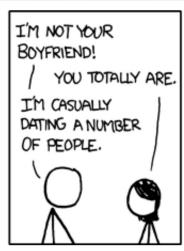
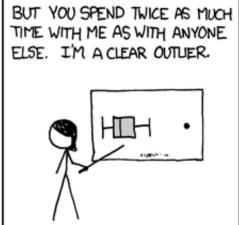
Binary Response Variables, Random vs Fixed Effects, and Outliers Biology 683

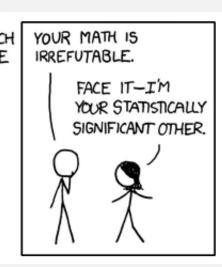
Lecture GLM3

Heath Blackmon









Other kinds of regression

Logistic regression allows us to fit a binary response variable (absent/present; alive/dead) with one or more categorical or continuous predictor variables.

Poisson regression allows us to fit a response variable that is Poisson distributed (number of extinctions in a unit of time, number of colonies per plate, (number of occurrences for rare events)) with one or more categorical or continuous predictor variables.

```
fit.logi <- glm(obs ~ pred2 , family="binomial")
fit.pois <- glm(obs ~ pred2, family="poisson")</pre>
```

GLM and LM function in R

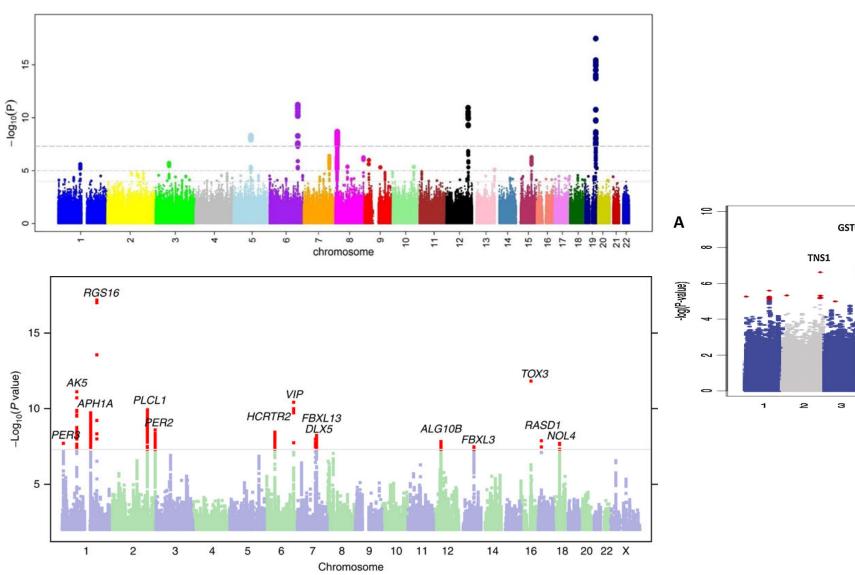
- The GLM and LM function in R takes equations that can be described with the following operators
- + +X include this variable
- : X:Z include the interaction between these variables
- * X*Y include these variables and the interactions between them
- $^{\prime}$ (X + Z + W)³ include these variables and all interactions up to three way

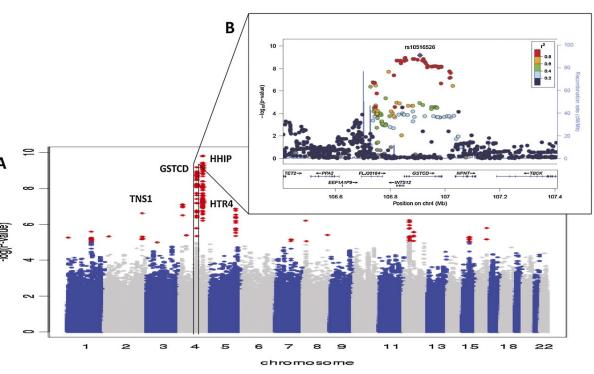
R versus the math implied

glm(y ~ X + W)
$$y_i = \beta_0 + \beta_1 X_i + \beta_2 W_i + \epsilon_i$$

glm(y ~ X * W)
$$y_i = \beta_0 + \beta_1 X_i + \beta_2 W_i + \beta_3 X_i W_i + \epsilon_i$$

GWAS





GWAS

GWAS: Genome wide association study.

