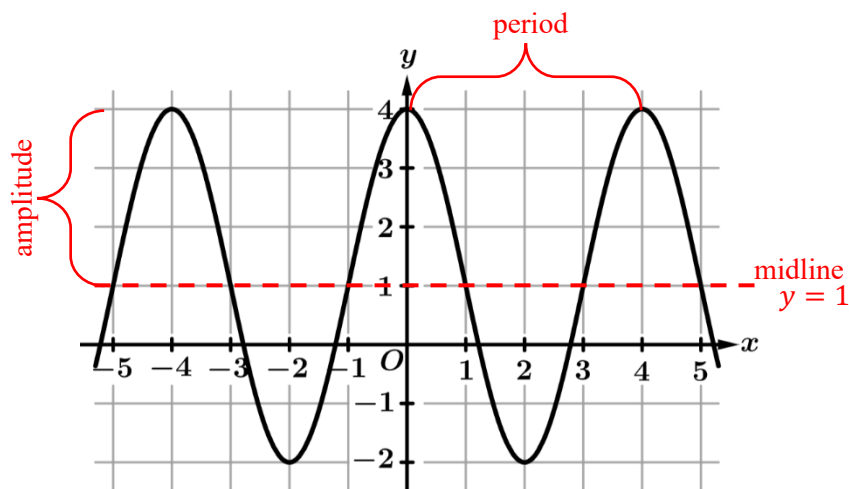
**Graph of h**

1. The graph of the sinusoidal function h is shown in the figure above. The function h can be written as $h(\theta) = a \sin(b\theta) + d$. Find the values of the constants a , b , and d .

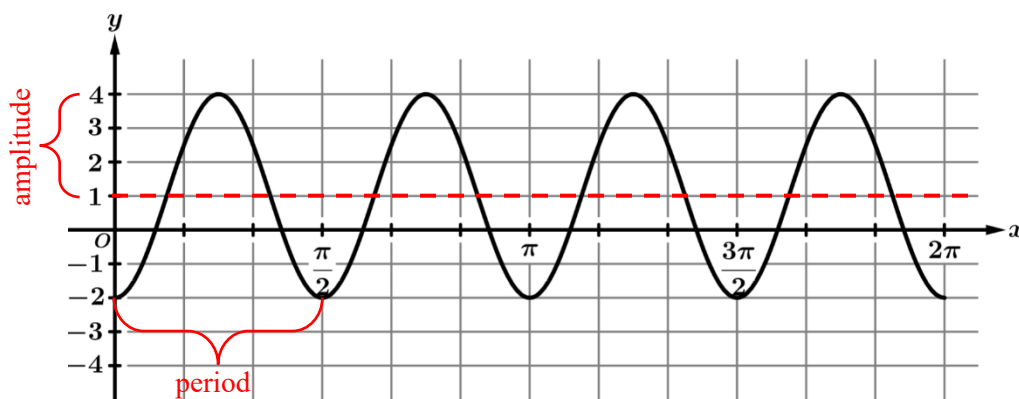
$a = -2$ the amplitude and reflection over the midline. period $= \pi = \frac{2\pi}{b} \Rightarrow b = \frac{2\pi}{\pi} = 2$

$d = 1$ the vertical translation

**Graph of f**

2. The graph of the sinusoidal function f is shown in the figure above. The function f can be written as $f(\theta) = a \cos(b\theta) + d$. Find the values of the constants a , b , and d .

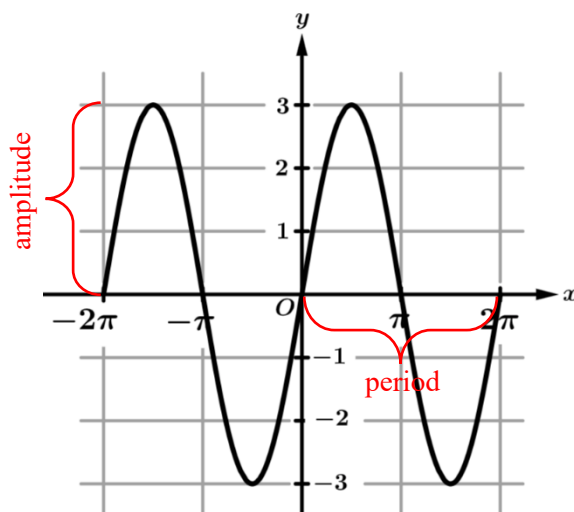
$a = 3$ the amplitude period $= 4 = \frac{2\pi}{b} \Rightarrow b = \frac{2\pi}{4} = \frac{\pi}{2}$ $d = 1$ the vertical translation



