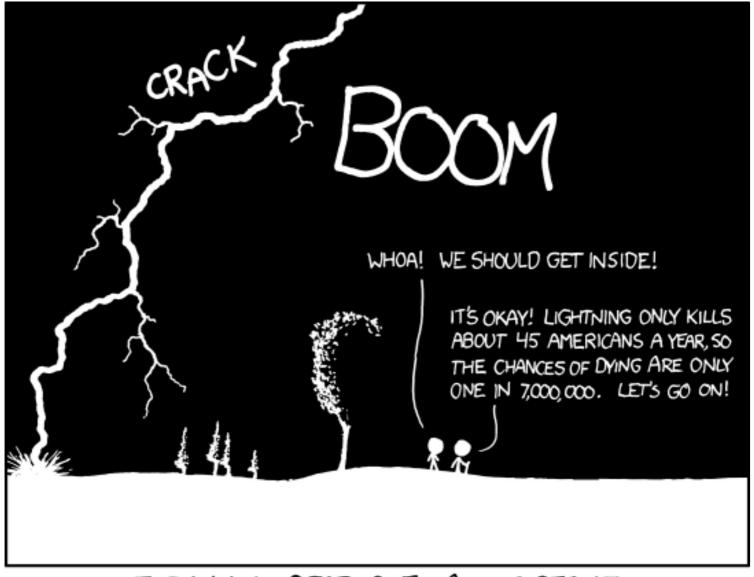
Categorical Variables

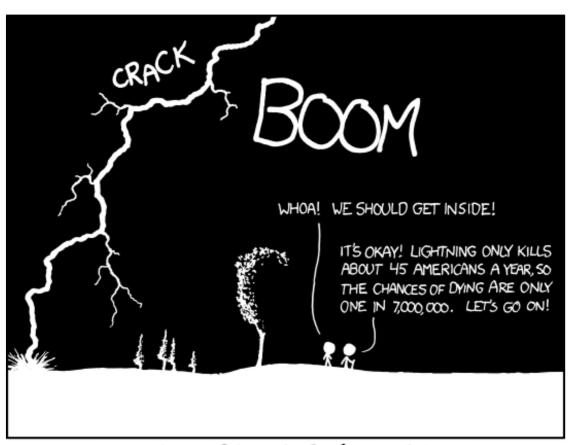
Biology 683



Heath Blackmon

THE ANNUAL DEATH RATE AMONG PEOPLE WHO KNOW THAT STATISTIC IS ONE IN SIX.

Conditional Probability



THE ANNUAL DEATH RATE AMONG PEOPLE WHO KNOW THAT STATISTIC IS ONE IN SIX.

	Knows the statistic	Doesn't know the statistic
Dies from lightning strike	43	2
Doesn't die from lightning strike	258	328,000,000

Analyzing Proportions

The experiment boils down to this:

- Your subjects have some alternative outcomes
- Each individual has some probability of each outcome
- You are trying to find the conditions that impact that probability

When would this type of problem come up in the biological sciences?

A test to determine whether or not the observed proportion adheres to the expected proportion under the null hypothesis

Some possible uses:

- Are frogs equally likely to be right or left handed?
- Is the sex ratio half male and half female?
- Are the offspring phenotypes a 3:1 ratio?
- Do some beetles win more fights?

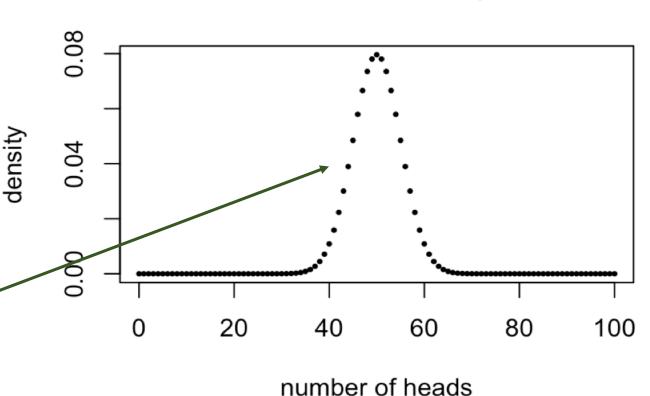
As in most statistical tests, a test statistic is compared to a distribution

In this case, the test statistic is just the observed number (number of right-handed toads, number of females in the population, number of fights won)

Note that this test is only appropriate when there are two categories of individuals and your hypothesis allows you to provide a probability of the outcomes.

With the binomial test our null hypothesis is the probability of one of the two outcomes. This probability and the number of observations defines the distribution we will compare our observation to.

Distribution when the null is 50% and we have 100 observations



use a simulation to see if you can replicate this curve

Lets look at an example with sex ratio. You are hybridizing closely related species (with XY sex chromosomes) so you know Haldane's rule states that the males might be more rare. When you survey the offspring you find 23 males out of 65 offspring. Does this result support Haldane's rule occuring in your system?

binom.test(x = 23, n = 65, p = .5)

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```
binom.test(x = 23, n = 65, p = .5)
```

```
data: 23 and 65 number of successes = 23, number of trials = 65, p-value = 0.02481
```

binom.test has an argument alternative

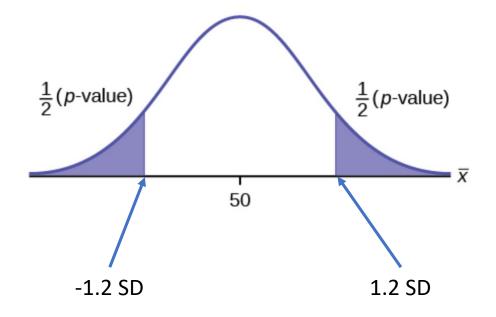
```
alternative indicates the alternative hypothesis and must
be one of "two.sided", "greater" or
"less". You can specify just the initial letter.
```

