



**80** Pages  
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# EXERCISE BOOK CAHIER D'EXERCICES

NAME/NOM Cole Shanks

SUBJECT/SUJET ELEC 301



ASSEMBLED IN CANADA WITH IMPORTED MATERIALS  
ASSEMBLÉ AU CANADA AVEC DES MATIÈRES IMPORTÉES

12107

# Lecture 0

9/05/19 Course Overview:

LEC

Mini Projects (15% each)  $\rightarrow$  60%

BiWeekly tests (10% each)  $\rightarrow$  40%

Office Hour  $\rightarrow$  KAIS 3040 or 3041

Mini Project 2 DIFFICULT

$\hookrightarrow$  3 weeks extended, so

also for test then

Email subject: ELEC301F19 followed by a space and question/subject.

9/09/19

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# Lecture 1

Figure 3  $\rightarrow$  Figure 4 (Miller's Thrm)

9/10/19

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# Lecture 2

9/12/19

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# Lecture 3

$$20 \log(\sqrt{2}) = 3\text{dB} \quad *0.707 \text{ used often as a point}$$

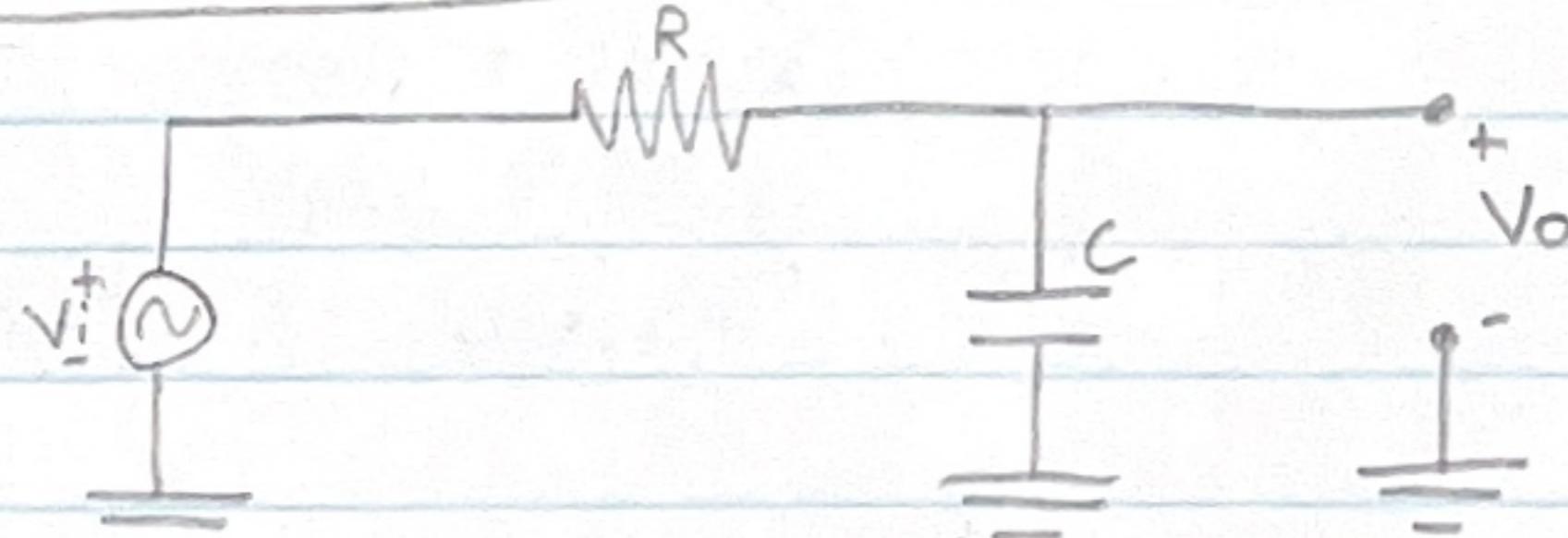
9/16/19

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# Lecture 4

\*Review Bode plots (Phase and amplitude)

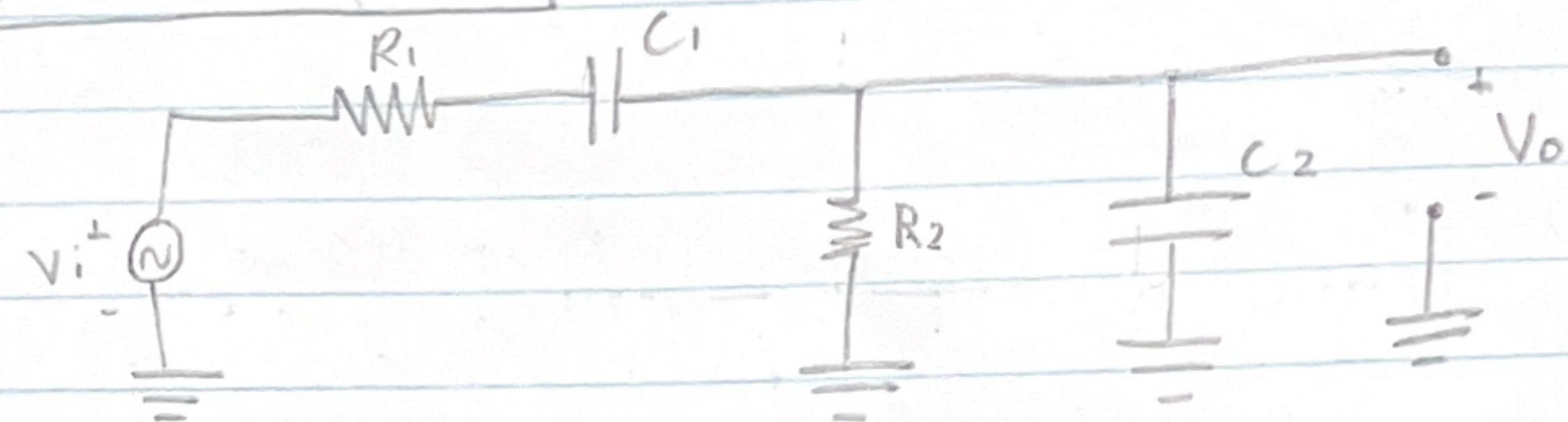
## Low-Pass Filter



Questions:

Band-Pass Filter

$$C_1 \gg C_2$$



- ① Capacitor @ high  $\omega \rightarrow$  short
- @ low  $\omega \rightarrow$  open
- How does  $C$  values influence this behaviour?

Large Blocking Capacitors:

Because  $C_1 \gg C_2$

→ terms like  $\left( \frac{1}{R_2 C_2} + \frac{1}{R_1 C_1} \right) \rightarrow \frac{1}{R_2 C_2}$

9/17/19

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## Lecture 5

3 DB (half power point)

P7.4 \*Understand this slide

Find Cutoff Frequencies: (High and Low)

- ① Poles are known
- ② Have circuit but don't know poles

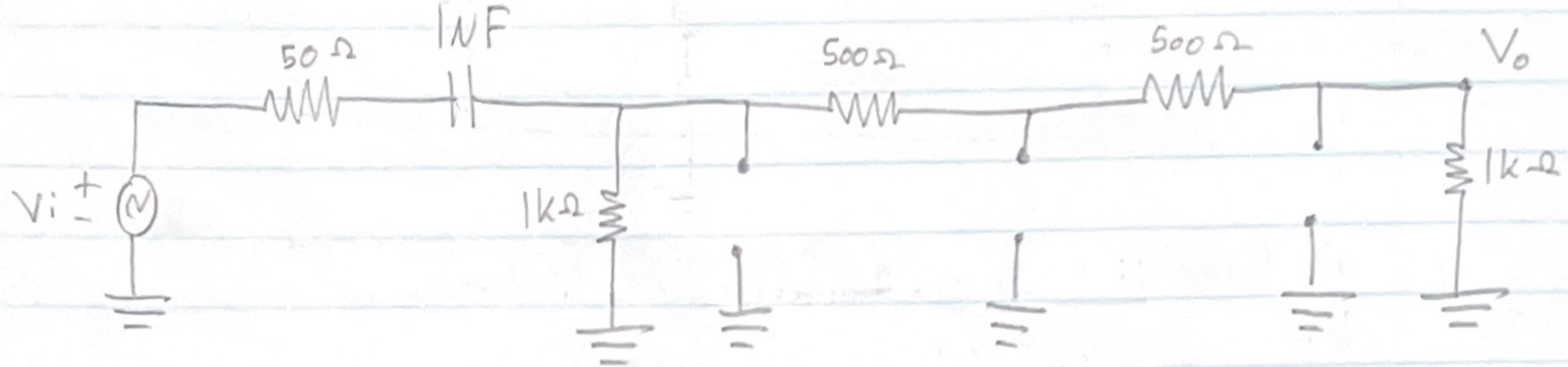
P7.10 Short circuit time constants:

• short all other capacitors and  $V$  sources  
and set resistance ( $a \rightarrow b$  therein) across  
the capacitor you're looking at

## Lecture 6

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Problem Set 2 Q3:



$$(1_E - 6)(50 + 1k || 2k) \\ = 0.000716 = T_{oc}$$

$$\rightarrow \frac{1}{0.00716} = 1395.35 \rightarrow \omega_{L3dB} = 1395.35 \text{ rad/s}$$

Time constants:

$$W_p = \frac{1}{T_{oc}}$$

\*Important  $\rightarrow P > 4$  (3dB)

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## Lecture 7

Problem Set 2:

