

# Learning Portable Representations for High-Level Planning

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# Introduction

- ▶ Planning in continuous state space and continuous action space is costly and inefficient.
- ▶ Learn symbolic representations of state space.
- ▶ Previous work of Konidaris et al. [3] shows a procedure to generate these symbolic representations.
- ▶ However, learned symbols are not general.

1. Learn symbols in *egocentric* state space with [3].
  2. Then, for each newly encountered environment, augment the environment specific representations.
- Results in sample efficiency.
- More general representations.

# Semi Markov Decision Processes

Framing the problem as Semi-Markov Decision Processes. (What is that?)

$$MDP = (States, Actions, Transitions, Rewards)$$

In MDP, time is discrete. In SMDP time is continuous

$$SMDP = (States, Options, Transitions, Rewards)$$

$$o_i \in Options = (\mathcal{I}_i, \pi_i, \beta_i)$$

$\mathcal{I}_i$ : initiation set,

$\pi_i$ : policy of  $o_i$ ,

$\beta_i$ : termination probability of  $o_i$ .

# High-Level Planning

High level planning operates using symbolic states and operators.

A set of propositions:

$$\mathcal{P} = \{p_1, p_2, \dots, p_n\}$$

A set of operators:

$$\mathcal{A} = \{\alpha_1, \alpha_2, \dots, \alpha_m\}$$

High level state is obtained by assigning truth values to  $p_i$ 's. Each operator is described as:

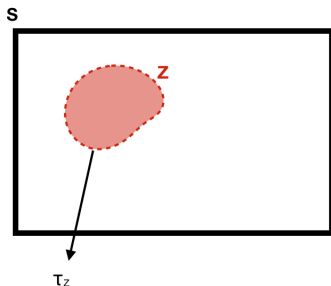
$$\alpha_i = (\text{precond}_i, \text{effect}_i^+, \text{effect}_i^-)$$

# Symbols and Plans

## Definition

A propositional symbol  $\sigma_Z$  is the name associated with a test  $\tau_Z$ , and the corresponding set of states  $Z = \{s \in S \mid \tau_Z(s) = 1\}$ .

We want our classifiers to efficiently compute:



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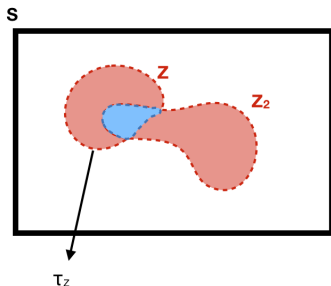


Figure: AND operation



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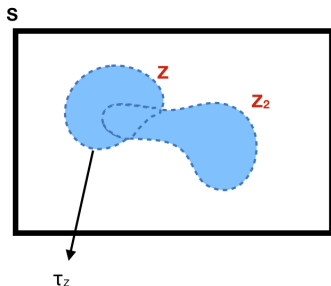


Figure: OR operation

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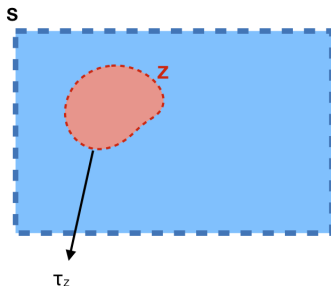
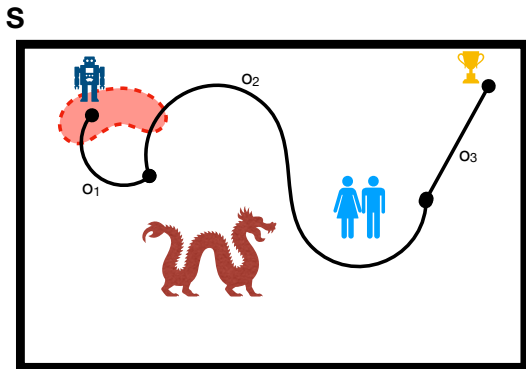


Figure: NOT operation

# Symbols and Plans

## Definition

A plan  $p = \{o_1, o_2, \dots, o_{p_n}\}$  from a state set  $Z \subseteq S$  is a sequence of options  $o_i \in O$ ,  $1 \leq i \leq p_n$ , to be executed from some state in  $Z$ .