Graph of h

3. The figure shows the graph of a sinusoidal function h . What are the values of the period and amplitude of h ?

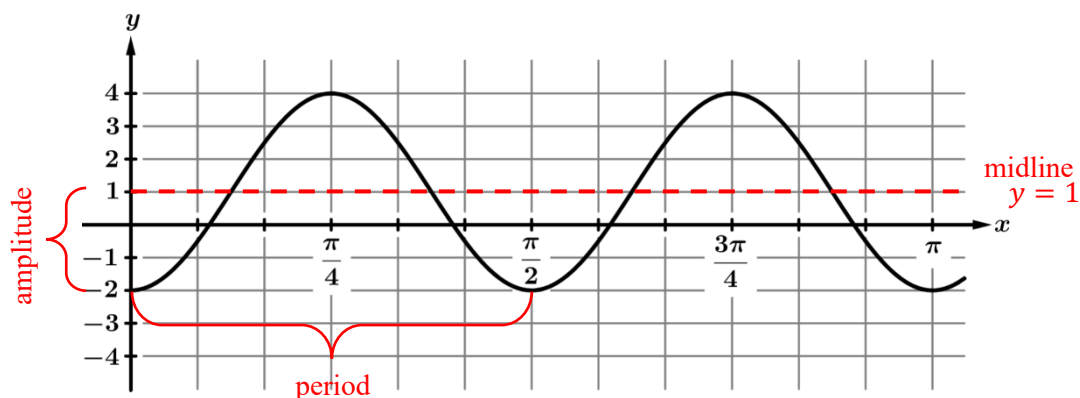
- (A) The period is π , and the amplitude is 3.
- (B) The period is π , and the amplitude is 6.
- (C) The period is $\frac{\pi}{2}$, and the amplitude is 3.
- (D) The period is $\frac{\pi}{2}$, and the amplitude is 6.



Graph of h

4. The figure shows the graph of a sinusoidal function h . What are the values of the period and amplitude of h ?

- (A) The period is π , and the amplitude is 3.
- (B) The period is π , and the amplitude is 6.
- (C) The period is 2π , and the amplitude is 3.
- (D) The period is 2π , and the amplitude is 6.



