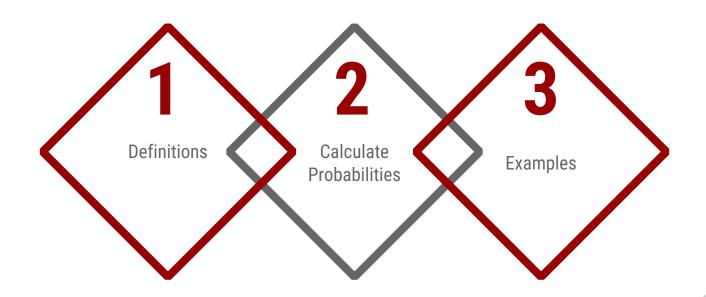
# 7.1 Intro to Probability





# **Goals for the Day**



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- An <u>experiment</u> or <u>trial</u> is the process by which a random observation or outcome is generated.
  - Ex: Flipping a coin, rolling a die, determining the sex of a baby
- An <u>outcome</u> is any possible individual observation of that experiment
  - Ex: If you flip a coin, you have two possible outcomes: heads, or tails. Heads is an outcome, and tails is another outcome.





- Sample space (S), which is the set of all possible outcomes of an experiment/trial.
  - EX: If you flip a coin twice,  $S = \{HH, HT, TH, TT\}.$







- An <u>event (E)</u>, is any collection of possible outcomes of an experiment (i.e., any subset of S).
  - Ex: If you flip a coin twice, you might be interested in getting two heads, which would be notated as  $A = \{HH\}$ .
  - Ex: ...getting at least one head, which is  $A = \{HH, HT, TH\}.$





#### **Example**



You are playing a game in which you roll a pair of 4-sided die. To determine your next move, you need to know the sum of the two die.

#### Using proper notation:

- Write the sample space:  $S = \{2,3,4,5,6,7,8\}$
- Write the event of rolling a sum that is even:  $E = \{2,4,6,8\}$
- Write the event of rolling a sum that less than 6:  $E = \{2,3,4,5\}$

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**Calculating Probabilities** 



## **Probability**



- Probability = likelihood of event occurring
  - $ightharpoonup 0 \le Probability \le 1$
  - □ 0 = NEVER occurs; 1 = ALWAYS occurs
  - ightharpoonup The probability of an event A happening is notated P(A)



## Classical (Theoretical) Probability



# Classical (Theoretical) Probability

If all outcomes are <u>equally likely</u>,

$$P(Event) = \frac{Number\ of\ outcomes\ in\ the\ event}{Number\ of\ outcomes\ in\ the\ sample\ space}$$

$$= \frac{Number\ of\ successes}{Number\ of\ possibilities}$$

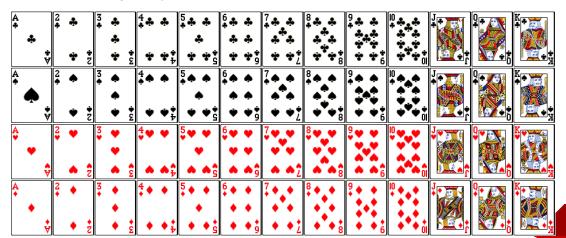


## **Classical (Theoretical) Probability**



# **Example**

Suppose you are randomly selecting cards from a standard 52card deck of playing cards.

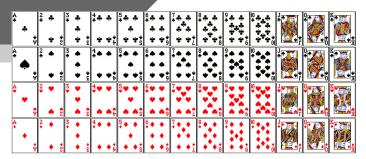








# **Examples**



Find the probability of drawing a red card.

$$P(Red) = \frac{\# Successes}{\# Possible} = \frac{26}{52} = \frac{1}{2} = 0.5$$

Find the probability of a King.

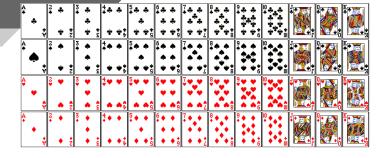
$$P(King) = \frac{\# Kings}{Total \# of \ cards} = \frac{4}{52} = \frac{1}{13} \approx 0.077$$







# **Examples**



Find the probability of drawing a Heart or a 10.

$$P(Heart\ or\ 10) = \frac{\# Hearts\ or\ 10s}{Total\ \#\ of\ cards} = \frac{13+3}{52} = \frac{16}{52} = \frac{4}{13}$$

Find the probability of drawing a card that is not a Club.

$$P(NOT \ a \ club) = \frac{\# \ Not \ Club}{Total} = \frac{39}{52} = \frac{52 - 13}{52} = \frac{3}{4}$$





# **Empirical probability**

Based on experiments (DATA).

$$P(Event) = \frac{Number\ of\ times\ the\ event\ occurs}{Number\ of\ times\ experiment\ is\ performed}$$

$$= \frac{Number\ of\ successes}{Number\ of\ trials}$$





# **Examples**

- Suppose we collected data on MATH 125 students and are selecting a single student randomly.
- Find the probability the student is a Math major.

$$P(Math) = \frac{\# Math}{\# Students} = \frac{23}{76}$$

Major	Number of Students
Math	23
Chemistry	15
Art	18
English	20





# **Examples**

Find the probability the student is not a Math major.

$$P(Not\ Math) = \frac{\#\ Not\ Math}{\#\ Students} = \frac{15 + 18 + 20}{76} = \frac{76 - 23}{76} = \frac{53}{76}$$

Major	Number of Students
Math	23
Chemistry	15
Art	18
English	20





# **Examples**

Find the probability the student is an Art or Chemistry major.

$$P(Art\ or\ Chem) = \frac{\#\ Art\ or\ Chem}{\#\ Students} = \frac{18+15}{76} = \frac{33}{76}$$

Major	Number of Students
Math	23
Chemistry	15
Art	18
English	20





# **Examples**

Find the probability the student is a Math, Chemistry, or English major.

$$P(Math, Chem, or\ English) = \frac{\#Successes}{\#Possibilities} = \frac{23 + 15 + 20}{76} = \frac{58}{76}$$

Major	Number of Students
Math	23
Chemistry	15
Art	18
English	20

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**Examples** 

#### **Example**



An experiment is performed where a fair 4-sided die is rolled, then a fair 3-color spinner is spun. The possible outcomes for each event are 1, 2, 3, and 4 for the 4-sided die and red (R), blue (B), and yellow (Y) for the 3-color spinner.

- a) Identify the sample space for this experiment.
- b) Find the probability of rolling a 3
- c) Find the probability of rolling an even number AND spinning red.
- d) Determine if this is classical or empirical probability.

a) 
$$S = \{1R, 1B, 1Y, 2R, 2B, 2Y, 3R, 3B, 3Y, 4R, 4B, 4Y\}$$

b) 
$$P(3) = \frac{3}{12}$$
 c)  $P(Even\ AND\ R) = \frac{2}{12}$   
d) Classical (Theoretical) Probability