

# Homework #10

## Section 6.4

$$2.6) (x+y)^5 = \binom{5}{0}x^5y^0 + \binom{5}{1}x^4y^1 + \binom{5}{2}x^3y^2 + \binom{5}{3}x^2y^3 + \binom{5}{4}x^1y^4 + \binom{5}{5}x^0y^5$$

$$= x^5 + 5x^4y + 10x^3y^2 + 10x^2y^3 + 5xy^4 + y^5$$

$$4) \binom{13}{8} = \frac{13!}{8!5!} = 1287$$

$$7.) \binom{19}{9} 2^{10} \cdot (-x)^9 = -\frac{19!}{9!10!} 2^{10} x^9 = -92378 \cdot 1024x^9 = \boxed{-94995072}$$

$$12.6) y^{15} = (y^3)^5$$

$$\binom{6}{5} \cdot (5x^2)^1 \cdot (2y^3)^5 = \frac{6!}{5!1!} \cdot 5x^2 \cdot 2^5 y^{15} = \frac{6!}{5!1!} \cdot 32x^2y^{15} = 960x^2y^{15}$$

$$= \boxed{-960}$$

$$16.) 1 \quad 11 \quad 55 \quad 165 \quad 330 \quad 462 \quad 462 \quad 330 \quad 165 \quad 55 \quad 11 \quad 1$$

## Section 7.1

$$7.) \text{each flip is } \frac{1}{2}$$

$$P(1) = \frac{1}{2} \quad P(2) = \frac{1}{2} \dots \dots \dots P(5) = \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} = \boxed{\frac{1}{64}}$$

$$12.) \frac{\binom{52}{5}}{\binom{4}{1} \cdot \binom{48}{4}} = \frac{3243}{10829}$$

$$21.) \text{outcomes} = 6^6 \quad \text{even outcomes} = 729 \quad \frac{729}{46656} = \frac{1}{64}$$

36.) 2 dice:  $\frac{1}{6} \cdot \frac{1}{6} = \frac{1}{36}$  Since there's 5 combos,  $\frac{5}{36}$   
 3 dice:  $\frac{1}{6} \cdot \frac{1}{6} \cdot \frac{1}{6} = \frac{1}{216}$  Since 21 combos,  $\frac{21}{216}$   
 $\frac{5}{36} > \frac{21}{216}$  So 2 dice more likely.

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## Section 7.2

5.)  $(1,6), (2,5), (3,4), (4,3), (5,2), (6,1)$

$$P(1,6) = \frac{1}{6} \cdot \frac{1}{6} = \frac{1}{36} = P(2,5) = P(3,4) = P(4,3) = P(5,2) = P(6,1)$$

$$P(4,3) = \frac{2}{6} \cdot \frac{2}{6} = \frac{4}{36}$$

$\Rightarrow$

$$\frac{1+1+1+2^2+1+1}{7^2} = \boxed{\frac{9}{49}}$$

6.a)  $\{1,2,3\}, \{1,3,2\}, \{2,1,3\}$   
 $= \frac{3}{3!} = \frac{1}{2}$

6.b)  $\{3,2,1\}, \{3,1,2\}, \{2,3,1\}$   
 $= \frac{3}{3!} = \frac{1}{2}$

6.c)  $\{3,2,1\}, \{3,1,2\}$   
 $\frac{2}{3!} = \frac{1}{3}$

10.a)  $P(26,26) = 26!$   $P(13,13) = 13!$

Need to pick 13 remaining

A:  $\frac{13!}{26!}$

10.b)  $P(26,26) = 26!$   $P(24,24) = 24!$  still need to pick 24

A:  $\frac{24!}{26!} = \frac{1}{650}$

10.c)  $P(26,26) = 26!$   $P(25,25) = 25!$  a2 next each other is 1 permutation

A:  $\frac{2 \cdot 25!}{26!} = \frac{1}{13}$

10.d) A:  $\frac{26! - 2 \cdot 25!}{26!}$  Since a, b not next to each other

10.e) A:  $\frac{6 \cdot 24!}{26!}$  Since 6 ways to order a, z

10.f) A:  $\frac{\frac{26!}{3}}{\frac{26!}{1}} = \frac{1}{3}$  Z precedes a, b so its multiplied by  $\frac{1}{3}$

18a)  $1 \cdot \frac{1}{2} = \frac{1}{2}$

18.b)  $n=2, 1 - \frac{7}{7} \cdot \frac{6}{7} = \frac{1}{7}$   $n=3, 1 - \frac{7}{7} \cdot \frac{6}{7} \cdot \frac{5}{7} = \frac{19}{49}$   $n=4, \frac{223}{343}$   
 $n=5, \frac{2041}{2401}$   $n=6, \frac{16067}{16807}$   $n=7, \frac{116929}{17649}$   $n \geq 7, 1$

18.c)  $n \geq 4$

24.)  $P(A \cap B) = \frac{\binom{4}{4}}{2^5} = \frac{1}{32}$   $P(A) = \frac{1}{2}$   
 $P(B|A) = \frac{\frac{1}{32}}{\frac{1}{2}} = \frac{1}{16}$

30a)  $p = \frac{1}{2}$   
 $P(X=10) = \binom{10}{10} \cdot \left(\frac{1}{2}\right)^{10} \cdot (0.5)^0 = \frac{1}{1024}$

30b)  $p = 0.6$   
 $P(X=10) = \binom{10}{10} \cdot 0.6^{10} \cdot (1-0.6)^0 = \frac{59049}{9765625}$

30.c)  $P(x_i=1) = \frac{1}{2^i}$   $P(x_1=1) \cdot P(x_2=1) \dots P(x_{10}=1)$   
 $= \frac{1}{2^1} \cdot \frac{1}{2^2} \dots \frac{1}{2^{10}}$   
 $= \frac{1}{2^{55}} = \frac{1}{2^{55}}$