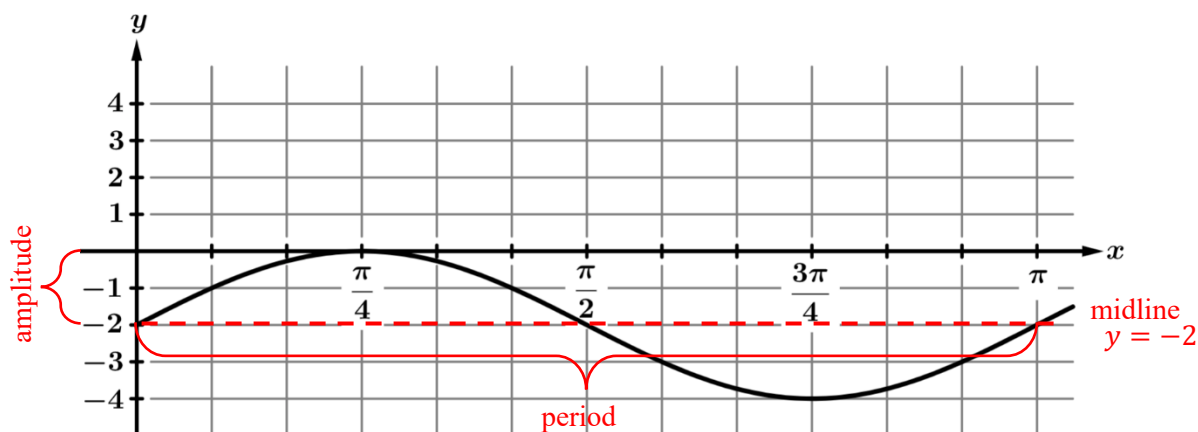
Graph of f

5. The figure shows the graph of a sinusoidal function f . Write an equation for f .

$a = 3$ the amplitude period $= \frac{\pi}{2} = \frac{2\pi}{b} \Rightarrow b = \frac{2\pi}{\frac{\pi}{2}} = 4$ $d = 1$ the vertical translation

The minimum is at $x = 0$, so this can be a cosine function reflected about the midline.

$f(x) = -3 \cos(4x) + 1$



Graph of g

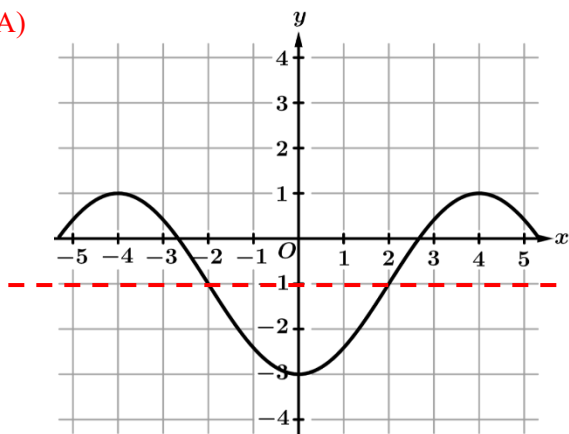
6. The figure shows the graph of a sinusoidal function g . Write an equation for g .

$a = 2$ the amplitude period $= \pi = \frac{2\pi}{b} \Rightarrow b = \frac{2\pi}{\pi} = 2$ $d = -2$ the vertical translation

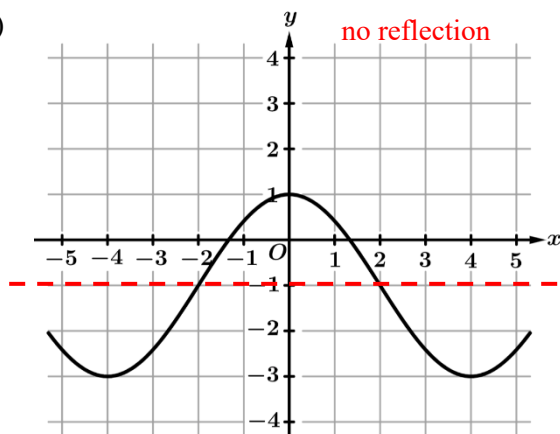
$g(x) = 2 \sin(2x) - 2$

7. The function f is given by $f(x) = -2\cos\left(\frac{\pi}{4}x\right) - 1$. Which of the following could be the graph of $f(x)$?

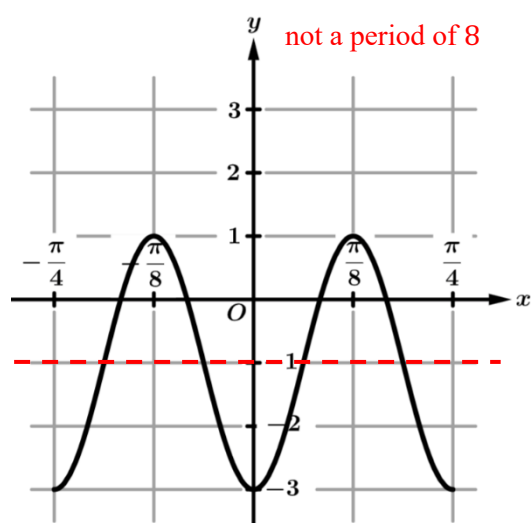
(A)