[Q1]

$$T_{C1}^{oc} = C_1(R_1 + R_2) \quad [\text{short source, open } C_2]$$

$$T_{C2}^{oc} = C_2 R_2 \quad [\text{short source, open } C_1]$$

\*  $C_1 = \text{sum of the open circuit time constants}$

[Q4]

$$W_{Z1L} = 100/\text{s}$$

$$W_{L3dB} = \sqrt{(200/\text{s})^2 + (50/\text{s})^2 - 2 \cdot (100/\text{s})^2}$$

$$W_{Z2L} = 0/\text{s}$$

$$= 150/\text{s}$$

$$W_{P1L} = 200/\text{s}$$

$$W_{P2L} = 50/\text{s}$$

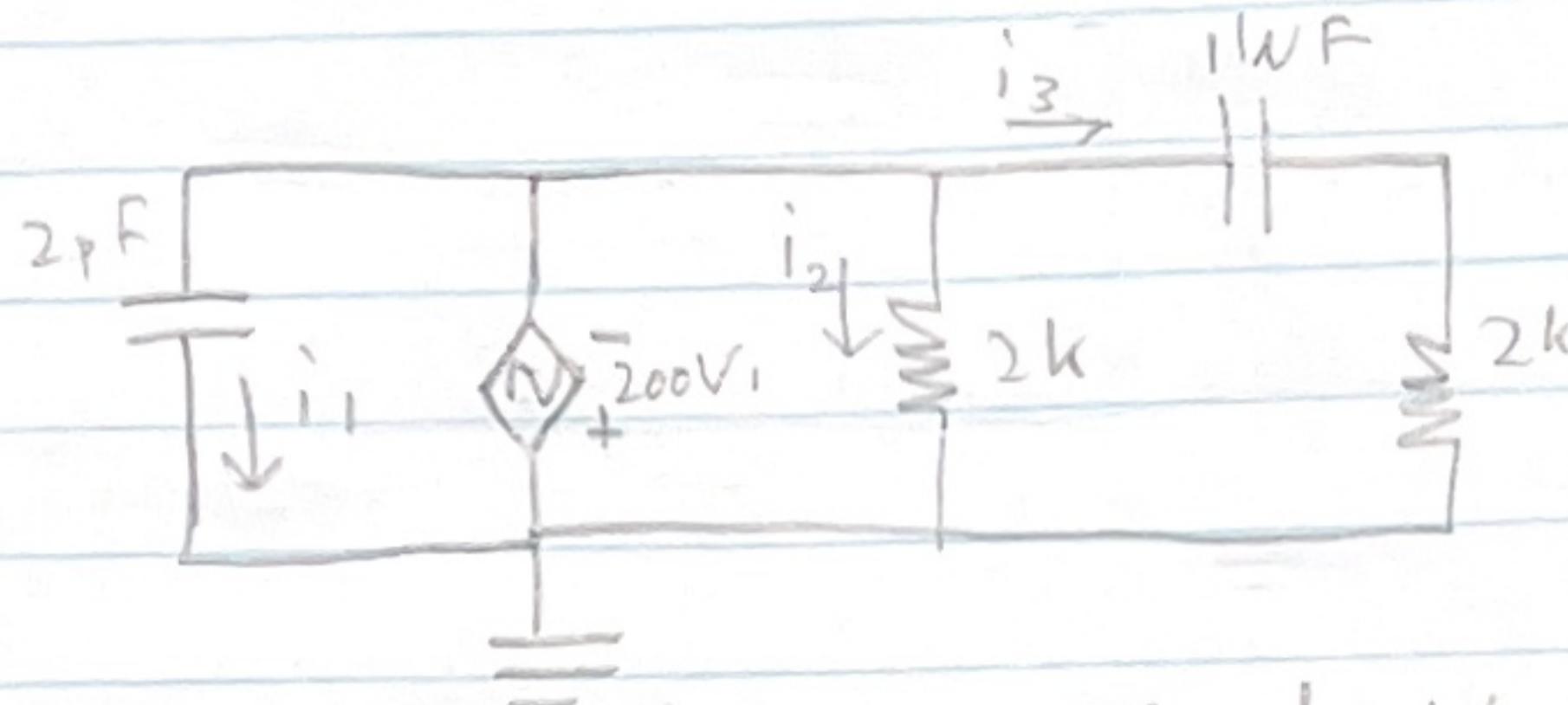
What is  $W_{L3dB} = ?$

# Lecture 9

9/26/19

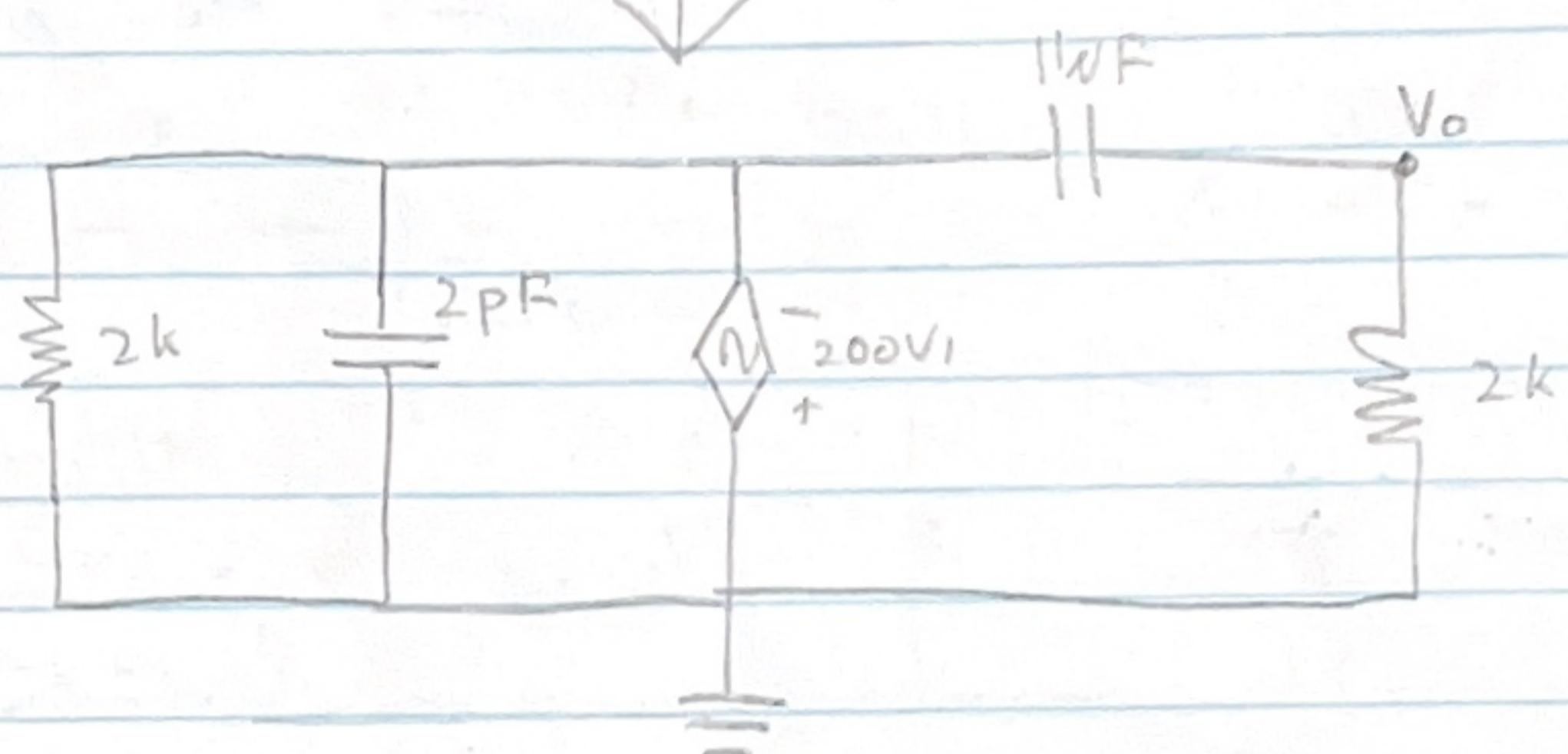
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PS2 Q5



Ideal Vsource

[really 3 parallel circuits]



$$V_o = i_3 \cdot 2k$$

~~$-200V_1 = i_3 \cdot 2k$~~

$$-200V_1 = i_3 \left( \frac{1}{j\omega \cdot 1nF} + 2k \right)$$

$$\frac{V_o}{-200V_1} = \frac{2k}{\frac{1}{j\omega \cdot 1nF} + 2k} \rightarrow \frac{V_o}{-200V_1} \Big|_{\omega \rightarrow \infty} = 1$$

$$\frac{|V_o(j\omega)|}{-200|V_i(j\omega)|} = \frac{1}{\sqrt{2}}$$

| 3dB is when  $\frac{V_o}{V_i} = \frac{1}{\sqrt{2}}$  |

PS2 Q6

Miller:

$$k = \frac{V_o}{V_{T\pi}} = -5k \parallel k \cdot \frac{0.1V \cdot V_{T\pi}}{V_{T\pi}}$$
$$= \frac{-5k}{1k+5k} \cdot 1k \cdot 100mV$$
$$= -0.833 \cdot 100$$
$$= -83.3$$

siemens

$$\omega_{HP1} = \frac{1}{50\Omega \parallel 50k\Omega \parallel 2.5k\Omega \cdot 88.3pF}$$

$$\omega_{HP2} = \frac{1}{833\Omega \cdot 1pF}$$

$$A_m = \frac{V_o}{V_i} = \frac{V_o}{V_{T\pi}} \cdot \frac{V_{T\pi}}{V_i}$$

$$= -83.3 \cdot \frac{50k \parallel 2.5k}{50k \parallel 2.5k + 50} \approx -83.3 \frac{V}{V}$$