# Symbols and Plans

## Definition

The plan space for an SMDP is the set of all tuples  $(Z, p)$ , where  $Z \subseteq S$  is a set of states in the SMDP, and  $p$  is a plan.

# Symbols for Propositional Planning

We need a symbol for the precondition for each option.

## Definition

The precondition of option  $o$  is the symbol referring to its initiation set:  $Pre(o) = \sigma_{I_o}$ .

Then, we need a symbol for the effect of each option.

## Definition

Given an option  $o$  and a set of states  $X \subseteq S$ , we define the image of  $o$  from  $X$  as:  $Im(X, o) = \{s' | \exists s \in X, P(s'|s, o) > 0\}$ .

# Symbols for Propositional Planning

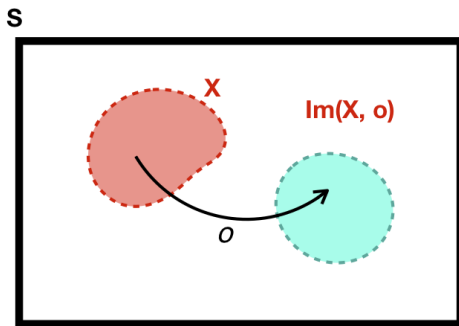


Figure: "Image" of option  $o$  from a set of states  $X$ .

# Symbols for Propositional Planning

## Theorem

*Given an SMDP, the ability to represent the preconditions of each option and to compute the image operator is sufficient for determining whether any plan tuple  $(Z, p)$  is feasible [3].*

## Proof.

Consider any plan tuple  $(Z, p)$ , with plan length  $n$ . We set  $z_0 = Z$  and repeatedly compute  $z_{j+1} = \text{Im}(z_j, p_j)$ , for  $j \in \{1, 2, \dots, n\}$ .

The plan tuple is feasible if and only if  $z_i \subseteq \text{Pre}(p_{i+1})$ ,

$\forall i \in \{0, 1, \dots, n-1\}$ .



# Symbols for Propositional Planning

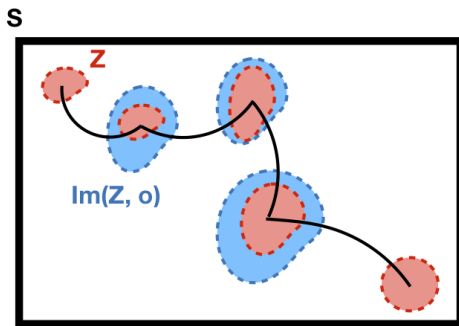


Figure: Informal proof



# Symbols for Propositional Planning

- ▶ It is the necessary condition.
- ▶ Checking feasibility  $\implies$  We have precondition. and image ops. symbols
- ▶ It is the sufficient condition.
- ▶ We have precondition. and image ops. symbols  $\implies$  Checking feasibility.
- ▶ Checking feasibility  $\iff$  We have precondition. and image ops. symbols.

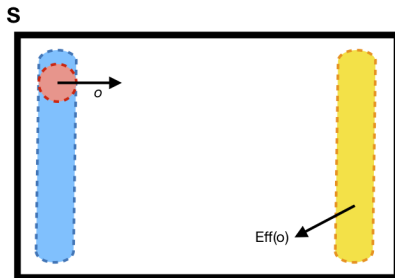
# Symbols for Propositional Planning

- ▶ However, representing  $\text{Im}(X, o)$  may be hard.
- ▶ There are good alternatives that is appropriate for this framework.
- ▶ Subgoal options and abstract subgoal options.

# Symbols for Propositional Planning

## Definition

The effect set of subgoal option  $o$  is the symbol representing the set of all states that an agent can possibly find itself in after executing  $o$ :  $Eff(o) = \{s' | \exists s \in S, t, P(s', t | s, o) > 0\}$ .



