

## 6.1 Understanding Interest – Overview

### Definitions / Key Ideas

**Interest** – Amount charged for borrowing money or earned from investing

**Principal** – Initial investment or loan amount.

**Annual Percentage Rate (APR)** – Yearly interest rate (normally given as percentage per year).

**Simple Interest** – Only calculated on the principal.

**Compound Interest** – Calculated on principal and accrued interest.

**Continuously Compounded Interest** – Interest is compounded continuously.

**Annual Percentage Yield (APY)** – Effective annual interest rate (accounts for compounding).

(n values)

**Table 1: Compounding Intervals**

Compounding	Number per Year
Annually	1
Semiannually	2
Quarterly	4
Monthly	12
Weekly	52
Daily	365

### Formulas and Examples

#### 1. Simple Interest

$$I = P \cdot r \cdot t$$

Interest      Principal      rate (decimal)      time

How much money will I have if... And how much interest will I earn if...

Ex: I invest \$500 at 10% APR with simple interest for 8 years? For 6 months?

$$I = 500(0.10)8$$

$$\downarrow = \$400$$

$$A = P + I$$

$$\downarrow = 500 + 400 = \$900$$

$$I = 500(0.10)\frac{6}{12}$$

$$\downarrow = \$25$$

$$A = P + I$$

$$\downarrow = 500 + 25 = \$525$$

#### 2. Compound Interest (regular)

$$A = P \left(1 + \frac{r}{n}\right)^{nt}$$

Future (total) value      # of compounding periods

Ex: I invest \$500 at 10% APR for 8 years, compounded monthly? Quarterly?

$$A = 500 \left(1 + \frac{0.10}{12}\right)^{12(8)}$$

$$\downarrow = \$1109.09$$

$$I = A - P$$

$$\downarrow = 1109.09 - 500 = \$609.09$$

$$A = 500 \left(1 + \frac{0.10}{4}\right)^{4(8)}$$

$$\downarrow = \$1101.88$$

$$I = A - P$$

$$\downarrow = 1101.88 - 500 = \$601.88$$

#### 3. Compound Interest (continuous)

$$A = Pe^{rt}$$

Ex: I invest \$500 at 10% APR for 8 years with continuous compounding?

$$A = 500 e^{0.10(8)}$$

$$\downarrow = \$1112.77$$

$$I = A - P$$

$$\downarrow = 1112.77 - 500 = \$612.77$$

#### 4. Annual Percentage Yield

$$APY = \left[ \left(1 + \frac{r}{n}\right)^n - 1 \right] \times 100$$

Ex: What is the Annual Percentage Yield (APY) for example 2?

$$APY_{\text{monthly}} = \left[ \left(1 + \frac{0.10}{12}\right)^{12} - 1 \right] \times 100$$

$$\downarrow = 10.47\%$$

★ calculator tip → Type all in one step ★

## Examples

**Example 1:** Suppose you wish to borrow \$200 for five weeks and the amount of interest you must pay is \$20 per \$100 borrowed. What is the APR at which you are borrowing money?

Simple Interest

$$I = Prt$$

$$I = \$20 / \$100 \Rightarrow \$40 \text{ for } \$200 \text{ borrowed}$$

$$P = \$200$$

$$r = ?$$

$$t = \frac{5 \text{ weeks}}{52 \text{ weeks}} = 5/52$$

$$\frac{40}{200} = \frac{200}{200} r \left( \frac{5}{52} \right)$$

$$\frac{52}{5} \cdot \frac{1}{5} = r \frac{5}{52} \times \frac{52}{5}$$

$$r = 2.08 \xrightarrow[\text{Convert to \%}]{\times 100}$$

$$r = 208\%$$

**Example 2:** Suppose that \$13,000 is deposited for eight years at 4% APR. Calculate the interest earned if interest is compounded weekly. Round your answer to the nearest cent.

★ Compound Interest

$$A = P \left( 1 + \frac{r}{n} \right)^{nt}$$

$$A = 13,000 \left( 1 + \frac{0.04}{52} \right)^{52(8)}$$

$$\downarrow \approx \$17,900.46$$

$$A = \$13,000$$

$$r = 4\% = 0.04$$

$$n = 52 \text{ (weeks)}$$

$$t = 8 \text{ (years)}$$

$$I = A - P$$

$$= 17,900.46 - 13,000$$

$$\downarrow = \$4,900.46$$