COMP 2230_02

Assignment 10



COMP 2230 - Data Structures and Algorithm Analysis

Assignment #10: Sets, Maps and Graphs

Due Date: Section 01 Nov. 28th Section 02 Nov 29th, 2024

Chapter 22 Sets and Maps

1. What is a set?

A set is a collection of elements that contain unique (no duplicates) values with a primary purpose of determining if an element exists in the collection.

2. What is a map?

A map is a collection that creates a relationship between a key and a value with the primary purpose of providing an efficient way of finding a value given its key. A map contains unique values and keys with one key matching the one value per key, but multiple keys can be mapped to the same value.

- 3. What is the difference between a set and a map?

 The difference between a set and a map is the purpose of the collections, the map is made for finding values whereas the set is made for seeing if it exists.
- 4. Create a Set ADT (set class to hold integers using an array as the underlying data structure) that has the following methods:
 - a. add(int)
 - b. remove(Int)
 - c. boolean contains(int)

```
private void expandCapacity() {
    set = Arrays.copyOf(set, set.length * 2);
}

public void remove(int element) {
    for (int i = 0; i < set.length; i++) {
        if (set[i] == element) {
            set[i] = 0;
            break;
        }
    }

public boolean contains(int element) {
    boolean result = false;
    for (int e : set) {
        if (e == element) {
            result = true;
            break;
        }
    }
    return result;
}

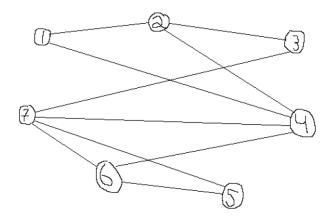
// just so we can see what's happening to test it public String toString() {
        return Arrays.toString(set);
}
</pre>
```

Output:

```
[0, 0, 0, 0, 0]
[8, 5, 7, 12, 0]
[8, 5, 7, 12, 0]
[8, 0, 7, 12, 0]
[8, -26, 7, 12, 0]
```

Chapter 24 Graphs

1. Draw the undirected graph that is represented as follows: Vertices 1, 2, 3, 4, 5, 6, 7 Edges (1, 2), (1, 4), (2, 3), (2, 4), (3, 7), (4, 7), (4, 6), (5, 6), (5, 7), (6, 7)



2. Is the graph from question 1 connected?

Yes. The graph is connected as all vertices have a path to each other.

3. List all the cycles in the graph from question 1.

Cycles (*Technically these are all the circuits):

$$1 \rightarrow 2 \rightarrow 4 \rightarrow 1$$

$$1 \rightarrow 2 \rightarrow 3 \rightarrow 7 \rightarrow 4 \rightarrow 1$$

$$1 \rightarrow 2 \rightarrow 3 \rightarrow 7 \rightarrow 6 \rightarrow 4 \rightarrow 1$$

$$1 \rightarrow 2 \rightarrow 3 \rightarrow 7 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1$$

$$2 \rightarrow 3 \rightarrow 7 \rightarrow 4 \rightarrow 2$$

$$2 \rightarrow 3 \rightarrow 7 \rightarrow 6 \rightarrow 4 \rightarrow 2$$

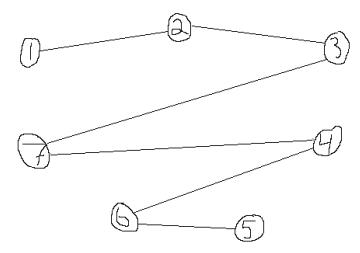
$$2 \rightarrow 3 \rightarrow 7 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 2$$

$$4 \rightarrow 6 \rightarrow 7 \rightarrow 4$$

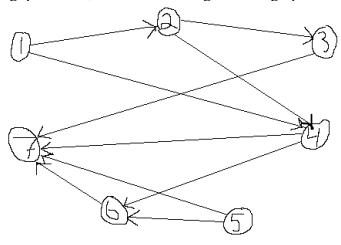
$$4 \rightarrow 6 \rightarrow 5 \rightarrow 7 \rightarrow 4$$

$$5 \rightarrow 6 \rightarrow 7 \rightarrow 5$$

- *All the cycles could be rewritten starting from any vertex in the cycle (Eg. $1 \rightarrow 2 \rightarrow 4 \rightarrow 1$ is also $2 \rightarrow 4 \rightarrow 1 \rightarrow 2$).
- *All the cycles could be rewritten backward (Eg. $1 \rightarrow 2 \rightarrow 4 \rightarrow 1$ is also $1 \rightarrow 4 \rightarrow 2 \rightarrow 1$).
- *Some of the cycles can be combined to create more larger cycles (Eg. Combine $1 \rightarrow 2 \rightarrow 4 \rightarrow 1$ with $4 \rightarrow 6 \rightarrow 7 \rightarrow 4$ to get the cycle $1 \rightarrow 2 \rightarrow 4 \rightarrow 6 \rightarrow 7 \rightarrow 4 \rightarrow 1$ that goes through 4 twice).
- 4. Draw a spanning tree for the graph from question 1.



5. Using question 1, draw the resulting directed graph.



- 6. Is the directed graph of question 5:
 - a. Connected?

The directed graph is not connected as there is not necessarily a path from any vertex to any other (Eg. no path from 7 to 5).

b. Complete?

Graph is incomplete since there is not the maximum edges connecting vertices such as no edge between 4 and 5 and no edge between 1 and 7 etc.

7. List all of the cycles in graph of question 5.

There are no cycles in the graph as no vertices can be both start and end. For vertices 1 and 5, there are only edges going away, so once you leave them, you can never come back. The opposite is true for vertex 7; you can arrive but never leave. The only way to arrive at 2 is from 1 (which we already determined does not work), so it cannot be part of a cycle either. The same logic applies when you try to leave 6 or 3 because of 7. After that, only 4 remains, which is not enough to create a cycle.

8. Draw a spanning tree for the graph of question 5.

