#### EECE488: Analog CMOS Integrated Circuit Design

Set 3

#### **Differential Amplifiers**

Shahriar Mirabbasi
Department of Electrical and Computer Engineering
University of British Columbia
shahriar@ece.ubc.ca

1

#### Overview

Reading: Chapter 4 of the Textbook nost important circuit inventions.

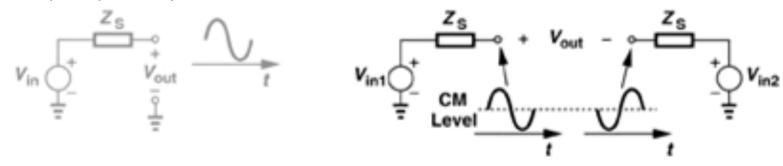
Their invention dates back to vacuum tube era (1930s).

 Alan Dower Blumlein (a British Electronics Engineer, 1903-1942) is regarded as the inventor of the vacuum-tube version of differential pair.

 Differential operation offers many useful properties and is widely used in analog and mixed-signal integrated circuits

## Single-ended and Differential Signals

- A "single-ended" signal is a signal that is measured with respect to a fixed potential (typically ground).
- "Differential signal" is generally referred to a signal that is measured as a difference between two nodes that have equal but opposite-phase signal excursions around a fixed potential (the fixed potential is called common-mode (CM) level).



# Board Notes (Differential Amplifiers)

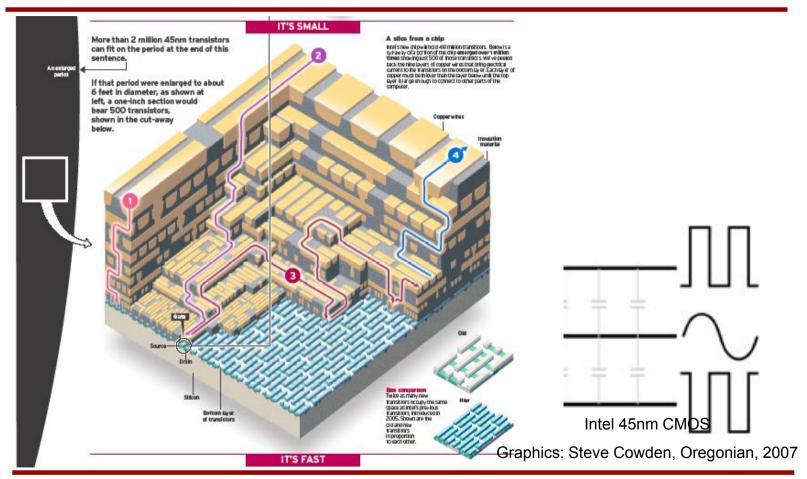
## Why Differential?

Better immunity to environmental noise

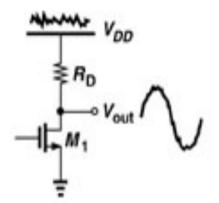
Improved linearity

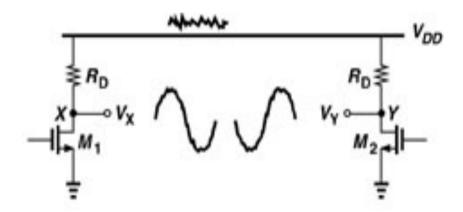
Higher signal swing compared to single-ended