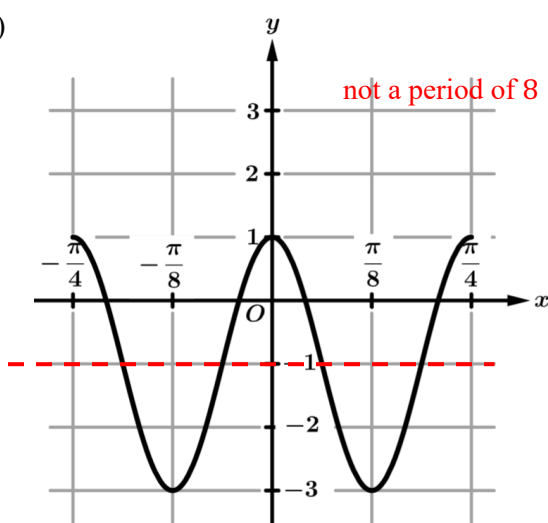
(B)



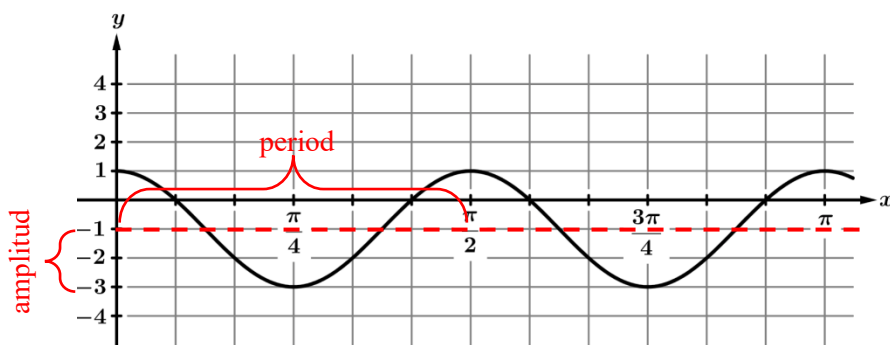
(C)



(D)



$a = -2$ the amplitude and reflection over $y = -1$ period $= \frac{2\pi}{b} = \frac{2\pi}{\frac{\pi}{4}} = 8$ $d = -1$ the midline



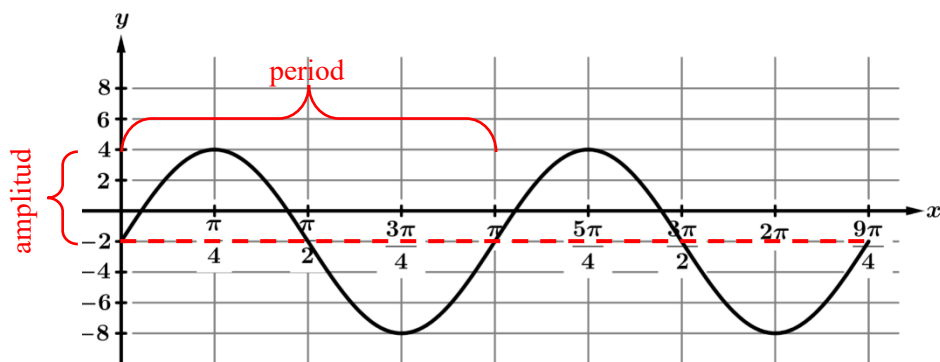
$a = 2$ the amplitude
period $= \frac{\pi}{2} = \frac{2\pi}{b}$
 $\Rightarrow b = \frac{2\pi}{\pi/2} = 4$
 $d = -1$ the midline

Graph of g

8. The figure shows the graph of a trigonometric function g . Which of the following could be an expression for $g(x)$?

- (A) $2\sin(4x) - 1$ (B) $2\sin\left(4\left(x - \frac{\pi}{2}\right)\right) - 1$ (C) $2\cos\left(4\left(x - \frac{\pi}{4}\right)\right) - 1$ (D) $-2\cos\left(4\left(x - \frac{3\pi}{4}\right)\right) - 1$

$g(x) = 2\cos(4x) - 1$ is not a choice. If $g(x)$ is shifted $\frac{\pi}{4}$ or $\frac{3\pi}{4}$ to the right there will need to be a reflection about the midline $y = -1$. This is choice (D).