$$\omega_{LP1} = \frac{1}{(50\Omega + 50k \parallel 2.5k) 2\pi F}$$

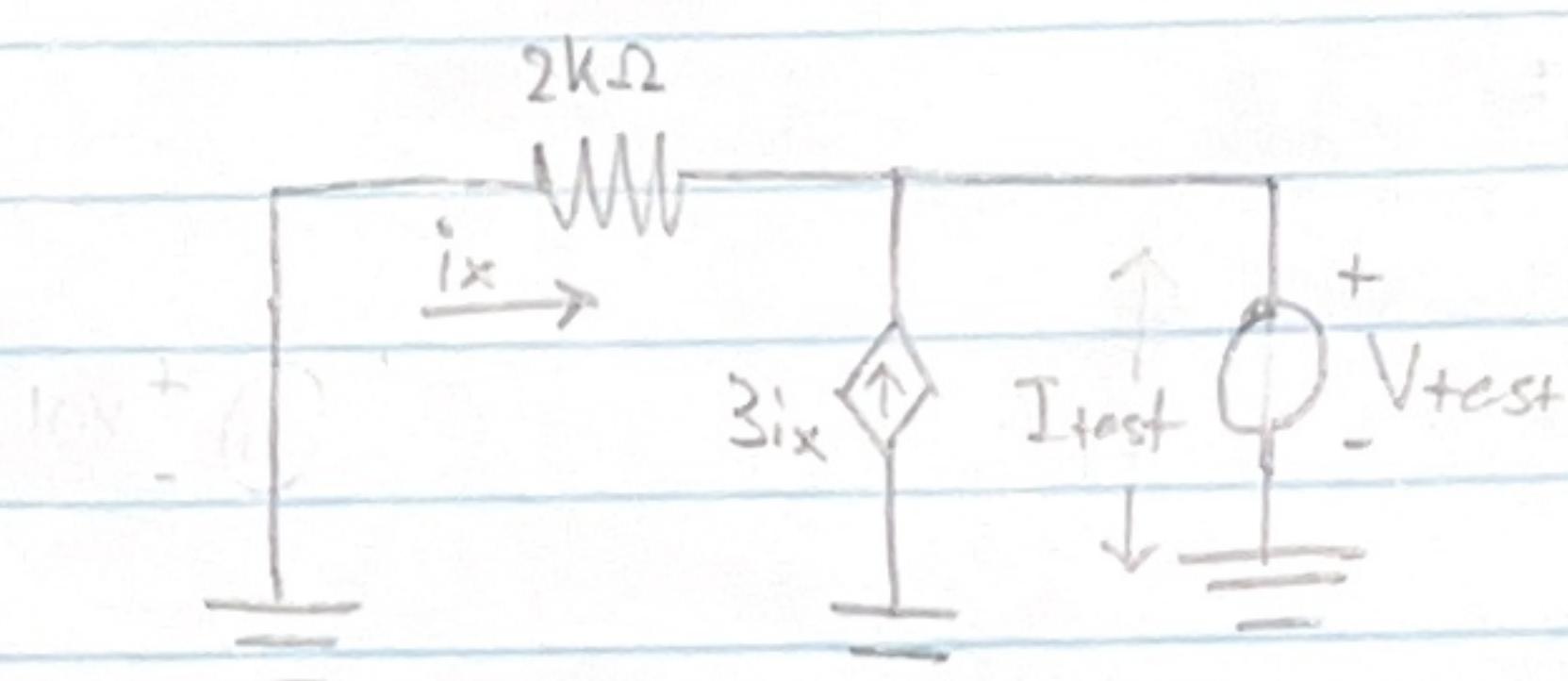
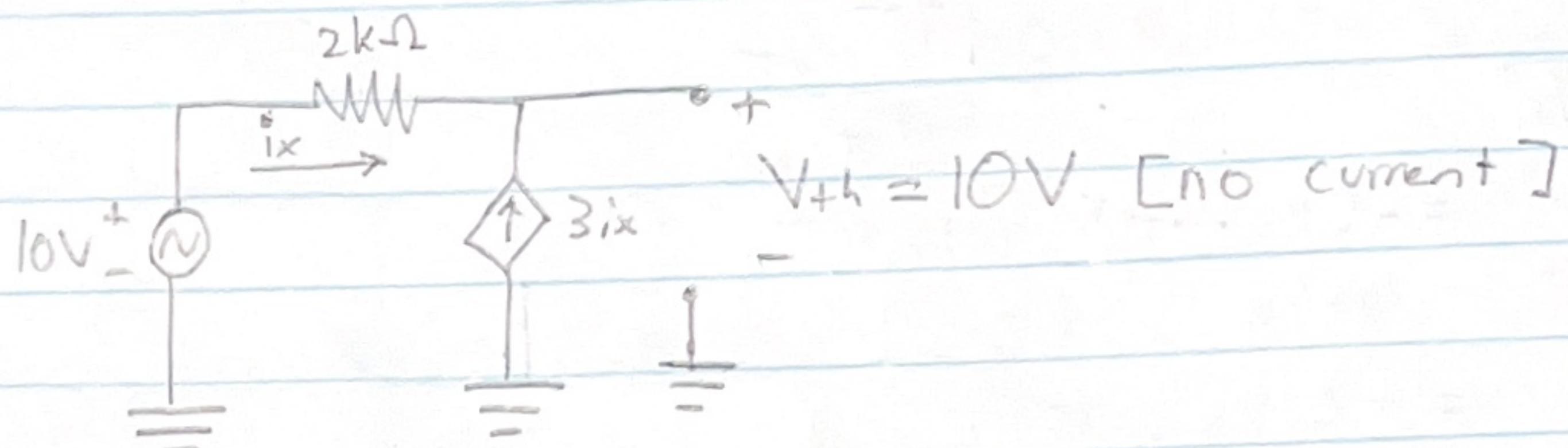
$$\omega_{LP2} = \frac{1}{6k \cdot 0 \cdot \text{INF}}$$

$$T(s) = A_m \cdot \frac{s}{s + \omega_{LP1}} \cdot \frac{s}{s + \omega_{LP2}} \cdot \frac{\omega_{HP1}}{s + \omega_{HP1}} \cdot \frac{\omega_{HP2}}{s + \omega_{HP2}}$$

$$\omega_{L3DB} = 1680/s$$

$$\omega_{L3DB} = \sqrt{\omega_{LP1}^2 + \omega_{LP2}^2}$$

PS1 Q2



$$ix = \frac{V_{test}}{2k}$$

$$I_{test} = 4ix$$

$$R_{test} = \frac{V_{test}}{I_{test}} = \frac{ix \cdot 2k}{4ix} = 500\Omega = R_{th}$$

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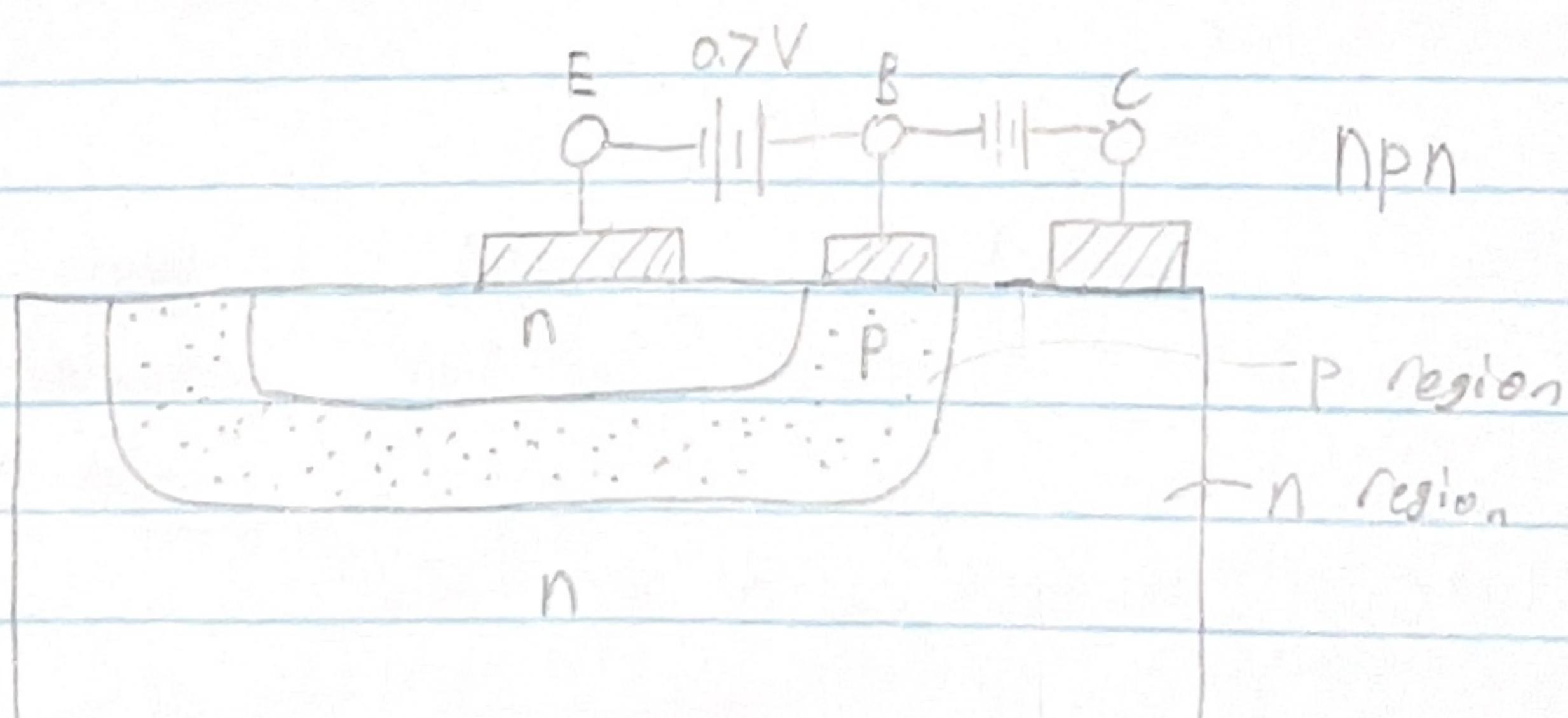
## Lecture 10