# Higher Immunity to Noise Coupling



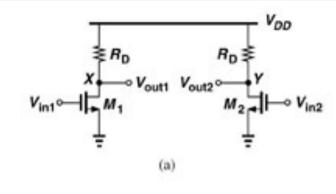
# **Supply Noise Reduction**

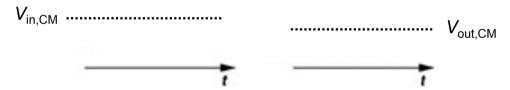




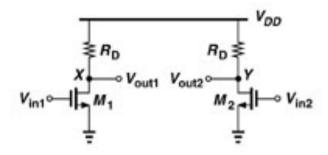
# **Board Notes (Improved Linearity)**

#### **Basic Differential Pair**



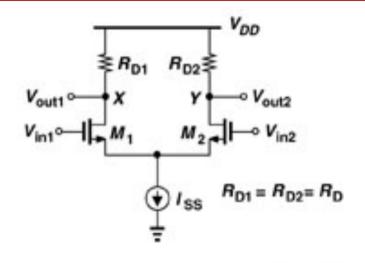


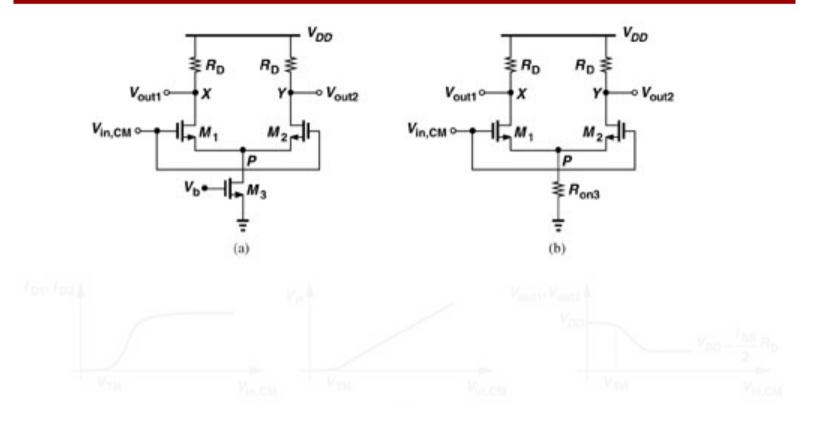
#### **Basic Differential Pair**



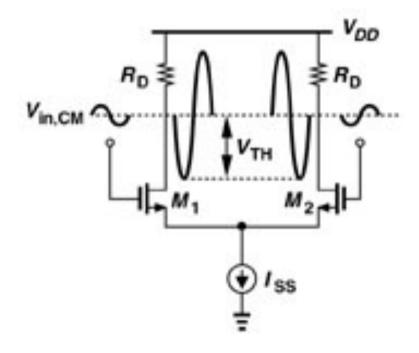
- Problem: Sensitive to input common-mode (CM) level
  - Bias currents of the transistors M<sub>1</sub> and M<sub>2</sub> changes as the input CM level changes
  - g<sub>m</sub> of the devices as well as output CM level change
- Can we think of a solution?

#### **Differential Pair**



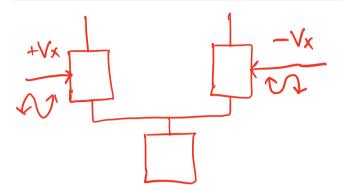


# Common-Mode Input versus Output Swing



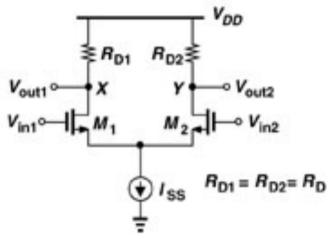
# Board Notes ("Half-Circuit" Concept)

# Board Notes ("Half-Circuit" Concept)



## Example

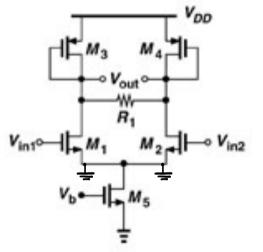
 Using the half-circuit concept, calculate the small-signal differential gain of the following circuit (for two cases of λ=0 and λ≠0).



# Gote and Drain Connected = Diode Connected Example

Using the half-circuit concept, calculate the small-signal differential gain of the following circuit (for two cases of λ=0 and

λ**≠**0).