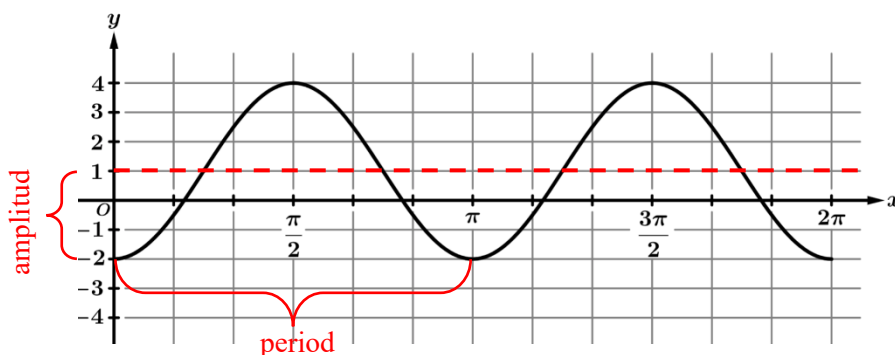
Graph of f

9. The figure shows the graph of a trigonometric function f . Which of the following could be an expression for $f(x)$

- (A) $6\sin(2x)+2$ (B) $6\sin\left(2\left(x-\frac{\pi}{2}\right)\right)-2$ (C) $-6\sin\left(2\left(x-\frac{3\pi}{2}\right)\right)-2$ (D) $-6\sin(2(x-2\pi))-2$

$a = 6$ the amplitude period $= \pi = \frac{2\pi}{b} \Rightarrow b = \frac{2\pi}{\pi} = 2$ $d = -2$ the midline

$f(x) = 6\sin(2x) - 2$ is not a choice If $f(x)$ is shifted $\frac{3\pi}{2}$ to the right there will need to be a reflection about the the midline $y = -2$. This is choice (C).



Graph of h

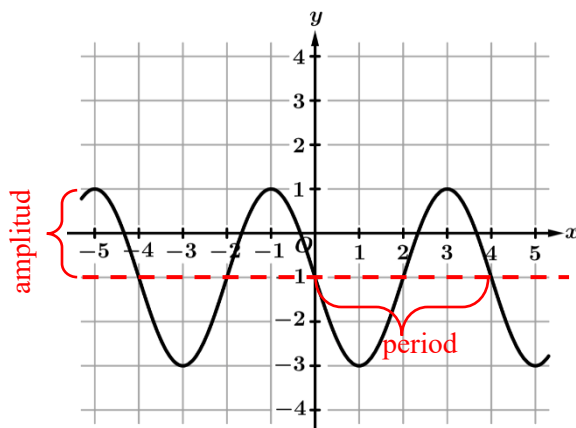
10. The figure shows the graph of a trigonometric function h . Which of the following could be an expression for $h(x)$

- (A) $-3\cos(2x)-2$ (B) $3\cos\left(2\left(x-\frac{\pi}{2}\right)\right)+1$ (C) $3\sin\left(2\left(x-\frac{\pi}{2}\right)\right)+1$ (D) $-3\sin(2(x-\pi))+1$

$a = -3$ the amplitude with a reflection over $y = 1$ period $= \pi = \frac{2\pi}{b} \Rightarrow b = \frac{2\pi}{\pi} = 2$ $d = 1$ the midline

$h(x) = -3\cos(2x) + 1$ is not a choice

If $h(x)$ is shifted $\frac{\pi}{2}$ to the right there will no need for a reflection about the the midline $y = 1$. This is choice (B).



Graph of k

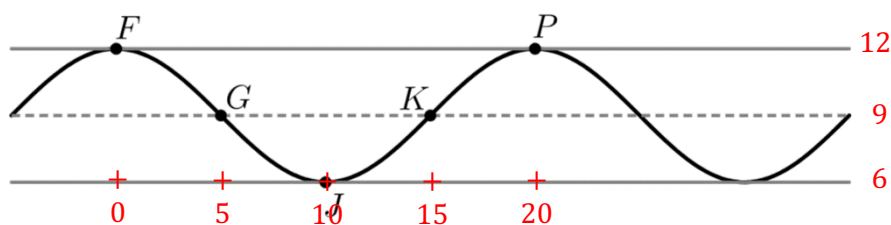
11. The figure shows the graph of a trigonometric function k . Which of the following could be an expression for $k(x)$

