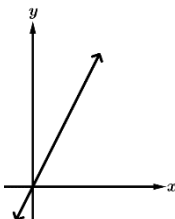
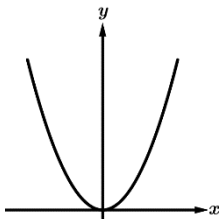
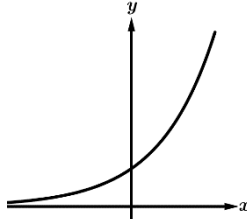
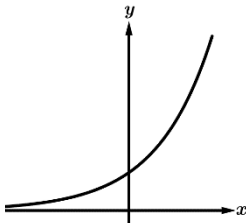
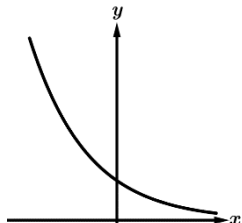


Notes: (Topic 2.3) Exponential Functions

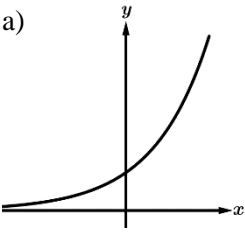
In math, we study several different types of functions. Three types of functions seem to keep showing up in every math course from Algebra 1 to Calculus. These three families of functions are also featured predominantly on the SAT and ACT!

Function	$f(x) = 2x$	$g(x) = x^2$	$h(x) = 2^x$
Name	Linear	Quadratic	Exponential
Graph			

Exponential functions are some of the most important functions in the real world. They appear in many places including population growth, money (interest and debt), radioactive decay, spread of disease, etc... In addition, the SAT will include several questions that require an understanding of exponential functions.

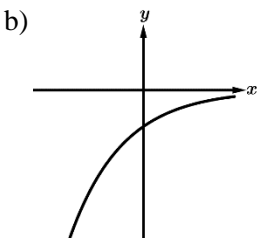
Key Characteristics of Exponential Functions	
<p>An exponential function has the general form</p> $f(x) = a(b)^x, \quad b > 0$ <p>where a and b are constants with $a \neq 0$ and $b \neq 1$.</p>	<p>a represents the _____ amount.</p> <p>b represents the _____.</p>
<p>Exponential Growth</p> <p>$a > 0$ and $b > 1$</p> 	<p>Exponential Decay</p> <p>$a > 0$ and $0 < b < 1$</p> 
<p>Increasing vs. Decreasing</p> <p>Exponential functions are always increasing or always decreasing! They will never switch from one to the other, so they have no relative (local) extrema.</p>	<p>Concave Up vs. Concave Down</p> <p>Exponential functions are always concave up or always concave down! They will never switch concavity, so they have no points of inflection.</p>
<p>End Behavior</p> <p>For exponential functions in general form, as the input values (x) increase/decrease without bound, the output values (y) will increase/decrease without bound or they will approach zero.</p>	<p>End Behavior Limit Statements</p> $\lim_{x \rightarrow \pm\infty} ab^x = \infty \text{ or } \lim_{x \rightarrow \pm\infty} ab^x = -\infty \text{ or } \lim_{x \rightarrow \pm\infty} ab^x = 0$

Example 1: Write limit statements for the end behavior of the following exponential functions.

a) 

Left: _____

Right: _____

b) 

Left: _____

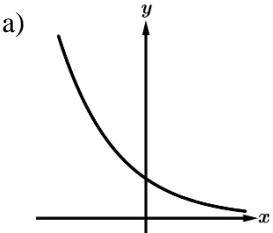
Right: _____

c) $g(x) = 5\left(\frac{2}{3}\right)^x$

Left: _____

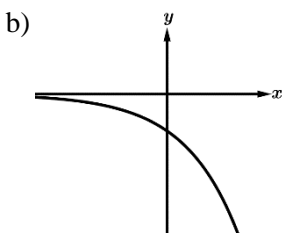
Right: _____

Example 2: For each of the following, determine if the exponential function is increasing/decreasing and concave up/down.

a) 

Concave Up or Concave Down

Increasing or Decreasing

b) 

Concave Up or Concave Down

Increasing or Decreasing

c) $h(x) = 3(4)^x$

Concave Up or Concave Down

Increasing or Decreasing

x	$f(x)$
1	3
6	5
11	9
16	17
21	33

Example 3: Selected values of the function f are shown in the table above. Determine if f could be linear, quadratic, exponential, or none of these.