

Quiz 7

● Graded

Student

Colin Cano

Total Points

6 / 10 pts

Question 1

Death Star

2 / 4 pts

Elements are incorrect. Select all that apply.

✓ - 1 pt Student does not correctly plug in $r = 60 * (.5) = 30$.

8

✓ - 1 pt Student does not correctly plug in $\frac{dr}{dt} = 60$.

7

6 This last r should be r'

Question 2

Zombie Breakout

2 / 3 pts

Elements are incorrect. Select all that apply.

✓ - 1 pt Student does not correctly solve for r using $10e^{r^1} = 1000$

1

Question 3

Related Rates

2 / 3 pts

Elements are incorrect. Select all that apply.

✓ - 0.5 pts The student does not plug in $\frac{dy}{dt} = 4$ correctly, or does not plug in $(x, y) = (1, 2)$ correctly.

5

You reversed $x = 1$ and $y = 2$

✓ - 0.5 pts An algebra mistake was made.

3

2 This is an implicit equation $yx^2 = 2$. It is not a function $f(x) = \dots$

4 You missed $\frac{dx}{dt}$ here, although it is in the next line

Name: Colin Cano

Student ID: _____

1. A moon-sized battle station explodes in outer space. The spherical explosion of shrapnel travels at $60 \frac{\text{km}}{\text{sec}}$. How fast is the volume of the sphere increasing after .5 seconds? You may leave your answer in terms of π . Hint: The formula for the volume of a sphere is $V = \frac{4}{3}\pi r^3$.

$$\frac{dV}{dt} = 4\pi r^2 \cdot \frac{dr}{dt}$$

$$r(0) = 0$$

$$r(t) = 0 + 60t$$

$$60 \text{ km/s} \quad t = .5$$

$$\frac{dV}{dt}(0.5) = 8\pi(60)^2 \text{ km/s}$$

2. In a crowded city, an initial population of 10 zombies escapes from a secret lab and begins infecting humans. Their population grows to 1,000 zombies in just 1 hour. The zombies infect people at a rate proportional to the size of the zombie population. Find an expression for the number of zombies after t hours.

$$P_0 e^{kt}$$

$$P_0 = 10$$

$$P_1 = 1000$$

$$P(t) = P_0 \cdot e^{kt}$$

$$= 10e^{k \cdot 1}$$

$$\frac{\ln(n)}{10} = k$$

3. If $yx^2 = 2$ and $\frac{dy}{dt} = 4$, find $\frac{dx}{dt}$ when $(x, y) = (1, 2)$.

$$f(x) = y(x) \cdot x(x)^2$$

$$f'(x) = y'(t) \cdot x^2 + y(t) \cdot 2x(x) = 0$$

$$4 \cdot 1^2 + 1 \cdot 4 \cdot \frac{dx}{dt} = 0$$

$$\frac{4dx}{dt} = -\frac{17}{4}$$

$$\frac{dx}{dt} = -\frac{17}{4} \text{ at } (1, 2)$$

SCRATCH PAPER