The goal of GWAS is to determine what genes have alleles that are responsible for a trait of interest. The trait can be any measurable trait in any organism that you wish to study. For instance, a disease in humans, an economically important trait of a crop or domestic animal, an adaptation like a certain color pattern in birds, etc.

GWAS – Discrete condition (often disease)



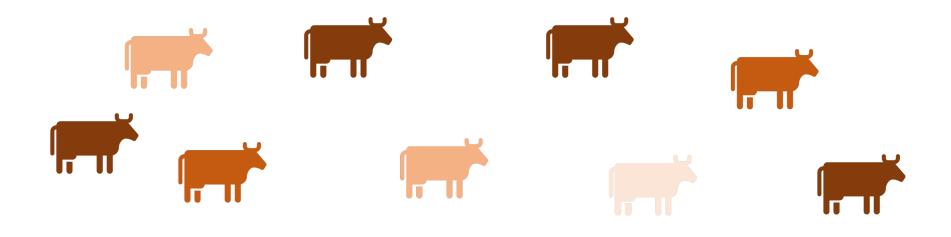
>case 1

CATACTACTGAACGTTTGCTCCTGCtactatctctctctctctctctctctctctctctctCATGC >case 2

CATACTACTGAACGTTTGCTCCTGCtactatctctctctctctctctctctctctctctctctCATGC >control 1

CATACTACTGAACGTTTGCTCCTGCtactatctctctctctctctctctctctctctctctCATGC >control 3

GWAS – Continuous trait



>sample 1

 ${\tt CATACTACTGAACGTTTGCTCCTGCtactatctctctctctctctctctctctctctctctct}$

>sample 2

>sample 3

 ${\tt CATACTACTGAACGTTTGCTCCTGCtactatctctctctctctctctctctctctctctctct}$

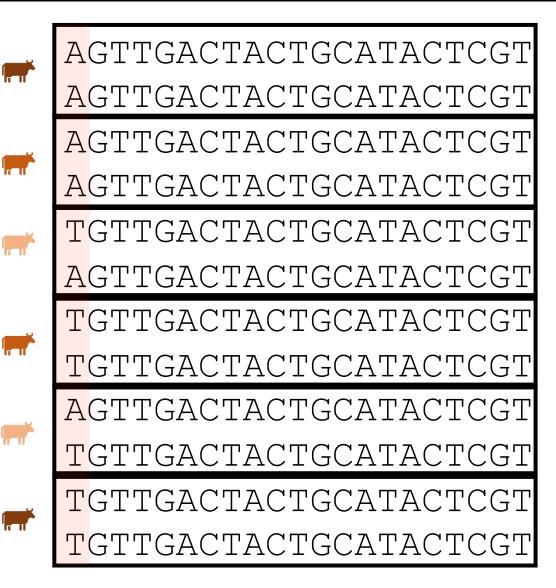
>sample 4

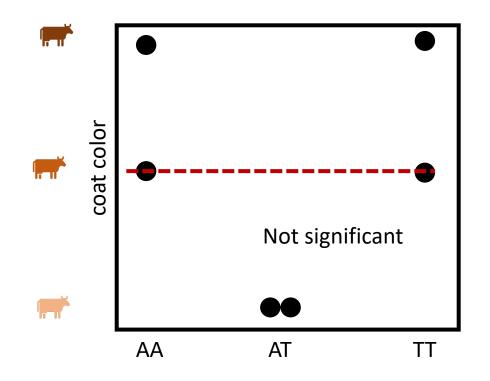
>sample 5

CATACTACTACTGAACGTTTGCTCCTGCtactatctctctctctctctctctctctctctctctctCATGC

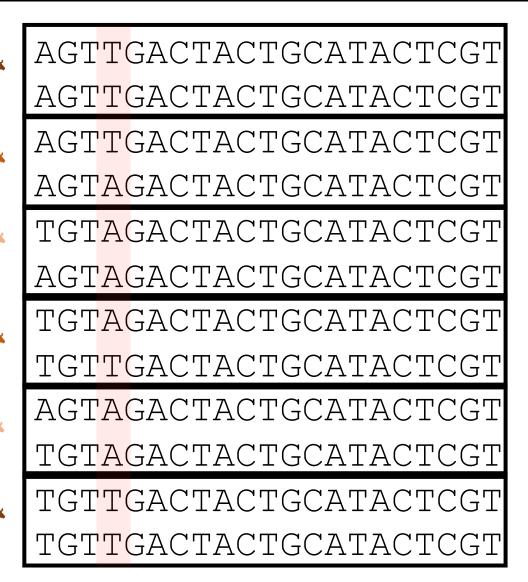
>sample 6

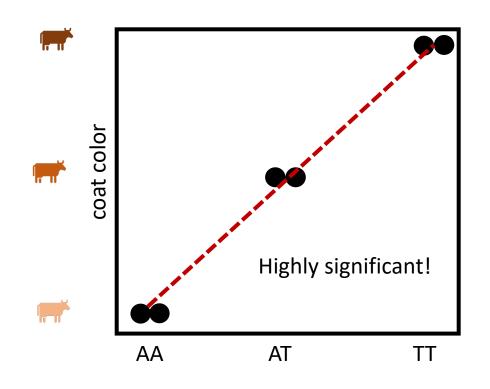
GWAS – Continuous trait





GWAS – Continuous trait





GWAS - Problems

What is the problem with doing this across the whole genome?

Multiple tests lead to more false positives!

- 1) require a higher level of significance 5x10⁻⁸
- 2) only look at the very most significant
- 3) lots of more complicated approaches too!

What is one of the most basic requirements of almost all statistical tests?

