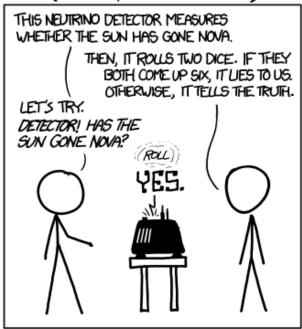
Bayesian Stats and MCMC

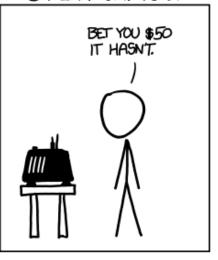
DID THE SUN JUST EXPLODE? (IT'S NIGHT, SO WE'RE NOT SURE.)



FREQUENTIST STATISTICIAN:

THE PROBABILITY OF THIS RESULT HAPPENING BY CHANCE IS \$\frac{1}{36}\$ = 0.027. SINCE P<0.05, I CONCLUDE THAT THE SUN HAS EXPLODED.

BAYESIAN STATISTICIAN:



Frequentist approach

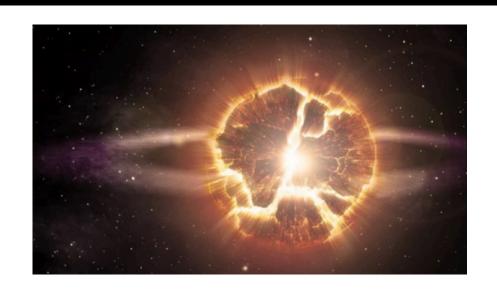
You have a null hypothesis and calculate the probability of observing your data under that hypothesis.

Null: The sun has not exploded

$$Pr(det \ yes \mid sun \ is \ ok) = 0.027 = \frac{1}{6} \times \frac{1}{6}$$

this is less than the typical \propto level of 0.05 so we reject the null that the sun is ok.

Bayesian approach



$$Pr(A|B) = \frac{Pr(B|A) \times Pr(A)}{Pr(B)}$$

$$Pr(nova|det\ yes) = \frac{Pr(det\ yes|nova) \times Pr(nova)}{Pr(det\ yes)}$$

$$Pr(nova|det\ yes) << 0.00000000037 \frac{1 \times 0.0000000001}{0.027}$$

Bayesian approach

Imagine a genetic mutation present in 1 person per 100,000. If you take a test that correctly returns a positive result 99.9% of the time when someone is infected but has a false positive rate of 0.5%.

How likely are you to have the disease if you test positive?

Should you be concerned if you test positive?

Bayes' theorem provides a natural way to think about this.

Lets do this!

Bayesian approach

$$Pr(inf|pos.test) = \frac{Pr(pos.test|inf) \times Pr(inf)}{Pr(pos.test)}$$

$$Pr(inf|pos.test) = 0.001 = \frac{0.999 \times 0.00001}{0.00501}$$

Which means that you have only a 0.1% chance of having the disease even if you test positive.

What if your doctor noticed a symptom that made them give you this test what changes?

Priors

$$Pr(A|B) = \frac{Pr(B|A) \times Pr(A)}{Pr(B)}$$

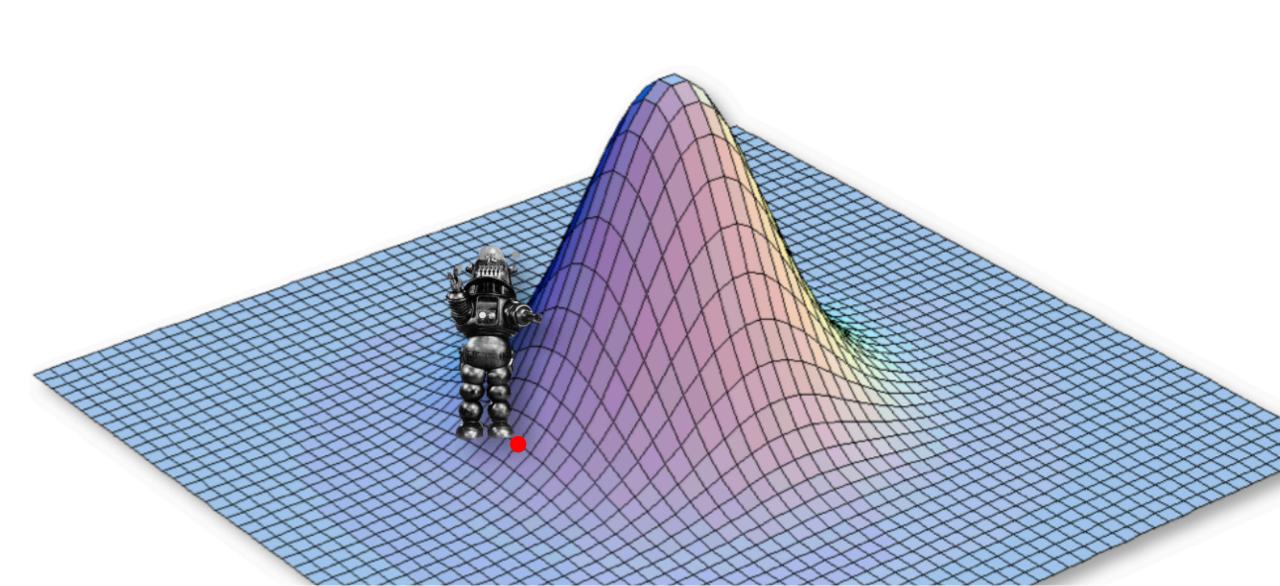
Pr(A) this is the prior. It is powerful because it allows you to incorporate previous knowledge into your analysis, but it can lead to very bad inference if you are careless.

