

Homework 1

Section 1.1

Colin Cano

12. a. $\neg P$: The election isn't decided
 b. $P \vee q$: The election is decided or the votes have been counted
 c. $\neg P \wedge q$: The election isn't decided and the votes have been counted.
 d. $q \rightarrow P$: If the votes have been counted, then the election has been decided.
 e. $\neg q \rightarrow \neg P$: If the votes have not been counted, then the election is not decided.
 f. $\neg P \rightarrow \neg q$: If the election isn't decided, then the votes have not been counted.
 g. $P \leftrightarrow q$: The election is decided if and only if the votes have been counted.
 h. $\neg q \vee (\neg P \wedge q)$: The votes have not been counted or the election isn't decided and the votes have been counted.

30. b. If it's a sunny summer day, then I go to the beach
 Contra positive: If I do not go to beach, then it is not a sunny day.

Converse: If I go to the beach, then it is a sunny summer day

Inverse: If it isn't a sunny summer day, then I do not go to the beach

34 d.

P	q	$P \wedge q$	$P \vee q$	$(P \wedge q) \rightarrow (P \vee q)$
T	T	T	T	T
T	F	F	T	T
F	T	F	T	T
F	F	F	F	T

f.

P	q	$P \leftrightarrow q$	$P \leftrightarrow \neg q$	$(P \leftrightarrow q) \oplus (P \leftrightarrow \neg q)$
T	T	T	F	T
T	F	F	T	T
F	T	F	T	T
F	F	T	F	T

48 a. $11000 \wedge (01011 \vee 11011) = 11000$

$$\begin{array}{r} 11000 \\ 11011 \wedge \\ \hline 11000 \end{array}$$

$$\begin{array}{r} 01011 \\ 11011 \vee \\ \hline 11011 \end{array}$$

b. $(01111 \wedge 10101) \vee 01000 = 01101$

$$\begin{array}{r} 01111 \\ 10101 \wedge \\ \hline 00101 \end{array}$$

$$\begin{array}{r} 00101 \\ 01000 \vee \\ \hline 01101 \end{array}$$

c. $(01010 \oplus 11011) \oplus 01000 = 11001$

$$\begin{array}{r} 01010 \\ 11011 \oplus \\ \hline 10001 \end{array}$$

$$\begin{array}{r} 10001 \\ 01000 \oplus \\ \hline 11001 \end{array}$$

d. $(11011 \vee 01010) \wedge (10001 \vee 11011) = 11011$

$$\begin{array}{r} 11011 \\ 01010 \vee \\ \hline 11011 \end{array}$$

$$\begin{array}{r} 10001 \\ 11011 \vee \\ \hline 11011 \end{array}$$

$$\begin{array}{r} 11111 \\ 11011 \wedge \\ \hline 11011 \end{array}$$

Section 1.2

$w \leftrightarrow (d \vee s)$

10. p: Software is being upgraded

q: User's can access file system

r: User's can save new files.

$p \rightarrow \neg q \quad \neg q \rightarrow r$

Negation

$\neg r \rightarrow \neg p \equiv p \rightarrow r$

18.

empty	+ in 1	+ in 2
T1	T2	T3

$p \rightarrow \neg q \quad \not\models p \rightarrow r$

Contradiction

T1	T2	T3
T	T	T
T	T	F
T	F	T
T	F	F
F	T	T
F	T	F
F	F	T
F	F	F

X - can't all be true

a. False

b. True, Trunk 1 and trunk 3

c. False

d. False

X - can't all be false

28.) A: C is knave B: A is knight C: I am the spy

A	B	C	
T	T	T	① C can't be 2 things at once
T	T	F	✓
T	F	T	②
T	F	F	Alex can't be knight if B is false
F	T	T	③ Alex can't be knight and lie
F	T	F	④
F	F	T	A+B cannot both be false if C is true
F	F	F	Knights can't lie

A is the knight, B is the spy, C is the knave.

49.a) $\neg p \vee \neg q$

49.b) $p \vee (\neg p \wedge q)$

$\neg(\neg p \wedge q) \vee p$