**SS8** The BJT as an amplifier:

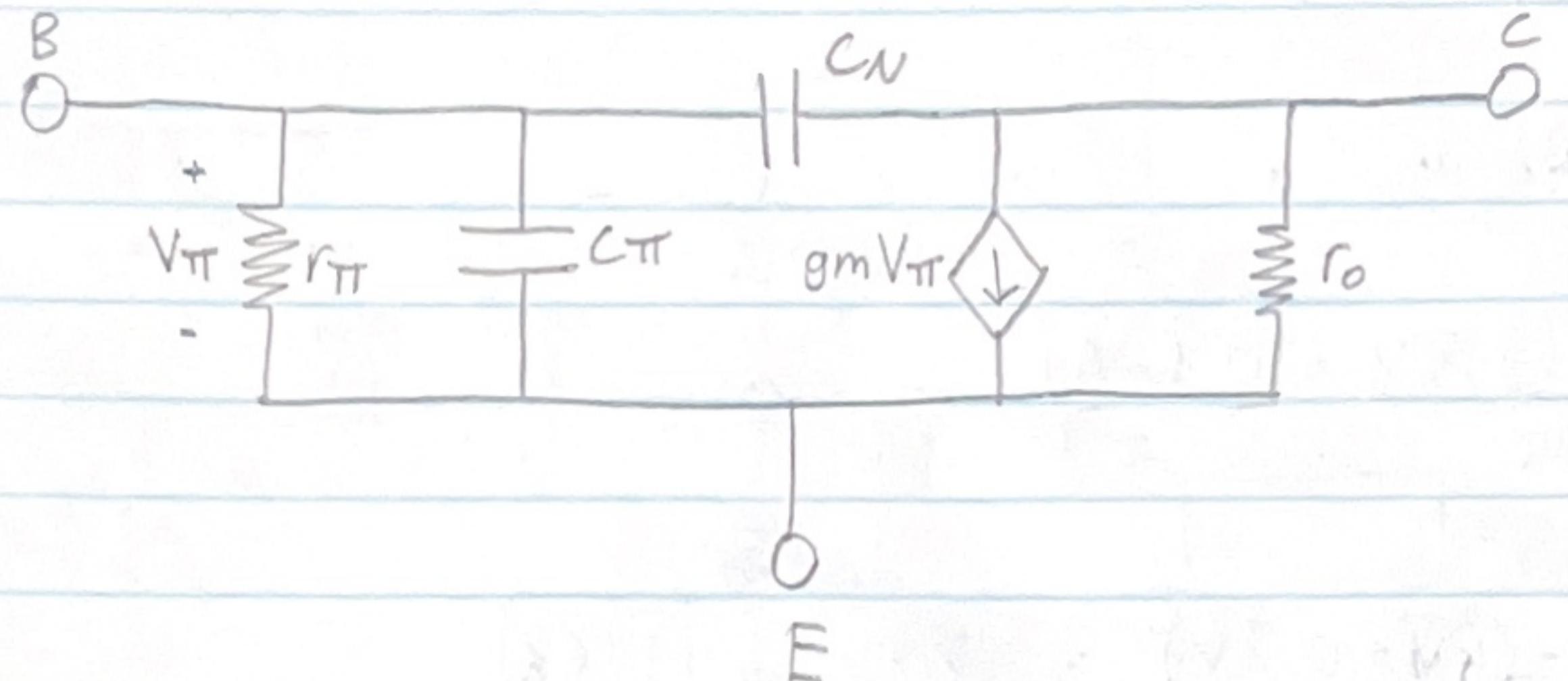
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## Lecture 11



## Hybrid- $\pi$ small signal Model:



Formulas:

$$i_c = \frac{I_c}{V_t} \cdot V_{be} = g_m V_{be}$$

$$r_\pi = \frac{V_{be}}{i_b}$$

PS3 Q1     $V_{cc} = 15V$   
 $I_c = 2mA$

$$R_C = \frac{V_{cc} - V_C}{I_C} = \frac{\frac{1}{3}V_{cc}}{I_C} = \frac{5V}{2mA} = 2.5k\Omega$$

$$I_E \approx I_C = 2mA$$

$$V_E = V_B - 0.7V = 4.3V$$

$$R_E = \frac{4.3V}{2mA} = 2.15k\Omega$$

$$R_{B1} = \frac{V_{cc} - V_B}{0.1(2mA)} = \frac{10V}{0.2mA} = 50k\Omega$$

$$R_{B2} = \frac{V_B - V_E}{0.2mA - I_E/100} = \frac{5V}{0.18mA} = 27.8k\Omega$$

# Lecture 12

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PS3 Q2

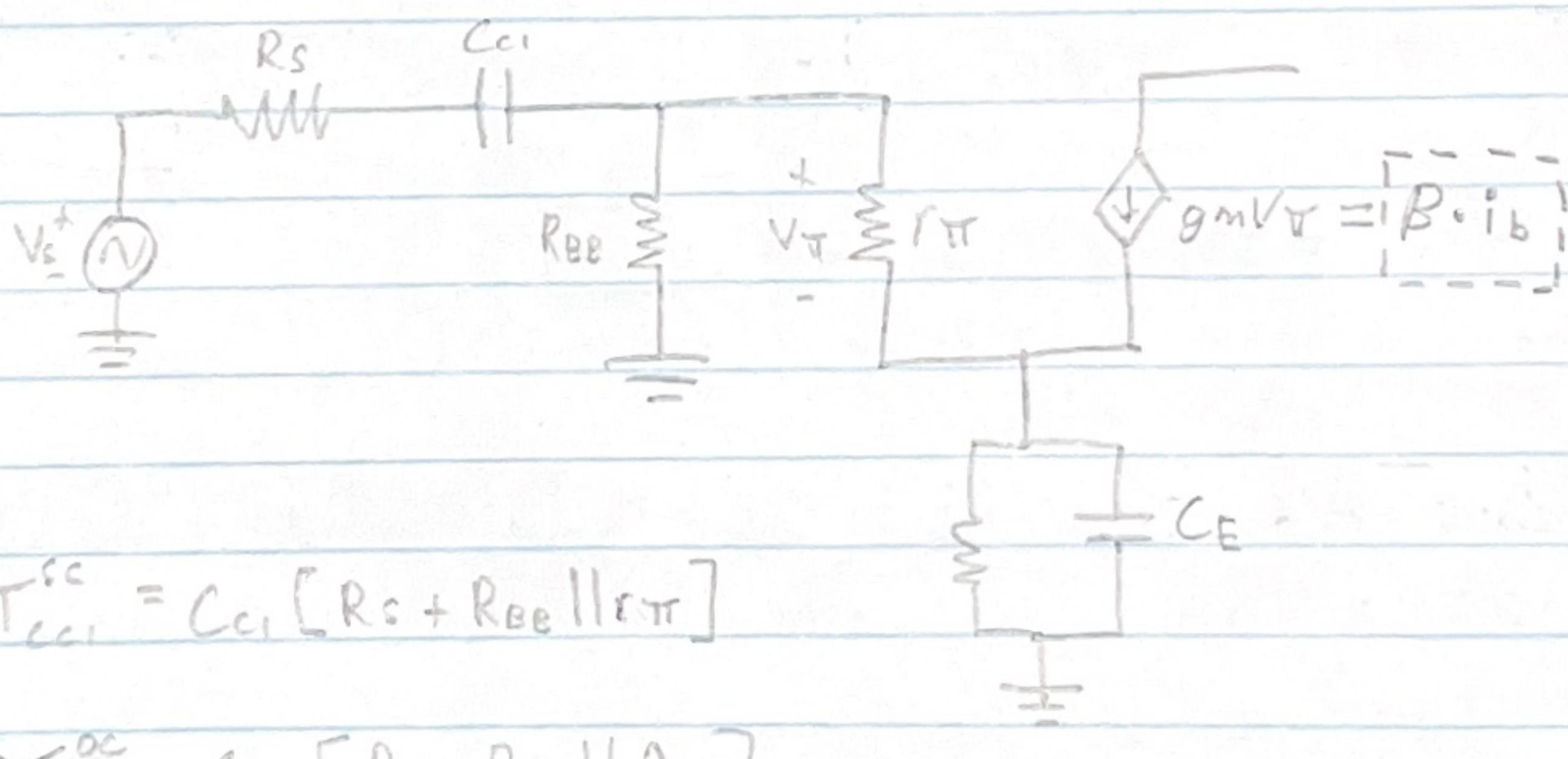
$$R_E = 8k = R_C$$

$$I_C = \frac{12V - (2/3)8V}{8k} = 0.5mA$$

$$R_{B1} = \frac{(12V - (4V + 0.7V))}{0.5mA/10} = \frac{7.3V}{0.05mA} = 146k$$

$$R_{B2} = \frac{4.7V}{0.5mA/10 - 0.5mA/100} = \frac{4.7V}{0.045mA} = 104.4k$$

Low frequency Response Small signal:



$$T_{C_{C1}}^{ac} = C_{C1} [R_S + R_{EE} || r_{\pi}]$$

$$T_{C_{B1}}^{ac} = C_{C1} [R_S + R_{EE} || R_B]$$

where:

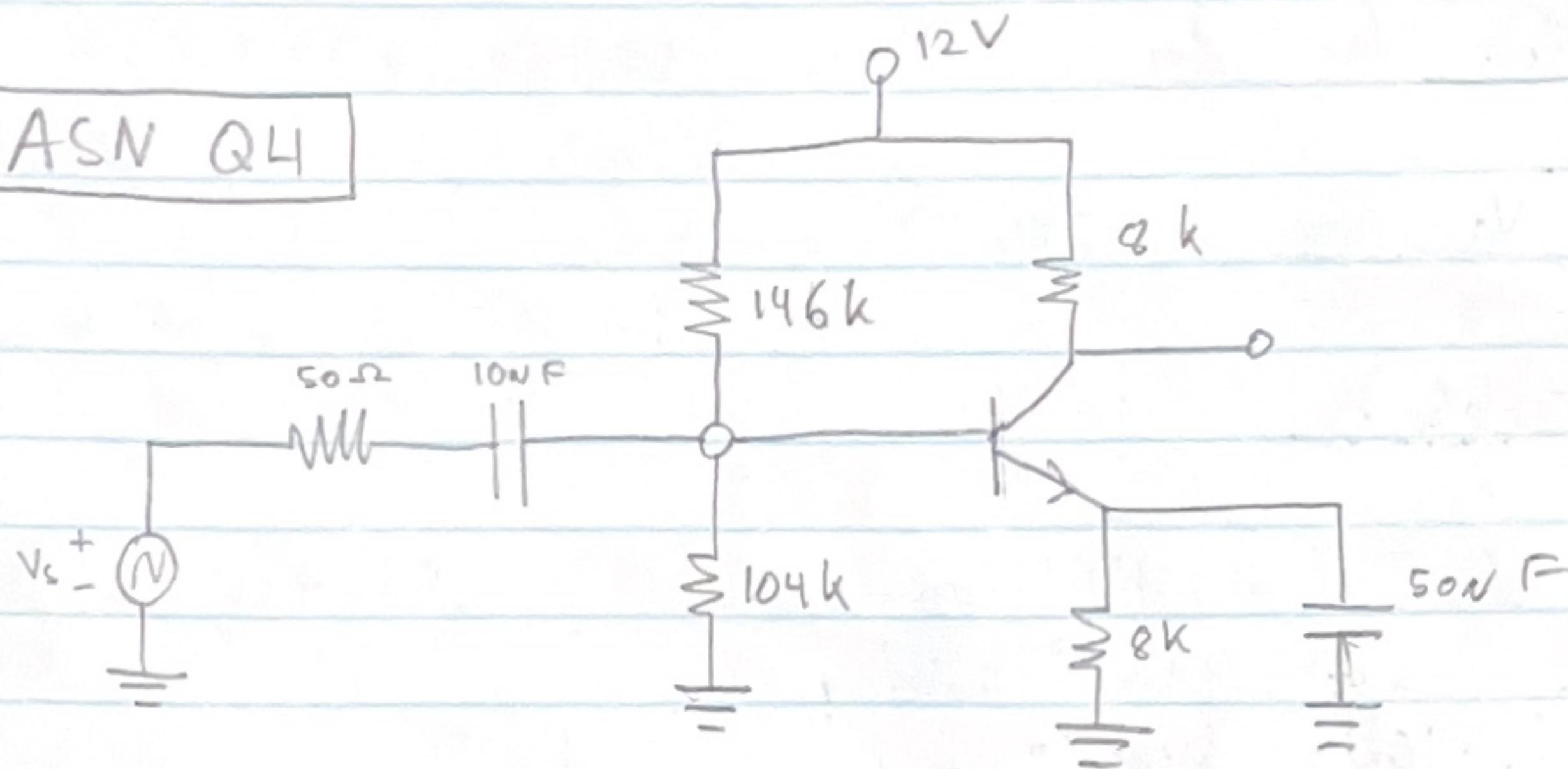
$$R_B = r_{\pi} + (1 + \beta) R_E$$

# Lecture 13

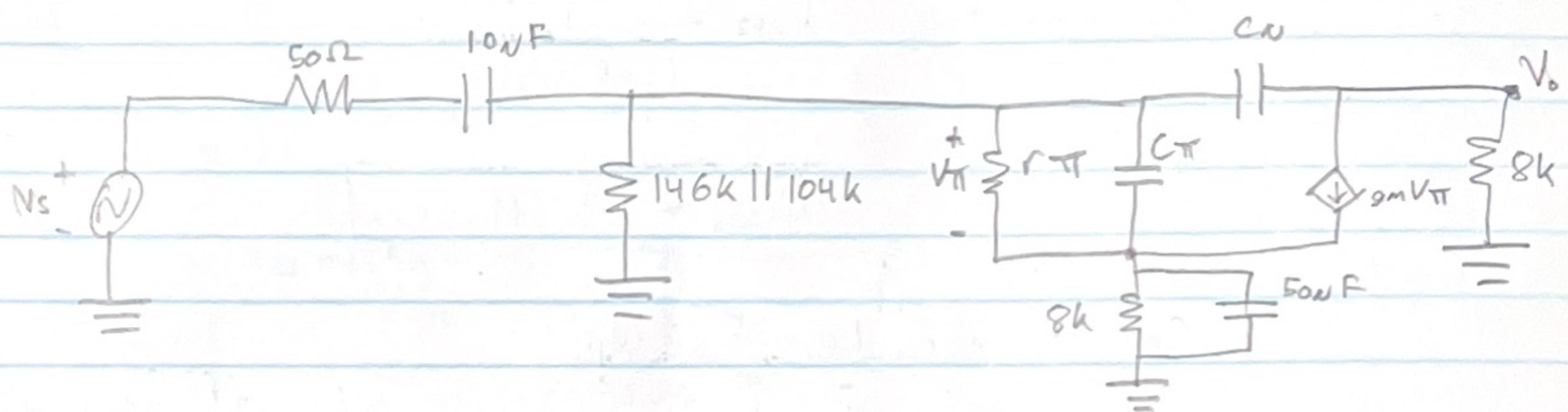
10/10/19

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**ASN Q4**



Small signal - Model:



Low FREQ model:

- Open  $C_{\pi}$  and  $C_N$

Midband FREQ model:

- ① Open  $C_{\pi}$  and  $C_N$
- ② short  $100F$  and  $50nF$

High FREQ model:

- Short  $100F$  and  $50nF$

Solving for  $A_M$ :

\* note  $r_{\pi} = 5k$

\* note  $(5k \parallel 60.7k) = 4.62k$

$$A_M = \frac{V_o}{V_{\pi}} \cdot \frac{V_{\pi}}{V_s} = -20mV \cdot 8k \cdot \frac{4.62k}{4.67k}$$

$$A_M = -158 \frac{V}{V}$$

Solving for High FREQ:

$$K = \frac{V_o}{V_{\pi}} = -160, \quad \omega_{HP1} = \frac{1}{(50\Omega \parallel 4.62k\Omega)(C_{\pi} + C_N \cdot 16l)}$$

$$\omega_{HP2} = \frac{1}{(2pF)(8k)}$$

$$\omega_{HP3dB} = 43.4 \text{ M rad/s}$$

Solving for Low FREQ:

Zero at 50nF capacitor:

$$8k + \frac{1}{SC_E} \rightarrow 0 \quad [\text{For } g_M V_{\pi} = 0]$$

# Lecture 14

10/15/19

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SS 11.5 Midband Analysis:

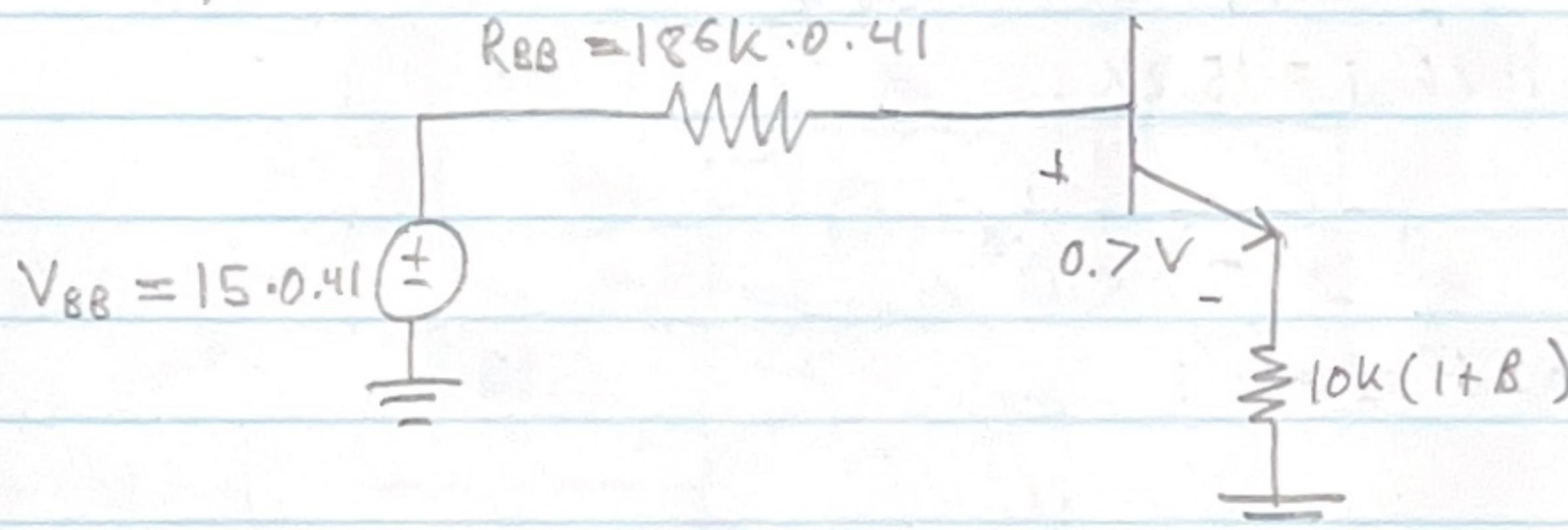
$$A_M = \frac{V_o}{V_s} = \frac{V_o}{V_{\pi}} \cdot \frac{V_{\pi}}{V_s}$$

$$\frac{V_o}{V_{\pi}} = -g_m R_c || R_L \quad , \quad \frac{V_{\pi}}{V_s} = -\frac{R_e || r_{\pi} / (1 + \beta)}{R_e || r_{\pi} / (1 + \beta) + R_s}$$

