

ATTENDANCE QUIZ (WEEK 10)

COLTON GRAINGER (MATH 1300)

Your name (print clearly in capital letters): _____

This is an **ungraded** quiz that will count for attendance; it is due by the end of recitation.

1. DEFINITIONS AND COMMENTS

1. A **zero** (or a **root**) of a function f is

a point r such that $f(r) = 0$.

- i. The term *root* is traditionally¹ used for the study of polynomial functions.
- ii. For example, if r is a root of the polynomial function p (that is, if $p(r) = 0$), then

$$p(x) = (x - r)q(x) \quad \text{for some polynomial function } q.$$

2. A **critical point** of a function f is

a point a such that $f'(a) = 0$.

- i. The number $f(a)$ itself is called a **critical value** of f .

3. A **point of local extremum** of a function f is

a point of either local maximum or minimum.

- i. If b is a point of local extremum, we say $f(b)$ is a **local extreme value**.

4. An **inflection point** of a function f is

a point c such that the tangent line to f at $(c, f(c))$ crosses the graph of f .

- i. In order for c to be an inflection point of a function f , it is necessary that f'' should have different signs to the left and right of c .
- ii. For example (see figure), $\sqrt{1/3}$ and $-\sqrt{1/3}$ are inflection points of $f(x) := 1/(1 + x^2)$.

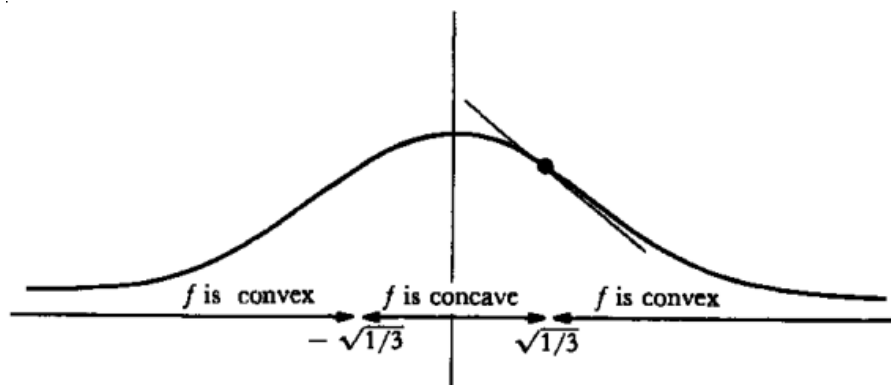


FIGURE 1. Inflection points

Date: 2019-03-17.

¹“The **roote quadrat** of the whole number, is the desired distance or line Hypothenusal.” (Digges, *Pantom*, 1571).

2. MULTIPLE CHOICE

1. Consider the function $f: \mathbf{R} \rightarrow \mathbf{R}$ defined by $f(x) = x^3(x-1)^4(x-2)^2$. Which of the following is **true**?
- (A) 0, 1, and 2 are all critical points and all of them are points of local extrema.
 - (B) 0, 1, and 2 are all critical points, but only 0 is a point of local extremum.
 - (C) 0, 1, and 2 are all critical points, but only 1 and 2 are points of local extrema.
 - (D) 0, 1, and 2 are all critical points, and none of them is a point of local extremum.
 - (E) 1 and 2 are the only critical points.

Your answer: _____

2. Say $f: \mathbf{R} \rightarrow \mathbf{R}$ is a differentiable function. What information **can not** be determined from **only** the first derivative f' ?
- (A) roots of the function
 - (B) critical points
 - (C) points of inflection
 - (D) local extreme values
 - (E) neither (D) nor (A)

Your answer: _____

3. Say $f: \mathbf{R} \rightarrow \mathbf{R}$ is a twice-differentiable function. What information **can** be determined from **only** the second derivative f'' ?
- (A) intervals where the function is positive or negative
 - (B) intervals where the function increases and decreases
 - (C) intervals where the function is concave up and concave down
 - (D) y -values of horizontal asymptotes
 - (E) all of the above

Your answer: _____

4. Suppose f and g are continuously differentiable functions on \mathbf{R} . Suppose f and g are both concave up. Which of the following is **always true**?
- (A) $f + g$ is concave up.
 - (B) $f - g$ is concave up.
 - (C) $f \cdot g$ is concave up.
 - (D) $f \circ g$ is concave up.
 - (E) All of the above.

Your answer: _____

3. REFERENCES

The definitions are from Spivak [1]. The questions are adapted from Naik's Math-152 notes [2].

[1] M. Spivak, *Calculus*, 3rd ed. Publish or Perish, Inc., 1994.

[2] V. Naik, "Math 152 Course Notes," 2012.