Supervised Classification Boosting

AdaBoosting

• Weight Assignment: $w_{i,0} = \frac{1}{n}$

$$= \underbrace{\hat{y}_{j}^{(i)} \neq y^{(i)}}^{\sum\limits_{i=1}^{N} w^{(i)}}$$

- Error Rate: $r_j = \frac{\sum\limits_{i=1}^{N} w^{(i)}}{\sum\limits_{i=1}^{N} w^{(i)}}$
- Predictor Weight: $\alpha_i =$ $\eta \ln \left(\frac{1-r_j}{r_i} \right)$

Hard SVM

•
$$y(x) = w^T \phi(x) + b = 0$$

- Margin: $\frac{1}{||w||}$
- Objective: $\min_{w,h} \frac{1}{2} ||w||^2$
- Discriminant Function: f(x) = $w^T \phi(x) + b$
- Support Vectors: $y_i(w^T\phi(x_i) +$
- Polynomial Kernel: K(x,y) = $(1 + \langle x, y \rangle)^d$
- Gaussian **Kernel:** $K(x,y) = \exp\left(-\frac{\|x-y\|^2}{2\sigma^2}\right)$

Soft SVM

- Objective: $\min_{w,b,\xi} \frac{1}{2} ||w||^2 +$ $C\sum_{i=1}^{N} \xi_i$
- Constraints: $y_i(w^T\phi(x_i) + b) \ge$ $1 - \xi_i$
- Slack Variables: $\xi_i \geq 0$
- Lagrangian: $\mathcal{L}(w,b,\xi,\alpha,\beta) =$ $\frac{1}{2}||w||^2 + C\sum_{i=1}^{N} \xi_i - \sum_{i=1}^{N} \alpha_i (y_i(w^T \phi(x_i) + b) - 1 + i)$ ξ_i) $-\sum_{i=1}^{N} \beta_i \xi_i$
- KKT Conditions: $\alpha_i \geq 0, \beta_i \geq$ $0, \alpha_i(y_i(w^T\phi(x_i) + b) - 1 + \xi_i) =$

$$0, \beta_i \xi_i = 0$$

- **Dual Problem:** $\max_{\alpha} \sum_{i=1}^{N} \alpha_i \frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} \alpha_i \alpha_j y_i y_j K(x_i, x_j)$
- Predictor: f(x) $\sum_{i=1}^{N} \alpha_i y_i K(x, x_i) + b$

Dimensionality Reduction Curse of Dimensionality

- Volume: $V_d(r) = r^d$
- Ratio: $ratio = \frac{V_{crust}}{V_{S_1}} = \frac{V_{S_1} V_{crust}}{V_{S_1}}$
- Vol Eqn: $V = \frac{r^D \cdot \pi^{D/2}}{o(D/2+1)}$

• ratio = $1 - (1 - \frac{\epsilon}{r})^D$

Feature Selection

- Embedded: L1: $||\mathbf{w}||_1 =$ $\sum_{i=0}^{M} |w_i|$
- Wrappers: Recursive Feature Elimination using Greedy Search
- Feature Extraction: PCA, LDA
- PCA: