

**Directions:** Write limit statements for the end behavior of the following logarithmic functions.

1.  $f(x) = 3\log_2 x$

2.  $g(x) = -2\log x$

3.  $h(x) = \frac{3}{4}\log_{\pi} x$

Left: \_\_\_\_\_

Left: \_\_\_\_\_

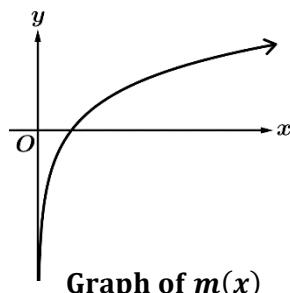
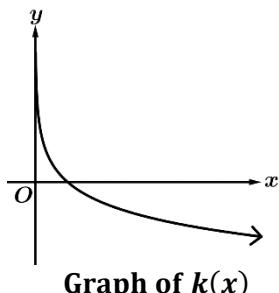
Left: \_\_\_\_\_

Right: \_\_\_\_\_

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Right: \_\_\_\_\_

**Directions:** The graphs of  $k$  and  $m$  are shown below. Use the graphs to answer the following.



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|--|---|
| <p>4. The graph of <math>k</math> is<br/>           (A) increasing at an increasing rate.<br/>           (B) increasing at a decreasing rate.<br/>           (C) decreasing at an increasing rate.<br/>           (D) decreasing at a decreasing rate.</p> <p>5. Which of the following pairs of limit statements correctly describes the end behavior of <math>k</math>?<br/>           (A) <math>\lim_{x \rightarrow 0^+} k(x) = -\infty</math> and <math>\lim_{x \rightarrow \infty} k(x) = -\infty</math><br/>           (B) <math>\lim_{x \rightarrow 0^+} k(x) = -\infty</math> and <math>\lim_{x \rightarrow \infty} k(x) = \infty</math><br/>           (C) <math>\lim_{x \rightarrow 0^+} k(x) = \infty</math> and <math>\lim_{x \rightarrow \infty} k(x) = -\infty</math><br/>           (D) <math>\lim_{x \rightarrow 0^+} k(x) = \infty</math> and <math>\lim_{x \rightarrow \infty} k(x) = \infty</math></p> <p>6. Which of the following could be the equation for <math>k</math>?<br/>           (A) <math>k(x) = -2\log_4 x</math>      (B) <math>k(x) = 2\log_4 x</math><br/>           (C) <math>k(x) = -4(2)^x</math>      (D) <math>k(x) = 4\left(\frac{1}{2}\right)^x</math></p> <p>7. Which of the following equations could be <math>k^{-1}</math>?<br/>           (A) <math>k^{-1}(x) = \left(\frac{1}{2}\right)^x</math>      (B) <math>k^{-1}(x) = -(2)^x</math><br/>           (C) <math>k^{-1}(x) = \frac{-1}{2\log_4 x}</math>      (D) <math>k^{-1}(x) = -2\log_4 x</math></p> | <p>8. The graph of <math>m</math> is<br/>           (A) increasing at an increasing rate.<br/>           (B) increasing at a decreasing rate.<br/>           (C) decreasing at an increasing rate.<br/>           (D) decreasing at a decreasing rate.</p> <p>9. Which of the following pairs of limit statements correctly describes the end behavior of <math>m</math>?<br/>           (A) <math>\lim_{x \rightarrow 0^+} m(x) = -\infty</math> and <math>\lim_{x \rightarrow \infty} m(x) = -\infty</math><br/>           (B) <math>\lim_{x \rightarrow 0^+} m(x) = -\infty</math> and <math>\lim_{x \rightarrow \infty} m(x) = \infty</math><br/>           (C) <math>\lim_{x \rightarrow 0^+} m(x) = \infty</math> and <math>\lim_{x \rightarrow \infty} m(x) = -\infty</math><br/>           (D) <math>\lim_{x \rightarrow 0^+} m(x) = \infty</math> and <math>\lim_{x \rightarrow \infty} m(x) = \infty</math></p> <p>10. Which of the following could be the equation for <math>m</math>?<br/>           (A) <math>m(x) = -3\log_8 x</math>      (B) <math>m(x) = 3\log_8 x</math><br/>           (C) <math>m(x) = -3(8)^x</math>      (D) <math>m(x) = 3(8)^x</math></p> <p>11. Which of the following equations could be <math>m^{-1}</math>?<br/>           (A) <math>m^{-1}(x) = \left(\frac{1}{2}\right)^x</math>      (B) <math>m^{-1}(x) = -(2)^x</math><br/>           (C) <math>m^{-1}(x) = 2^x</math>      (D) <math>m^{-1}(x) = \frac{1}{3\log_8 x}</math></p> |
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**Directions:** Selected values of the several logarithmic functions are shown in the tables below. For each table, find the value of the constant  $k$ .

12.

| $x$  | $f(x)$ |
|------|--------|
| 0.3  | 2      |
| 3    | 5      |
| 30   | 8      |
| $k$  | 11     |
| 3000 | 14     |

13.

| $x$           | $g(x)$ |
|---------------|--------|
| $\frac{3}{4}$ | 1      |
| 3             | 2      |
| $k$           | 3      |
| 48            | 4      |

14.

| $x$   | $h(x)$  |
|-------|---------|
| $12k$ | $k - 1$ |
| $6k$  | $k$     |
| $3k$  | $k + 1$ |
| 6     | $k + 2$ |
| 3     | $k + 3$ |

15.

| $x$   | $l(x)$ |
|-------|--------|
| $3^7$ | 4      |
| $3^5$ | 6      |
| 27    | 8      |
| 3     | 10     |
| $k$   | 12     |

16. Let  $f(x) = 3\log_5(x+4)$ .

- a) Find the domain and range of the function  $f$ .
  
  
  
  
  
- b) If  $g(x) = -2f(x-3)$ , find the domain and range of  $g$ .
  
  
  
  
  
- c) If  $k(x) = f(2x)+7$ , find the domain and range of  $k$ .