

COMP4300 Spring 2021

Homework 1

Due 11:59pm, Feb 12, 2021

Each problem worth 20 points

1. For a PDP-8, generate assembly code to multiply the number in hex address 0x200 by 4, and store the result in address 0x201. The program should start in address 0x100. You can assume the number in 0x200 is positive and less than 0x100. You will need to consult the PDP-8 programming card for mnemonics and instruction formats. Note in particular that the PDP-8 has no multiply instruction. Be sure to give the address of each instruction.

Address in hex	mnemonic	binary
0x100	CLA	111 010 000 000
0x101	TAD 0x200	001 000 000 000
0x102	TAD 0x200	001 000 000 000
0x103	TAD 0x200	001 000 000 000
0x104	TAD 0x200	001 000 000 000
0x105	DCA 0x201	011 000 000 001

Notes: 0x200 = 0b1000000000

0x201 = 0b 1000000001

Reasoning:

I'm adding what is in address 0x200 4 times to my memory and then storing it in 0x201.

Then the memory gets cleared. *I'm afraid my indirect addressing is wrong, but I hope that at least my logic makes sense.*

2. From the following assembly language code for a 32-bit MIPS processor, generate the binary machine language for this code fragment. Consult the Internet, for example: <http://max.cs.kzoo.edu/cs230/Resources/MIPS/MachineXL/InstructionFormats.html> for the bit patterns for opcodes and register numbers (5 points/instruction).

Start: LW R1,40(R2)

LW R3,1000(R0)

ADDU R1, R2, R3

J Start:

(where Start is at 32-bit address 0x00001000)

**** ORDER IS BIG-ENDIAN ****

Tell what bits go in each memory address. Remember that an address holds 8 bits.

1) LW R1, 0x40(R2)

LW	r2	r1	offset
100011	00010	00001	0000000001000000

Encoded instructions: Binary: 10001100010000010000000001000000

Hex: 0x8C410040

2) LW R3, 0x1000(R0)

LW	R0	R3	offset
100011	00000	00011	0001000000000000

Encoded instructions: Binary: 10001100000000011000100000000000

Hex: 0x8C031000

3) ADDU R1, R2, R3

SPECIAL	R2	R3	R1	0	ADDU
000000	00010	00011	00001	00000	100001

Encoded Instruction in:

Binary: 00000000010000110000100000100001

Hex: 0x00430821

4) J Start

J	target
000010	00000000000001000000000000

Encoded Instruction in:

Binary: 00001000000000000001000000000000

Hex: 0x08001000

Our program in Hex:
0x8C410040
0x8C031000
0x00430821
0x08001000

Putting the program in memory (starting at 0x0001000):

Address	Data in hex
0x00001000	8C
0x00001001	41
0x00001002	00
0x00001003	40
0x00001004	8C
0x00001005	03
0x00001006	10
0x00001007	00
0x00001008	00
0x00001009	43
0x0000100A	08
0x0000100B	21
0x0000100C	08
0x0000100D	00
0x0000100E	10
0x0000100F	00

Suppose a given optimization to the ALU speeds up execution for the system as a whole by a factor of 1.75. After optimization, ALU operations take up 1/6 of the total execution time. What fraction of execution time BEFORE OPTIMIZATION was taken up by ALU operations? What was the speedup factor to ALU operations due to the optimization?

Speed up execution of system = 1.75

ALU takes up 1/6 of execution time after the speedup.

We keep in mind that the rest of the system (5/6 of exec time) stayed the same.

Equation of new system:

$$1.75 = (5/6) + (1/6)*X$$

$$X = 5.5$$

This means that the ALU Operations have shrunk *5.5 during optimization

So the size of ALU before was $1/6 * 5.5 = 11/12$

The rest of the execution time is $10/12$

To find the percentage that that ALU took up before we divide $11/(10+11)$

=> **Before optimization, ALU took up 52.38%**

=> **Its speedup factor is 5.5**

Check if numbers add up with Amdahl's Law:

$$\frac{1}{1 - 0.5238 + \frac{0.5238}{5.5}} = 1.7499...$$

3. For a particular computer, the CPI for certain types of instructions is as follows:

ALU operations, 2 cycles, make up 25% of dynamic (run-time) instruction count

Load/store operations, 10 cycles, 30% of dynamic instruction count

Control flow, 3 cycles, 20% of dynamic instruction count

All other instructions, 1 cycle

What is the average CPI?

$$\text{avg cpi} = \frac{\sum_{\text{instr type } i} IC_i \cdot CPI_i}{IC_0} = \sum_i f_{\text{freq}_i} \times CPI_i$$

Following this logic:

$$\begin{aligned} \text{Avg cpi} &= 2 \cdot 0.25 + 10 \cdot 0.3 + 3 \cdot 0.2 + 1 \cdot 0.25 \\ &= 4.35 \end{aligned}$$

Suppose there is an optimization in which the CPI of load/store is reduced to 5, but cycle time is lengthened by 20%. What is the speedup due to this optimization?

Same formula, different numbers:

$$\begin{aligned} \text{Avg cpi} &= 2 \cdot 0.25 + 5 \cdot 0.3 + 3 \cdot 0.2 + 1 \cdot 0.25 \\ &= 2.85 \end{aligned}$$

Formula: “Execution time = Total instruction count * CPI * cycle time”

*Suppose our old cycle time is T, therefor new cycle time is 1.2T

Old execution time = 100% * 4.35 * T = 4.35T

New Execution Time = 100% * 2.85 * 1.2T = 3.42T (1.2T because of 20% increase)

Formula: “Speedup = old exec time / new exec time”

Speedup = 4.35T / 3.42T

Speedup = 1.27

4. Suppose for the problem in question 4, Load/store operations were made to take 1 cycle, without lengthening the cycle time. What would be the speedup due to that optimization?

$$\text{Avg pci} = 2 \cdot 0.25 + 1 \cdot 0.3 + 3 \cdot 0.2 + 1 \cdot 0.25 = 1.65$$

Since cycle time is not lengthened,

$$\text{Speedup} = 4.35 / 1.65 = 2.63$$