

22.09.2021.

1. Уопшеници ДН: 10 цифара 21 позиција

$$\Rightarrow 21 = 2 \cdot 10 + 1$$

↳ јар 3 нисе
(не важи за 20)

$$2. \binom{5}{3} \binom{5}{4} + \binom{5}{4} \binom{5}{3} + \binom{5}{5} \binom{5}{2}$$

3. Број графова $2^{\binom{5}{2}}$
↳ број могућности
↳ има ниса граке



$$N(S_a) = N(S_b) = \dots = 2^{\binom{5-1}{2}} \rightarrow \text{узоровање 1}$$

$$N(S_a S_b) = \dots = 2^{\binom{5-2}{2}} \rightarrow \text{узоровање 2}$$

$$N(S_a S_b S_c) = \dots = 2^{\binom{5-3}{2}} = 2 \rightarrow \text{узоровање 3}$$

$$N(S_a S_b S_c S_d) = 1 \quad N(S_a S_b S_c S_d S_e) = 1$$

$$N(S_a' S_b' S_c' S_d') = 2^{\binom{5}{2}} - \binom{5}{1} 2^{\binom{4}{2}} + \binom{5}{2} 2^{\binom{3}{2}} - \binom{5}{3} 2^{\binom{2}{2}} + \binom{5}{4} - \binom{5}{5}$$

$$4. f_{n+2} + 4f_{n+1} + 4f_n = 7 \quad f_0 = 1 \quad f_1 = 2$$

$$t^2 + 4t + 4 = 0 \quad \leftarrow \text{карактер. једн}$$

$$(t+2)^2 = 0 \Rightarrow t_1 = -2 = t_2$$

$$f_n^{(h)} = (4n+3)(-2)^n$$

$$f_n^{(p)} = n^0 C \cdot 1^n = C$$

$$C + 4C + 4C = 7 \Rightarrow C = \frac{7}{9}$$

$$f_n^{(p)} = \frac{7}{9}$$

$$f_n = (An+B)(-2)^n + \frac{7}{9}$$

$$f_0 = 1 = B + \frac{7}{9} \Rightarrow B = \frac{2}{9}$$

$$f_1 = 2 = \left(A + \frac{2}{9}\right)(-2) + \frac{7}{9} = -2A - \frac{4}{9} + \frac{7}{9} = -2A + \frac{3}{9} = -2A + \frac{1}{3}$$

$$\Rightarrow -2A = \frac{5}{3} \Rightarrow A = -\frac{5}{6}$$

$$f_n = \left(-\frac{5}{6}n + \frac{2}{9}\right)(-2)^n + \frac{7}{9}$$