- (A) $2 \sin\left(\frac{\pi}{2}x\right) - 1$ (B) $-2 \sin\left(\frac{1}{4}x\right) - 1$ (C) $2 \sin\left(\frac{\pi}{2}(x-2)\right) - 1$ (D) $-2 \cos\left(\frac{\pi}{2}(x+1)\right) - 1$

$a = -2$ the amplitude with a reflection over $y = -1$ period $= 4 = \frac{2\pi}{b} \Rightarrow b = \frac{2\pi}{4} = \frac{\pi}{2}$ $d = -1$ the midline

$k(x) = -2 \sin\left(\frac{\pi}{2}x\right) - 1$ is not a choice

If $k(x)$ is shifted 2 to the right there will no need for a reflection about the the midline $y = -1$. This is choice (C).



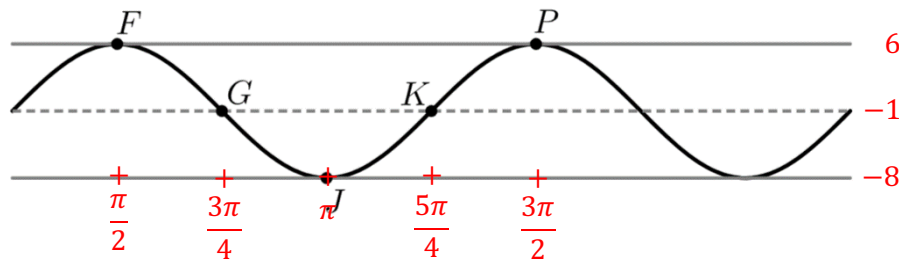
12. The graph of h and its dashed midline for two full cycles is shown. Five points, F , G , J , K , and P are labeled on the graph. No scale is indicated, and no axes are presented.

The coordinates for the five points: F , G , J , K , and P are: $F(0, 12)$, $G(5, 9)$, $J(10, 6)$, $K(15, 9)$, $P(20, 12)$.

The function h can be written in the form $h(t) = a \sin(b(t+c)) + d$. Find values of constants a , b , c , and d .

There is one period from F to P , so the period is 20. The midline is $y = 9$ and the amplitude is $12 - (9) = 3$. There is a horizontal shift because the sine function reaches its maximum at $t = \frac{\pi}{2}$, so the sine graph is shifted to the left 5.

$$\frac{2\pi}{b} = 20 \Rightarrow b = \frac{2\pi}{20} = \frac{\pi}{10} \quad a = 3 \quad d = 9 \quad \frac{\pi}{10}(0+c) = \frac{\pi}{2} \quad c = \frac{\pi}{2} \cdot \frac{10}{\pi} = 5 \quad h(t) = 3 \sin\left(\frac{\pi}{10}(t+5)\right) + 9$$



13. The graph of h and its dashed midline for two full cycles is shown. Five points, F , G , J , K , and P are labeled on the graph. No scale is indicated, and no axes are presented.

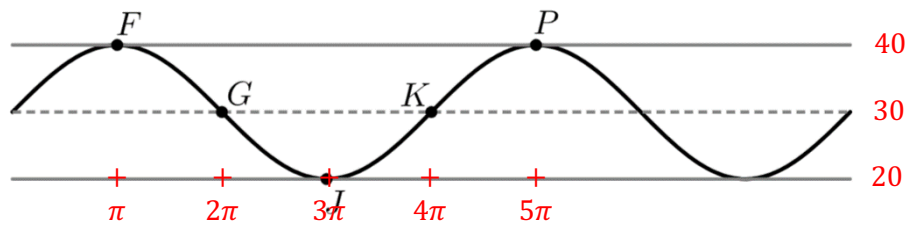
The coordinates of F , G , J , K , and P are: $F\left(\frac{\pi}{2}, 6\right)$, $G\left(\frac{3\pi}{4}, -1\right)$, $J(\pi, -8)$, $K\left(\frac{5\pi}{4}, -1\right)$, $P\left(\frac{3\pi}{2}, 6\right)$.