$$A_M =$$

PS4 Q2

$$\frac{127k}{186k + 127k} = 0.41$$



$$V_{BB} = I_B R_{BB} + 0.7V + I_B (10k)$$

$$I_B = \frac{15 \cdot 0.41 - 0.7}{186k \cdot 0.41 + 1.01M\Omega} = 5nA$$

$$I_C = \beta I_B = 500nA$$

$$g_m = 20mU \quad , \quad V_{\pi} = 5k$$

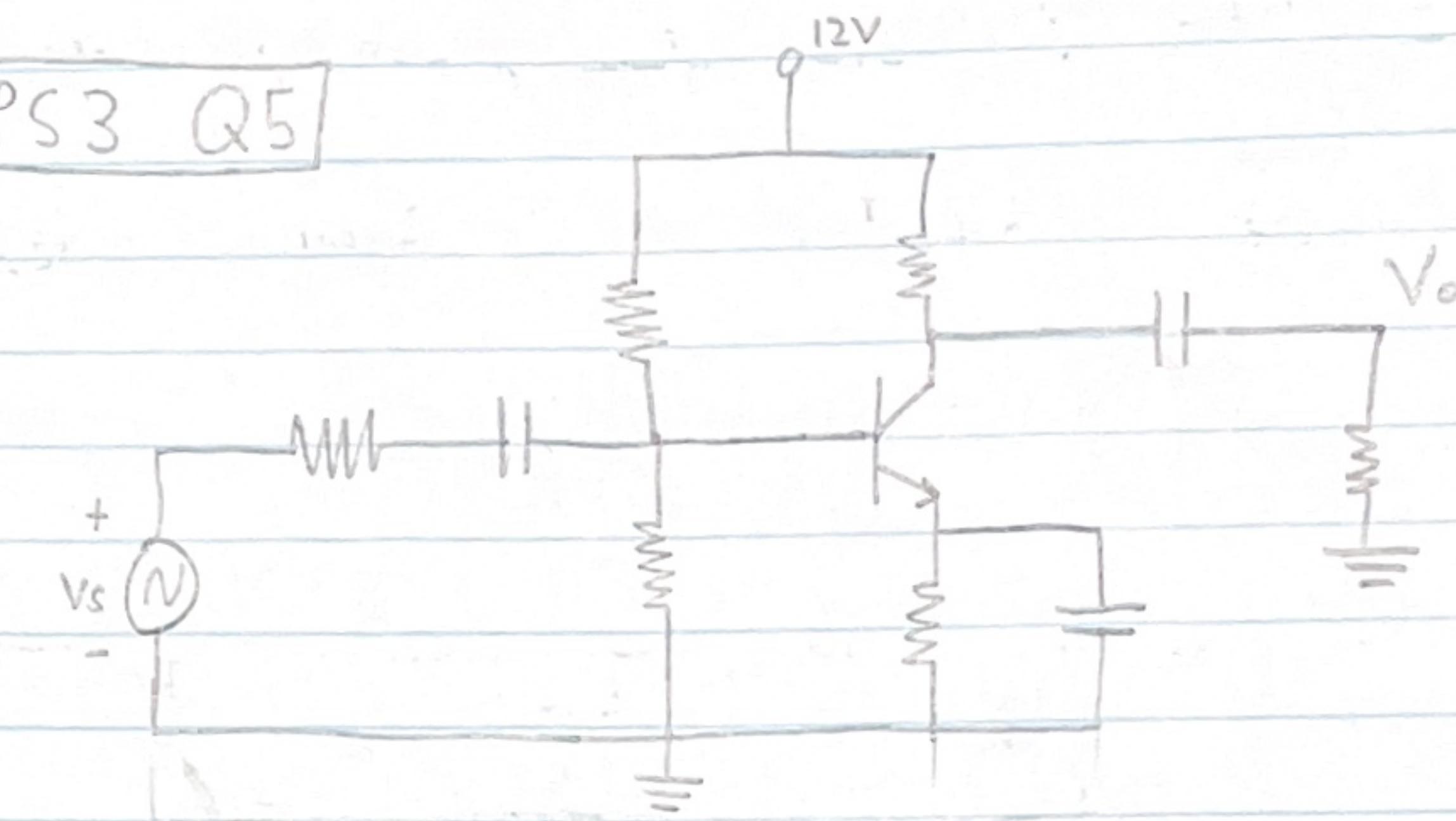
# Lecture 15

10/17/19

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\* No  $\gamma_3$  rule for already biased circuits  
ie: Q1, Q3

PS3 Q5



$$I_C = 2 \text{ mA}$$

$$\beta = 100$$

$$V_m = 80 \text{ mV}$$

$$r_{\pi} = 1.25 \text{ k}\Omega$$

$$r_{BB} = 36.5 \parallel 26.1 = 15.2 \text{ k}\Omega$$

\* V<sub>ce</sub> model from  
SS 10.4

$$W_{LP3} = \frac{1}{4k \cdot 0.5 \text{ nF}} = 0.5 \times 10^3 \text{ /sec}$$

$$T_{CE}^{sc} = \frac{50 \text{ nF} \cdot 2 \text{ k} \parallel (r_{\pi} + r_{BB} \parallel r_{\pi})}{1 + \beta} \quad \checkmark \text{ Higher FREQ dominant pole}$$

$$* T_{CE}^{sc} < T_{CC}^{sc}$$

$$T_{CC}^{sc} = 50 \text{ nF} \cdot (50 \Omega + r_{BB} \parallel r_{\pi})$$

$$W_{LP2} = \frac{1}{T_{CE}^{sc}} = 1.666 \times 10^3 \text{ /s}$$

# Lecture - 16

10/21/19

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## Questions

- ①  $I_C$  vs  $V_{CE}$  with variable  $V_{BE}$ , sweep parameters for  $V_{BE}$
- ② Transconductance  $g_m = \frac{I_C}{V_T}$  'or' from slope of  $I_C$  vs  $V_{BE}$

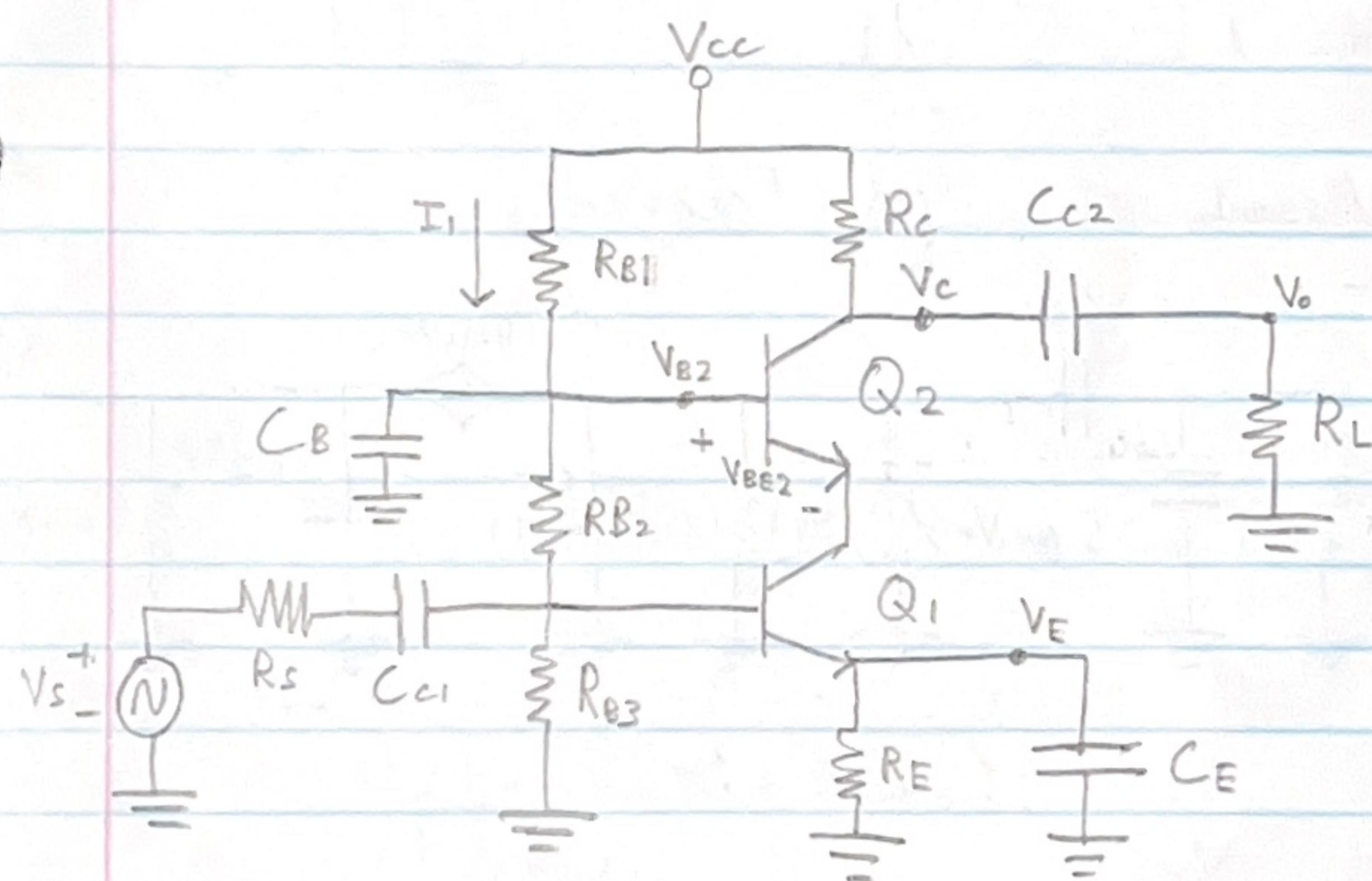
0.6 - 0.7

10/24/19

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# Lecture 17

## (CASCODE AMPLIFIER)



### Y<sub>4</sub> Rule Biasing

$$\text{Note: } V_{B1} = \frac{1}{4}V_{cc} + V_{BE1} \quad (\text{By biasing})$$

$$I_1 = 0.1 I_E$$

$$① V_{cc} - V_c = \frac{1}{4}V_{cc}$$

$$② V_E = \frac{1}{4}V_{cc}$$

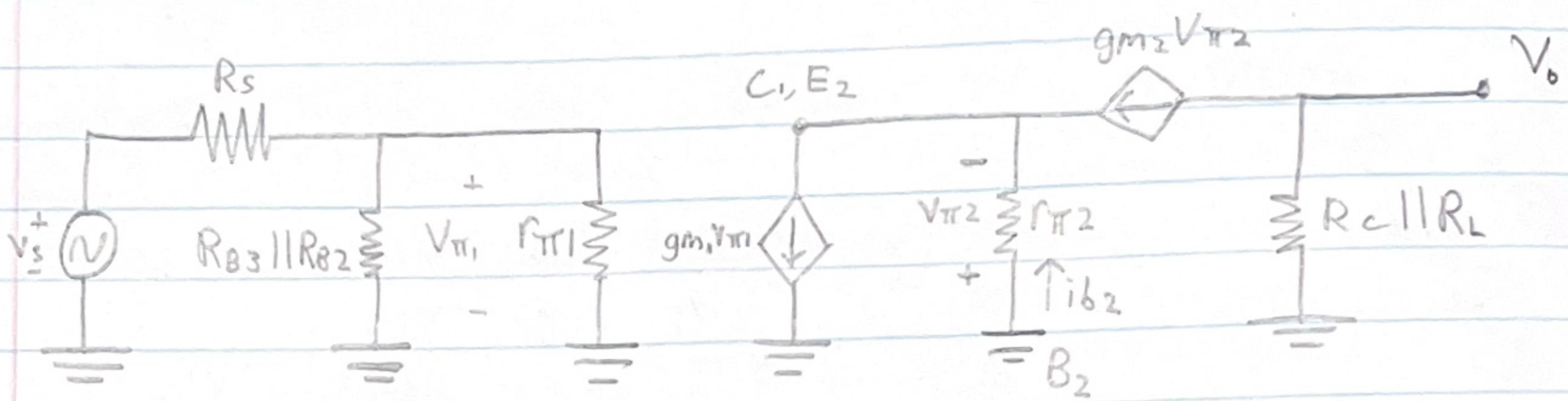
$$③ V_{B2} = \frac{1}{2}V_{cc} + V_{BE2}$$

