



80 Pages
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EXERCISE BOOK CAHIER D'EXERCICES



NAME/NOM Cole Shanks

SUBJECT/SUJET ELEC 215



ASSEMBLED IN CANADA WITH IMPORTED MATERIALS
ASSEMBLÉ AU CANADA AVEC DES MATIÈRES IMPORTÉES

12107

Lecture 0

9/03/19

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Course Overview:

1 midterm \rightarrow 25%

1 Final \rightarrow 50%

Assignments throughout \rightarrow 15%

Participation (Iclicker) \rightarrow 10%

Japan Solar Workshop \rightarrow 10-3:00pm Kaiser

Office hours:

Tuesday \rightarrow 11:00 - 12:00

4:00 - 5:00

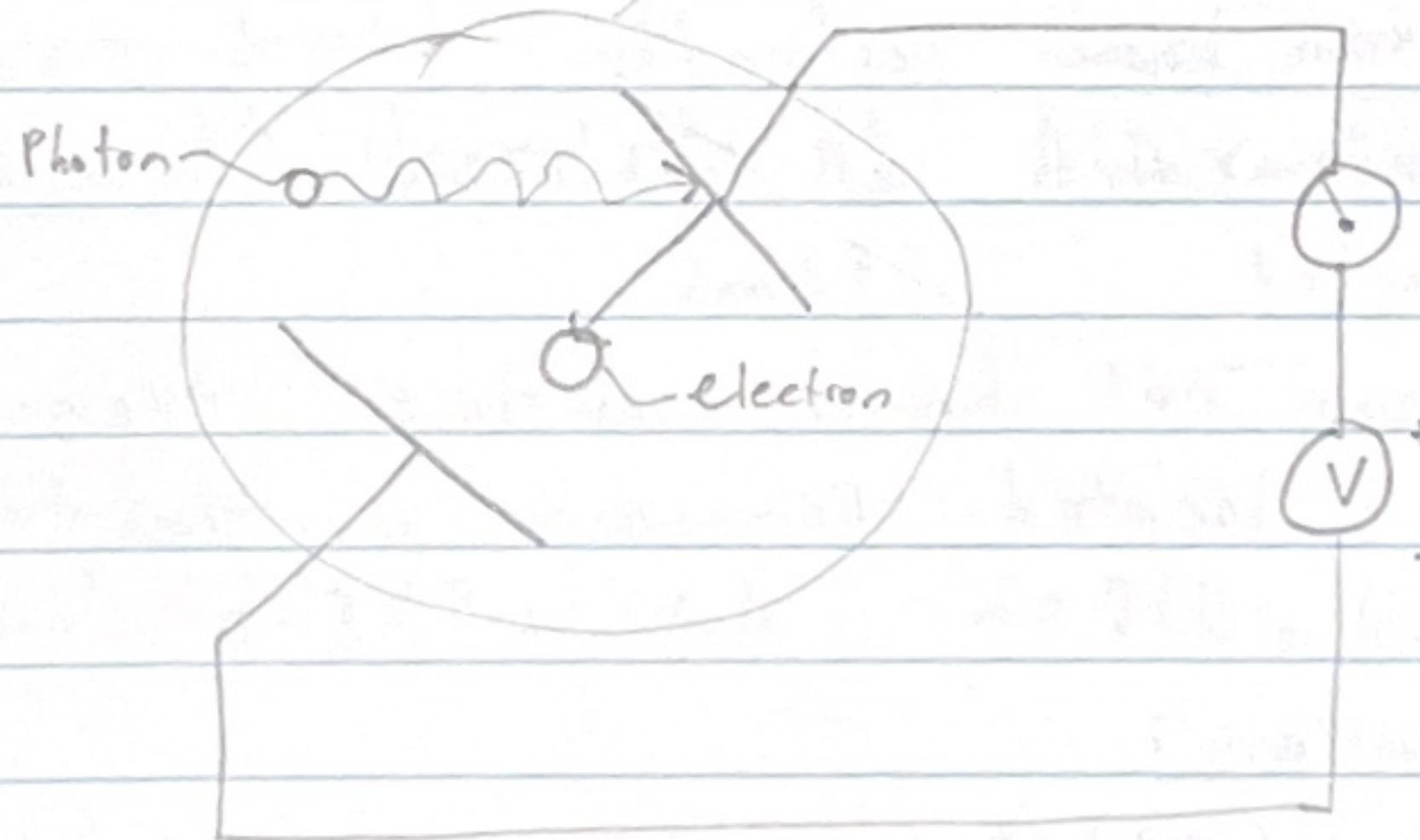
9/09/19

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Lecture 1

Photoelectric effect:

Vacuum (e's don't travel far in air)



Conservation of energy: energy of incoming photon = energy for electron to get out

$$KE_{\text{Max}} = -e\theta + h\nu$$

↳ Plank's constant
↳ Frequency

+
Kinetic energy
for the electron

Photons:

$$\text{Energy} = h\nu$$

$$(\text{Momentum}) \ p = \frac{h}{\lambda}$$

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Lecture 2

Conservation of energy: (assuming perfect collision)

Photon(energy) = Work function + Kinetic energy

- we use voltage to slow down approaching electrons

∴ Photon(energy) = Work function + applied voltage

(at the point where current cuts off)

Heisenberg Uncertainty Principle:

① Perfect sinusoid

- momentum known perfectly

- $(-\infty, \infty)$ can't be localized to a point/region

② Wave packet

- momentum not known (multiple frequencies)

