

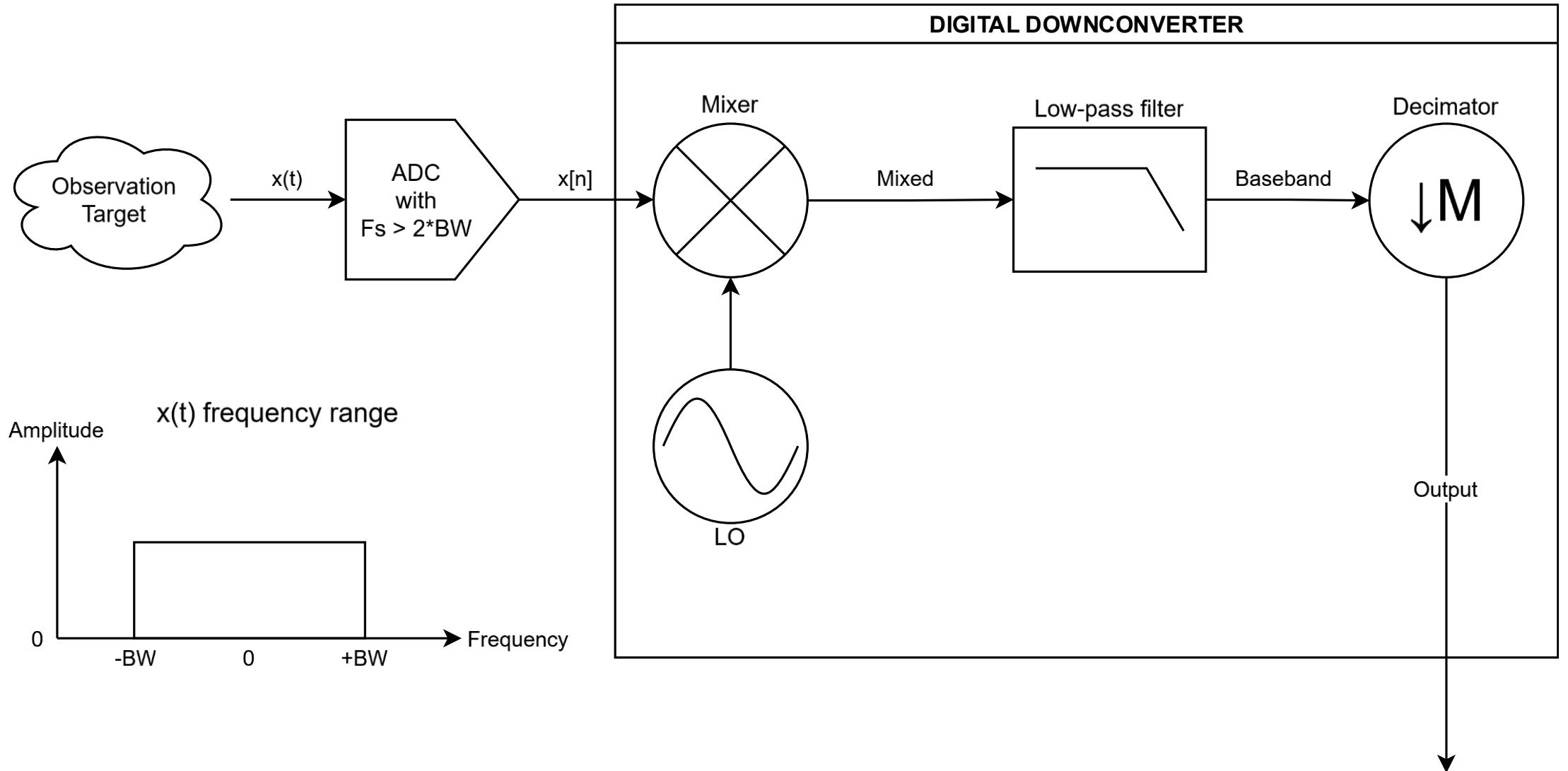
# The Digital Downconverter

Colin Wessels

# Description

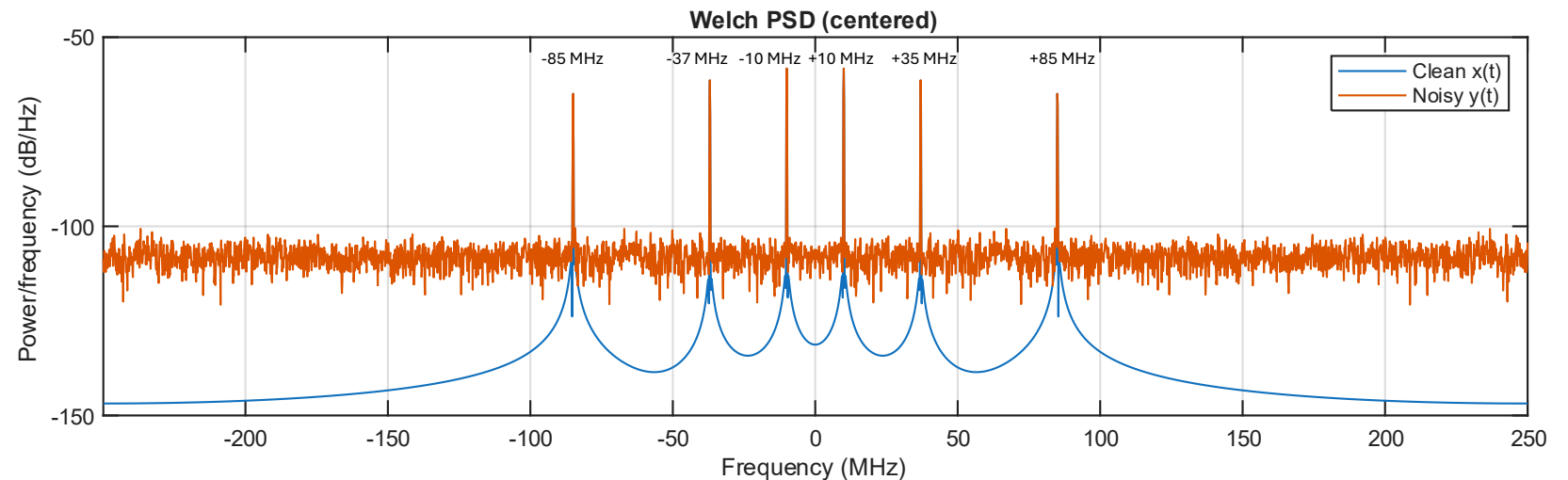
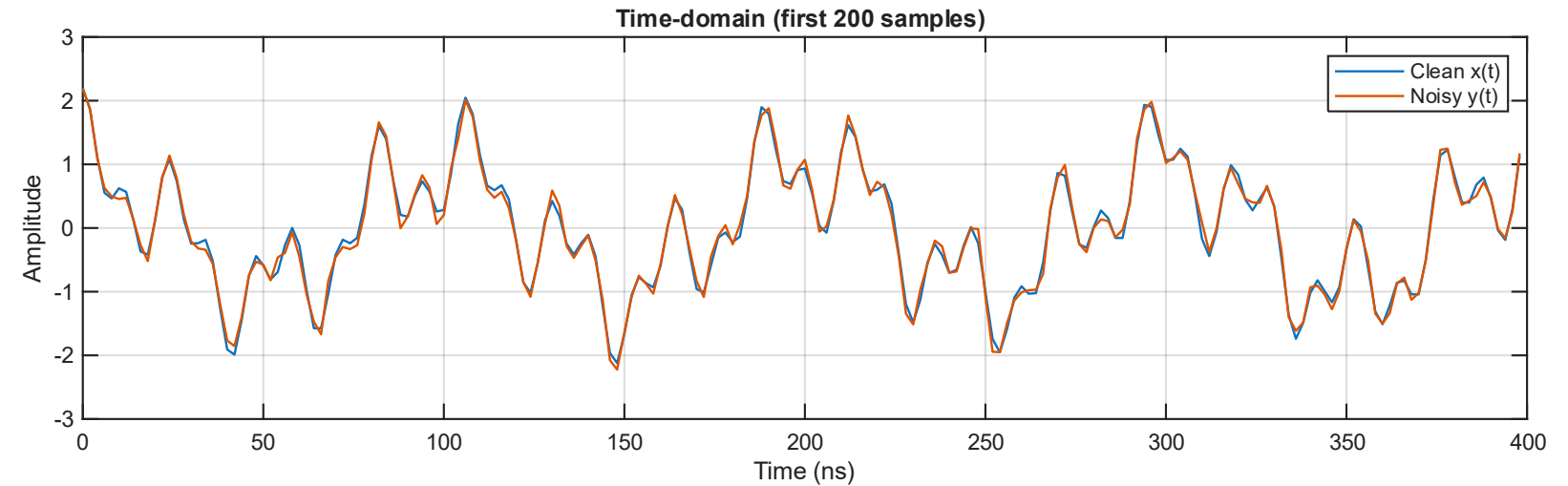
- Used to lower the frequency of a high-frequency signal
- Lossless process
- Components
  - Local oscillator (LO)
  - Mixer
  - Low-pass filter (LPF)
  - Decimator / Downsampler