$$V_{BE2} = 0.7V$$

$$= 0.7V$$

$$r_{\pi} = \frac{B V_T}{I_c}$$

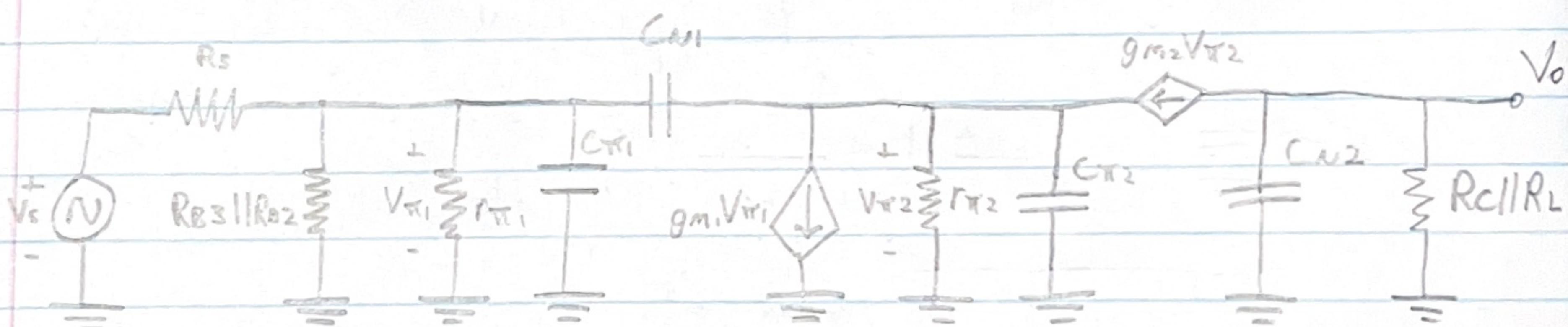
### Small Signal Model at Midband:



$$\frac{g_m V_{\pi_1}}{r_{\pi 2}} = V_{\pi 2} + g_{m2} V_{\pi 2}$$

$$\frac{B}{r_{\pi 1}} N_{\pi 1} = \left( \frac{1 + B_2}{r_{\pi 2}} \right) V_{\pi 2}$$

### Small Signal Model at High Frequency:



$$A_M = \frac{V_o}{V_{\pi 2}} = \frac{V_{\pi 2}}{V_{\pi 1}} \cdot \frac{V_{\pi 1}}{V_s}$$

Calculated  
above

$$= -g_{m2} R_L || R_c \cdot \frac{1 + R_{B3} || R_{B2} || r_{\pi 1}}{R_{B3} || R_{B2} || r_{\pi 1} + R_s}$$

# Lecture 14

10/31/19

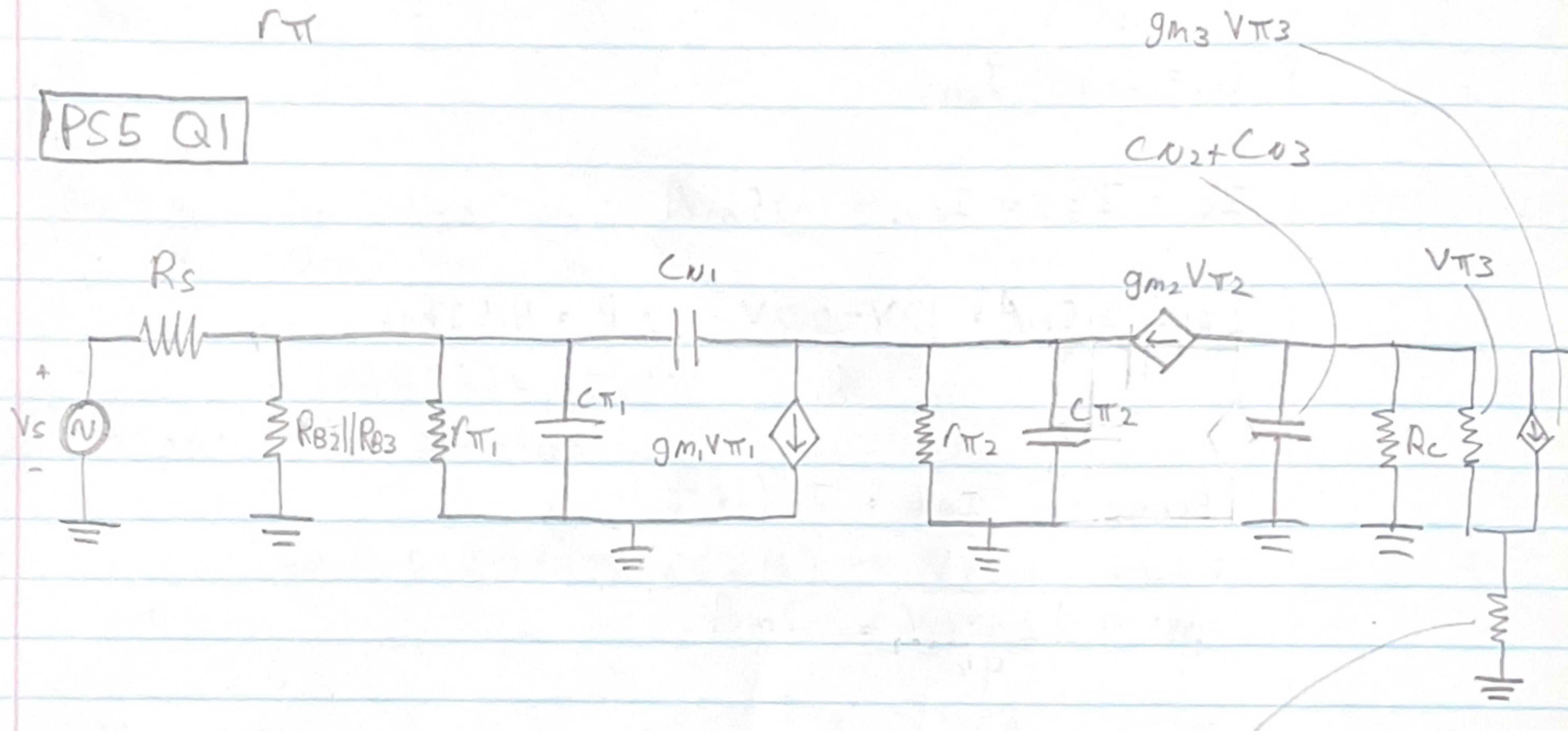
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SS 14.1

Figure 1 → Figure 2 [small signal mode]

$$g\pi = \frac{1}{r\pi}$$

PS5 Q1



$$W_{HP1} = \frac{1}{R_s || R_{B2} || R_{B3} || r_{\pi_1} (C_{\pi_1} + 2C_{n1})} = R_{E3} || R_L$$

$$W_{HP2} = \frac{1}{\left( \frac{r_{\pi_2}}{1+\beta_2} \right) (C_{\pi_2} + 2C_{n1})}$$

$$W_{HP3} = \frac{1}{[R_c || (r_{\pi_3} + (1+\beta_3)R_{E3} || R_L)] (C_{n2} + C_{n3})} \quad [\text{Lowest HFP (dominant)}]$$

# Lecture 15

11/4/19

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PS6 Q1

$$a) I_{(8k)} = \frac{12V - 2V}{8k\Omega} = \frac{10V}{8k\Omega} = 1.25mA$$

$$I_{c1} = I_{c2} \approx I_{(8k)}$$

$$I_{E1} = I_{E2} = I_{c1,2} = 1.25mA$$

$$I_{R1} = 2.5mA = \frac{12V - 0.7V}{R_1} \quad \therefore R_1 = 4.52k\Omega$$

Because  $I_{REF} = I_0 \left(1 + \frac{2}{\rho}\right)$  negligible for large  $\beta$

$$I_{(4k)} = \frac{12V - 4V}{4k} = 2mA$$

$$I_{o2} = 4mA$$

$$R_2 = \frac{12V - 0.7V}{4mA} = 2.825k\Omega$$

$$b) I_{c1} = I_{c2} = 1.25mA$$

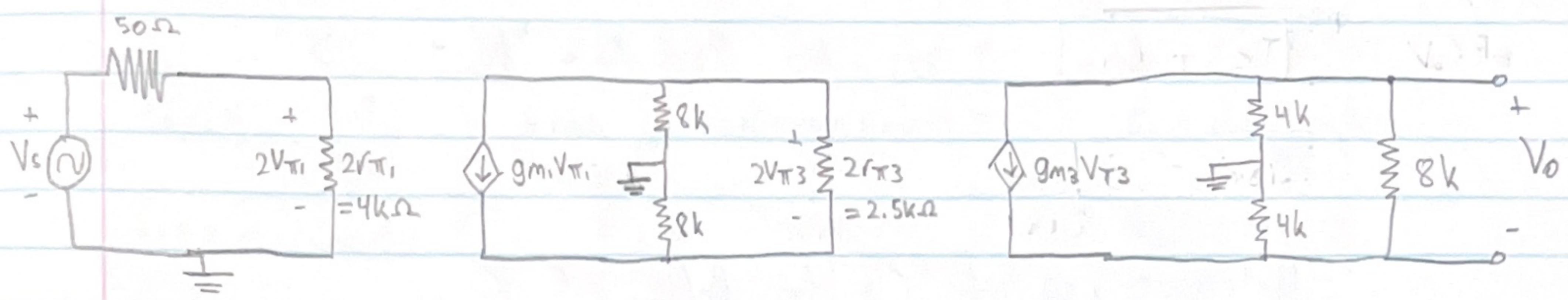
$$I_{c3} = I_{c4} = 4mA$$

$$g_{m1} = g_{m2} = 50mV$$

$$g_{m3} = g_{m4} = 80mV$$

$$r_{\pi 1} = r_{\pi 2} = \frac{100 \cdot 25mV}{1.25mA} = 2k\Omega$$

$$r_{\pi 3} = r_{\pi 4} = 1.25k\Omega$$



$$A_M = \frac{V_o}{V_s} = \frac{V_o}{V_{\pi_3}} \cdot \frac{V_{\pi_3}}{V_{\pi_1}} \cdot \frac{V_{\pi_1}}{V_s}$$

$$\frac{V_o}{V_{\pi_3}} = -g_{m_3} (8k \parallel 8k) = -320 \frac{V}{V}$$

$$\frac{2V_{\pi_3}}{V_{\pi_1}} = -g_{m_1} (2.5k \parallel 16k) = (5)(2)(2.16) \rightarrow \frac{V_{\pi_3}}{V_{\pi_1}} = -54.1 \frac{V}{V}$$

$$\frac{V_{\pi_1}}{V_s} = \frac{2V_{\pi_1}}{V_s} \cdot \frac{1}{2} = \frac{4k}{4.05k} \cdot \frac{1}{2} \approx \frac{1}{2} \frac{V}{V}$$

$$\therefore A_M = 8640 \frac{V}{V}$$

## Lecture 16

11/5/19

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\*\* [Test Q3] → up to PS6 Q1 \* Not Q2