- $(-\infty, \infty)$ located somewhere in the region X

Basic Equations:

① $E = h\nu$ (ν) Frequency

 (h) Planck's constant

② $\lambda = \frac{h}{p}$

$$\sin(kx - \omega t) \quad | \quad k = \frac{2\pi}{\lambda} \quad | \quad \omega = 2\pi f \quad | \quad v = \lambda f$$

Kinetic energy:

$$KE = \frac{p^2}{2m} \quad | \quad KE = \frac{h^2}{2m\lambda^2} \quad | \quad KE = -\frac{\hbar^2}{2m\Psi} \cdot \frac{d^2\Psi}{dx^2}$$

Schrödinger Equation:

$$i \cdot \hbar \cdot \frac{d\Psi}{dt} = -\frac{\hbar^2}{2m} \cdot \frac{d^2\Psi}{dx^2} + V \cdot \Psi$$

$$E(n) = \frac{n^2 \pi^2 \hbar^2}{2mL^2}$$

Lecture 3

$$\hbar = \frac{h}{2\pi}$$

(More confined \rightarrow more discrete)

(less discrete energy levels)

[1D Confinement]: $E(n) = \frac{n^2 \pi^2 \hbar^2}{2mL^2}$

[2D Confinement]: $E(nx, ny)$

$$= \frac{\hbar^2}{8m} \left(\frac{nx^2}{x_0^2} + \frac{ny^2}{y_0^2} \right)$$

Atomic Orbitals:

$n=1$ (S orbital) $n=2$ (P orbitals) $n=3$ (D orbitals)

(Degrees of degeneracy) = (# of wave functions @ specific energy level)

Lecture 4

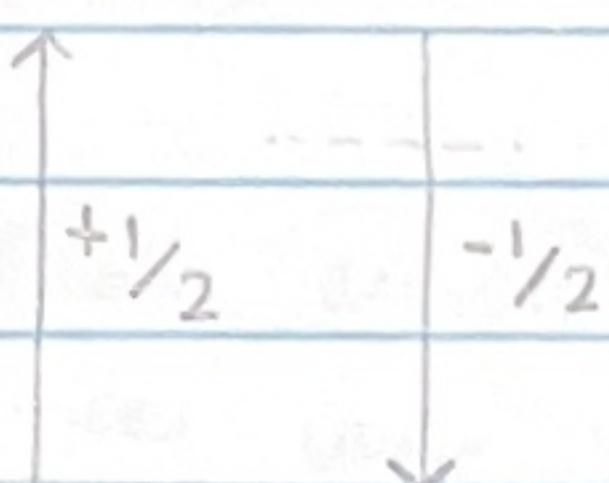
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Covalent Bonding: (Bringing two H atoms close together)

- Energy levels split into new more levels
- Solid structure of many atoms can start to have a continuous looking number of energy levels (why solar cell can absorb anywhere)

Electron Spin:



• Quantized (up or down)