# The Digital Downconverter



# Incoming Frequencies

- Tones at 10, 37, 85 MHz with additive white gaussian noise on  $y(t)$
- $BW = 85$  MHz,  $F_s = 500$  MHz
- Real signal: complex symmetry



# Mixing Stage

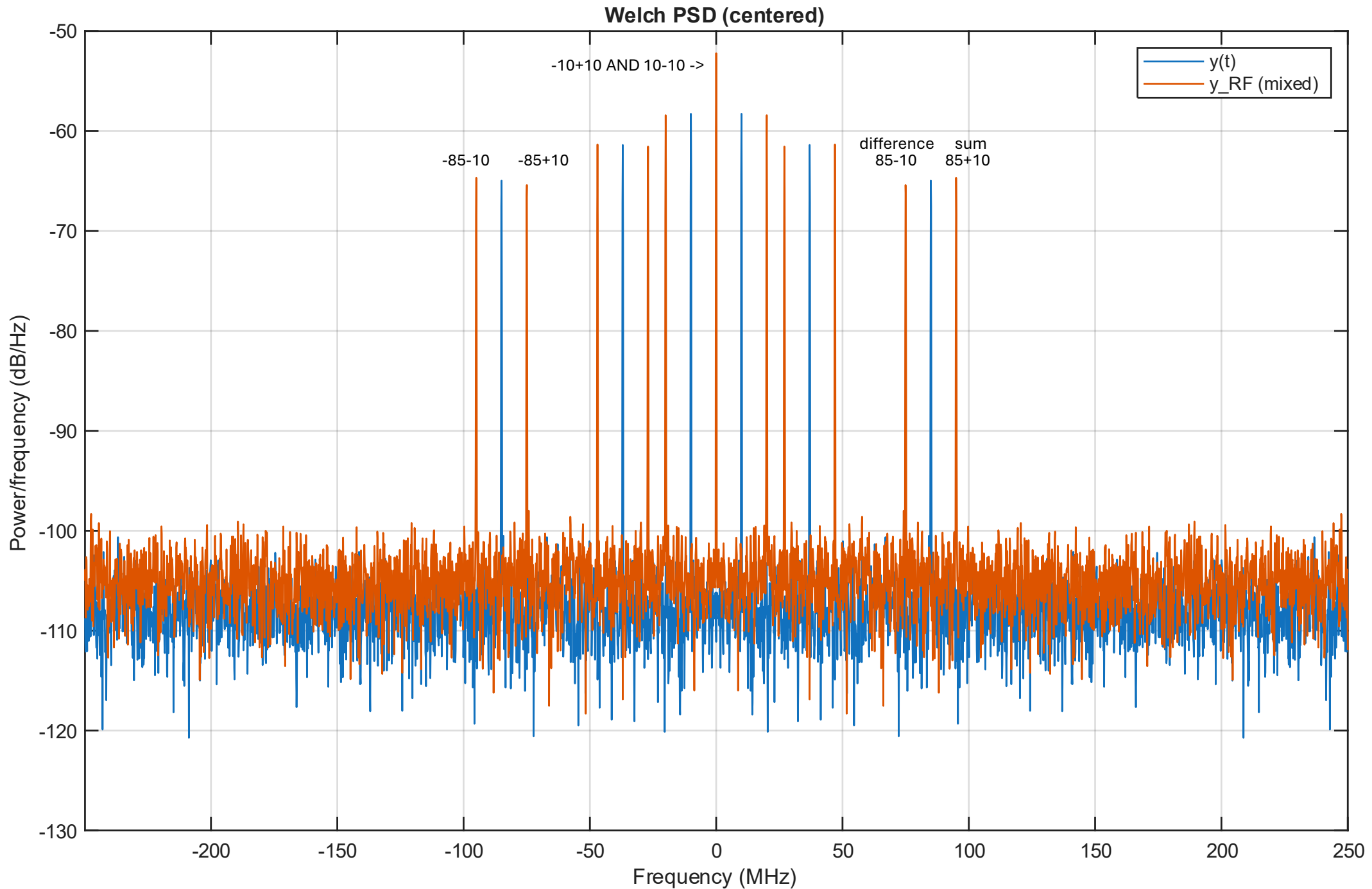
- Mixing is multiplication of  $x[n]$  and the LO of a constant frequency
  - LO frequency is chosen to be 10 MHz