Tests normally assume independence of the data points!

- 1) Samples from a population will be related to each other due to ancestry (trees!)
- DNA sequencing is not done equally in all groups of people (western samples are usually over represented

GWAS - Problems

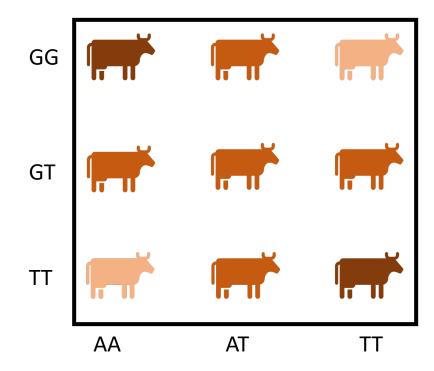
What is epistasis?

It is the case where the impact of a genotype at one locus depend on the genotype at another locus!

To find this type of effect you would need to look at all pairs of genotypes. How many tests would we need to do then?

About 6 orders of magnitude more tests would be required.

Humans have around 4,000,000 sites that are variable like this which equates to 7,999,998,000,000



GWAS - Problems

What about the environment?

Many diseases have a strong environmental component (heart disease, diabetes, cancer, etc.)

If these are left out of the study often what is discovered is actually genetic variation that happens to coincide with environmental factors?

If a disease is more common in Europeans than Africans or Asians but it is because of a lifestyle characteristic any genetic variation that is common in Europeans but rare in Africans and Asians could appear associated with the disease.

Mixed models

Mixed models are models that include fixed and and random effects.

Fixed effects can be repeated by other researchers. These are the variables that you are interested in studying.

Random effects are usually nuisance parameters. These are variables that other researchers cannot replicate and you are not interested in inferring anything about them.