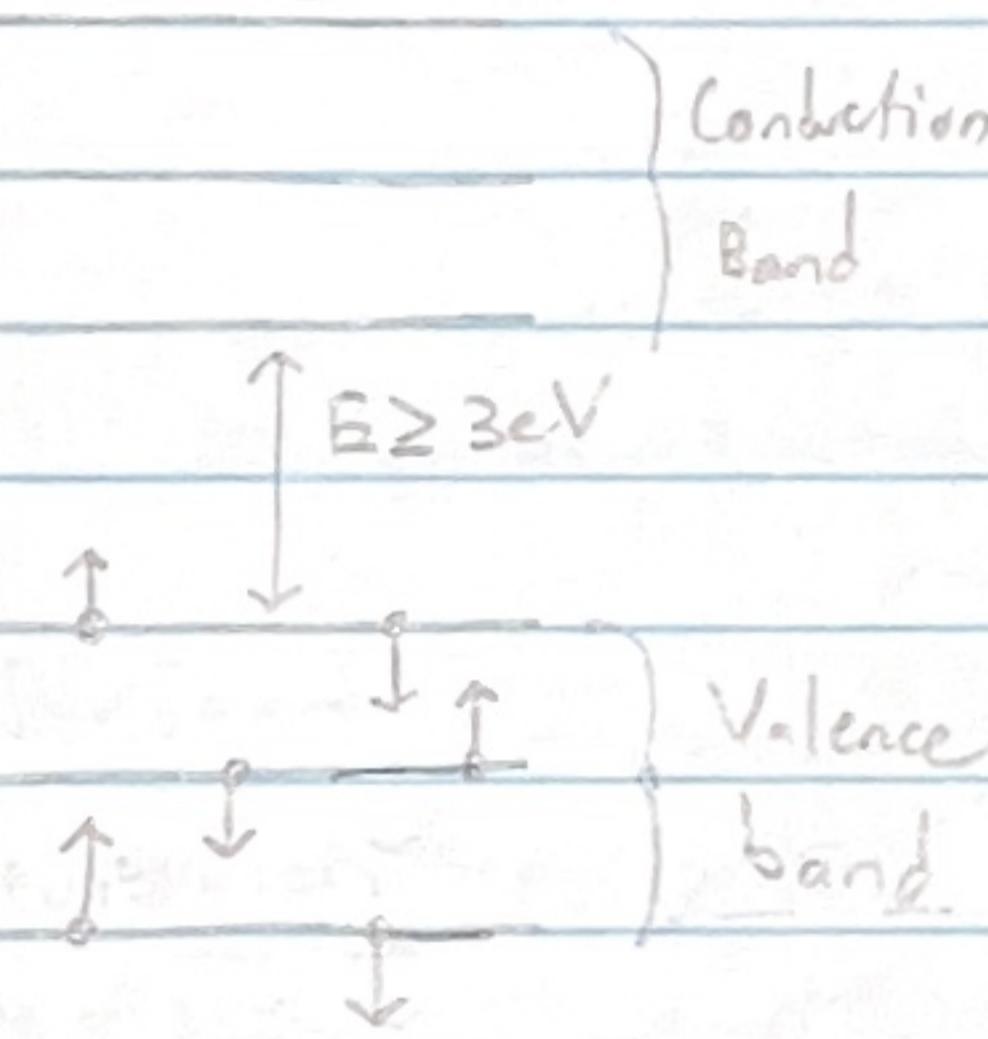
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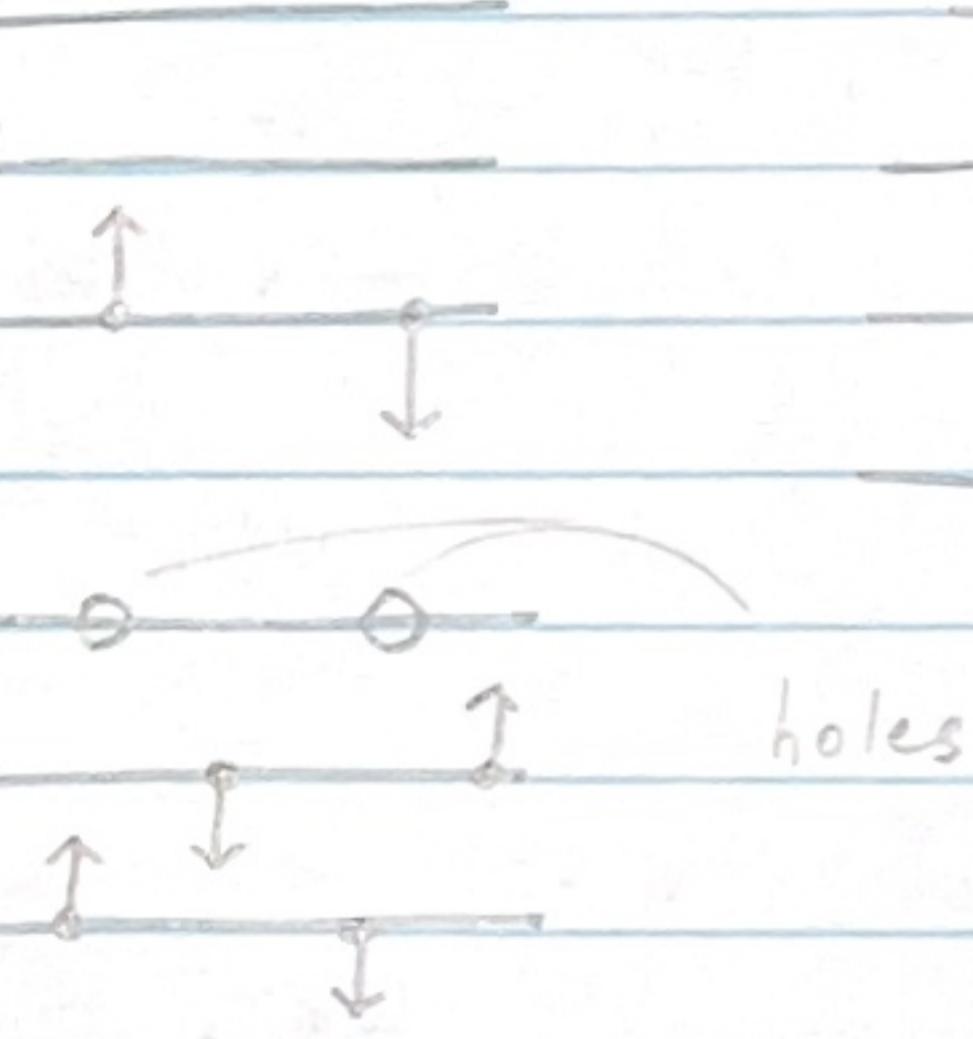
Lecture 5 (solids and Semiconductors)

SLIDE SET

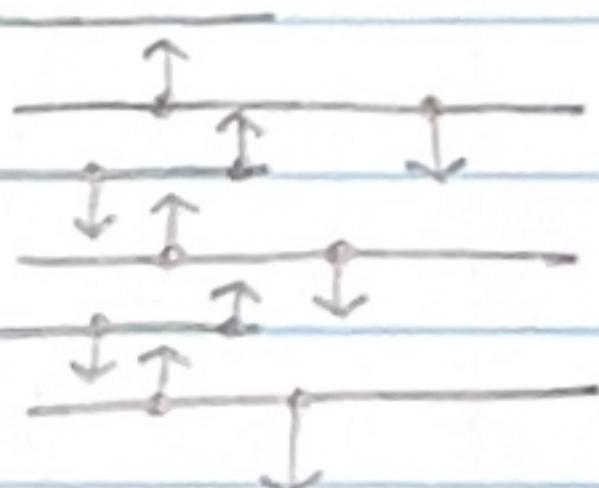
Insulator:



Semiconductor:



Conductor (metal):