- Multiplication of two periodic signals follows this trigonometric identity:

$$\cos a \cos b = \frac{\cos(a - b) + \cos(a + b)}{2}$$

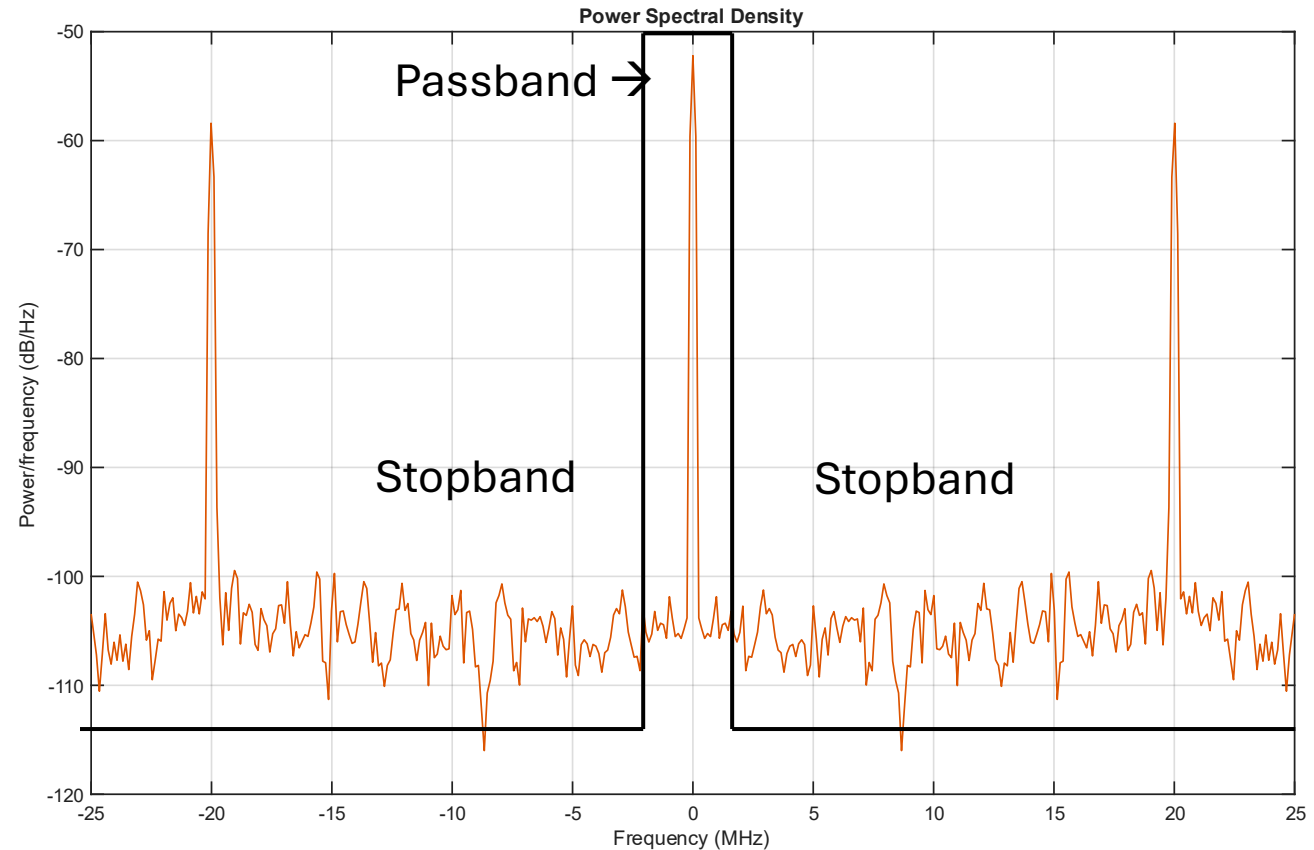
- The goal of downconversion is to frequency shift the signal of interest near 0 Hz.
  - This is why the LO frequency is equal to the frequency of the signal of interest (10 MHz)
- Keep the lower frequency  $\cos(a-b)$  component (**difference**)
- Discard the higher frequency  $\cos(a+b)$  component (**sum**)

- Original frequencies are blue peaks
- Mixed signal frequencies are orange peaks
- LO frequency = 10 MHz
- **Orange peaks are +/- 10 MHz apart from blue peaks**
- At DC: the sum image of -10 MHz and the difference image of +10 MHz combine, essentially doubling the amplitude



