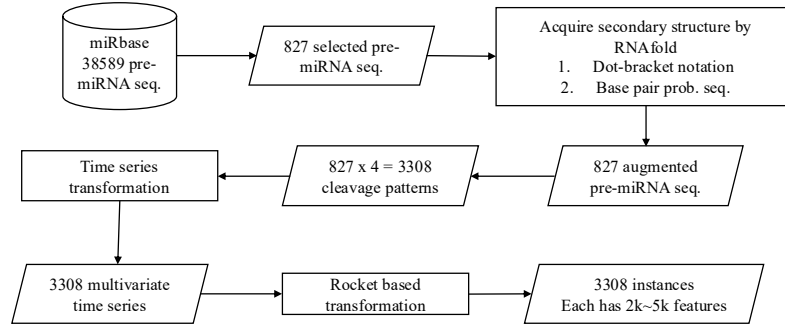


Fig. 4 Pipeline. Cylinder: Database / Dataset, Rectangle (Box): Process / Task / Transformation, Parallelogram: Input / Output, Rounded Rectangle (Capsule shape): Model / Component

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	Name	Numeric representation	Example for $s = G, A, G, A, U, A, A, C, U, A$
1	Single value mapping	for $i = 1$ to $ s $: $t_i = \begin{cases} 2 & \text{if } s_i = A \\ 1 & \text{if } s_i = G \\ -1 & \text{if } s_i = C \\ -2 & \text{if } s_i = U \end{cases}$ return t	$t = 1, 2, 1, 2, -2, 2, 2, -1, -2, 2$
2	Grouped variable-length channel mapping	$j = 1, k = 1$ for $i = 1$ to $ s $: $t_j^1 = \begin{cases} 1, & j = j + 1 & \text{if } s_i = A \\ -1, & j = j + 1 & \text{if } s_i = U \end{cases}$ $t_k^2 = \begin{cases} 1, & k = k + 1 & \text{if } s_i = G \\ -1, & k = k + 1 & \text{if } s_i = C \end{cases}$ return $t^1[1:j], t^2[1:k]$	$t^1 = 1, 1, -1, 1, 1, -1, 1$ $t^2 = 1, 1, -1$
3	Grouped fixed-length channel mapping	for $i = 1$ to $ s $: $t_i^1 = \begin{cases} 1, & j = j + 1 & \text{if } s_i = A \\ -1, & j = j + 1 & \text{if } s_i = U \\ 0 & \text{otherwise} \end{cases}$ $t_i^2 = \begin{cases} 1, & k = k + 1 & \text{if } s_i = G \\ -1, & k = k + 1 & \text{if } s_i = C \\ 0 & \text{otherwise} \end{cases}$ return t^1, t^2	$t^1 = 0, 1, 0, 1, -1, 1, 1, 0, -1, 1$ $t^2 = 1, 0, 1, 0, 0, 0, 0, -1, 0, 0$
4	Cumulative mapping	$t_1 = 0$ for $i = 1$ to $ s $: $t_{i+1} = \begin{cases} t_i + 2 & \text{if } s_i = A \\ t_i + 1 & \text{if } s_i = G \\ t_i - 1 & \text{if } s_i = C \\ t_i - 2 & \text{if } s_i = U \end{cases}$ return t	$t = 0, 1, 3, 4, 6, 4, 6, 8, 7, 5, 7$
5	Cumulative grouped variable-length channel mapping	$t_1^1 = 0, t_1^2 = 0$ $j = 1, k = 1$ for $i = 1$ to $ s $: $t_{j+1}^1 = \begin{cases} t_j^1 + 1, & j = j + 1 & \text{if } s_i = A \\ t_j^1 - 1, & j = j + 1 & \text{if } s_i = U \end{cases}$ $t_{k+1}^2 = \begin{cases} t_k^2 + 1, & k = k + 1 & \text{if } s_i = G \\ t_k^2 - 1, & k = k + 1 & \text{if } s_i = C \end{cases}$ return $t^1[1:j], t^2[1:k]$	$t^1 = 0, 1, 2, 1, 2, 3, 2, 3$ $t^2 = 0, 1, 2, 1$
6	Cumulative grouped fixed-length channel mapping	$t_0^1 = 0, t_0^2 = 0$ for $i = 1$ to $ s $: $t_{i+1}^1 = \begin{cases} t_i^1 + 1 & \text{if } s_i = A \\ t_i^1 - 1 & \text{if } s_i = U \\ t_i^1 & \text{otherwise} \end{cases}$ $t_{i+1}^2 = \begin{cases} t_i^2 + 1 & \text{if } s_i = G \\ t_i^2 - 1 & \text{if } s_i = C \\ t_i^2 & \text{otherwise} \end{cases}$ return t^1, t^2	$t^1 = 0, 0, 1, 1, 2, 1, 2, 3, 3, 2, 3$ $t^2 = 0, 1, 1, 2, 2, 2, 2, 2, 1, 1, 1$

Table 4 Time series transformation for RNA string s . The ending index in indexing is exclusive.

