
Subject and name index

*A page number in bold type refers to a definition or description,
and (p) denotes a problem.*

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