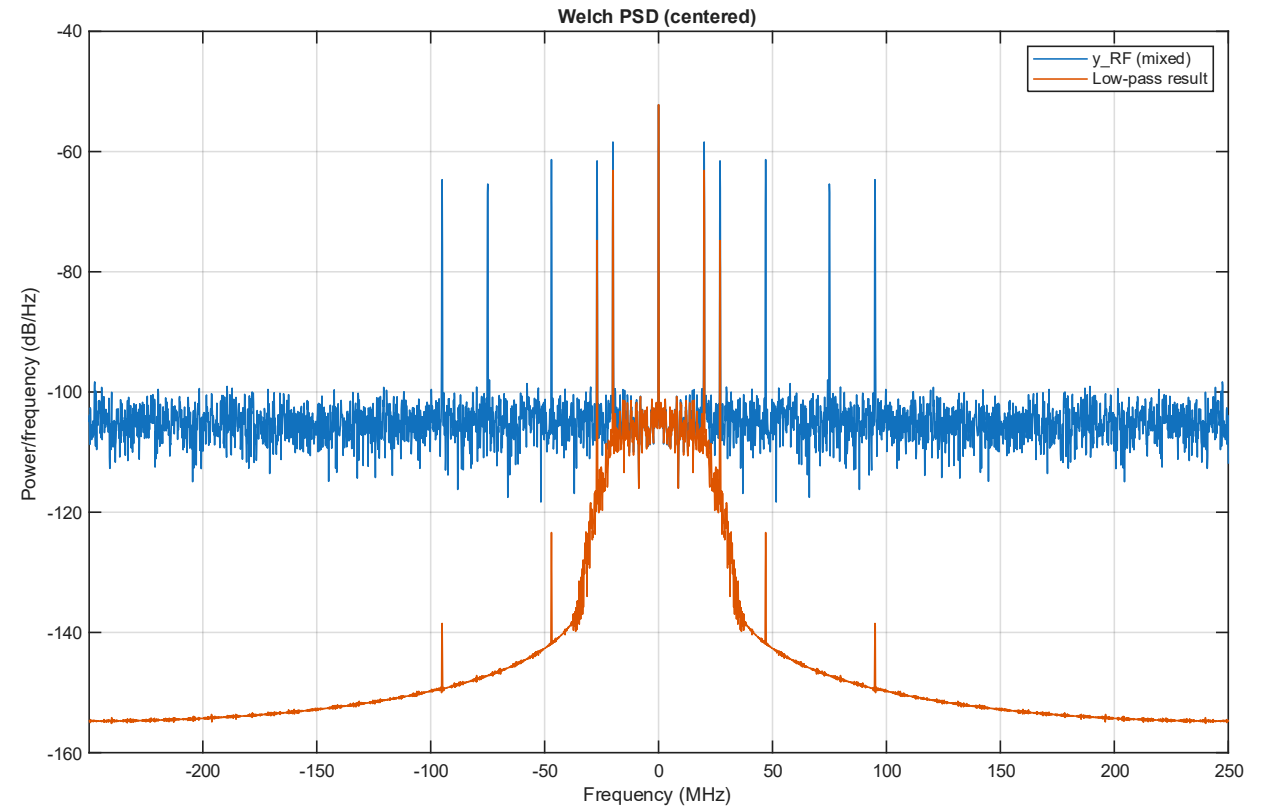