Mixed models

Fixed effects are the variables whose impact we wish to determine

- Characteristics of the media or habitat
- Experimental treatments
- Age groups
- Time points
- Mutant genotypes

Conclusions that you reach are only applicable to the groups or treatments you include in the study

Example of fixed effects

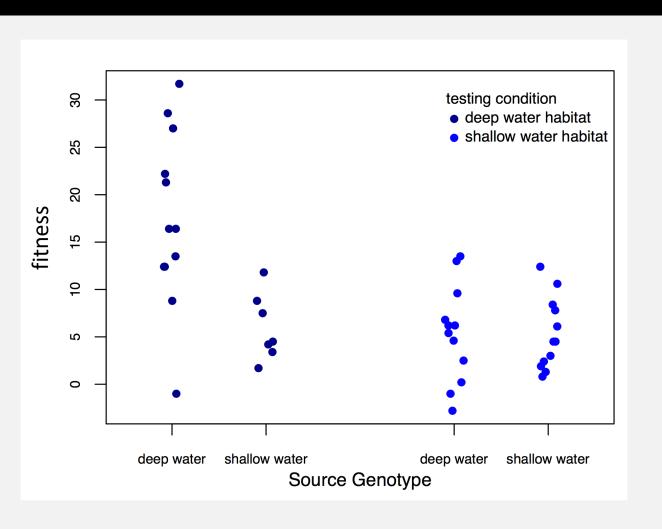
Reciprocal relocation experiment to investigate how genotype and habitat interact to determine the fitness of stickleback fish (Rundle 2002).

Course	habitat
Source	Habitat

		Shallow	Deep
Test	Shallow	12 fish	11 fish
	Deep	7 fish	11 fish



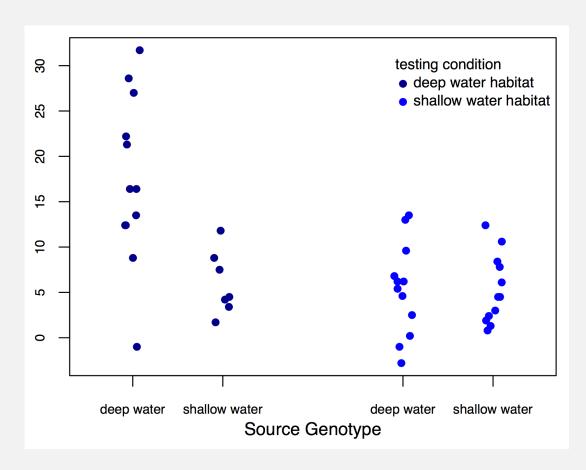
Example of fixed effects (two factor ANOVA)



```
> anova(lm(fitness ~ genotype * test.habitat))
Analysis of Variance Table
Response: fitness
                       Df Sum Sq Mean Sq F value
                                                      Pr(>F)
                           363.49 363.49 9.7045 0.0034403 **
genotype
                          550.55 550.55 14.6986 0.0004485 ***
test.habitat
genotype:test.habitat 1
                          333.58 333.58 8.9059 0.0048864 **
Residuals
                       39 1460.77
                                    37,46
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
> summary(lm(fitness ~ genotype * test.habitat))
Call:
lm(formula = fitness ~ genotype * test.habitat)
Residuals:
    Min
                  Median
-18.4750 -3.6917
                           3.4583 14.2250
                 -0.8083
Coefficients:
                                 Estimate Std. Error t value Pr(>|t|)
(Intercept)
                                   17.475
                                                      9.891 3.49e-12 ***
                                  -11.489
genotypeshallow
                                               2.911 -3.947 0.000321 ***
test.habitatshallow
                                  -12.125
                                              2.499 -4.853 1.99e-05 ***
genotypeshallow:test.habitatshallow 11.448
                                              3.836
                                                      2.984 0.004886 **
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' '1
Residual standard error: 6.12 on 39 degrees of freedom
                             Adjusted R-squared: 0.4192
Multiple R-squared: 0.4606,
F-statistic: 11.1 on 3 and 39 DF, p-value: 2.093e-05
```