```
binom.test(x = 23, n = 65, p = .5, alternative = "t") # p-value 0.02481 binom.test(x = 23, n = 65, p = .5, alternative = "g") # p-value 0.99370 binom.test(x = 23, n = 65, p = .5, alternative = "l") # p-value 0.01241
```

Alternative = two.sided

What is the probability that I would see a skew in the sex ratio this great or greater.

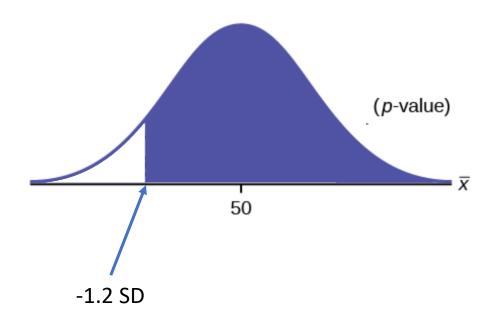
In this case our observed number of males was -1.2 standard deviations from the mean. So our p-value is the area under the curves above 1.2SD and below -1.2SD.



Alternative = greater

What is the probability that I would see a larger number of males.

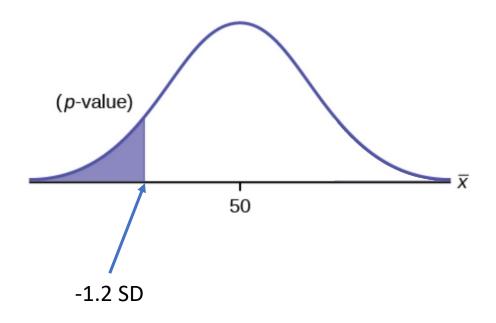
In this case our observed number of males was -1.2 standard deviations from the mean. So our p-value is the area under the curves above -1.2SD.



Alternative = less

What is the probability that I would see this many or fewer males.

In this case our observed number of males was -1.2 standard deviations from the mean. So our p-value is the area under the curves below -1.2SD.



If before we collected this data we wanted to answer the question: "Are males more rare than females?" Then we have an apriori hypothesis that we should see fewer males than females so we could justify using this more powerful test.

Reporting the Results

Our offspring ratio shows a significantly fewer males than would be expected under a 1:1 sex ratio (0.35, 95% CI: 0.24-0.48, binomial test, n = 65, p < 0.025).

Reporting the Results

This populations shows a significantly fewer males than would be expected under a 1:1 sex ration (0.35, 95% CI: 0.24-0.48, binomial test, n = 65, p < 0.025).

For very small p-values, we just say that p is very small (< 0.001 or < 0.0001).

Most journals/subdisciplines will have conventions about how certain tests are reported.

Most journals italicize mathematical variables, so n and p would be italicized. They also normally would be lower case.

This test compares the observed number in each category to expectations based on the null hypothesis (if there are only two categories, it approximates the binomial test with probability of 50%)

It can also be used to test for independence of two variables, and then it is called a contingency $\chi 2$ -test.

We will use data from the Titanic and see if some females were more likely to survive than others.

Female adults on the Titanic			
	Survived	Died	
1st	140	4	
2nd	80	13	
3rd	76	89	
Crew	20	3	

To calculate the statistic we just sum up the standardized deviations from the expected values in each category.

$$\chi^{2} = \sum_{i=1}^{n} \frac{(O_{i} - E_{i})^{2}}{E_{i}}$$

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Female adults on the Titanic			
	Survived	Died	total
1st	140	4	144
2nd	80	13	93
3rd	76	89	165
Crew	20	3	23
total	74.4%	25.6%	

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Expected		
	Survived	Died
1st	.744 x 144	.256 x 144
2nd	.744 x 93	.256 x 93
3rd	.744 x 165	.256 x 165
Crew	.744 x 23	.256 x 23

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1st	107	37	
2nd	69	24	
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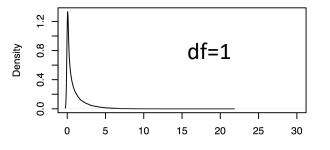
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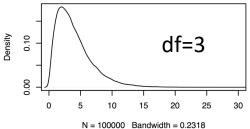
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1st	140	4
2nd	80	13
3rd	76	89
Crew	20	3

Expected		
	Survived	Died
1st	107	37
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$$\chi^2 = 117$$

The shape of the chi square distribution depends on the degrees of freedom (df).





Female adults on the Titanic			
Survived Died			
1st	140	4	
2nd	80	13	
3rd	76	89	
Crew	20	3	

$$df = (4-1)(2-1)$$

 $df = 3$

Pearson's Chi-squared test

Practice Problems

- Evaluate sex ratio of in two frog crosses (both have XY sex determination). We cross species 1 and 2 and obtain 126 offspring 52 of them are male.
- 1) what is our null hypothesis going to be?
- 2) does this result support Haldane's rule?
- 3) what is the minimum number of offspring required to detect a significant deviation from our expectation under the null hypothesis?

 We cross females from one strains of fish with males from another strain. A proportion of our offspring have an unusual color pattern.

	Males	Females
Color Pattern Present	31	4
Color Pattern Absent	68	89

- 1) What null might we construct for this data?
- 2) Can we reject this null?
- 3) What might we infer from this data?