11.3 Describing and Analyzing Data - Overview

Measures of Center

Mean (Average Value)

- Simple, arithmetic <u>average</u> of the data.
 - Sum all numbers and divide by the sample size (*n*).
- Same calculation for the population and sample mean (just different notation).
 - O Sample mean = \bar{x} (pronounced "x-bar")
 - \circ Population mean = μ (Greek letter mu)
- Mean is NOT a resistant measure.
 - This means it is heavily affected by outliers.

Median (Middle Value)

- The middle value in an ordered list.
- Median IS a <u>resistant</u> measure.
 - NOT affected by outliers.

Mode (Most Common Value)

- The most frequently occurring value(s).
 - Unimodal data has one mode.
 - Bimodal data has 2 modes.
 - Multimodal data has more than 2 modes.
 - -> Ex) Case 1, No unde Can be no modes (every value is distinct).
- This is the only measure of center that can be used with categorical data.

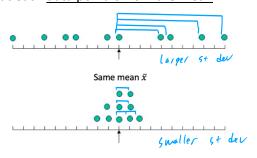
Measures of Spread (Dispersion)

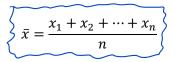
Range

- Range = Max Min
- Gives idea of the entire "range" of values, how much distance do they span in total.
- Ex) Case 2 above: Range = 10 1 = 9

Standard Deviation

Complex formula that measures the average distance that each data point is from the mean.





Example 1 – Mean

Data: 1, 5, 2, 9, 3

$$\bar{X} = \frac{1+5+2+9+3}{5} = Y$$

Example 2 - Median

Case 1 – Odd *n*

7 Obs: 10, 5, 6, 1, 3, 9, 8

Sorted: 1, 7, 4, 6, 8, 9, 16

Case 2 – Even *n*

8 Obs: 10, 5, 6, 1, 3, 9, 8, 3

Sample Standard Deviation = $S = \sqrt{\frac{\sum (x-\bar{x})^2}{n}}$

<u>Population</u> Standard Deviation $\in \sigma$ =

Sorted: 13, 8, 8, 16

(Greek letter sigma)

- Ex) Most common favorite color (can't average this)

Using your Calculator!

Using TI-83/84 (and TI-30 XS MultiView / XIIS) to calculate mean, median, sample / population st dev.

Steps for the TI-83/84

1. Enter data: STAT → Edit → Enter data in L

(Demo dataset: 10, 23, 4, 6, 9, 3, 15, 6)

2. Calculate: STAT \rightarrow CALC \rightarrow 1-Var Stats

a) List is L₁.

b) Leave FreqList blank.

c) Calculate!

Steps for the TI-30XS MultiView

- 1. Data \rightarrow Enter data in L₁
- 2. $2^{nd} \rightarrow \text{stat} \rightarrow 1\text{-Var Stats}$
- a) DATA: L1
- b) FRQ: ONE
- c) CALC

Steps for the TI-30 XIIS

- 1. $2^{nd} \rightarrow STAT \rightarrow 1-VAR$ (Enter)
- 2. DATA

 $X_1 = \# (scroll down)$

FRQ = 1 (for ALL Xs, scroll down)

 $X_2 = \#$ (scroll down)

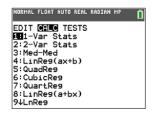
- 3. STATVAR (scroll across)
- 4. To exit this menu: $2^{nd} \rightarrow EXIT STAT \rightarrow Y$

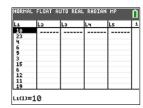
Inputs

Data here:

10, 23, 4, 6, 9, 3, 15, 6, 12, 11, 19, 10, 6, 8, 15

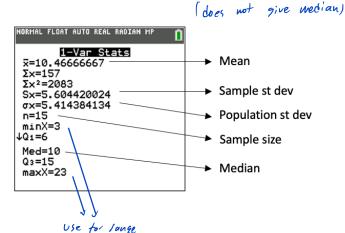








Results



ex) 15, 37, 38, 38, 65, 70

Example 3

Find the mean, median, mode and sample standard deviation of the following dataset.

