

1. Road map of the module
2. Topology (in \mathbb{R}) true/false
 - (a) A set S is closed iff it is not open
 - (b) A finite set is always closed
 - (c) All intersections of open sets are open
 - (d) An open set that contains every rational number must contain all of \mathbb{R}
3. Prove that the intersection of two open sets in \mathbb{R}^n is open (using the definitions of open sets in \mathbb{R}^n , not just general facts about open sets)
4. Prove that a singleton set (set of one element) in \mathbb{R}^n is closed
5. Using integration, solve the differential equation (of one variable) $\dot{x} = kx$. How does this relate to the technique we used this week for solving (some) differential equations of multiple variables?
6. Using the Taylor-series definition, prove that if D is a diagonal matrix, then the exponentiation rule we learned back in Module 1 works.
7. If time: Suppose that $\dot{\vec{v}} = A\vec{v}$, where $A = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$, and that $v_0 = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$. Given this, solve for \vec{v} . Notice that there is only one eigenvalue, so there is no basis of eigenvectors.