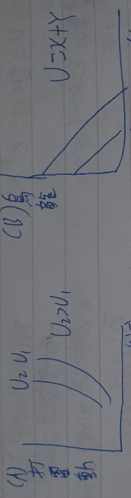


Content:

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二①



② (1)  $MRS_{xy} = \frac{\frac{1}{2}X^{-\frac{1}{2}}Y^{\frac{1}{2}}}{\frac{1}{2}X^{\frac{1}{2}}Y^{-\frac{1}{2}}} = \frac{Y}{X} \Rightarrow \frac{Y}{X} = \frac{20}{10} \Rightarrow 4X=Y$

代入得  $20X+40X=320$

$X=5 \quad Y=20$

(2)  $U = f(X,Y) = X+Y$  (3)  $U = f(X,Y) = \ln X + \ln Y$

$320 = 20X + 10Y$   $320 = 20 \times 5 + 10Y$

$MRS_{xy} = \frac{1}{3} < \frac{10}{20}$   $X=2, Y=10 \Rightarrow$

$\Rightarrow X=2, Y=30$   $320 = 40Y + 10Y$

$Y=6, X=12$

③ (1)  $U = f(X,Y) = X^{\frac{1}{2}}Y^{\frac{1}{2}}$

$320 = 20X + 10Y$

$MRS_{xy} = \frac{Y}{X} = \frac{10}{20} = \frac{1}{2} \quad X=2, Y=20$

(2) 假设  $U = X^{\frac{1}{2}}Y^{\frac{1}{2}} = 5^{\frac{1}{2}}20^{\frac{1}{2}} = 2000^{\frac{1}{2}}$

代入  $\Rightarrow Y = 20X \quad X = 2000^{\frac{1}{2}}$

$\Rightarrow (40)^{\frac{1}{2}} = 2000^{\frac{1}{2}}$

$\Rightarrow X=5, Y=20 \quad X=500, Y=4000$

所得效果

(4)  $U = f(X,Y) = (500)^{\frac{1}{2}}(4000)^{\frac{1}{2}} \Rightarrow \sqrt{10,000}$

(1) 替代效果

(2)  $(5,20) \Rightarrow \sqrt{(500)^{\frac{1}{2}}(4000)^{\frac{1}{2}}}$

$\sqrt{5} = 500^{\frac{1}{2}} - 5 > 0$