The function h can be written in the form $h(t) = a \sin(b(t+c)) + d$. Find values of constants a , b , c , and d .

There is one period from F to P , so the period is π . The midline is $y = -1$ and the amplitude is $6 - (-1) = 7$. There is a horizontal shift because the sine function reaches its maximum at $t = \frac{\pi}{2}$, so the sine graph is shifted to the right $\frac{\pi}{4}$.

$$\frac{2\pi}{b} = \pi \Rightarrow b = \frac{2\pi}{\pi} = 2 \quad a = 7 \quad d = -1 \quad 2\left(\frac{\pi}{2} + c\right) = \frac{\pi}{2} \quad \left(\frac{\pi}{2} + c\right) = \frac{\pi}{4} \quad c = \frac{\pi}{4} - \frac{\pi}{2} = -\frac{\pi}{4}$$

$$h(t) = 7 \sin\left(2\left(t - \frac{\pi}{4}\right)\right) - 1$$



14. The graph of h and its dashed midline for two full cycles is shown. Five points, F , G , J , K , and P are labeled on the graph. No scale is indicated, and no axes are presented.

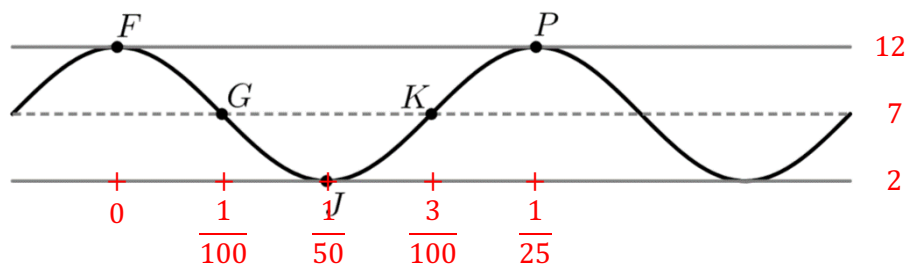
The coordinates for the points F , G , J , K , and P are $F(\pi, 40)$, $G(2\pi, 30)$, $J(3\pi, 20)$, $K(4\pi, 30)$, $P(5\pi, 40)$.

The function h can be written in the form $h(t) = a \cos(b(t+c)) + d$. Find values of constants a , b , c , and d .

There is one period from F to P , so the period is 4π . The midline is $y = 30$ and the amplitude is $40 - 30 = 10$. There is a horizontal shift because the cosine function reaches its maximum at $t = 0$, so the cosine graph is shifted to the right π .

$$\frac{2\pi}{b} = 4\pi \Rightarrow b = \frac{2\pi}{4\pi} = \frac{1}{2} \quad a = 10 \quad d = 30 \quad \frac{1}{2}(\pi + c) = 0 \quad c = -\pi$$

$$h(t) = 10 \cos\left(\frac{1}{2}(t - \pi)\right) + 30$$



15. The graph of h and its dashed midline for two full cycles is shown. Five points, F , G , J , K , and P are labeled on the graph. No scale is indicated, and no axes are presented.

The coordinates of F , G , J , K , and P are $F(0, 12)$, $G\left(\frac{1}{100}, 7\right)$, $J\left(\frac{1}{50}, 2\right)$, $K\left(\frac{3}{100}, 7\right)$, $P\left(\frac{1}{25}, 12\right)$.

The function h can be written in the form $h(t) = a \cos(b(t+c)) + d$. Find values of constants a , b , c , and d .

There is one period from F to P , so the period is $\frac{1}{25}$. The midline is $y = 7$ and the amplitude is $12 - 7 = 5$. There is a horizontal shift because the cosine function reaches its maximum at $t = 0$, so the cosine graph is shifted to the right $\frac{\pi}{4}$.

$$\frac{2\pi}{b} = \frac{1}{25} \Rightarrow b = 50\pi \quad a = 5 \quad d = 7 \quad 50\pi(0+c) = 0 \quad c = 0$$

$$h(t) = 5 \cos(50\pi(t)) + 7$$