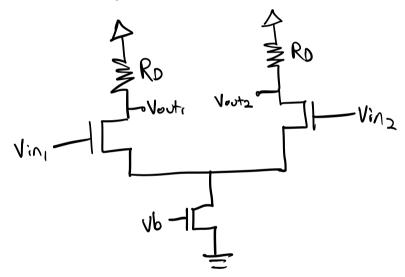


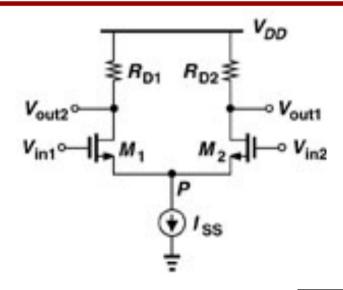
- Common Source Amplifier with diode connected load in parallel with resistive

$$\frac{Vod}{Vid} = -9 \, \text{m.} \left( \frac{1}{9m_3} \left| \left| \frac{R_1}{2} \right| \right) \frac{Vod}{Vid} = -9 \, \text{m.} \left( \frac{1}{9m_3} \left| \left| \frac{Co_3}{co_1} \right| \right| \right)$$

## Example

 Sketch the small-signal gain of a differential pair as a function of its input common-mode level.





$$V_{in1} - V_{in2} = V_{GS1} - V_{GS2}, \qquad V_{GS} = \sqrt{\frac{2I_D}{\mu_n C_{ox} \frac{W}{L}}} + V_{TH}$$

$$V_{in1} - V_{in2} = \sqrt{\frac{2I_{D1}}{\mu_n C_{ox} \frac{W}{L}}} - \sqrt{\frac{2I_{D2}}{\mu_n C_{ox} \frac{W}{L}}}$$

$$(V_{in1} - V_{in2})^2 = \frac{2}{\mu_n C_{ox} \frac{W}{L}} (I_{D1} + I_{D2} - 2\sqrt{I_{D1}I_{D2}})$$

$$\frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{in1} - V_{in2})^2 - I_{SS} = -2\sqrt{I_{D1}I_{D2}}$$

$$\frac{1}{4}(\mu_n C_{ox} \frac{W}{L})^2 (V_{in1} - V_{in2})^4 + I_{SS}^2 - I_{SS} \mu_n C_{ox} \frac{W}{L} (V_{in1} - V_{in2})^2 = 4I_{D1}I_{D2}$$

Using:

$$4I_{D1}I_{D2} = (I_{D1} + I_{D2})^2 - (I_{D1} - I_{D2})^2 = I_{SS}^2 - (I_{D1} - I_{D2})^2$$

and

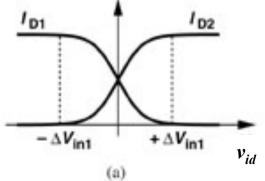
$$4I_{D1}I_{D2} = \frac{1}{4}(\mu_n C_{ox} \frac{W}{L})^2 (V_{in1} - V_{in2})^4 + I_{SS}^2 - I_{SS} \mu_n C_{ox} \frac{W}{L} (V_{in1} - V_{in2})^2$$

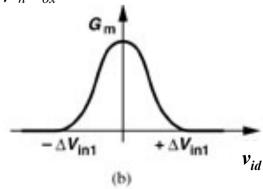
We have:

$$I_{D1} - I_{D2} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} \underbrace{(V_{in1} - V_{in2})}_{\text{voltey c}} \sqrt{\frac{4I_{SS}}{\mu_n C_{ox} \frac{W}{L}} - (V_{in1} - V_{in2})^2}$$

$$i_{d} = \frac{1}{2} \mu_{n} C_{ox} \frac{W}{L} v_{id} \sqrt{\frac{4I_{SS}}{\mu_{n} C_{ox} \frac{W}{L}} - v_{id}^{2}}$$

$$\frac{\partial I_{d}}{\partial v_{id}} = G_{m} = \frac{1}{2} \mu_{n} C_{ox} \frac{W}{L} \frac{\frac{4I_{SS}}{\mu_{n} C_{ox} W / L} - v_{id}^{2}}{\sqrt{\frac{4I_{SS}}{\mu_{n} C_{ox} W / L} - v_{id}^{2}}}$$





• For small  $v_{id}$ :

