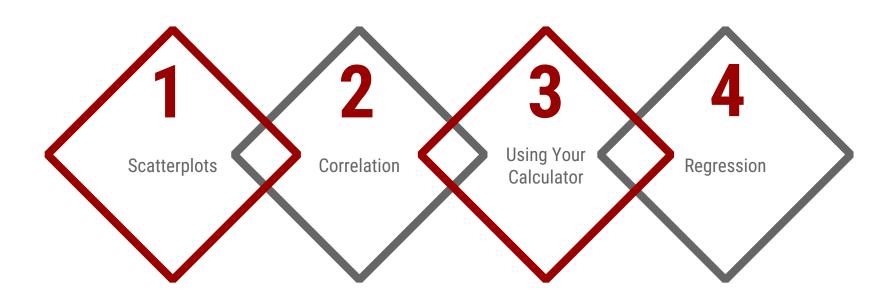
# 12.3 Data Exploration





# **Goals for the Day**



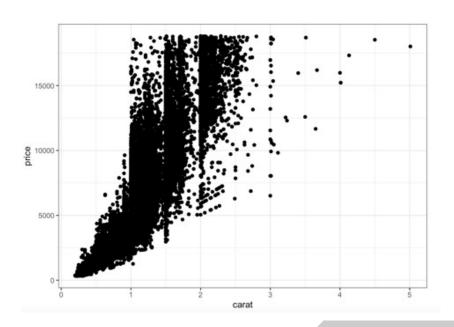
**Scatterplots** 



### **Scatterplots**



- Displays the relationship between **two quantitative** variables measured on the same individuals.
- Useful to determine if an **association** exists!
  - So is there a <u>pattern</u> where some values of one variable tend to occur with some values of the other variable.
  - Ex) Smaller carat diamonds tend to have lower prices, and as the carat increases prices tend to increase as well.



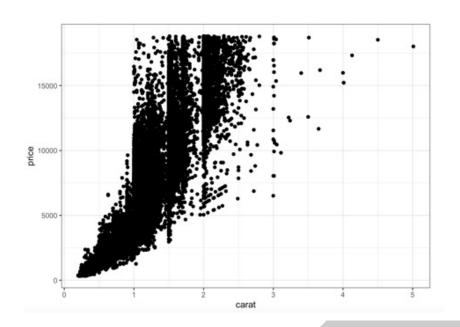


### Scatterplots



#### Setup of axes

- The <u>explanatory</u> (independent) variable goes on the X (<u>horizontal</u>) axis.
- The <u>response</u> (dependent) variable goes on the Y (vertical) axis.
- Ex) How large a diamond is impacts how much it costs → Carat = X; Price = Y.





### **Interpreting Scatterplots**



- Interpreting a scatterplot (what we are looking for in a scatterplot)
- Form (pattern of the dots)
  - Linear → Points follow a general linear trend; Straight line.
  - Curved → Points show some evidence of curvature; NOT a straight line.
  - Random scatter → No pattern, points are just scattered about randomly kinda like a cloud of points.





### **Interpreting Scatterplots**



- Interpreting a scatterplot (what we are looking for in a scatterplot)
- **Direction** (of the association; only applies to <u>linear relationships</u>)
  - Positive → Upward trend.
  - $\rightarrow$  Negative  $\rightarrow$  Downward trend.
  - No Association → There is no pattern or general trend (corresponds to random scatter).



### **Interpreting Scatterplots**

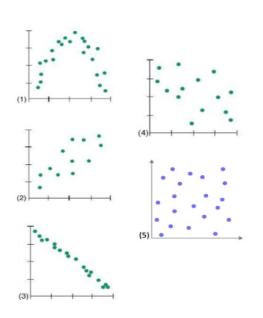


- Interpreting a scatterplot (what we are looking for in a scatterplot)
- **Strength** (how strong the association is; how well the data fits the pattern; only applying this to linear relationships)



## **Interpreting Scatterplots Example**





#### **Example**

	Form	Direction	Strength		
(1)	Curved	N/A (+/-)	N/A (strong)		
(2)	Linear	Positive	Moderate		
(3)	Linear	Negative	Strong		
(4)	Roughly linear	Negative	Weak		
(5)	Random scatter	No association	Very weak		

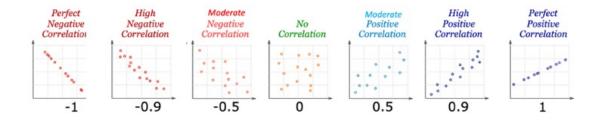
Correlation



#### Correlation



- The **correlation** (r) s an index that expresses the <u>direction</u> and <u>strength</u> of the relationship.
  - lt combines both of these aspects into a single number measure.
  - Often referred to as the correlation coefficient (or Pearson's correlation).
- Interpreting correlation
  - Sign = Direction
  - Absolute value |r| = Strength





#### Correlation



- Properties of Correlation
  - Scale goes from -1 to 1  $\rightarrow$  -1  $\leq r \leq 1$
  - Only applies to <u>LINEAR relationships</u>.



r has no units and is the same regardless of which variable is X or Y.



Does NOT imply a cause-and-effect relationship.

Ex) Ice cream sales and shark attacks have a strong positive correlation.

**Using Your Calculator** 

### **Using Your Calculator**

Using TI-83/84 (and TI-30 XS MultiView / XIIS) to calculate correlation (and regression line).