Interpreting Coefficients

```
> summary(lm(fitness ~ genotype * test.habitat))
Call:
lm(formula = fitness ~ genotype * test.habitat)
Residuals:
    Min
                   Median
                                        Max
-18.4750 -3.6917 -0.8083
                            3.4583 14.2250
Coefficients:
                                   Estimate Std. Error t value Pr(>|t|)
                                     17.475
                                                        9.891 3.49e-12 ***
(Intercept)
                                                1.767
genotypeshallow
                                    -11.489
                                                2.911 -3.947 0.000321
test.habitatshallow
                                    -12.125
                                                2.499 -4.853 1.99e-05 ***
genotypeshallow:test.habitatshallow 11.448
                                                3.836
                                                        2.984 0.004886 **
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' '1
Residual standard error: 6.12 on 39 degrees of freedom
Multiple R-squared: 0.4606,
                               Adjusted R-squared: 0.4192
F-statistic: 11.1 on 3 and 39 DF, p-value: 2.093e-05
```



What is a random effect

These are randomly sampled categories of a variable that represent groups of individual measurements. Usually random effects are not repeatable.

- Study sites
- Environmental chambers
- Families made up of siblings
- Measurements within individuals

Conclusions that you reach are applicable only to the sample being studied.

What is a random effect

Sometimes random effects are a nuisance

- Field sites
- Environmental chambers
- Field plots
- Repeated measures

Occasionally random effects are of great interest

- Families Heritability
- Individuals Breeding value

Example of random effects

Impact of selective regime on horn size.

Measure both the left and right horn in 25 beetles from two different selective regimes.

Horn size	Beetle	Selective regime	
256	1	High	134
276	1	High —	
321	2	High	1366
321	2	High —	
423	3	Low	1366
401	3	Low —	
381	4	Low	136
409	4	Low —	



Example of random effects

Identifying the predictors for the presence or absence of Chrysina beetles.

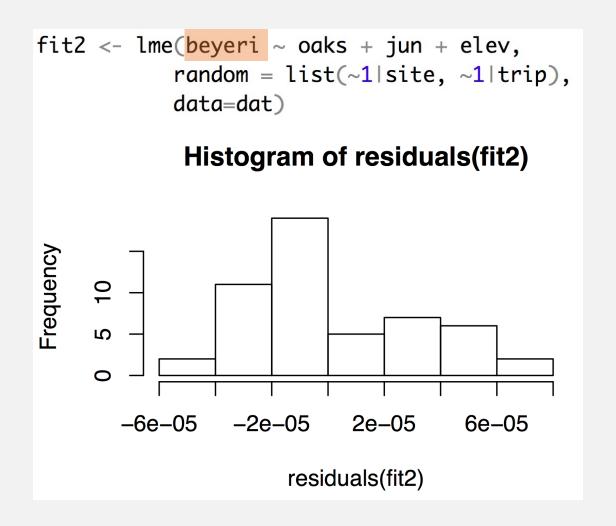
Number collected	oak	juniper	site	date	trip
8	1	0	21	210	Α
2	1	1	13	210	Α
1	0	1	31	211	Α
5	0	1	15	212	Α
4	1	1	21	242	В
6	1	0	13	242	В
0	1	1	31	245	В
7	1	1	15	245	В

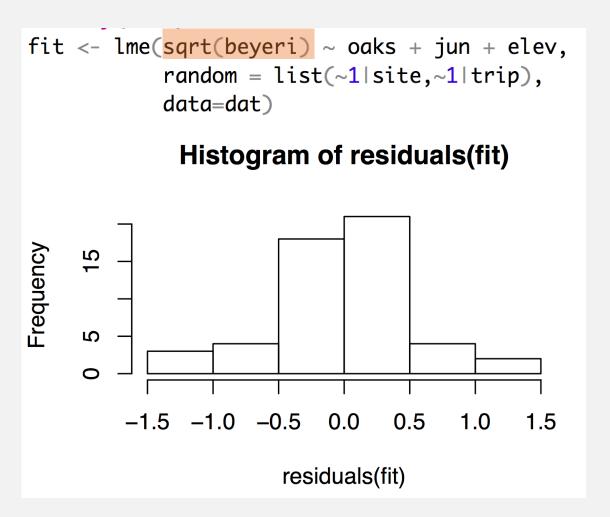


Implementing a mixed effects model

Mixed effect models can be fit using the LME function from the package nlme.