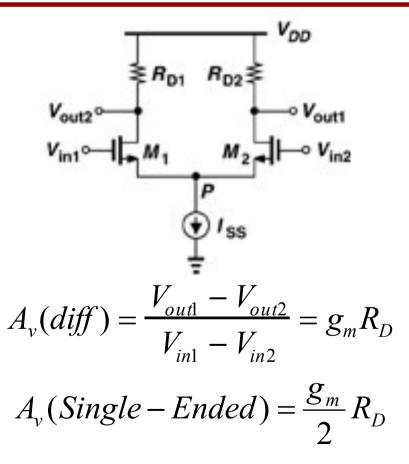
$$G_{m} = \frac{\partial i_{d}}{\partial v_{id}} = \sqrt{\mu_{n} C_{ox} \frac{W}{L} I_{SS}} = g_{m1} = g_{m1}$$

We have:

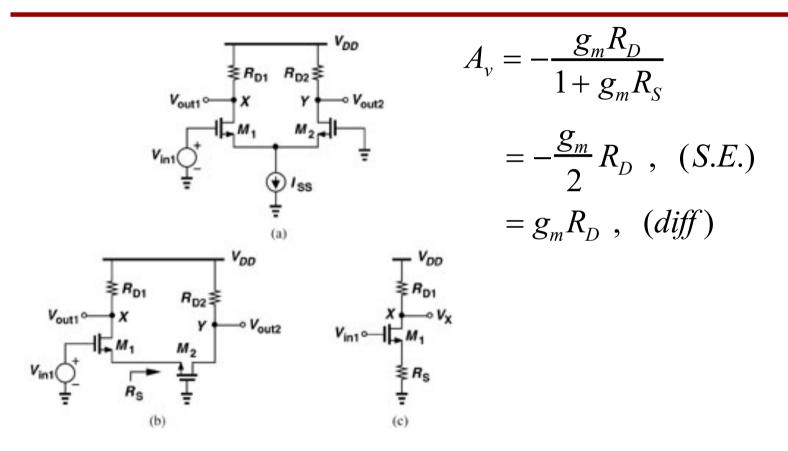
$$V_{out1} - V_{out2} = R_D(I_{D1} - I_{D2}) = R_DG_m(V_{in1} - V_{in2})$$

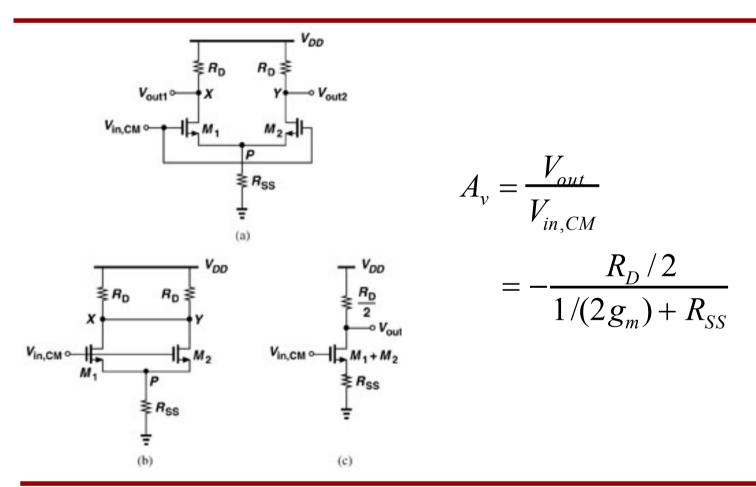
$$\frac{V_{out1} - V_{out2}}{V_{in1} - V_{in2}} = g_{m1}R_D$$