[Q 6 c-d] (6-c-d) total energy = kinetic energy

[Q 8g] Assume $n_x = n_y = n_z = 1$ (ground state) assume material is silicon

Polycrystalline:

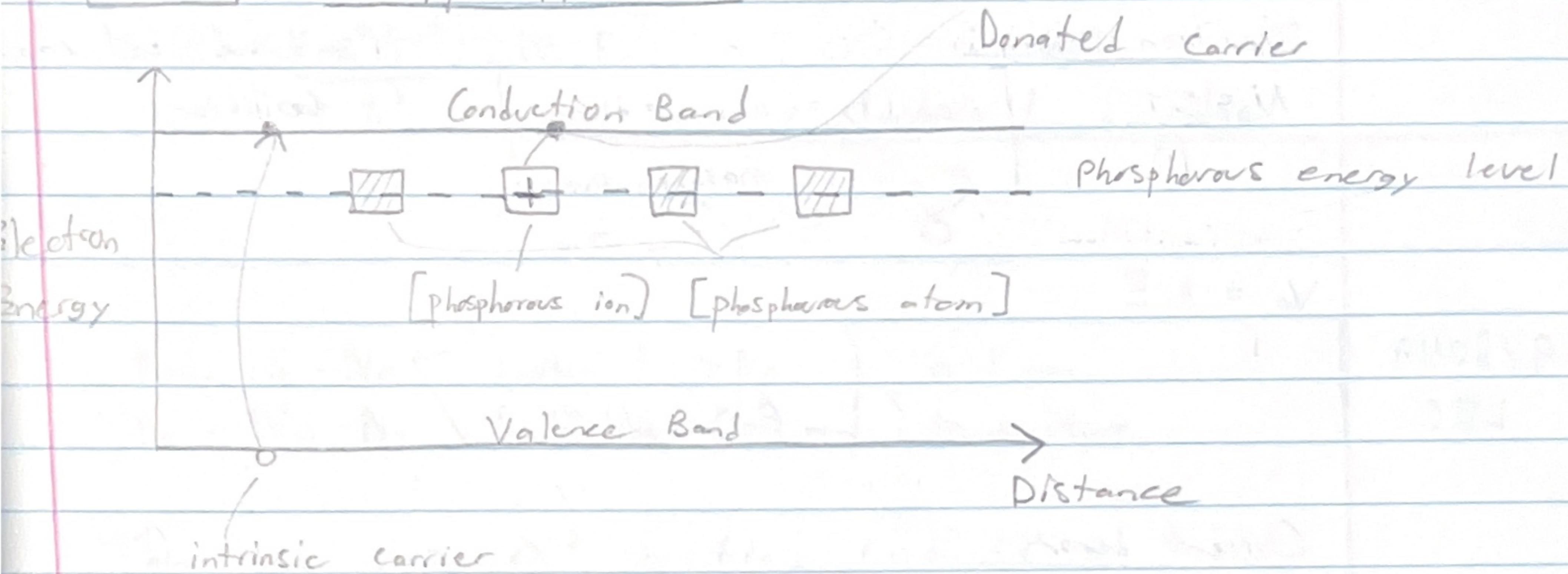
Grain boundaries non-conductive

[SS11] i subscript means intrinsic ie: undoped

$N_i = P_i \rightarrow$ # holes in valence band
 \hookrightarrow # e's in conduction band

Lecture 6

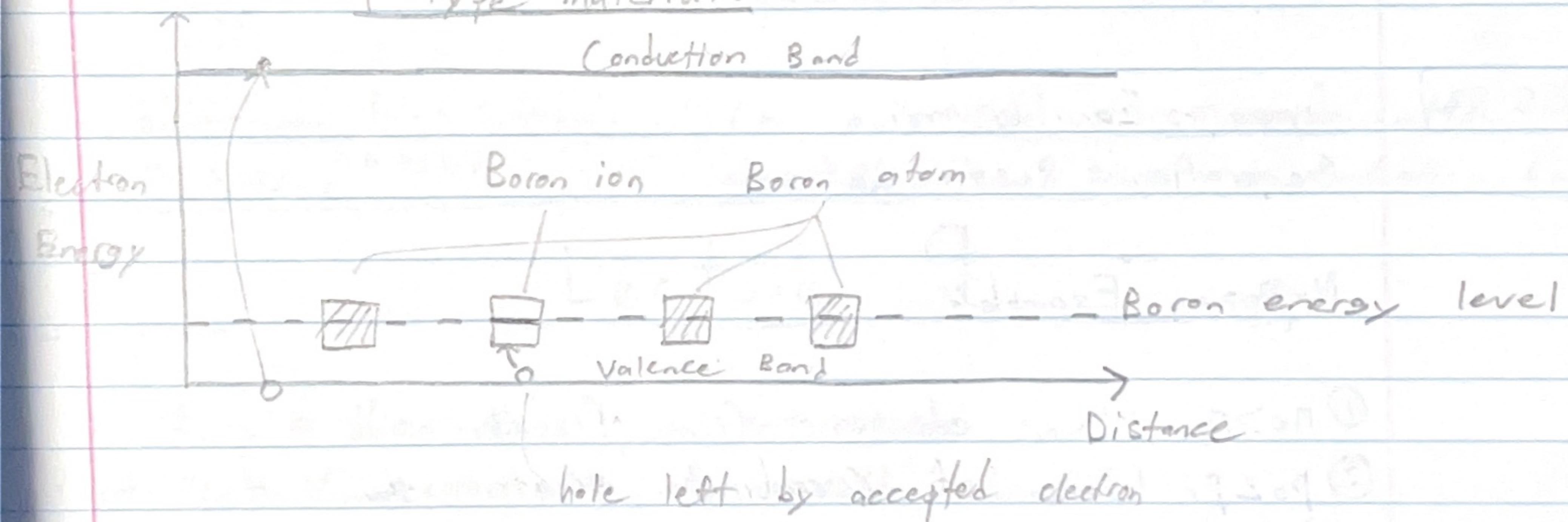
SS 15 n-Type Material:



Electron effective mass:

$$m_0 = 9.1 \times 10^{-31} \text{ kg} \quad [\text{Free electron mass}]$$

p-Type material:



Current:

$$J = \sigma E \quad (\text{current density} = \text{conductivity} \cdot \text{Electric field})$$

What effects Conductivity:

- ① time between collisions
- ② electron mobility (effective mass)
- ③ # of carriers per unit volume

$$\text{Current} = L \cdot A \cdot N_e \cdot v_e \quad \text{where: } \frac{L}{T} = v_e$$

Electron Mobility:

$$N = \frac{eT}{m}$$

$$\left[\begin{array}{l} \text{mobility} = \frac{e \cdot \text{charge}}{\text{mass} \cdot \text{effective}} \cdot \text{time} \end{array} \right]$$

$T = \text{time between collisions}$

$$v_e = NE$$

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Lecture 7

Current density:

$$J = eE(N_e v_e + P_h v_h)$$

where: N_e = electron density in conduction band

P_h = hole density in valence band

v_e = electron mobility

v_h = hole mobility

[SS 52]

Dynamic Equilibrium:

Generation = Recombination

N-Doping Example:

① $N_d > N_i$ (Donor electrons from Phosphorus)

② $P_o < P_i$ (Rate of recombination greater than at intrinsic)

[SS 60]

Rate of Generation:

[@ Equilibrium] $R = G$

$$G = f_g(\text{Temp})$$

Rate of Recombination:

$$R = f_r(\text{Temp}) N_e P_o$$

$$N_e P_o = N_i P_i$$

$$\therefore N_e P_o = N_i^2$$

Density of States: (3D) [how many states per unit volume at the given energy level (E)]

$$g_c(E) = \frac{(m_e^*)^{3/2}}{\pi^2 \hbar^3} \int_0^E 2(E - E_c)^{1/2} dE$$

Conduction band edge

Lecture 8

$$N_D = N_D - N_A \quad (\text{when } N_D > N_A) \quad @ \text{ Room}$$

$$P_D = N_A - N_D \quad (\text{when } N_A > N_D) \quad \text{temperature}$$

Then, use $N_D P_D = n_i^2$ to find n_D, P_D

Counting electrons: where:

n = total # e's in conduction band

$$n = \int_{CB} g_c(E) \cdot f(E) dE \quad g_c(E) = \text{Density of states}$$

$f(E) = \text{occupancy probability}$

Boltzmann Distribution: (Can only use this approximation above the fermi level i.e. conduction band)

Lecture 9

$$N_D = \# \text{ donor atoms per unit volume}$$

$$N_A = \# \text{ acceptor atoms per unit volume}$$

N-doped material:

$$n_D = N_D \quad (@ \text{ room temperature})$$

P-doped material:

$$P_D = N_A \quad (@ \text{ room temperature})$$

Counting holes:

$$P_0 = \int_{\text{Bottom VB}}^{\text{Top VB}} g_V(E) (1 - f(E)) dE$$

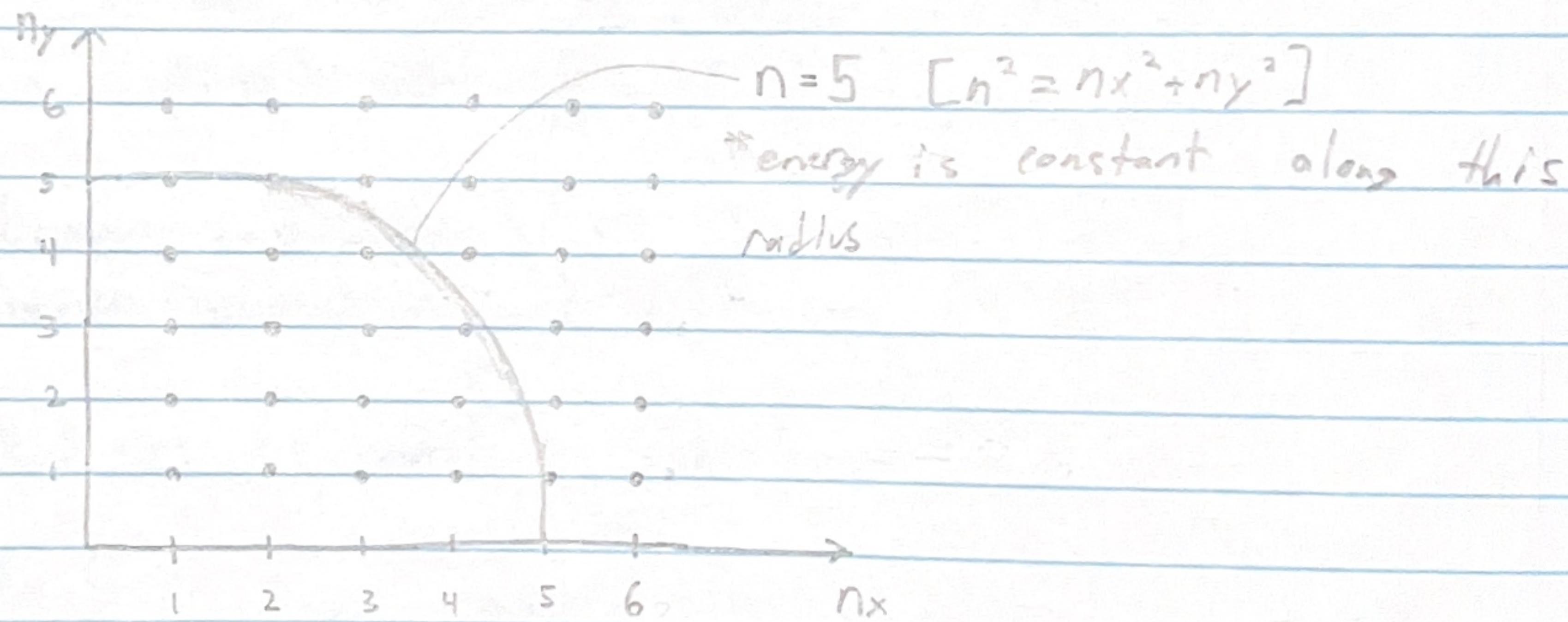
3D box:

$$E = \frac{h^2}{8m} \left[\frac{n_x^2}{L_x^2} + \frac{n_y^2}{L_y^2} + \frac{n_z^2}{L_z^2} \right]$$

2D box: if ($L_z \ll L_x$ and L_y) and ($L_x = L_y$)

$$E_{2D} = \frac{h^2}{8m L_x^2} [n_x^2 + n_y^2]$$

Find Density of States:



$$N = \frac{\pi n^2}{2}$$

Intrinsic e's:

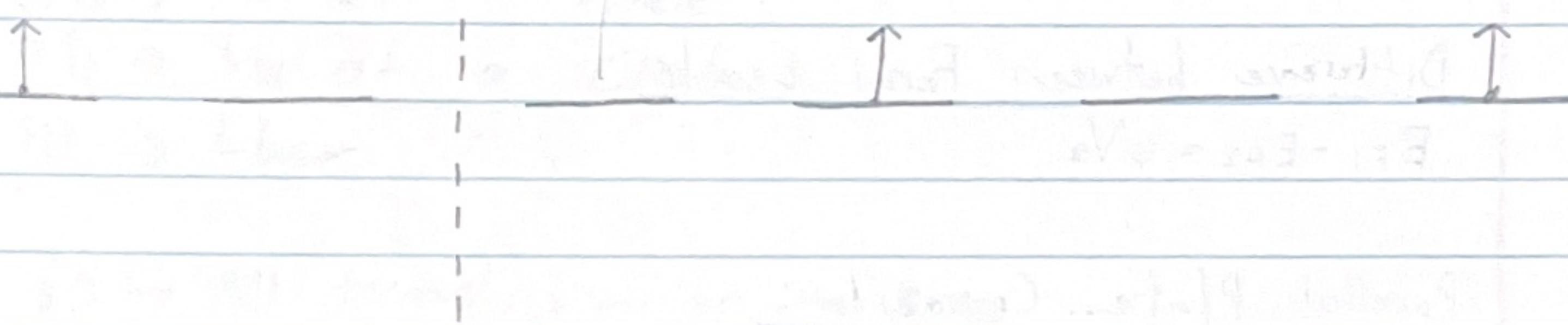
$$n_i^2 = 10^{20}$$

Lecture 10

Filling Level:

room for 2 e's

n

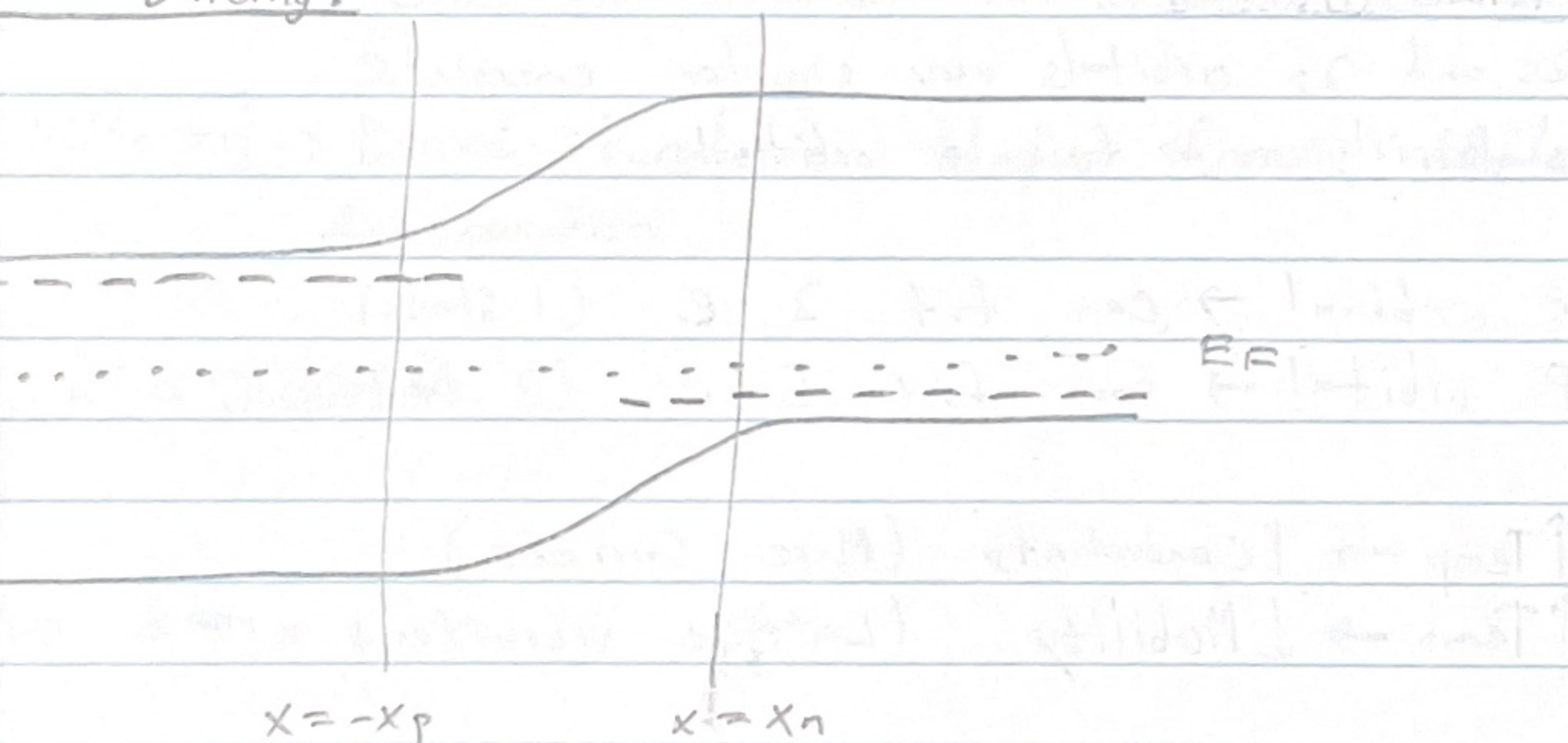


$$E_F = \frac{1}{4}$$

$$E_F = \frac{2}{8} = \frac{1}{4}$$

Lecture 11

Band Bending:



SS 173] $U(x) \propto \frac{+e\alpha}{2\epsilon} x^2$

SS 179] ASN 3 Q3 Derivation

Lecture 12

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Diode Equation:

$$I = I_o(e^{\frac{eV_a}{RT}} - 1)$$

Difference between Fermi Levels:

$$E_{F1} - E_{F2} = eV_a$$

Parallel Plate Capacitor:

$$C = \epsilon_r \epsilon_0 A$$

$$\frac{1}{d}$$

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Lecture 13

Review Orbitals:

2s and 2p orbitals very similar energies

i.e.: Berrillyum \rightarrow full p orbital

S orbital \rightarrow can fit 2 e (1 state)

P orbital \rightarrow can fit 6 e (3 states)

Intrinsic Material {
 \uparrow Temp \rightarrow \uparrow Conductivity (More carriers)
 \uparrow Temp \rightarrow \downarrow Mobility (Lattice vibrations = more collisions)}

* But $n_i \gg N_e$

Doped Material {
 \uparrow Temp \rightarrow \downarrow Conductivity
 \uparrow Temp \rightarrow \downarrow Mobility
 $N_d \gg n_i$ so $n_d = \text{Fixed}$ $\therefore N_e$ dominates

\uparrow Temp \rightarrow \uparrow Conductivity (Intrinsic Semiconductor)

\uparrow Temp \rightarrow \downarrow Conductivity (Metal)

\uparrow Temp \rightarrow $\downarrow \rightarrow \uparrow$ Conductivity (Doped Semiconductor)

Midterm → Derive either 1D, 2D or 3D $g(B)$
or ~~a~~ midterm

3D → $\frac{1}{8}$ of a sphere

2D → $\frac{1}{4}$ of a circle

1D → Line

3D → All terms similar in size

2D → One term much bigger (ie: small L)

1D → Two terms much bigger (ie small L 's)

Silicon Band Gap = 1.12eV

Midterm → One PN Junction Band diagram (either eqv, Fwd, reverse)

Midterm → Derive Parabolic shape from depletion Approximation

$$kT = 0.025 \text{ eV}$$

Lecture 14

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Common Exam Question \rightarrow SS.24

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Lecture 15

Polarization:

$$P = P_0 e^{-\gamma T} \rightarrow P(w) = \frac{P_0}{\gamma T + i w}$$

Susceptibility:

$$\chi(w) = \frac{P(w)}{\epsilon_0 E_0} = \frac{\chi_0}{\gamma T + i w}$$

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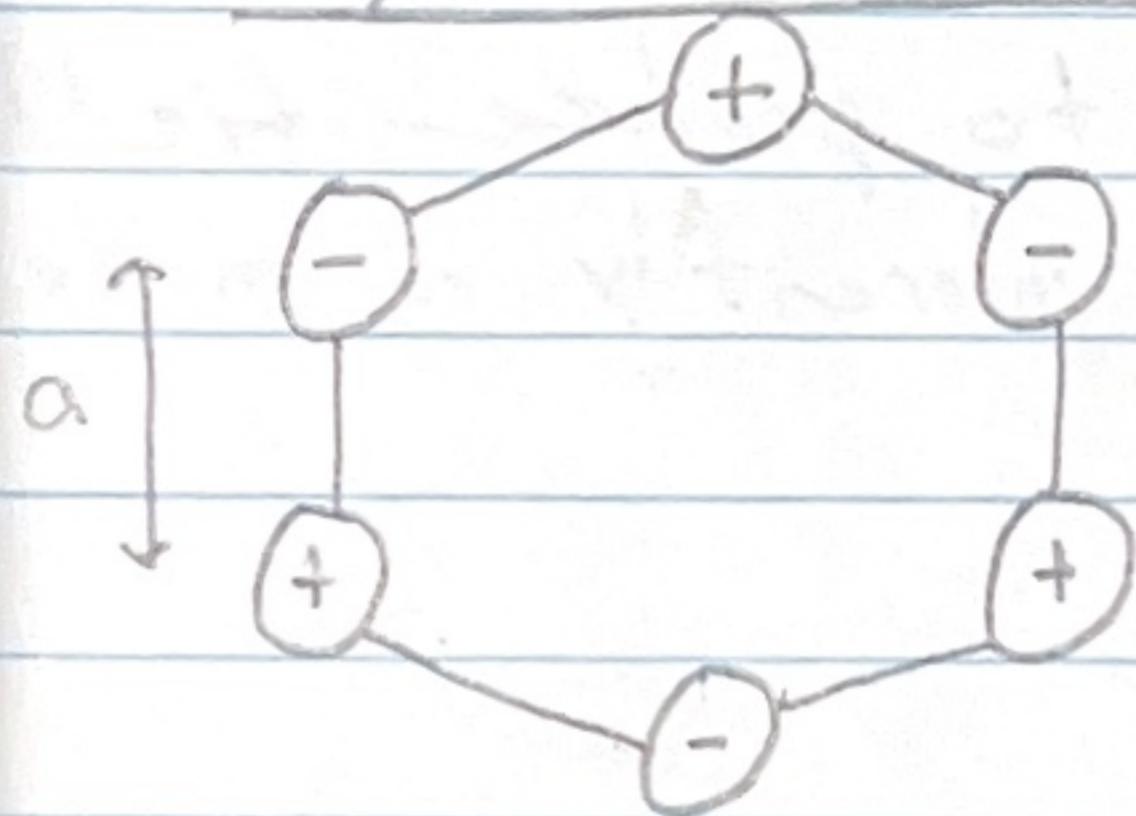
Lecture 15

$$\text{Energy} = \frac{1}{2} C V^2$$

$eE\lambda \geq E_g$ (For electron to be promoted)

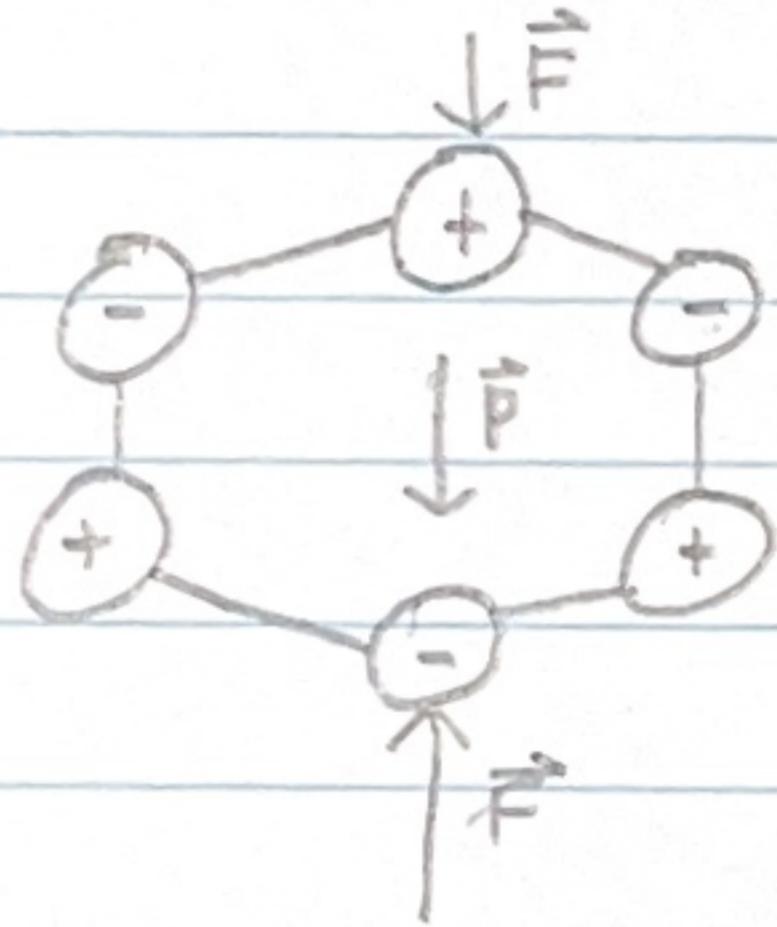
Lecture 16

Crystal Structure A:



- No dipole moment
- $\vec{P} = 0$

Crystal Structure (B) [Compressed]:



- Net dipole moment
- \vec{P} is non-zero

Direct Piezoelectric Equation:

$$P_x = d_x T_x \text{ where:}$$

P_x = Polarization

T = applied stress \vec{F}/Area

d_x = piezoelectric constant

$$\frac{\Delta L}{L} = d E$$

$$E = \frac{\Delta L}{\delta L}$$

$$E = \frac{\Delta L}{L^2}$$

$$V = \frac{\Delta L}{\delta L}$$