Data (7 obs): 35, 70, 31, 37, 65, 38, 38

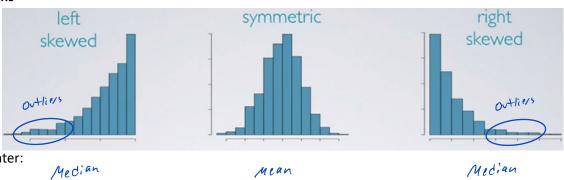
Mean = 44.86 = 15. 72

Other Considerations

Outliers

- Data values that are extreme when compared to the rest of the data.
- Can significantly impact measures of center and spread.

Types of Distributions



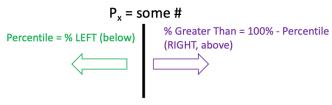
Mean

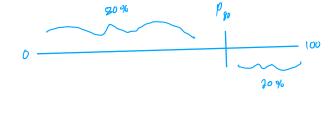
Best measure of center:

Measures of Relative Position

Percentiles

- A **percentile** tells you the percent of observations/individuals you are higher than.
 - o Interpreting example: You are told you scored in the 90th percentile on GRE. This means you have a score that is higher than 90% of all others that took the test.
 - o Range from 0th to 100th percentile.
 - o There is complement aspect to percentiles as well; for example, if you are the 80th percentile, there is greater than you!
- Best way to remember!





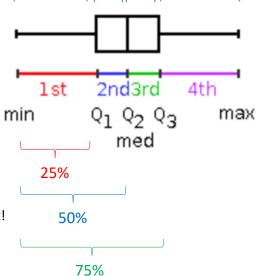
25%

Notation: X^{th} Percentile = P_x

5-Number Summaries and Boxplots

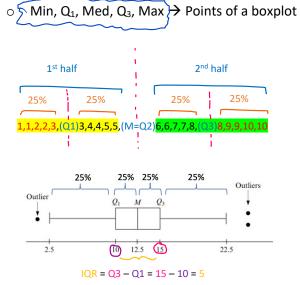
- **Quartiles** are specific percentiles.
 - O Q₁ is the 25th Percentile.
 - o Q₃ is the 75th Percentile.
 - O Q₂ is the 50th Percentile = Median.
- Inner Quartile Range (IQR)
 - Another measure of variation, less informative than the standard deviation.
 - Uses quartiles to measure how far data is spread out around the median. Specifically, it measures the range of the middle 50% of the data

Visualized very well in boxplots! It is the length of the box!



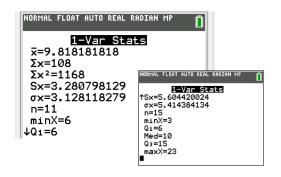
25%

5-number summary



Example 4

a) Using this output from a 1-Var Stat, what is the IQR?

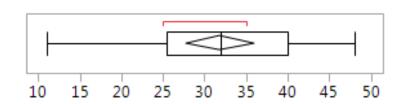


$$\int 0R = 03 - 0,$$

$$\int = 15 - 6$$

$$= 9$$

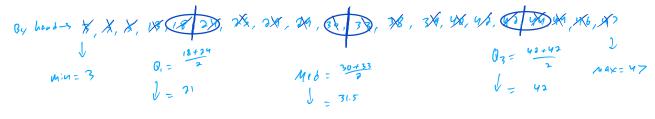
b) Find the IQR from this boxplot.



Example 5

a) Calculate the 5-number summary of the following dataset (20 numbers):

38, 33, 5, 5, 47, 29, 24, 42, 3, 18, 30, 46, 25, 44, 40, 42, 39, 44, 29, 13



b) Draw a boxplot based on the 5-number summary from (a).