#### **Differential Gain**



# Differential Pair as a CS and CD-CG Amplifier

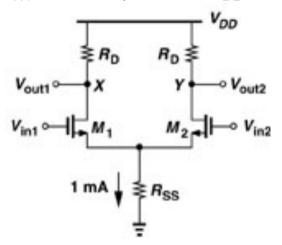




### **Board Notes**

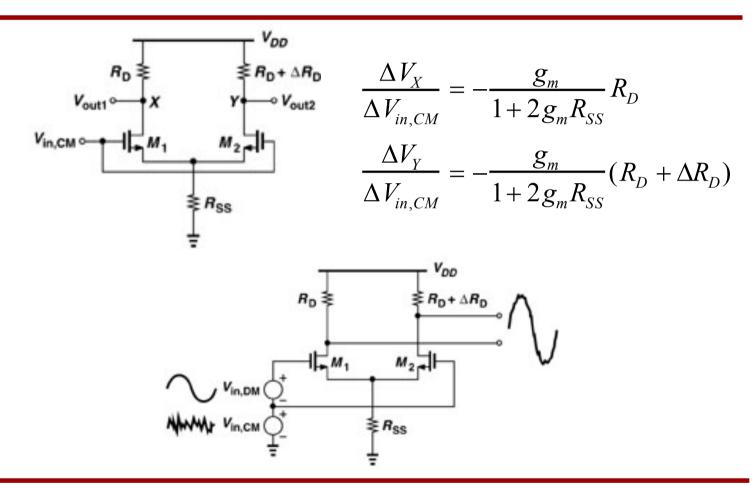
#### Example

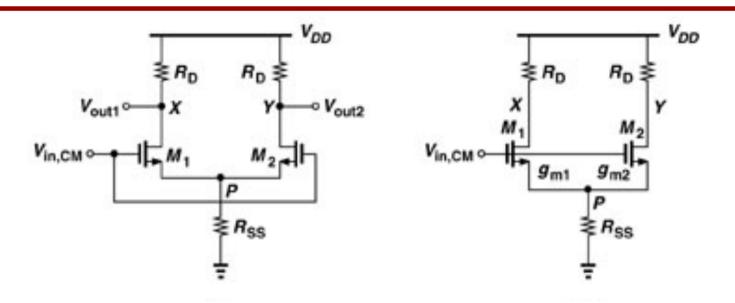
• In the following circuit assume that  $R_{SS}$ =500 $\Omega$  and W/L=25/0.5,  $\mu_n C_{ox}$ =50 $\mu$ A/V²,  $V_{TH}$  =0.6,  $\lambda$ = $\gamma$ =0 and  $V_{DD}$ =3V.



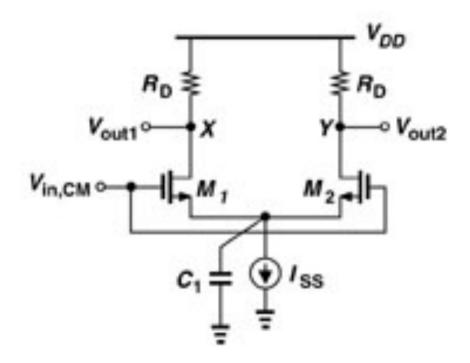
- a) What is the required input CM for which R<sub>SS</sub> sustains 0.5V?
- b) Calculate  $R_D$  for a differential gain of 5V/V.
- c) What happens at the output if the input CM level is 50mV higher than the value calculated in part (a)?

### **Board Notes**

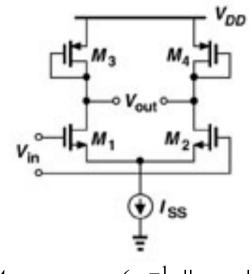




$$\frac{V_X - V_Y}{V_{in,CM}} = -\frac{g_{m1} - g_{m2}}{(g_{m1} + g_{m2})R_{SS} + 1}R_D$$

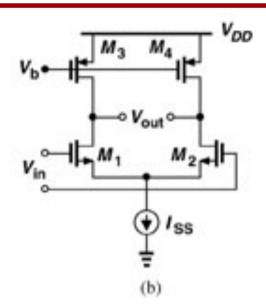


#### Differential Pair with MOS Loads



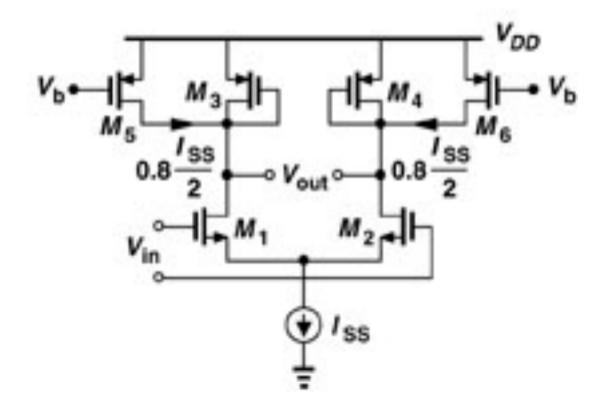
$$A_{v} = -g_{mN}(g_{mP}^{-1} \| r_{oN} \| r_{oP})$$