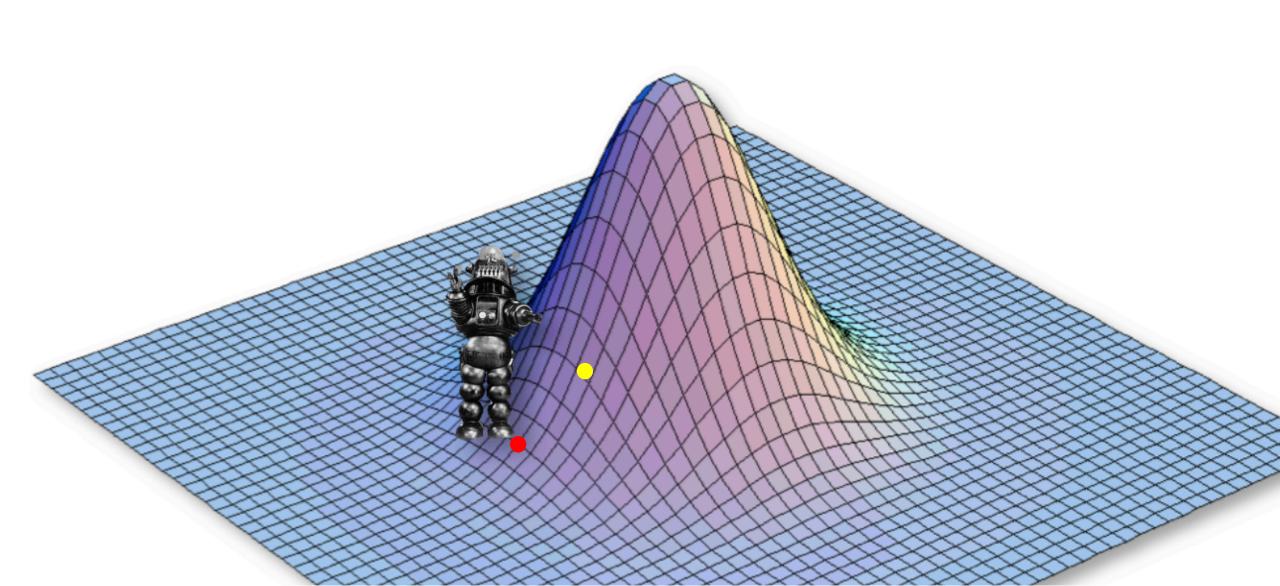
In practice our models are quite complex with many parameters we would like to estimate. Each of these has its own prior distribution. The way that we explore the space of solutions is using an MCMC.