# Symbols for Propositional Planning

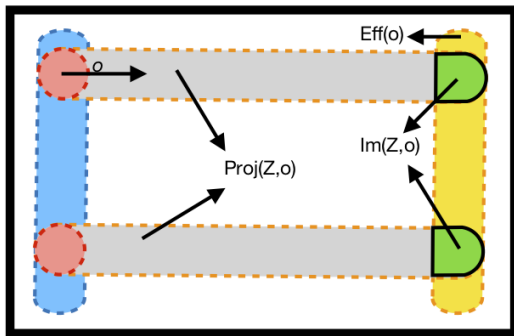
## Definition

Given an option  $o$  and a set of states  $Z \subseteq S$ , we define the projection of  $Z$ , with respect to  $o$  (denoted  $Project(Z, o)$ ) as:  
 $Project(Z, o) = \{[a, b] \mid \exists a', [a', b] \in Z\}.$

Then, image operator for an abstract subgoal option can be computed as:  $Im(Z, o) = Project(Z, o) \cap Eff(o).$

# Symbols for Propositional Planning

S



# Constructing a PDDL Domain Description

So far, we only created symbols for  $Pre(o)$ . We also need  $Im(X, o)$ .

mask( $o_1$ )	{	$\overline{s_1}$
		$\overline{s_2}$
mask( $o_2$ )	{	$\overline{s_3}$
		$\overline{s_4}$
mask( $o_3$ )	{	$\overline{s_5}$
		$\overline{s_6}$
		$\overline{s_7}$

Factor	State Variables	Options
$f_1$	$s_1, s_2$	$o_1$
$f_2$	$s_3$	$o_1, o_2$
$f_3$	$s_4$	$o_2$
$f_4$	$s_5$	$o_2, o_3$
$f_5$	$s_6, s_7$	$o_3$

Figure: Reprinted from [3].

# Constructing a PDDL Domain Description

- ▶ Executing an option  $o_i$  projects the factors it changes and intersects with  $Eff(o_i)$ .
- ▶ A future execution of option  $o_j$  projects the overlapping factors out of  $Eff(o_i)$ .
- ▶ This may result in a combinatorial explosion if we would not be careful.
- ▶ Remember, we need to enumerate these combinations since all we want is  $Im(X, o)$ .

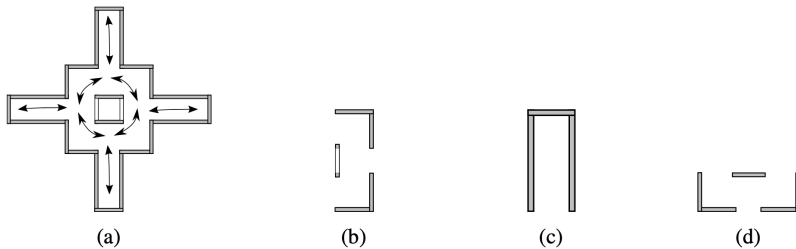
# Problem with Environment Specific State Space



**Figure:** We cannot use the symbol learned in the left environment for the right environment. Reprinted from [2].



# Symbolic Representations in Egocentric Space



**Figure:** (a) Possible actions are shown with arrows. (b-d) Local egocentric observations. Reprinted from [2].

# Symbolic Representations in Egocentric Space

Option	Precondition	Effect
Clockwise1	wall-junction	window-junction
Clockwise2	window-junction	wall-junction
Anticlockwise1	wall-junction	window-junction
Anticlockwise2	window-junction	wall-junction
Outward	wall-junction $\vee$ window-junction	dead-end
Inward	dead-end	$\begin{cases} \text{window-junction w.p. 0.5} \\ \text{wall-junction w.p. 0.5} \end{cases}$

Figure: Subgoal options learned in egocentric space. Reprinted from [2].

