

# OFFICIAL MIDTERM 1 SYLLABUS

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*Here's an "official" midterm syllabus that I dug up from Canvas. We covered this and different content in class, and used more sophisticated terminology.*

*To critique the following syllabus, start noticing::*

- *they're only sketches of recipes for performing "pseudo-mathematics",*
- *they're dated by the job market*
- *they're constrained by calculator computation,*

*However, I want all y'all to succeed in the midterm. Let's have a "cautious" look at the material together.*

## 1. CONTENT ON MIDTERM 1

1. Sampling Techniques
  - Stratified
  - Clustered
  - Simple random sample (SRS)
  - Systematic
2. Classifying Variables
  - Quantitative
  - Qualitative
3. Levels of Measurement
  - Nominal
  - Ordinal
  - Interval
  - Ratio
4. Statistics vs. Parameters
  - Samples vs. statistics
  - Populations vs. parameters
5. Experiments vs. Observational studies
  - Control vs. treatment groups
  - Variable = what we are measuring
  - Placebo

6. Histograms
  - Quantitative
  - Class width
    - Max – Min divided by number classes (round up to nearest whole number)
    - Midpoint = middle of class
  - Class boundaries
    - Subtract 0.5 from lower limit
    - Add 0.5 to upper limit
7. Other graphs/charts
  - Ogive vs. time series
  - Circle graph
    - Mutually exclusive portions of the pie ONLY
  - Bar graph vs. pareto
  - Stem & leaf
  - Box & whisker
8. Shapes of distributions
  - Mound/symmetric
  - Skewed
  - Uniform
  - Bimodal
9. Frequency tables
  - L1 = data points
  - L2 = frequency of each data point
10. 5% trimmed mean
  - Determine  $n$  (number of data points)
  - $N * 0.05$  (yields number to trim off of top and bottom)
  - Re-compute mean using 1-var stats
11. Weighted averages
12. Basic Stats
  - Mean
  - Median
  - Quartiles (Q1, Q3, IQR)
  - Min/Max
  - Mode
13. Coefficient of variation
  - take  $\sigma / \mu$ , then convert to percentage
  - What % of the mean is the standard deviation?
14. Chebyshev's Theorem
  - $1 - 1/(k^2)$  gives the proportion of data that lies within a radius of  $k$  standard deviations from the mean
  - therefore, at least 75% lies within 2 standard deviations

## 15. Probability

- Mutually exclusive events vs. independent events
  - mutually exclusive events are represented by disjoint sets
  - Independent = one thing doesn't affect probability of another thing
- With vs. without replacement & how that affects 2-component probability problems
- Sample space  $\Omega = \{x, y, z\}$
- $P(A)$  vs.  $P(A)^c$
- if  $E_1, E_2, \dots$  are disjoint events, and their union is the entire sample space  $\Omega$ , then  $\mathbf{P}(E_1) + \mathbf{P}(E_2) + \dots = \mathbf{P}(E_1 \sqcup E_2 \sqcup \dots) = \mathbf{P}(\Omega) = 1$ .
- Common examples:
  - 6 sided die
  - 52 card deck
  - roulette
- “Given” probabilities & contingency tables
- $P(A \text{ or } B) = P(A \cup B)$  vs.  $P(A \& B) = P(A \cap B)$
- Continuous vs. discrete random variables
- Probability distribution tables
  - Calculate average or expected value and variance based on probability distribution

## 16. Odds

- the “odds for an event” is the ratio of the number ways  $P(E)$  to get the event  $E$  you want against the number of ways  $P(E^c)$  to not get what you want  $E^c$
- the “odds against an event” is the reverse ratio
  - these are also called “betting odds”
- What's the relation to of betting odds to probability?

## 17. Binomials

- using the TI-84 with the  $(n, p, k)$  notation
  - $n$  trials
  - $p$  probability of success
  - $r$  observed successes
- `binompdf` gives the PMF (or the exact number of outcomes)
- `binomcdf` gives the CMF (or the cumulative number of outcomes up to a specified number of observed successes)
  - the calculator counts from 0 to number you put in for  $k$
  - Use `binomcdf` for following scenarios:
    - \* “at most  $k$ ”
    - \* “ $k$  or less”
    - \* “fewer than  $k$ ”
  - Use `1~binomcdf` for the following scenarios:
    - \* “at least  $k$ ”
    - \* “ $k$  or more”
    - \* “greater than  $k$ ”
- Rules for using binomials
  - the trials are independent
  - each trial has only 2 outcomes (success or failure)
  - the probability of success for each trial is constant

18. Normal Distributions

- Normal vs. Standard Normal
- Symmetrical properties
- Empirical rule
  - 68% within  $1\sigma$ , 95% within  $2\sigma$ , 99.7% within  $3\sigma$  of  $\mu$
- Z-scores (Negative vs. positive z-scores and how they relate to  $\mu$ )
  - $Z = \frac{x - \mu}{\sigma}$
- Find the cumulative probability given a Z-score or x-value (`normalcdf`)
- Find the Z-score given a cumulative probability (`invNorm`)

19. Control Signals

- 9 consecutive values are above mean or 9 consecutive values are below mean
- Any value is outside  $3\sigma$
- 2 of 3 consecutive values have absolute value greater between  $2\sigma$  and  $3\sigma$

20. Central Limit Theorem

- As the number of samples  $n$  increases, the mean of the various samples  $\bar{x}$  approaches the normal distribution
- one needs  $n \geq 30$  if one doesn't know that the original distribution is normal

## 2. CALCULATOR FUNCTIONS

Be comfortable with:

1. INPUTTING DATA INTO LISTS (L1, L2)
2. 1-VAR STATS
3. BINOMPDF
4. BINOMCDF
5. TABLE FUNCTION TO FIND N FOR BINOMIALS
6. NORMALCDF
7. INVNORM