Implementing a mixed effects model





Implementing a mixed effects model

Mixed effect models can be fit using the LME function from the package nlme.

```
fit <- lme(sqrt(beyeri) ~ oaks + jun + elev,
             random = list(~1|site,~1|trip),
             data=dat)
> summarv(fit)
Linear mixed-effects model fit by REML
Data: dat
      AIC
                     logLik
               BIC
 153.6247 166.7231 -69.81233
Random effects:
Formula: ~1 | site
        (Intercept)
StdDev: 2.272341e-05
Formula: ~1 | trip %in% site
       (Intercept) Residual
StdDev: 0.8169537 0.00264004
Fixed effects: sqrt(beyeri) ~ oaks + jun + elev
               Value Std.Error DF t-value p-value
(Intercept) -1.6788177 1.5125428 26 -1.109931 0.2772
            0.9707025 0.2943403 22 3.297892 0.0033
           -0.0860503 0.2460159 22 -0.349775 0.7298
jun
            0.0012513 0.0008072 22 1.550167 0.1354
elev
Correlation:
    (Intr) oaks jun
oaks 0.530
    0.197 -0.097
elev -0.993 -0.584 -0.250
```

```
fit <- lme(sqrt(beyeri) ~ oaks + elev,
            random = list(~1|site,~1|trip),
            data=dat)
> summarv(fit)
Linear mixed-effects model fit by REML
 Data: dat
       AIC
               BIC logLik
 150.7722 162.1231 -69.3861
Random effects:
 Formula: ~1 | site
         (Intercept)
StdDev: 2.191491e-05
 Formula: ~1 | trip %in% site
        (Intercept)
                      Residual
StdDev: 0.8096043 0.002598713
Fixed effects: sqrt(beyeri) ~ oaks + elev
                Value Std.Error DF t-value p-value
(Intercept) -1.5744919 1.4695032 26 -1.071445 0.2938
            0.9607576 0.2903283 23 3.309211 0.0031
oaks
            0.0011807 0.0007746 23 1.524404 0.1410
elev
 Correlation:
     (Intr) oaks
oaks 0.563
elev -0.994 -0.631
```

```
fit <- lme(sqrt(beyeri) ~ oaks,
            random = list(~1|site,~1|trip),
            data=dat)
> summary(fit)
Linear mixed-effects model fit by REML
 Data: dat
       AIC
                      loaLik
                BIC
 138.5902 148.1504 -64.29512
Random effects:
 Formula: ~1 | site
        (Intercept)
StdDev: 2.309943e-05
 Formula: ~1 | trip %in% site
       (Intercept)
                      Residual
StdDev: 0.8202517 0.002667513
Fixed effects: sqrt(beyeri) ~ oaks
               Value Std.Error DF t-value p-value
(Intercept) 0.6514133 0.1674341 26 3.890566
                                             6e-04
            1.2400606 0.2281742 24 5.434710
oaks
                                             0e+00
 Correlation:
     (Intr)
oaks -0.734
```

Considerations for models with random effects

- Most software will assume that all factors are fixed unless you specify them as mixed.
- Designating factors as random effects takes extra work.
- The lm function treats all predictors as fixed effects.
- Treating random effects as fixed effects is fundamentally wrong.

Links

MCMCMglmm: Fit mixed models with phylogenetic or pedigree information in a Bayesian framework.

Outlier Package: Apply outlier tests to identify possible outlier datapoints - I don't recommend this.