# Transferring Egocentric Symbols

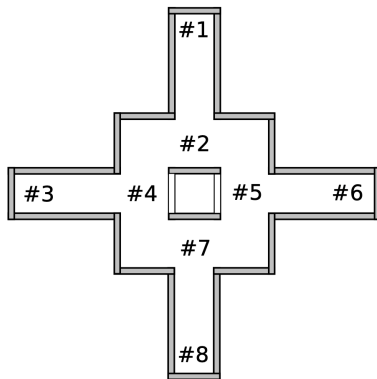
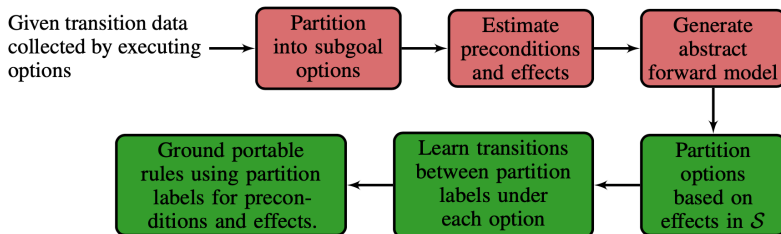


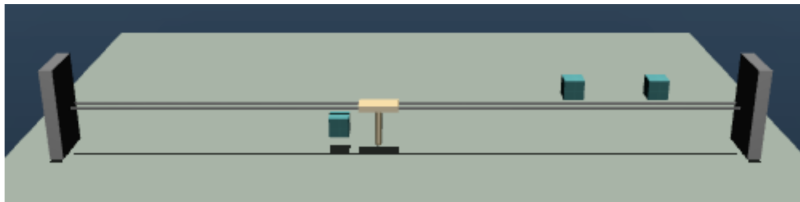
Figure: Environment-specific states are clustered. Reprinted from [2].

# Pipeline



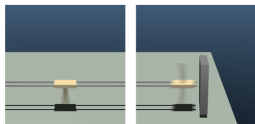
**Figure:** General pipeline for learning portable representations. Reprinted from [2].

# Experiments

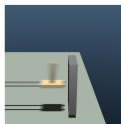


**Figure:** The rod-and-block domain. Available high-level options are `GoLeft`, `GoRight`, `RotateUp`, and `RotateDown`. Reprinted from [2].

# Experiments



(a)



(b)

```
(:action Up Clockwise_1
:parameters()
:precondition (and (symbol_18)
                  (symbol_11)
                  (notfailed))
:effect (and (symbol_12)
            (not symbol_18))
)
```

(c)

**Figure:** An example learned rule in PDDL. (a) Preconditions, (b) effect.  
Reprinted from [2].

# Experiments



(a)



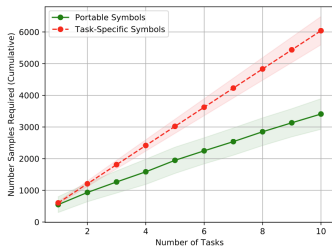
(b)

```
(:action DownLadder_1
:parameters()
:precondition (and (symbol_80)
                  (notfailed))
:effect (and (symbol_622)
             (not symbol_80))
)
```

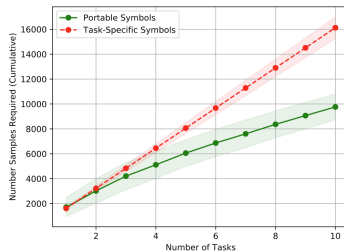
(c)

**Figure:** An example learned rule in PDDL. (a) Up, precondition. Down, effect. (b) States in which this option can be executed. Reprinted from [2]. Also, the character is taken from the amazing game Braid [1].

# Experiments



(a) Results for the *Rod-and-Block* domain.



(b) Results for the *Treasure Game* domain.

**Figure:** The usage of egocentric state space reduces the necessary sample size. Reprinted from [2].



- [1] Jonathan Blow. Braid.  
[https://en.wikipedia.org/wiki/Braid\\_\(video\\_game\)](https://en.wikipedia.org/wiki/Braid_(video_game)),  
2008.
- [2] Steven James, Benjamin Rosman, and George Konidaris.  
Learning portable representations for high-level planning. *arXiv preprint arXiv:1905.12006*, 2019.
- [3] George Konidaris, Leslie Kaelbling, and Tomas Lozano-Perez.  
Constructing symbolic representations for high-level planning.  
In *Twenty-Eighth AAAI Conference on Artificial Intelligence*,  
2014.