Game Day

Contents

	Introduction	1
Sol	lutions	2
	Probability	2
	Sampling Distributions	3
	Confidence Intervals	4
	General Topics	ŀ

Introduction

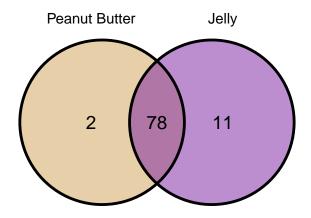
In addition to functions already included in R, below contains the code you will need to load to be prepared to answer questions for Jeopardy

```
library(dplyr)
library(ggplot2)
theme_set(theme_bw(base_size = 16))
## Bootstrap Function
bootstrap <- function(x, statistic, n = 1000L) {</pre>
  bs <- replicate(n, {</pre>
    sb <- sample(x, replace = TRUE)</pre>
    statistic(sb)
  })
  data.frame(Sample = seq_len(n),
             Statistic = bs)
}
se <- function(x) sd(x) / sqrt(length(x))</pre>
source("https://collinn.github.io/f24/labs/clt_lab_functions.R")
## College data
college <- read.csv("https://collinn.github.io/data/college2019.csv")</pre>
## Hawks data
hawks <- read.csv("https://collinn.github.io/data/hawks.csv")</pre>
## Fix penguin data
penguins <- read.csv("https://collinn.github.io/data/penguins.csv")</pre>
penguins <- filter(penguins, !is.na(bill_length_mm))</pre>
```

Solutions

Probability

Probability 1



Probability 2

$$\left(\frac{3}{12}\right)\left(\frac{4}{11}\right)\left(\frac{5}{10}\right) = 0.045$$

Probability 3

1. No

$$0.15 = P(A \text{ and } B) = P(A|B) \times P(B) \neq P(A)P(B) = 0.2 \times 0.8 = 0.16$$

2.

$$0.15 = P(A \text{ and } B) = P(A|B) \times P(B) = P(A|B) \times 0.8 \implies P(A|B) = 0.1875$$

Probability 4

$$\begin{split} &P(Box)=0.8,\,P(Pass|Box)=0.86\,\,P(Pass|\text{No Box})=0.65\\ &P(Box|Pass)=\frac{P(Pass|Box)\times P(Box)}{P(Pass)}=0.841 \end{split}$$

Probability 5

$$P(M|V) = \frac{P(V|M)P(M)}{P(V|M)P(M) + P(V|I)P(I)} = 0.7959$$

Sampling Distributions

Sampling Dist 1

Normal:

- Mean
- Standard Deviation/Standard Error

t-distribution

• Degrees of freedom (n-1)

Sampling Dist 2

Sample size and population standard deviation (σ)

Sampling Dist 3

- 1. You would need a large n
- 2. You can bootstrap and see if it looks normally distributed

Sampling Dist 4

```
## Collect 100,000
samp \leftarrow rt(n = 1e5, df = 15)
## Proportion absolute greater than 1
mean(abs(samp) > 1) # 0.33
## [1] 0.33477
mean(abs(samp) \le 1) # 0.66
## [1] 0.66523
## Finding the middle 50% tells you most likely range
## Since middle 50 so far less than 1, this is best bet since over
## 50% will be less than 1
qt(c(0.25, 0.75), df = 15)
## [1] -0.6912 0.6912
Sampling Dist 5
peng <- filter(penguins, species == "Adelie")</pre>
## Have to bootstrap to get sampling distribution
median_boot <- bootstrap(peng$flipper_length_mm, median)</pre>
## Standard deviation of samp dist is std. error
sd(median_boot$Statistic)
```

[1] 0.37733

Confidence Intervals

Conf Int 1

A has more variability – you can tell by the distance of the points from the mean (black line). The bars are shorter than in B, but this is because B is using a larger critical value, as is indicated by the fact that it has much higher proportion of coverage

Conf Int 2

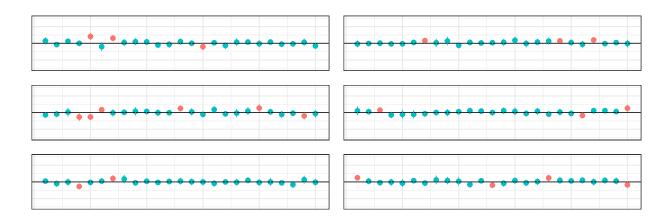
This was just random, but one way to play the odds is to determine that < 4 corresponds to a failure rate of 3/25 = 0.12 or lower. Finding quantiles, we see

```
qnorm(c(0.06, 0.94))
```

```
## [1] -1.5548 1.5548
```

Since 1.6 is wider than this by just a tiny bit, the odds are slightly better if you choose < 4

```
## Simulate doing this 6 times
p <- lapply(1:6, function(x) simulateConfInt(m = 1.6))
do.call(gridExtra::grid.arrange, p)</pre>
```



Conf Int 3

```
## Original
qt(0.995, df = 38) * 25 / sqrt(100)

## [1] 6.7789
qt(0.995, df = 38) * 25 / sqrt(150)

## [1] 5.5349
qt(0.995, df = 38) * 20 / sqrt(100)

## [1] 5.4231
qt(0.975, df = 38) * 25 / sqrt(100) # largest change
## [1] 5.061
```

Conf Int 4

```
qnorm(c(0.15, 0.85), mean = 75, sd = 10)

## [1] 64.636 85.364

## Could also use critical values and Point estimate +/- method
qnorm(c(0.15, 0.85))

## [1] -1.0364  1.0364

Conf Int 5

(cv <- qnorm(c(0.05, 0.95)))

## [1] -1.6449  1.6449

## Does not contain 20
22.5 + cv * (6.4 / sqrt(25))</pre>
```

General Topics

[1] 20.395 24.605

General 1

Since this is just the t statistic, we can compare it directly to critical values

```
## This would contain our t-statistic
qt(c(0.025, 0.975), df = 14)
```

[1] -2.1448 2.1448

General 2

```
group_by(hawks, Species) %>%
summarize(mean(Wing))
```

```
## # A tibble: 3 x 2
## Species `mean(Wing)`
## <chr> <dbl>
## 1 CH 244.
## 2 RT 384.
## 3 SS 185.
```

General 3

This calculation can be easily performed by hand

```
## Generate Sample
p <- c(rep(1, 24), rep(0, 16))

## Compute standard error
(vv <- se(p))</pre>
```

```
## [1] 0.078446

## t dist with df = 39

mean(p) + qt(c(0.05, 0.95), df = 39) * vv
```

```
## [1] 0.46783 0.73217
```

General 4

0 1 ## 52 48

```
boot <- bootstrap(college$Adm_Rate, median)
quantile(boot$Statistic, c(0.1, 0.9))

## 10% 90%
## 0.6830 0.7002

General 5

samp <- rbinom(100, 1, p = 0.5)
table(samp)

## samp</pre>
```