#### Steps for the TI-83/84

Enter data: STAT → Edit →

Enter X data in L<sub>1</sub> Enter Y data in L<sub>2</sub>

- Calculate: STAT → CALC → LinReg(ax+b)
  - a) XList: L<sub>1</sub>.
  - b) YList: L<sub>2</sub>.
  - c) Rest leave blank.
  - d) Calculate!

#### Steps for the TI-30XS MultiView

Data →

Enter X data in L<sub>1</sub> Enter Y data in L<sub>2</sub>

- 2. 2<sup>nd</sup> → stat → 2-Var Stats
  - a) xDATA: L1
  - b) yDATA: L2
  - c) CALC

#### Steps for the TI-30 XIIS

- 1.  $2^{nd} \rightarrow STAT \rightarrow 2-VAR$  (Enter)
- DATA

 $X_1 = \#$  (scroll down)

 $Y_1 = \# (scroll down)$ 

... (repeat for all data points)

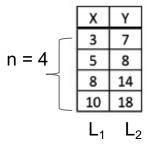
- 3. STATVAR (scroll across)
- To exit this menu: 2<sup>nd</sup> → EXIT STAT → Y

<sup>\*\*\*</sup> One time setup for TI-83/84:  $2^{nd} \rightarrow$  Catalog  $\rightarrow$  DiagnosticOn  $\rightarrow$  Enter

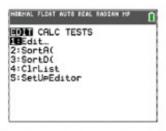


### **Using Your Calculator**

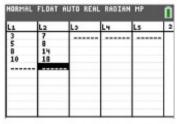
#### Demo dataset



#### Inputs

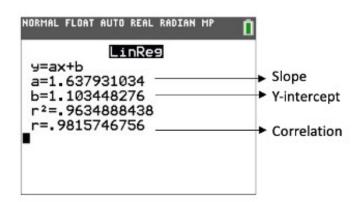


	_
NORMAL FLOAT AUTO REAL RADIAN MP	_ [
EDIT CALC TESTS	
1:1-Var Stats	
2:2-Var Stats	
3: Med-Med	
ELinReg(ax+b)	
5: QuadRe9	
6:CubicRe9	
7:QuartRe9	
8:LinReg(a+bx)	
9↓LnRe9	





#### <u>Results</u>

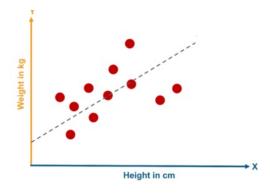


Regression





- Ultimately, we want to determine if we can use a straight line to model the relationship between two variables → If so, we can use that model to make predictions!
  - This process is called **Linear Regression**.



### Regression



Critical Values of the

**Pearson Correlation** Coefficient

 $\alpha = 0.05$ 

0.950

0.878

0.811

0.754

n

4 5

6

- Step 1  $\rightarrow$  Determine if there is a significant correlation (linear relationship).
- Calculate correlation.
- Compare it to the **Table of Critical Values or the Pearson Correlation Coefficient** to see if it is statistically significant.
  - Match the sample size n and the Level of significance  $\rightarrow$  (Probability our claims about the data are wrong) to the specific problem.

 $\rightarrow$  r = 0.982 > 0.950 = CV Demo ex) n = 4,  $\alpha = 0.05$ 

→ Significant → Can make predictions



 $\alpha = 0.01$ 

0.990

0.959

0.917

0.875





- Step 2  $\rightarrow$  Once we have a significant correlation, we can find the regression line.
  - Linear equation that fits our data best (aka 'line of best fit').
    - It is IMPORTANT to get the X and Y variables correct!
  - Our calculator gives us our equation!



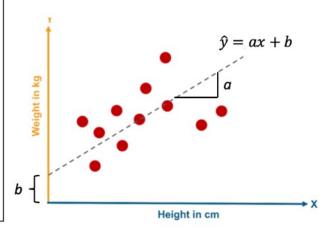


#### **Equation**

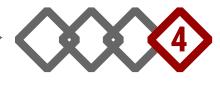
• Here is the form of our linear equation (written in slope-intercept form):

$$\hat{y} = ax + b$$

- x = Value of the explanatory variable
- $\hat{y}$  = Predicted value of the response variable for the given x
- a = Slope
  - · It measures the direction and steepness of the line
- b = Y intercept
  - It is the location where the regression line crosses the Y-axis (value of Y when X = 0)



### Regression



- Step 3 → Make predictions using the regression line.
- We can think of our regression line, and specifically  $\hat{y}$ , as <u>predicted values</u> of Y for all X values in the X range of our sample data!
- Calculating these is simple:
  - Just plug in the new X value to our equation and this will give us the predicted Y.
  - Demo example) Predict Y for X = 7.

$$\hat{y} = 1.638x + 1.103 \rightarrow \hat{y} = 1.638(7) + 1.103 = 12.569$$
  
ax + b



7	<b>(X)</b>

<b>Hours Spent on Homework</b>	41	20	34	43	9	20	54	52	10	21
Grade on Test	79	63	76	100	55	82	95	80	60	80

- a) Calculate the correlation for the dataset above and determine if it is statistically significant at a level of significance of  $\alpha = 0.05$ .
- b) If appropriate, determine the regression equation.
- c) If a student spends 35 hours on homework, make a prediction for their grade on the test.
- d) If a student spends 50 hours on homework, make a prediction for their grade on the test.

a) 
$$r = 0.779 > 0.632 \rightarrow Significant$$

b) Appropriate 
$$\rightarrow \hat{y} = 0.676x + 56.459$$

c) 
$$\hat{y} = 80.119$$

d) 
$$\hat{y} = 90.259$$