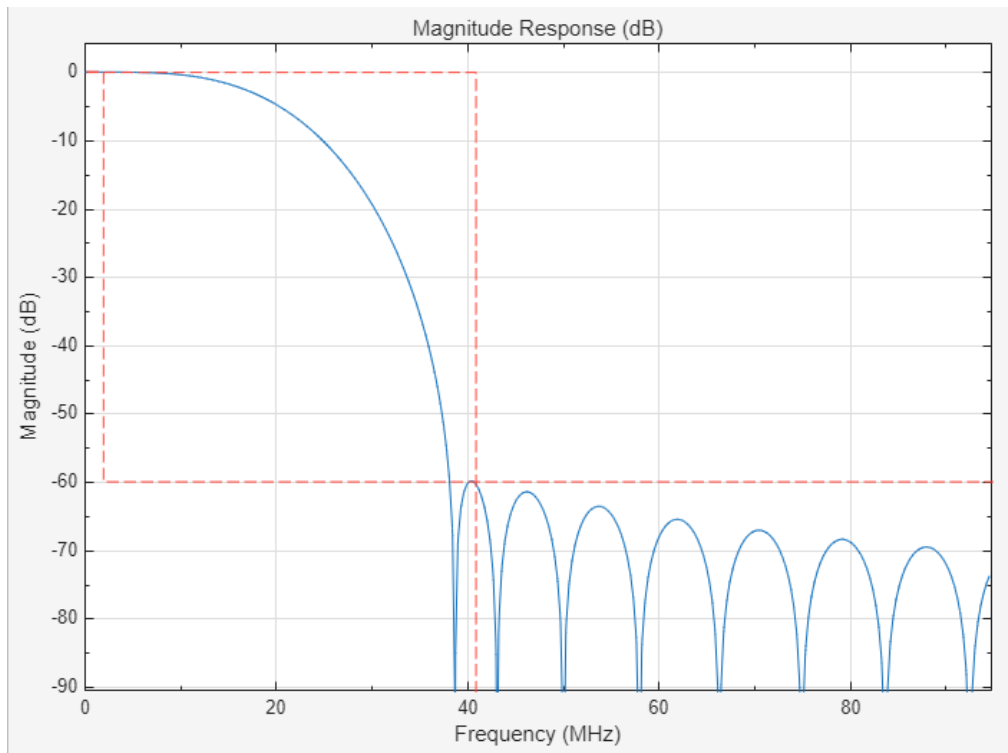
# Low-Pass Filtering