$$\approx -\frac{g_{mN}}{g_{mP}}$$

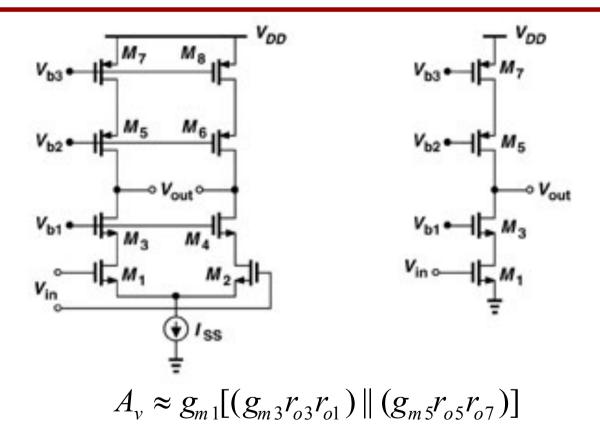


$$A_{v} = -g_{mN}(r_{oN} \parallel r_{oP})$$

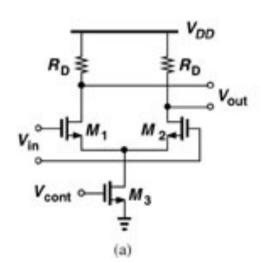
## **MOS Loads**

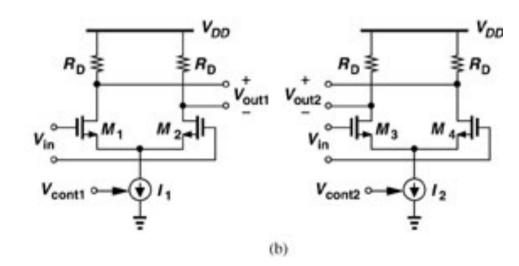


#### **MOS Loads**

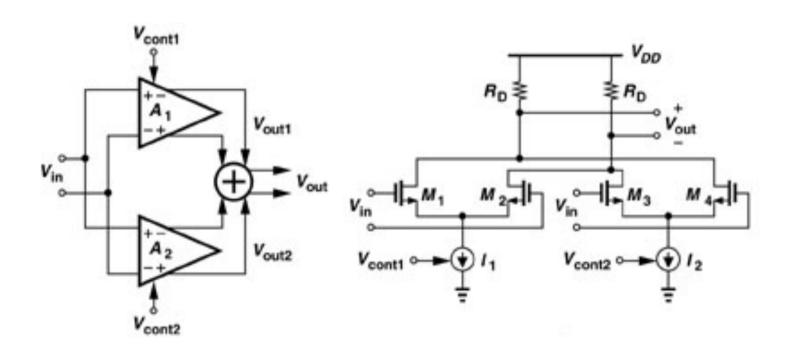


#### Gilbert Cell

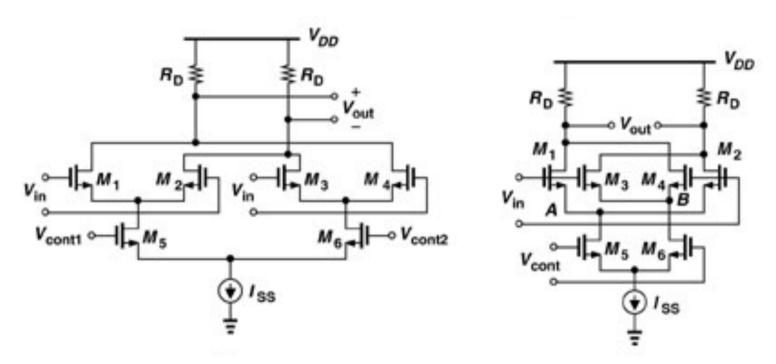




#### Gilbert Cell



#### Gilbert Cell



$$V_{OUT} = k V_{in} V_{cont}$$