PS5 Q3

Match zero of  $C_E$  to Pole of  $C_{C1}$

$$1500 \text{ rad/s} = \frac{1}{C_E (4k \parallel \frac{r_{\pi 1} + 50 + R_{B1} + R_{B2}}{1 + \beta_1})}$$

$$\begin{aligned} 1500 &\approx \frac{1}{C_E (4k \parallel \frac{5k + 50}{201})} \\ &\approx \frac{1}{C_E (25 \Omega)} \end{aligned}$$

$$\therefore C_E = 26.6 \text{ nF}$$

$$W_{ZCE} = W_{PC_{C1}} = \frac{1}{26.6 \text{ nF} (4k\Omega)} = 9.375 \text{ rad/s}$$

$$9.375 \text{ rad/s} = \frac{1}{C_{C1} [50 + R_{B1} \parallel R_{B2} \parallel (r_{\pi} + (\beta_1 + 1)4k)]}$$

$$R_{B1} = \frac{12V - 4V - 0.7V}{0.1mA} = 73k\Omega$$

$$R_{B2} = \frac{4 + 0.7V}{0.095mA} = 49.5k\Omega$$

$$C_{C1} = \frac{1}{9.375(28.5k)}$$

$$\therefore C_{C1} = 3.8 \text{ nF}$$

PS5 Q2

$$I_{E1} = 2.5 \text{ mA}$$

$$I_{E2} = 10 \text{ mA}$$

From given voltages

$$I = \frac{V}{R}$$

$$\beta_1 = \beta_2 = 100$$

$$g_{m1} = 100 \text{ mV}$$

$$g_{m2} = 400 \text{ mV}$$

$$r_{\pi 1} = 1 \text{ k}\Omega$$

$$r_{\pi 2} = 250 \Omega$$

Not Specified:

$$\beta = 100$$

$$C_{\pi} = 10 \text{ pF}$$

$$C_N = 1 \text{ pF}$$

$$V_{BE} = 0.7 \text{ V}$$

$$W_{LP3} = \frac{1}{[22 \Omega + 930 \Omega \parallel \frac{250 \Omega + 2 \text{ k}\Omega}{\beta + 1}] C_{\pi}} = 2300 \text{ rad/s}$$

11/7/19  
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## Lecture 17

PS5 Q2 (Cont'd)

$$W_{HP1} = \frac{1}{47.5 \Omega \cdot 12 \text{ pF}} = 1.74 \times 10^8 \text{ rad/s}$$

$$W_{HP2} = \frac{1}{1.1 \text{ k} \cdot 2 \text{ pF}} = 4.55 \times 10^8 \text{ rad/s} \quad A_M = -94 \text{ v}$$

\*\*  $C_{\pi 2}$  disappears by Pole-Zero Cancellation

\*\* [Test 03] → Up to SS. 14

# Lecture 18

11/19/19  
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PS7 Q4

$$V_{T1} = 64.6 \text{ kV}$$

$$V_{T2} = 5.81 \text{ kV}$$

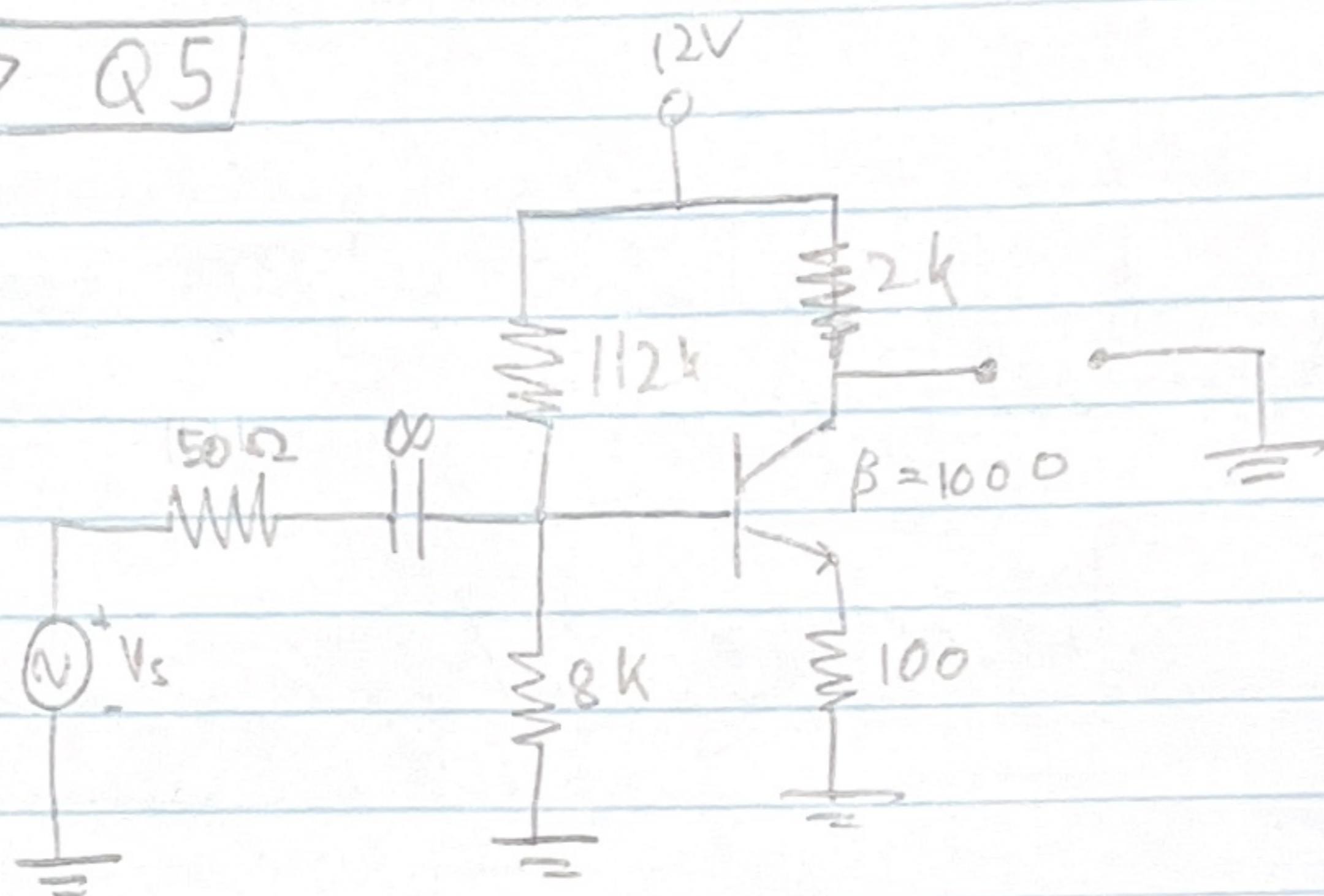
$$V_{T3} = 12.9 \text{ kV}$$

$$g_{m1} = 1.55 \text{ mV}$$

$$g_{m2} = 17.2 \text{ mV}$$

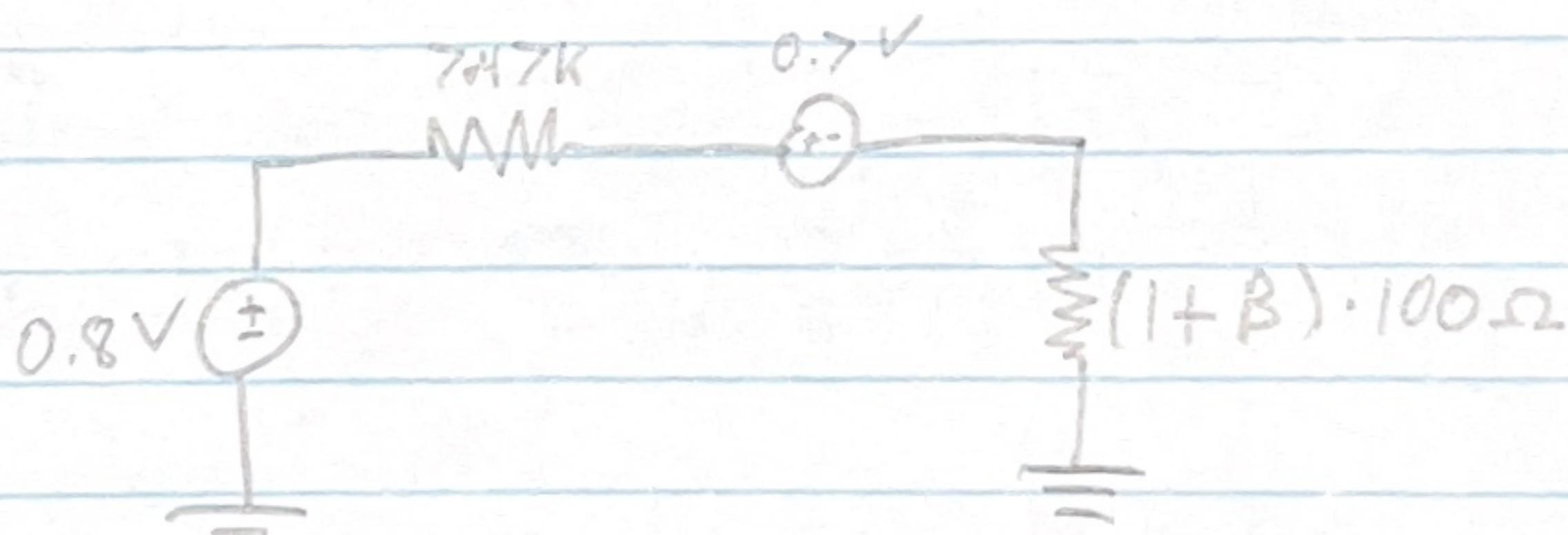
$$g_{m3} = 7.76 \text{ mV}$$

PS7 Q5



$$V_{BB} = \frac{12V \cdot 8k}{112k + 8k} = 0.8V$$

$$R_{BB} = \frac{112k \cdot 8k}{120k} = 7.47k\Omega$$



$$I_B = \frac{0.8V - 0.7V}{7.47k + (1+\beta) \cdot 100} = 0.93mA$$

$$I_C = 0.93mA \quad r_\pi = 26.9k\Omega \quad g_m = 37.2mV$$