- Mixing shifted the signal of interest to be centered at DC (0 Hz)
- An ideal low pass filter blocks all signals with frequencies greater than the cutoff frequency
- Cutoff frequency of 2 MHz will pass the signal centered at DC and block other signals



# Low-Pass Filtering (cont.)

- Non-ideal filter allows  $\pm 20$  and  $\pm 27$  MHz tones to pass
- -60 dB attenuation at 41 MHz



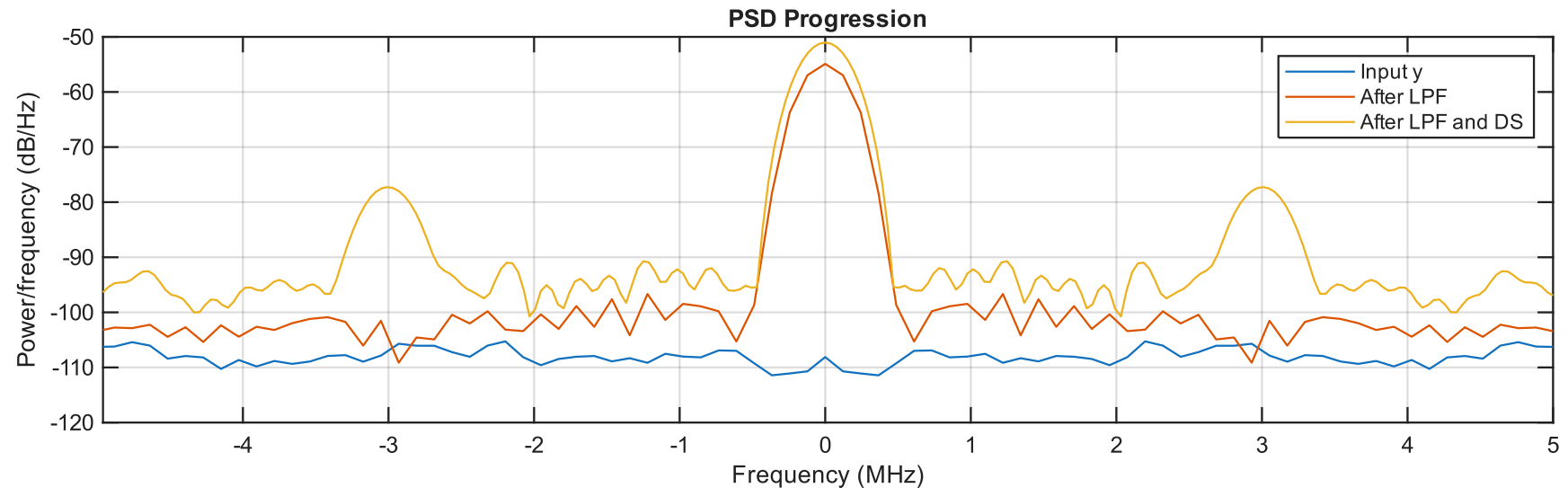
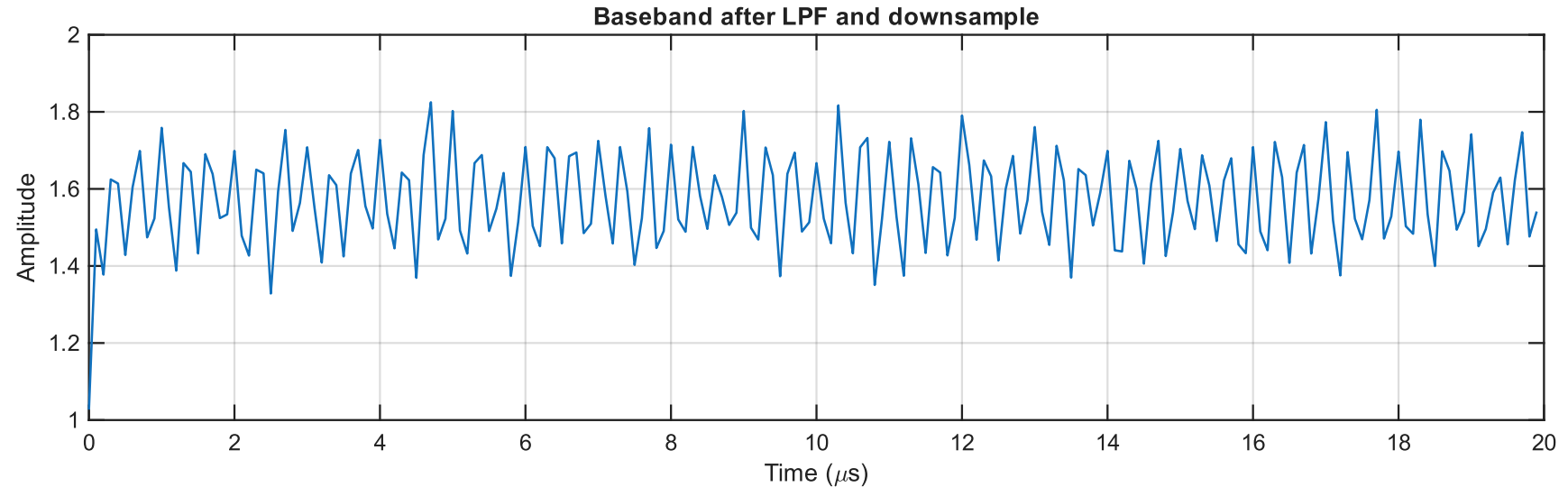