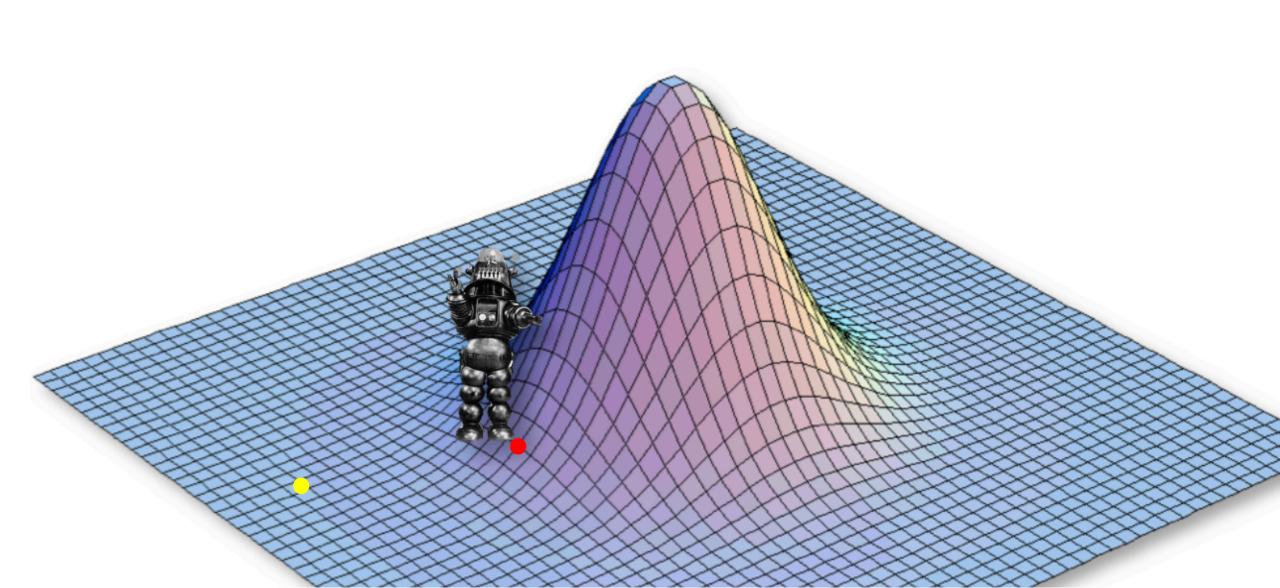
1) Pick an arbitrary starting point

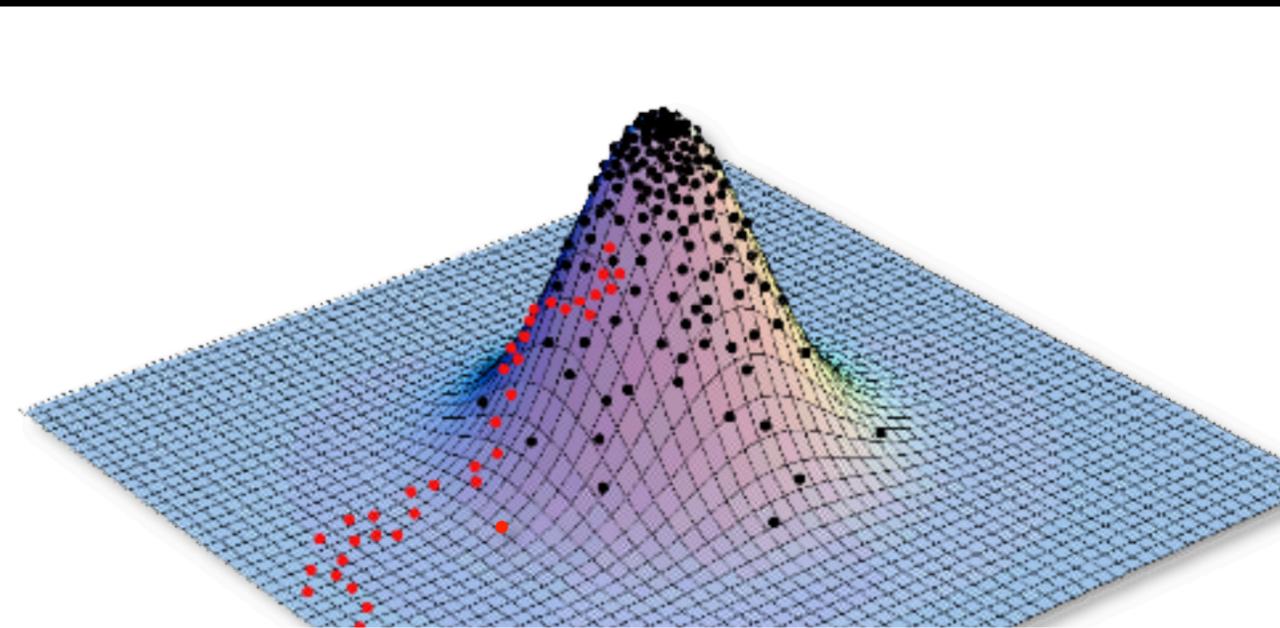
 $Pr(A|B) = \frac{Pr(B|A) \times Pr(A)}{Pr(B)}$

- 2) Calculate the current probability p_t
- 3) Generate a change to one of our parameters
- 4) Calculate the new probability p_{t+1}
- 5) Accept new parameter value with probability $\frac{p_{t+1}}{p_t}$
- 6) Return to step 3 (repeat for a really long time)





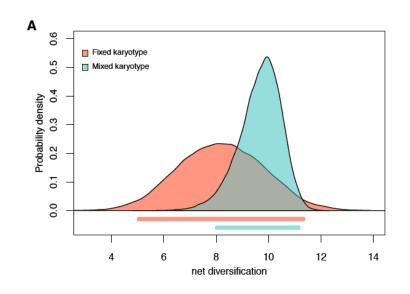


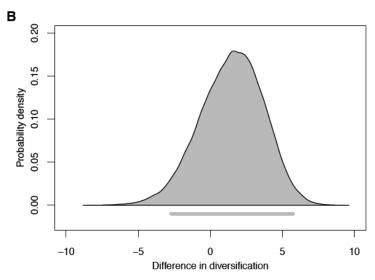


Bayesian methods

R example

The power of Bayesian approaches





With a Bayesian approach we can take into account all types of uncertainty and be more conservative.

- Phylogenetic
- Model selection uncertainty
- Parameter value uncertainty
- Uncertainty in measurements