

HW 4 Colin Wishart

1. X dist. in $-5 \leq x \leq 5$

$$F_X(x) = \frac{1}{b-a} = \frac{1}{5-(-5)} = \frac{1}{10}, \text{ if } -5 \leq x \leq 5$$

$$a. P(X < 1) = \int_{-5}^1 \frac{1}{10} dx = \frac{1}{10} x \Big|_{-5}^1$$

$$= \frac{1}{10} (1 - (-5)) = \left(\frac{6}{10} \right)$$

$1 \times \frac{1}{10} \neq 0$

$$b. P(|X-1| \geq 1) = P(X \leq 0) + P(X \geq 2)$$

$$= \int_{-5}^0 \frac{1}{10} dx + \int_2^5 \frac{1}{10} dx$$

$$= \frac{1}{10} x \Big|_{-5}^0 + \frac{1}{10} x \Big|_2^5 = \frac{5}{10} + \frac{1}{10} (5-2)$$

$$= \frac{5}{10} + \frac{3}{10} = \left(\frac{8}{10} \right)$$

$$2. \bar{x} = 5 \quad \lambda = \frac{1}{\bar{x}} = \frac{1}{5}$$

$$P(X > 8 | X > 3) = \frac{P(X > 8)}{P(X > 3)}$$

$$= \frac{e^{-(\frac{1}{5})(8)}}{e^{-(\frac{1}{5})(3)}} = \left(0.3679 \right)$$