	Name	Numeric representation	Example for $s = C, -, C, U, G, U, U, G, A, U$ $s^P = 0.843, 0.000, 0.807, 0.807, 0.793, 0.914, 0.982, 1.000, 0.999, 0.999$
1	Single value mapping	for $i = 1$ to $ s $: $t_i = \begin{cases} 2 \cdot s_i^P & \text{if } s_i = A \\ 1 \cdot s_i^P & \text{if } s_i = G \\ -1 \cdot s_i^P & \text{if } s_i = C \\ -2 \cdot s_i^P & \text{if } s_i = U \\ 0 & \text{if } s_i = - \end{cases}$ return t	Without base-pair probability: $t = -1, 0, -1, -2, 1, -2, -2, 1, 2, -2$ With base-pair probability: $t = -0.843, 0.000, -0.807, -1.614, 0.793, -1.829, -1.963, 1.000, 1.999, -1.998$
2	Grouped variable-length channel mapping	$j = 1, k = 1$ for $i = 1$ to $ s $: $t_j^1 = \begin{cases} 1 \cdot s_i^P, & j = j + 1 & \text{if } s_i = A \\ -1 \cdot s_i^P, & j = j + 1 & \text{if } s_i = U \\ 0, & j = j + 1 & \text{if } s_i = - \end{cases}$ $t_k^2 = \begin{cases} 1 \cdot s_i^P, & k = k + 1 & \text{if } s_i = G \\ -1 \cdot s_i^P, & k = k + 1 & \text{if } s_i = C \end{cases}$ return $t^1[1:j], t^2[1:k]$	Without base-pair probability: $t^1 = 0, -1, -1, -1, 1, -1$ $t^2 = -1, -1, 1, 1$ With base-pair probability: $t^1 = 0.000, -0.807, -0.914, -0.982, 0.999, -0.999$ $t^2 = -0.843, -0.807, 0.793, 1.000$
3	Grouped fixed-length channel mapping	for $i = 1$ to $ s $: $t_i^1 = \begin{cases} 1 \cdot s_i^P, & j = j + 1 & \text{if } s_i = A \\ -1 \cdot s_i^P, & j = j + 1 & \text{if } s_i = U \\ 0 & \text{otherwise} \end{cases}$ $t_i^2 = \begin{cases} 1 \cdot s_i^P, & k = k + 1 & \text{if } s_i = G \\ -1 \cdot s_i^P, & k = k + 1 & \text{if } s_i = C \\ 0 & \text{otherwise} \end{cases}$ return t^1, t^2	Without base-pair probability: $t^1 = 0, 0, 0, -1, 0, -1, -1, 0, 1, -1$ $t^2 = -1, 0, -1, 0, 1, 0, 0, 1, 0, 0$ With base-pair probability: $t^1 = 0.000, 0.000, 0.000, -0.807, 0.000, -0.914, -0.982, 0.000, 0.999, -0.999$ $t^2 = -0.843, 0.000, -0.807, 0.000, 0.793, 0.000, 0.000, 1.000, 0.000, 0.000$
4	Cumulative mapping	$t_1 = 0$ for $i = 1$ to $ s $: $t_{i+1} = \begin{cases} t_i + 2 \cdot s_i^P & \text{if } s_i = A \\ t_i + 1 \cdot s_i^P & \text{if } s_i = G \\ t_i - 1 \cdot s_i^P & \text{if } s_i = C \\ t_i - 2 \cdot s_i^P & \text{if } s_i = U \\ t_i & \text{if } s_i = - \end{cases}$ return t	Without base-pair probability: $t = 0, -1, -1, -2, -4, -3, -5, -7, -6, -4, -6$ With base-pair probability: $t = 0.000, -0.843, -0.843, -1.650, -3.265, -2.471, -4.300, -6.263, -5.264, -3.265, -5.263$
5	Cumulative grouped variable-length channel mapping	$t_1^1 = 0, t_1^2 = 0$ $j = 1, k = 1$ for $i = 1$ to $ s $: $t_{j+1}^1 = \begin{cases} t_j^1 + 1 \cdot s_i^P, & j = j + 1 & \text{if } s_i = A \\ t_j^1 - 1 \cdot s_i^P, & j = j + 1 & \text{if } s_i = U \\ t_j^1, & j = j + 1 & \text{if } s_i = - \end{cases}$ $t_{k+1}^2 = \begin{cases} t_k^2 + 1 \cdot s_i^P, & k = k + 1 & \text{if } s_i = G \\ t_k^2 - 1 \cdot s_i^P, & k = k + 1 & \text{if } s_i = C \end{cases}$ return $t^1[1:j], t^2[1:k]$	Without base-pair probability: $t^1 = 0, -1, -2, -3, -2, -3$ $t^2 = 0, -1, -2, -1, 0$ With base-pair probability: $t^1 = 0.000, -0.807, -1.722, -2.703, -1.704, -2.703$ $t^2 = 0.000, -0.843, -1.650, -0.857, 0.143$
6	Cumulative grouped fixed-length channel mapping	$t_0^1 = 0, t_0^2 = 0$ for $i = 1$ to $ s $: $t_{i+1}^1 = \begin{cases} t_i^1 + 1 \cdot s_i^P & \text{if } s_i = A \\ t_i^1 - 1 \cdot s_i^P & \text{if } s_i = U \\ t_i^1 & \text{otherwise} \end{cases}$ $t_{i+1}^2 = \begin{cases} t_i^2 + 1 \cdot s_i^P & \text{if } s_i = G \\ t_i^2 - 1 \cdot s_i^P & \text{if } s_i = C \\ t_i^2 & \text{otherwise} \end{cases}$ return t^1, t^2	Without base-pair probability: $t^1 = 0, 0, 0, 0, -1, -1, -2, -3, -3, -2, -3$ $t^2 = 0, -1, -1, -2, -2, -1, -1, -1, 0, 0, 0$ With base-pair probability: $t^1 = 0.000, 0.000, 0.000, 0.000, -0.807, -0.807, -1.722, -2.703, -2.703, -1.704, -2.703$ $t^2 = 0.000, -0.843, -0.843, -1.650, -1.650, -0.857, -0.857, -0.857, 0.143, 0.143, 0.143$

Table 5 Time series transformation for RNA complementary string s with its probability time series s^P . The ending index in indexing is exclusive.