# Downsampling

- Goal: resample with a lower sample frequency now that our signal bandwidth is much lower
  - Decimation factor:  $M = 50$ , keep every 50th sample
  - $F_{s,new} = F_{s,old}/M = 500 \text{ MHz}/50 = 10 \text{ MHz}$
- No aliasing will occur if Nyquist-Shannon sampling theorem is followed:  $F_s > 2 \cdot BW$ 
  - BW of low-passed signal is ideally 2 MHz, but realistically 27 MHz
- Due to non-ideal low-pass filter, **we expect to see aliasing after downsampling**
  - For no aliasing:  $M < F_{s,old}/(2 \cdot BW)$        **$M < 9.26$**  for BW of 27 MHz

# Downsampling (cont.)

- Time-series plot is lower frequency (x axis unit change)
- Downsamped result shows signals at +/- 3 MHz
  - This is an alias of the +/- 27 MHz signal, shifted by the new sample frequency of 10 MHz
  - $27 \text{ MHz} - 3 \cdot (10 \text{ MHz}) = -3 \text{ MHz}$
- Downsamped signal is slightly stronger at DC
  - This is an alias of the +/- 20 MHz signal
  - $20 \text{ MHz} - 2 \cdot (10 \text{ MHz}) = 0 \text{ MHz}$
- **Aliasing of other signals is interfering with signal of interest**



# Lessons learned

- Mixing two signals is equivalent to **multiplication**
- Mixing produces two images, the **sum** and **difference**
- The local oscillator frequency can be chosen to move a **signal of interest** to DC
  - The LO frequency equals the signal of interest frequency
  - In this case, a sum and difference image of both conjugates of the signal of interest will **combine at DC** = 0 Hz
- A low-pass filter is used to block all signals except the signal of interest near DC
- Downsampling **reduces the sample frequency** of the signal without aliasing, provided the LPF reduces the bandwidth enough
  - Reducing the sample frequency gets rid of unnecessary samples, making it practical to store and analyze the signal
- The result is 1 narrow-bandwidth signal **chosen** out of a wide range of frequencies