

## 1. Finding eigenvectors and eigenvalues

- (a) Using the characteristic polynomial method, find the eigenvectors and eigenvalues of

$$A = \begin{bmatrix} 1 & 2 \\ -1 & 4 \end{bmatrix}$$

- (b) Use Axler's method to find the eigenvectors and eigenvalues of
- $A$
- again.

## 2. Some quick useful facts and special cases of eigenvectors and eigenvalues

- (a) A triangular matrix has eigenvalues along its main diagonal:
  - (b) square of a triangular matrix and the eigenvalues
  - (c) Symmetric matrices have eigenvectors that are orthogonal
  - (d) eigenvalues of rotations through 90 and 180 degrees
3. Walk through Proof 4.2: For real  $n \times n$  matrix  $A$ , prove that all the polynomials  $p_i(t)$  are simple and have real roots iff there exists a basis for  $\mathbb{R}^n$  consisting of eigenvectors of  $A$ .
4. If  $\lambda$  is an eigenvalue  $A$  with  $\vec{v}$  the corresponding eigenvector, prove that  $\lambda - s$  is an eigenvalue of  $A - sI$  for any scalar  $s$ , with corresponding eigenvector  $\vec{v}$ .